

# A mathematical modeling toolbox for ion channels and transporters across cell membranes

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1 The following supplementary material is from " [A mathematical modeling toolbox for ion channels](#)  
2 [and transporters across cell membranes](#)" manuscript. It contains an overview of all equations  
3 related to Ion channels, Pumps, Cotransporters, and Symporters, organized in a table form. The  
4 detailed transporters along with the descriptions of their equations can be found from [here](#).

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14 1.2.2. Voltage Gated Sodium Channel (VGSC,  $Na_v$ ,  $VONa$ )

Voltage Gated Sodium Channel (VGSC, $Na_v$ , $VONa$ )	Ref
	[2, 13]
$I_{Na,Na_v} = g_{Na_v}^{max} m_{Na_v}^3 h_{Na_v} (V_m - V_{Na,rev}^{M-N}) \quad (33)$	
$\frac{dm_{Na_v}}{dt} = \frac{\bar{m}_{Na_v} - m_{Na_v}}{\tau_m} \quad (34)$	
$\frac{dh_{Na_v}}{dt} = \frac{\bar{h}_{Na_v} - h_{Na_v}}{\tau_h} \quad (35)$	
$\bar{m}_{Na_v} = \frac{1}{1 + \exp\left(\frac{-(V_m^{M-N} + V_{1/2,m}^{M-N} Na_v)}{k_m Na_v}\right)} \quad (36)$	
$\bar{h}_{Na_v} = \frac{1}{1 + \exp\left(\frac{(V_m^{M-N} + V_{1/2,h}^{M-N} Na_v)}{k_h Na_v}\right)} \quad (37)$	

Table 3: The corresponding equations describing the ionic current transported via voltage gated sodium channels (VGSCs,  $Na_v$ s,  $VONa$ s) across the cell membrane (part 1/3 continued from previous page)