

# kETH Properties

We will focus on specifying high level key properties. Most revert conditions will for example not be in scope for this document.

## Properties of *KETHVault*

### Invariants

- $totalSupply() \leq maxSupply$

### Function properties of *deposit*

In pre state, set  $A = totalAssets()$  and  $V = assetValue(a, x)$ . Suppose  $y = deposit(a, x, r, b)$  is applied to valid input, then

- $totalAssets()$  will increase by  $V$  modulo slippage
- In case  $a \neq dETH$  and  $b = true$  and  $kETHStrategy.autoSellFor() \neq 0$ , then  $kETHStrategy.assetValue(kETHStrategy.reserves(kETHStrategy.autoSellFor()))$  will increase by at least  $V - 0.011 ether$  modulo slippage
- In case  $a = dETH$ ,  $kETHStrategy.assetValue(kETHStrategy.reserves(savETH))$  will increase by at least  $V$  modulo slippage
- In case  $a \neq dETH$  and  $b = false$  and  $kETHStrategy.autoSellFor() \neq 0$ , then  $kETHStrategy.assetValue(kETHStrategy.reserves(a))$  will increase by at least  $V$  modulo slippage
- $y = amountToShare(V)$ , modulo slippage
- $totalSupply()$  will increase by  $y$
- $balanceOf(r)$  will increase by  $y$

### Function properties of *withdraw*

In pre state, let  $A = totalAssets()$  and  $T = totalSupply()$ . When calling  $withdraw(x, r)$  on valid input,

- $totalAssets()$  will decrease by  $shareToAmount(x)$  modulo rounding errors
- $strategy.dETH().balanceOf(r) + r.balance + strategy.giantLP().balanceOf(r)$  will increase by  $shareToAmount(x)$  modulo slippage and bounded asset loss
- $totalSupply()$  will decrease by  $x$
- $balanceOf(r)$  will decrease by  $x$

### Function properties of *shareToAmount* and *amoutToShare*

The same as those for *DETHVault*. See the Properties of *DETHVault* section.

## Function properties of *setStrategy*

In pre state let  $R_a = \text{strategy.reserves}(a)$  and  $T = \text{strategy.totalAssets}()$  and set  $s = \text{strategy}$ . Assuming that  $s \neq s'$ , after successful invocation of *setStrategy*( $s'$ ), for each  $a$  in *holdingAssets*(),

- $s.\text{reserves}(a) = s.\text{totalAssets}() = 0$
- $\text{strategy} = s'$
- $s'.\text{balance}(a)$  has increased by  $R_a$
- $s'.\text{reserves}(a) = s'.\text{balance}(a)$
- $s'.\text{totalAssets}()$  has increased by  $T$

## Properties of *SavETHManagerHandler*

*The properties of SavETHManagerHandler are properties of both KETHStrategy and DETHVault.*

### Invariants

- $\text{isolatedKeys}[i] \neq 0$  if and only if  $i < \text{numOfIsolatedKeys}$
- For each  $i < \text{numOfIsolatedKeys}$ , with  $s = \text{isolatedKeys}[i]$ ,  $\text{savETHManager.associatedIndexIdForKnot}(s.\text{blsPublicKey}) > 0$
- The BLS public keys  $\text{isolatedKeys}[i].\text{blsPublicKey}$  for  $i < \text{numOfIsolatedKeys}$  are pairwise distinct

## Function properties of *isolateKnotFromOpenIndex*

Suppose non-reverting call *isolateKnotFromOpenIndex*( $h, k$ ),

- $\text{numOfIsolatedKeys}$  is increased by one
- $\text{\_reserves}[\text{savETH}]$  is decreased by at least  $\text{savETHManager.dETHToSavETH}(\text{savETHManager.KNOT\_BATCH\_AMOUNT})$
- $\text{isolatedKeys}[\text{numOfIsolatedKeys} - 1] = (h, k)$

## Function properties of *addKnotToOpenIndex*

In pre state set  $s = \text{isolatedKeys}[i]$  and  $t = \text{isolatedKeys}[\text{numOfIsolatedKeys} - 1]$ . After successful call *addKnotToOpenIndex*( $i$ ),

- $\text{numOfIsolatedKeys}$  is decreased by one
- $\text{\_reserves}[\text{savETH}]$  is increased by at least  $\text{savETHManager.dETHToSavETH}(\text{savETHManager.KNOT\_BATCH\_AMOUNT})$
- $\text{isolatedKeys}[i] = t$
- $\text{savETHManager.associatedIndexIdForKnot}(s.\text{blsPublicKey}) = 0$

## Function properties of *rotateSavETH*

In pre state set  $s = \text{isolatedKeys}[i]$ . Assume successful call  $\text{rotateSavETH}(i, h, k)$ . Except for possible rounding errors, that is having the same effect on  $\text{reserves}(\text{savETH})$  as the sequence of calls  $\text{addKnotToOpenIndex}(i); \text{isolateKnotFromOpenIndex}(h, k)$ . Moreover the following properties are satisfied in the post state:

- $\text{isolatedKeys}[i] = (h, k)$
- $\text{savETHManager.associatedIndexIdForKnot}(s.\text{blsPublicKey}) = 0$ .

## Properties of *KETHStrategy*

### Invariants

- If  $\text{defaultSwapper}[i][j] = s \neq 0$  then  $\text{swapper}[i][j][s] = \text{true}$
- If  $\text{swapper}[i][j][s] = \text{true}$  then  $s.\text{inputToken}() = i$  and  $s.\text{outputToken}() = j$
- For all  $a \neq \text{savETH}$ ,  $\text{balance}(a) \geq \text{reserves}(a)$
- $\text{balance}(\text{savETH}) + \text{totalIsolatedSavETH}() \geq \text{reserves}(a)$
- $\text{reserves}(a) > 0$  implies  $\text{isHoldingAsset}(a)$
- $\text{isUnderlyingAsset}(a)$  implies  $\text{isHoldingAsset}(a)$
- Required holding assets, which swappers may assume
  - $\text{isHoldingAsset}(\text{giantLP})$
  - $\text{isHoldingAsset}(\text{dETH})$
  - $\text{isHoldingAsset}(\text{savETH})$
  - $\text{isHoldingAsset}(\text{ETH})$
- For all  $i$  satisfying  $\text{isHoldingAsset}(i)$  and  $i \notin \{\text{ETH}, \text{dETH}, \text{giantLP}, \text{savETH}\}$ ,  $\text{defaultSwapper}[i][\text{ETH}] \neq 0$

Comments:

- $\text{isUnderlyingAsset}(\text{stETH})$  is unused

## Function properties of *assetValue*

For any asset  $a$  such that  $\text{isHoldingAsset}(a)$ , the following properties are required

- $\text{assetValue}(a, 0) = 0$
- $\text{assetValue}(a, 1 \text{ ether}) > 0$
- $\text{assetValue}(a, x + y) = \text{assetValue}(x) + \text{assetValue}(y)$ , modulo rounding errors
- $\text{assetValue}(a, x + 1) \geq \text{assetValue}(a, x)$

## Function properties of *invokeSwap*

After successful invocation of  $\text{invokeSwap}(s, a, x, b, M, D)$ , then

- $\text{assetValue}(a, \text{reserves}(a))$  will decrease by  $\text{assetValue}(a, x)$  plus/minus 0.011 ether, modulo slippage
- $\text{assetValue}(b, \text{reserves}(b))$  will increase by at least  $\text{assetValue}(a, x) - 0.011 \text{ ether}$  modulo slippage

- $reserves(b)$  will increase by at least  $M$
- $totalAssets()$  is constant, modulo slippage

## Properties of *DETHVault*

### Invariants

- $dETH.balanceOf(address(this)) \geq reserves(dETH)$
- $savETH.balanceOf(address(this)) + totalIsolatedSavETH() \geq reserves(savETH)$
- $address(this).balance \geq reserves(ETH)$

### Function properties of *deposit*

After successful invocation of *deposit*( $x, r$ ):

- $balanceOf(r)$  will increase by  $amountToShare(x)$
- $dETH.balanceOf(r)$  will decrease by  $x$
- $reserves(savETH)$  will increase by  $savETHManager.dETHToSavETH(x)$

### Function properties of *withdrawToETH*

After successful invocation of *withdrawToETH*( $x, r$ ):

- $balanceOf(r)$  will decrease by  $x$
- $r.balance$  will increase by  $shareToAmount(x)$
- $reserves(ETH)$  will decrease by  $shareToAmount(x)$

### Function properties of *withdrawToDETH*

After successful invocation of *withdrawToDETH*( $x, r$ ):

- $balanceOf(r)$  will decrease by  $x$
- $dETH.balanceOf(r)$  will increase by  $savETHManager.savETHToDETH(savETHManager.dETHToSavETH(x))$
- $reserves(savETH)$  will decrease by  $savETHManager.dETHToSavETH(x)$

### Function properties of *swapETHToDETH*

After successful invocation of *swapETHToDETH*( $r$ ):

- $reserves(ETH)$  will increase by  $msg.value$
- $reserves(savETH)$  will decrease by approximately  $savETHManager.dETHToSavETH(msg.value)$
- $dETH.balanceOf(msg.sender)$  will increase by approximately  $msg.value$ .

### Function properties of *shareToAmount* and *amountToShare*

- $shareToAmount(amountToShare(x))$  is  $x$ , modulo rounding errors

- $\text{amountToShare}(\text{shareToAmount}(x))$  is  $x$ , modulo rounding errors
- $\text{shareToAmount}(0) = \text{amountToShare}(0) = 0$
- $\text{shareToAmount}(x + 1) \geq \text{shareToAmount}(x)$
- $\text{amountToShare}(x + 1) \geq \text{amountToShare}(x)$
- $\text{shareToAmount}(\text{totalSupply}()) = \text{totalAssets}()$
- $\text{amountToShare}(\text{totalAssets}()) = \text{totalSupply}()$
- $\text{shareToAmount}(x + y) = \text{shareToAmount}(x) + \text{shareToAmount}(y)$ , modulo rounding errors
- $\text{amountToShare}(x + y) = \text{amountToShare}(x) + \text{amountToShare}(y)$ , module rounding errors

## Properties of *ISwapper*

Let *KETHStrategy strategy* be given. Any *ISwapper* must satisfy the following. After non-reverting call  $\text{swap}(a, x, b, M, D)$ , then

- Sender's balance of  $a$  token will decrease in asset value corresponding to  $\text{strategy.assetValue}(a, x) - 0.011 \text{ ether}$ , modulo a constant bounded slippage
- Sender's balance of  $b$  token will increase in asset value corresponding to  $\text{strategy.assetValue}(a, x) - 0.011 \text{ ether}$ , modulo a constant bounded slippage
- Sender's balance of  $b$  token will increase by at least  $M$