

A mathematical modeling toolbox for ion channels and transporters across cell membranes

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1 The following supplementary material is from " [A mathematical modeling toolbox for ion channels](#)
2 [and transporters across cell membranes](#)" manuscript. It contains an overview of all equations
3 related to Ion channels, Pumps, Cotransporters, and Symporters, organized in a table form. The
4 detailed transporters along with the descriptions of their equations can be found from [here](#).

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Sodium Phosphate Symporter (NaPO4)	Ref
<div data-bbox="199 510 1257 728" style="border: 1px solid black; padding: 10px; margin-bottom: 10px;"> $J_{Na,NaPO_4}^{M,N(net)} = [E]_t \left(\frac{R_{NN} (g_{ENa}^M Na^M + g_{ENaPO_4}^M Na^M PO_4^M + g_{ENaPO_4Na}^M Na^M PO_4^M Na''^M)}{R_M R_{NN} + R_N R_{MM}} - \frac{R_{MM} (g_{EA}^N Na^N + g_{ENaPO_4}^N Na^N PO_4^N + g_{ENaPO_4Na}^N Na^N PO_4^N Na''^N)}{R_M R_{NN} + R_N R_{MM}} \right)$ </div> <div data-bbox="1177 728 1268 761" style="text-align: right;">(140a)</div> <div data-bbox="220 757 1145 974" style="border: 1px solid black; padding: 10px; margin-bottom: 10px;"> $J_{PO_4,NaPO_4}^{M,N(net)} = [E]_t \left(\frac{R_{NN} (g_{ENaPO_4}^M Na^M PO_4^M + g_{ENaPO_4Na}^M Na^M PO_4^M Na''^M)}{R_M R_{NN} + R_N R_{MM}} - \frac{R_{MM} (g_{ENaPO_4}^N Na^N PO_4^N + g_{ENaPO_4Na}^N Na^N PO_4^N Na''^N)}{R_M R_{NN} + R_N R_{MM}} \right)$ </div> <div data-bbox="1177 846 1268 880" style="text-align: right;">(140b)</div> <p>where $[E]_t = [E]_M + [ENa]_M + [ENaPO_4]_M + [ENaPO_4Na]_M + [ENaPO_4Na]_N + [ENaPO_4]_N + [ENa]_N + [E]_N$ $Na^M = \frac{[Na]_M}{K_{Na}^M}$, $PO_4^M = \frac{[PO_4]_M}{K_{NaPO_4}^M}$, $Na''^M = \frac{[Na]_M}{K_{NaPO_4Na}^M}$ $Na^N = \frac{[Na]_N}{K_{Na}^N}$, $PO_4^N = \frac{[PO_4]_N}{K_{NaPO_4}^N}$, $Na''^N = \frac{[Na]_N}{K_{NaPO_4Na}^N}$ $R_M = 1 + Na^M + Na^M PO_4^M + Na^M PO_4^M Na''^M$ $R_N = 1 + Na^N + Na^N PO_4^N + Na^N PO_4^N Na''^N$ $R_{MM} = g_E^M + g_{ENa}^M Na^M + g_{ENaPO_4}^M Na^M PO_4^M + g_{ENaPO_4Na}^M Na^M PO_4^M Na''^M$ $R_{NN} = g_E^N + g_{ENa}^N Na^N + g_{ENaPO_4}^N Na^N PO_4^N + g_{ENaPO_4Na}^N Na^N PO_4^N Na''^N$</p>	[34, 57]

Table 24: The corresponding equations describing the flux transported via sodium phosphate symporter across the cell membrane