

# A mathematical modeling toolbox for ion channels and transporters across cell membranes

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1 The following supplementary material is from " [A mathematical modeling toolbox for ion channels](#)  
2 [and transporters across cell membranes](#)" manuscript. It contains an overview of all equations  
3 related to Ion channels, Pumps, Cotransporters, and Symporters, organized in a table form. The  
4 detailed transporters along with the descriptions of their equations can be found from [here](#).

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\*This document is the result of the research project funded by the National Science Foundation.

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Proton-ATPase ( $H - ATPase$ )		Ref
$J_{H,HATPase}^{M-N(a)} = -J_{H,HATPase}^{max} \frac{1}{1 + \exp(\zeta(v_H^{M-N(a)} - v_{1/2,H-ATPase}^{M-N(a)}))}$	(112)	[32]
$J_{H,HATPase}^{M-N(b)} = J_{H,HATPase}^{max} \frac{1}{1 + \exp(-\zeta(v_H^{M-N(b)} - v_{1/2,H-ATPase}^{M-N(b)}))}$	(113)	
$J_{H,H-ATPase}^{M(i)-N(e)} = J_{H,HATPase}^{max} \frac{[H^+]_{M(cell)}}{K_{H,H-ATPase}^{M(cell)} + [H^+]_{M(cell)}}$	(114)	[29]

Table 11: The corresponding equations describing the flux and current transported via proton-ATPase (H-ATPase) pumps across the cell membrane