

Lecture 6: **Stack ADT & Queue ADT**

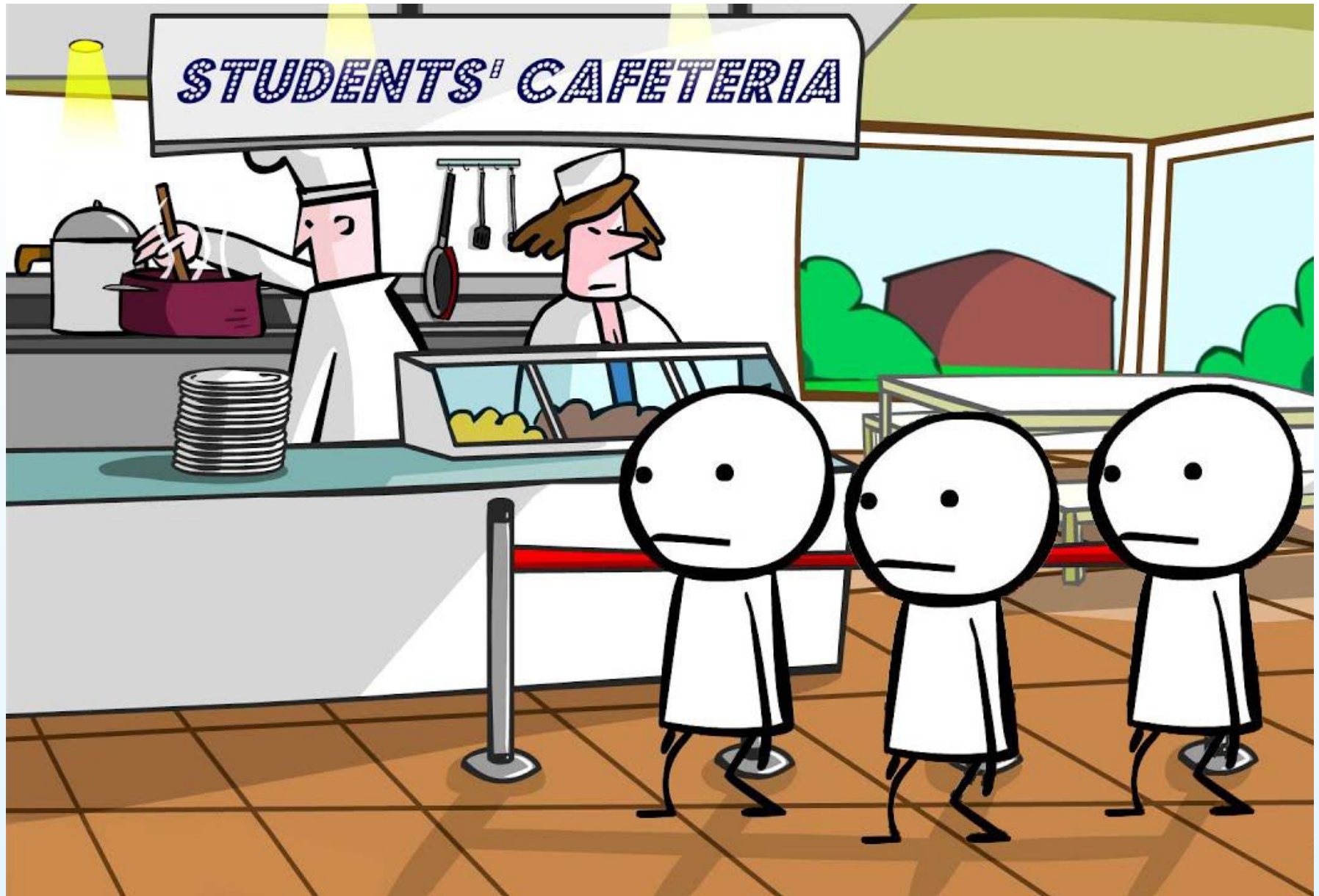
01204212 Abstract Data Types and Problem Solving

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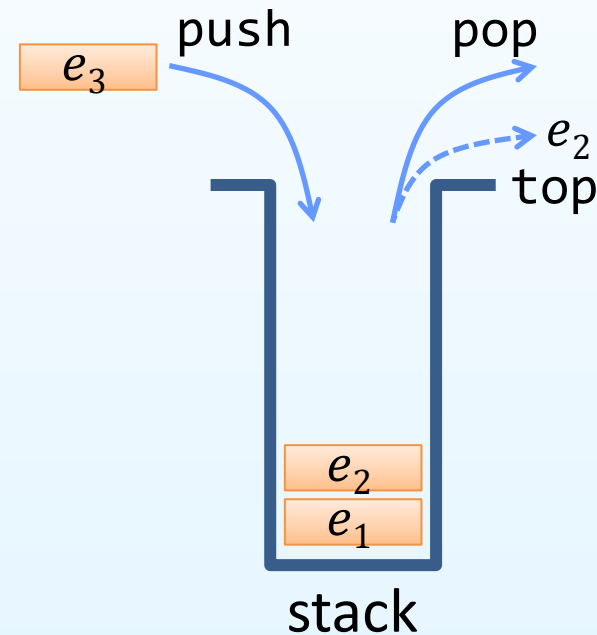




Stack ADT

What is a Stack ADT?

- Data:
 - Elements stored in a list linearly, but are allowed insertion and deletion only **at one end**
 - This mechanism is called **LIFO** – Last in, First out
- Common operations:
 - `push(stack, value)`
 - `pop(stack)`
 - `top(stack)/peek(stack)`
 - `is_empty(stack)`
 - `is_full(stack)`
 - ...



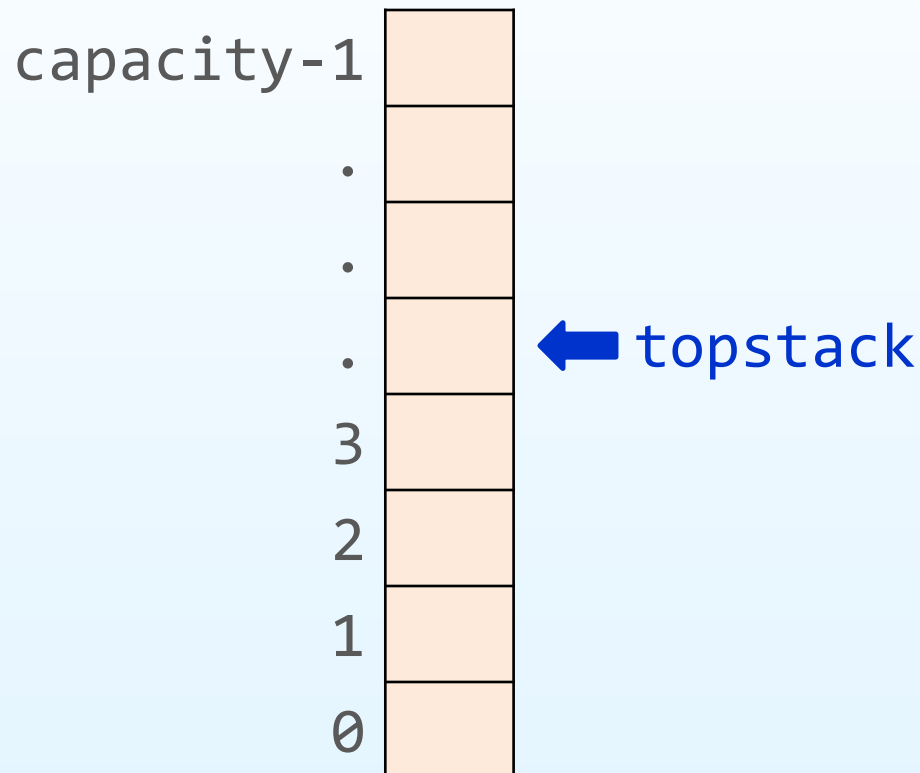
Stack Implementations

- Two types of implementation
 - Array-based stack
 - Pointer-based stack

Stack: Array Implementation

Basic idea:

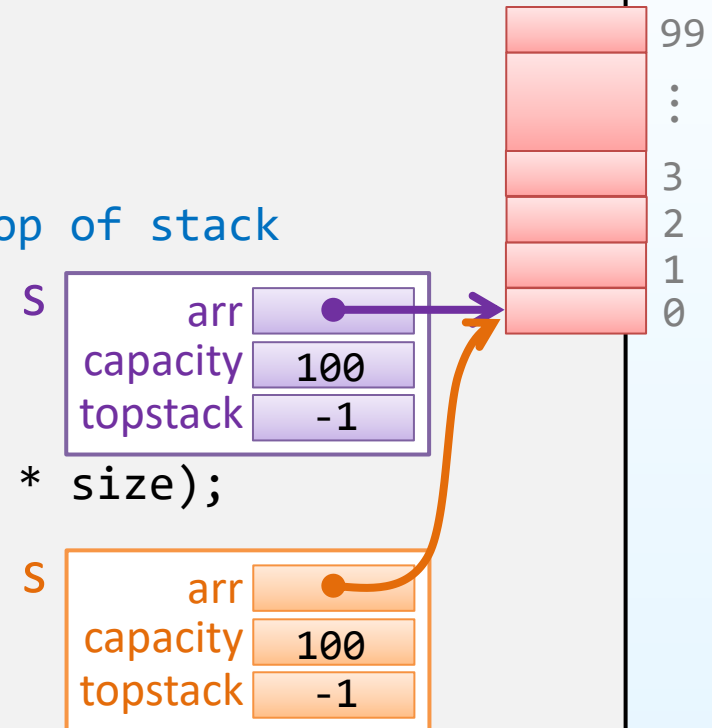
- **Allocate** a big array (of size capacity)
- **Keep track** of current size (using a variable topstack)



Stack: Array-based Construction

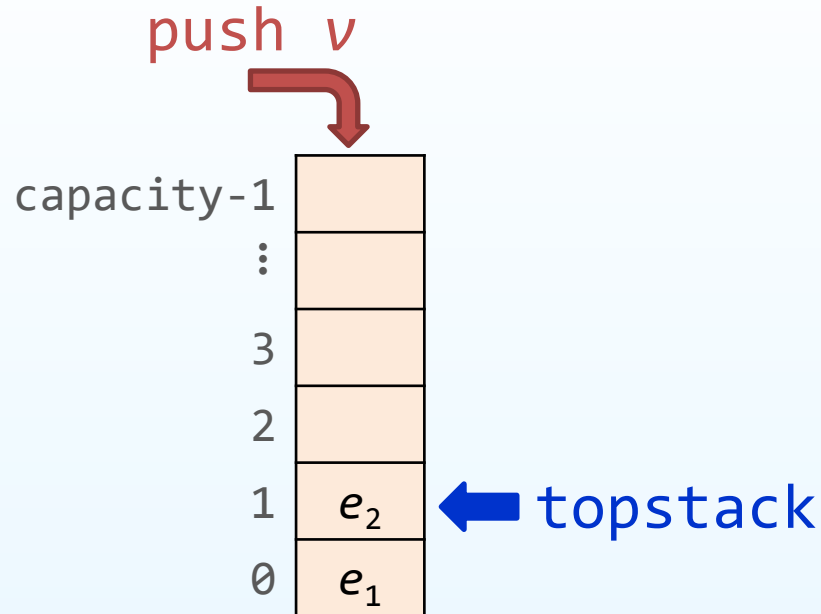
Assume that all data are positive integer

```
1: #include <stdio.h>
2: #include <stdlib.h>
3:
4: typedef struct stack {
5:     int *arr;        // array-based stack
6:     int capacity;    // size of stack
7:     int topstack;    // position at the top of stack
8: } stack_t;
9:
10: stack_t create(int size) {
11:     stack_t s = {NULL, size, -1};
12:     s.arr = (int *)malloc(sizeof (int) * size);
13:     return s;
14: }
15: int main(void) {
16:     stack_t s = create(100);
17:     return 0;
18: }
```



Array-based Stack: push() Operation

Push a value v at the top of stack s

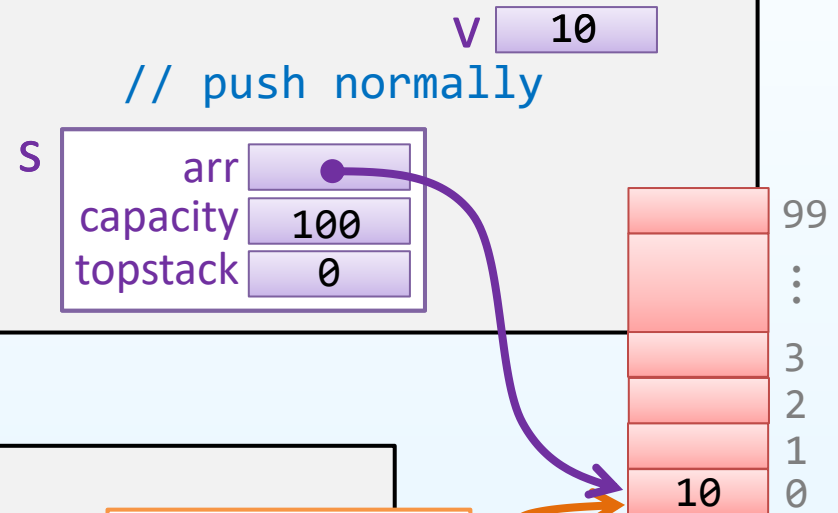


- If $\text{topstack} < \text{capacity}$, push v normally
- Otherwise, the stack is full

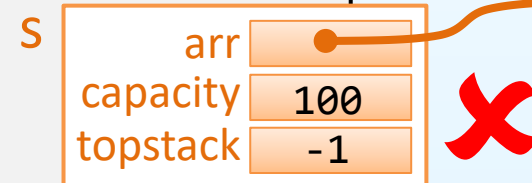
Array-based Stack: push() Operation

Push a value v at the top of stack s

```
1: int push(stack_t s, int v) {  
2:   if (s.topstack == s.capacity-1)    // stack is full  
3:     return 0;  
4:  
5:   s.topstack++;  
6:   s.arr[s.topstack] = v;  
7:  
8:   return 1;  
9: }
```



```
int main(void) {  
  stack_t s = create(100);  
  push(s, 10);  
  return 0;  
}
```



Array-based Stack: push() Operation

Push a value v at the top of stack s

```
1: int push(stack_t *s, int v) {  
2:   if (s->topstack == s->capacity-1) // stack is full  
3:     return 0;  
4:  
5:   s->topstack++; // push normally  
6:   s->arr[s->topstack] = v;  
7:  
8:   return 1;  
9: }
```

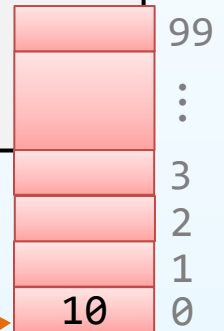
v 10

s

```
int main(void) {  
  stack_t s = create(100);  
  push(&s, 10);  
  return 0;  
}
```

s

arr
capacity 100
topstack 0



Exercise 1: Other Operations

Implement the following functions for an **array-based stack**

- `pop()` – remove the top element of stack s
 - Return v if the stack is not empty, otherwise -1
- `top()` – peek the top element of stack s
 - Return v if the stack is not empty, otherwise -1
- `is_empty()` – check whether stack s is empty
 - return 1 if the stack is empty, otherwise 0
- `is_full()` – check whether stack s is full
 - return 1 if the stack is full, otherwise 0



Array-based Stack: Running Time

Operation	Running Time
create()	$O(1)$
push()	$O(1)$
pop()	$O(1)$
top()	$O(1)$
is_empty()	$O(1)$
make_empty()	$O(1)$
is_full()	$O(1)$
destroy()	$O(1)$



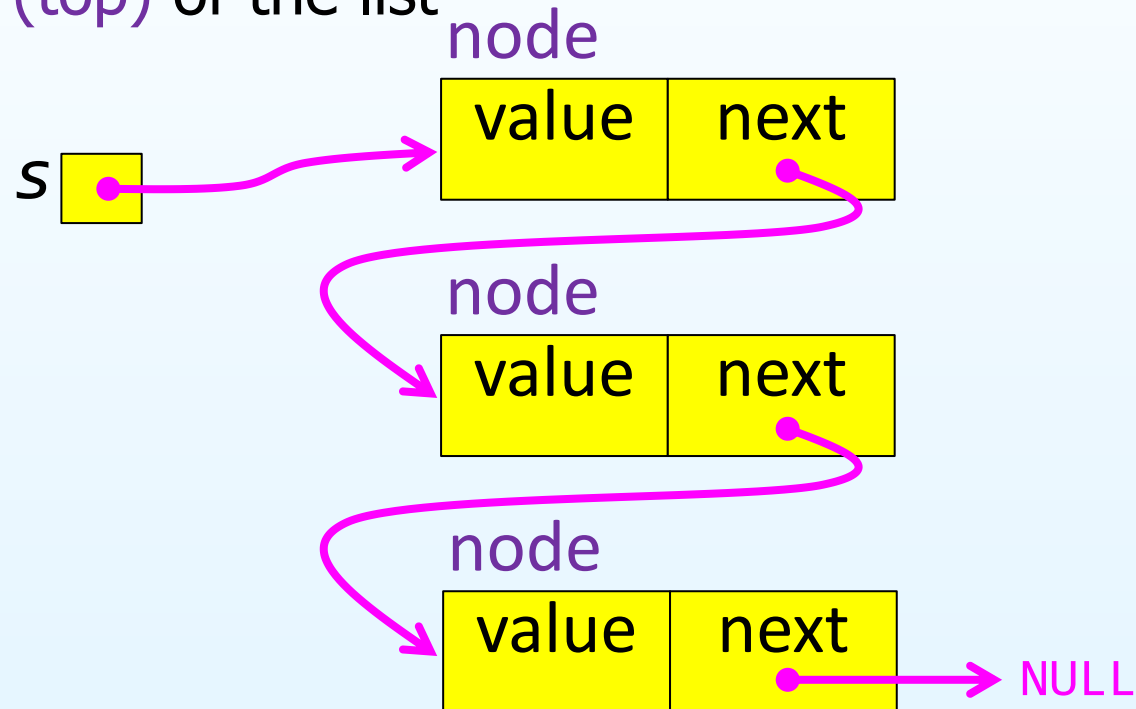
Limitation of Array-based Stack

- If the stack is **full**, **reallocate** a huge new array and **move** everything over

Stack: Pointer Implementation

Basic idea:

- Allocate **nodes** for elements, and link them as a list
- Form a stack by manipulating push and pop operations at the **head (top)** of the list

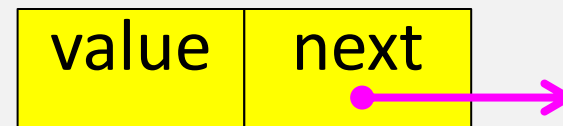


List-based Stack: Construction

Assume that all data are positive integer

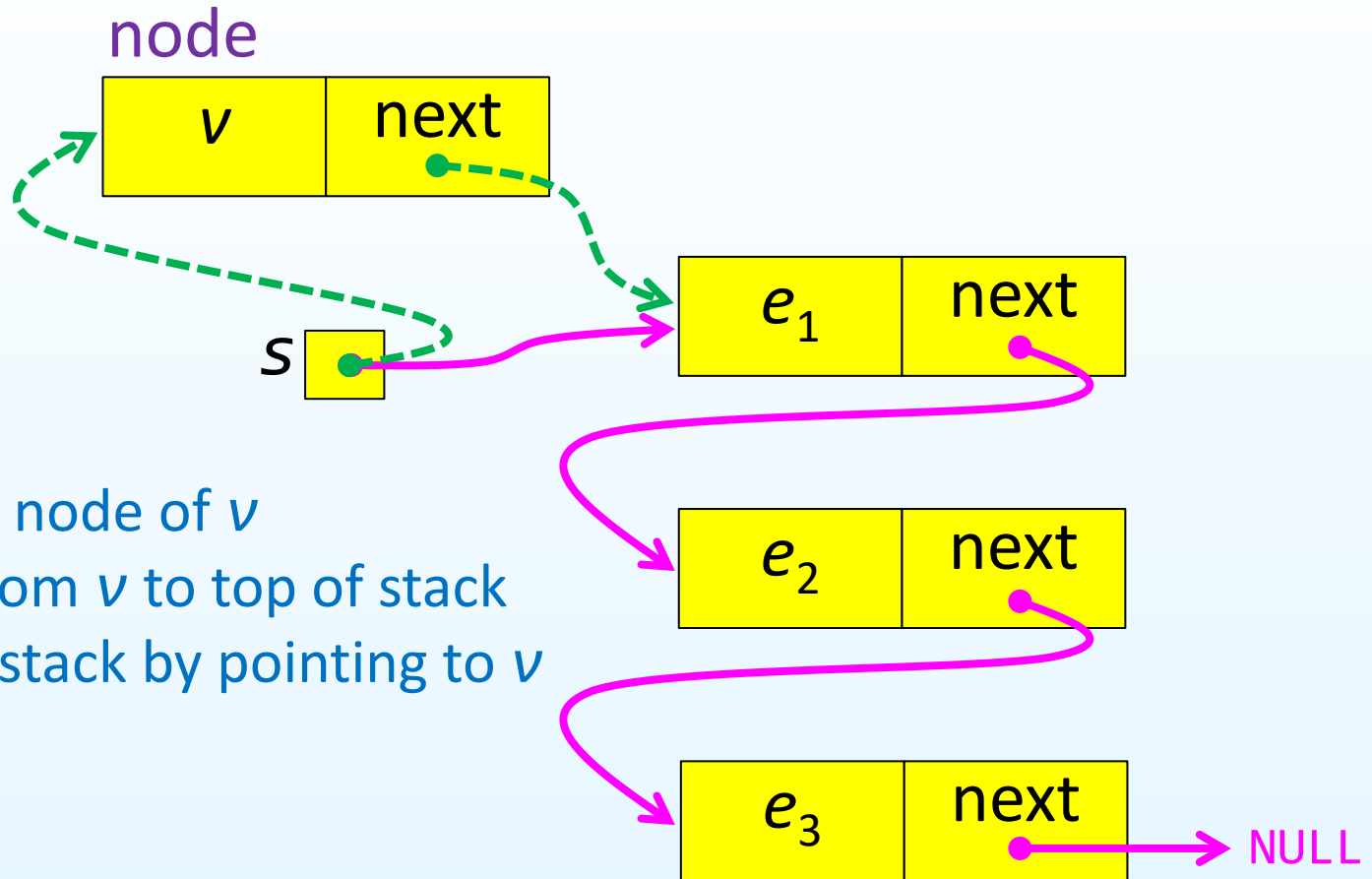
```
1: #include <stdio.h>
2: #include <stdlib.h>
3:
4: typedef struct node {
5:     int value;
6:     struct node *next;
7: } node_t;
8:
9: typedef node_t stack_t;
10:
11: int main(void) {
12:     stack_t *s = NULL;
13:     return 0;
14: }
```

node



List-based Stack: push() Operation

Push a value v at the top of stack s

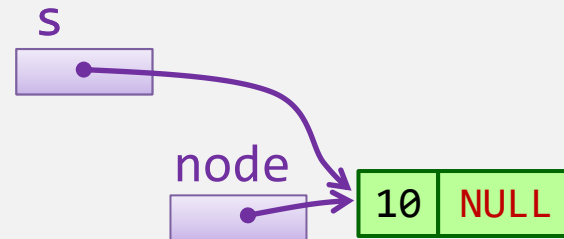


1. Allocate a new node of v
2. Create a link from v to top of stack
3. Change top of stack by pointing to v

List-based Stack: push() Operation

Push a value v at the top of stack s

```
1: void push(stack_t *s, int v) {  
2:   node_t *node = (node_t *)malloc(sizeof (node_t));  
3:   node->value = v;  
4:   node->next = NULL;  
5:  
6:   node->next = s;  
7:   s = node;  
8: }
```



```
int main(void) {  
  stack_t *s = NULL;  
  push(s, 10);  
  return 0;  
}
```

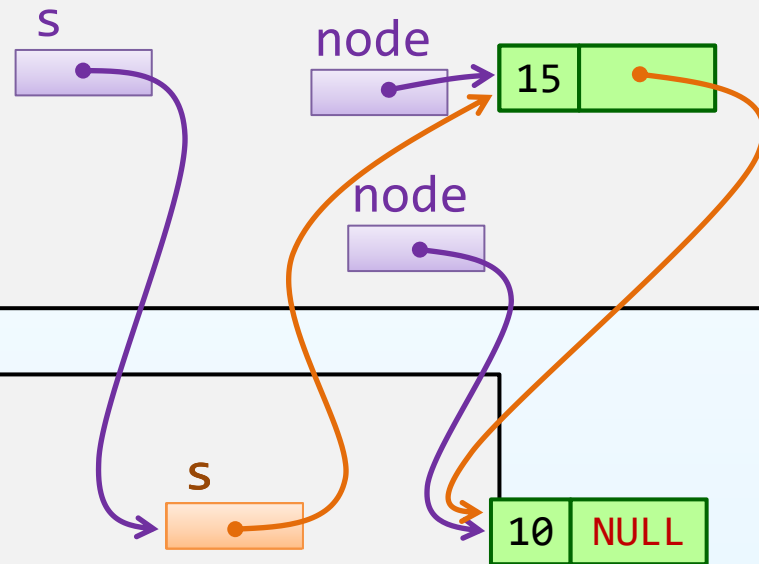


List-based Stack: push() Operation

Push a value v at the top of stack s

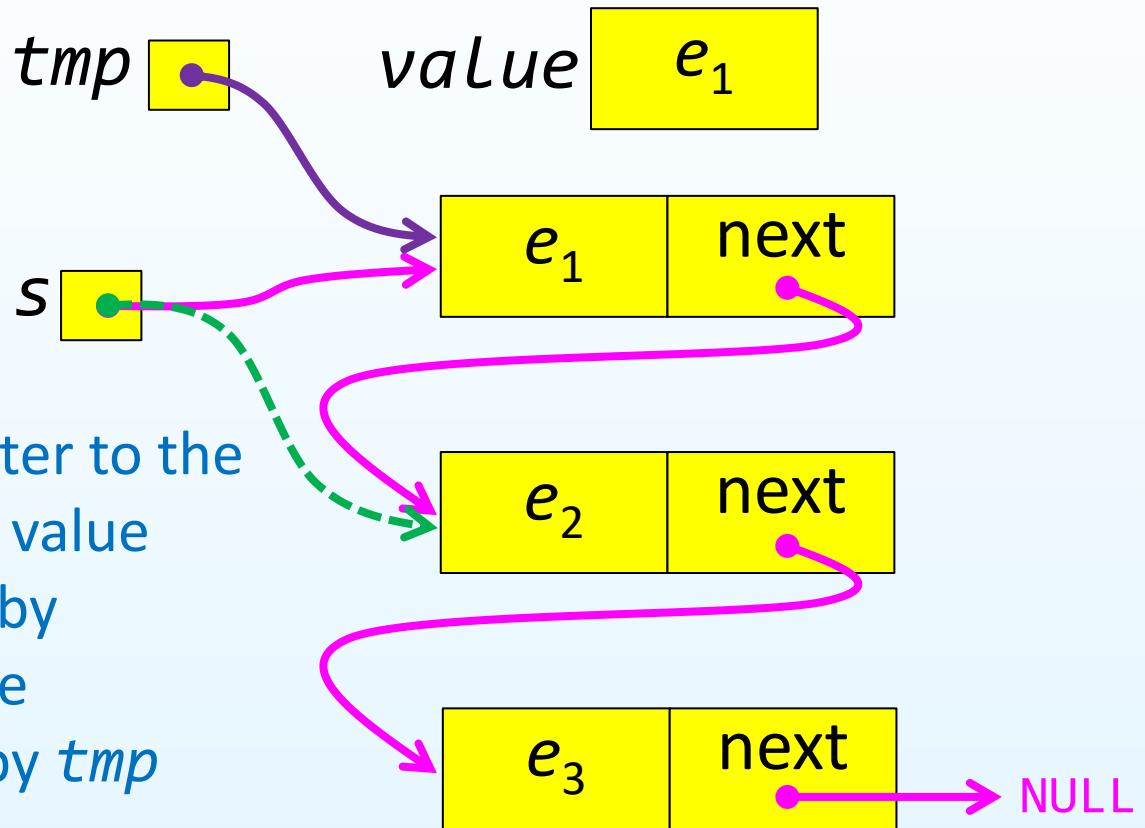
```
1: void push(stack_t **s, int v) {  
2:   node_t *node = (node_t *)malloc(sizeof (node_t));  
3:   node->value = v;  
4:   node->next = NULL;  
5:  
6:   node->next = *s;  
7:   *s = node;  
8: }
```

```
int main(void) {  
  stack_t *s = NULL;  
  push(&s, 10);  
  push(&s, 15);  
  return 0;  
}
```



List-based Stack: pop() Operation

Remove the top of stack s and then return that value



1. Assign a temporary pointer to the top of stack, and get the value
2. Change the top of stack by pointing to the next node
3. Free the node pointing by tmp

Exercise 2: Other Operations

Implement the following functions for a **list-based stack**

- `pop()` – remove the top element of stack s
 - Return v if the stack is not empty, otherwise -1
- `top()` – peek the top element of stack s
 - Return v if the stack is not empty, otherwise -1
- `is_empty()` – check whether stack s is empty
 - return 1 if the stack is empty, otherwise 0



List-based Stack: Running Time

Operation	Running Time
push()	$O(1)$
pop()	$O(1)$
top()	$O(1)$
is_empty()	$O(1)$
make_empty()	$O(n)$



Limitation of List-based Stack

- Potentially **a lot of calls** to `malloc()` and `free()` if the stack is actively used
 - In practice, memory allocation and release require **expensive** trips through the operating system

How can you solve this problem?

Application: Balancing Symbols

Are the followings correct?

- Arithmetic expression

$$(1+5*(17-2)/(6*3))$$

- Python syntax

```
print(''He said, "I 'do not' care."''')
```

- HTML code

```
<html>  
<head><title>hello</title></head>  
<body>test</body>  
</html>
```

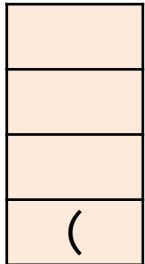
Application: Balancing Symbols

$(1+5*(17-2)/(6*3))$

1. Create an empty stack
2. If encounter ' (', push onto stack
3. If encounter ') ',
 - 3.1 If stack is empty, report error
 - 3.2 Else, pop the stack
 - 3.3 If the popped value is not ' (', report error
4. If EOF and stack is not empty, report error

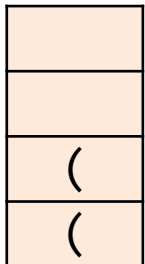
Application: Balancing Symbols

1



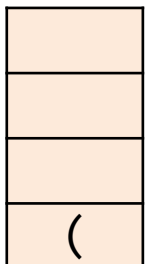
↓
(1+5*(17-2)/(6*3))
push(' (');

2



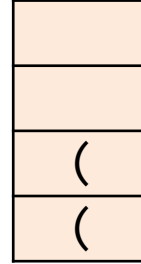
↓
(1+5*(17-2)/(6*3))
push(' (');

3



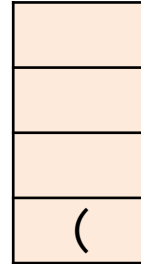
↓
(1+5*(17-2)/(6*3))
sym = pop();
→ Match

4



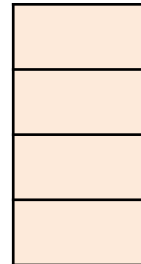
↓
(1+5*(17-2)/(6*3))
push(' (');

5



↓
(1+5*(17-2)/(6*3))
sym = pop();
→ Match

6



↓
(1+5*(17-2)/(6*3))
sym = pop();
→ Match



Application: Arithmetic Expression

What is the result of following expressions?

- Infix notation

$$10 + 6 * 5 / 2 - 4$$

- Postfix notation

$$10 \ 6 \ 5 \ * \ 2 \ / \ + \ 4 \ -$$

- Prefix notation

$$+ \ 10 \ - \ * \ 6 \ / \ 5 \ 2 \ 4$$

Application: Infix to Postfix Conversion

10 + 6 * 5 / 2 - 4

Algorithm

```
1: s ← create_stack()
2: while (data ← input() and data != EOF)
3:     if (data is an operand)
4:         print(data)
5:     if (data is an operator)
6:         while (!is_empty(s))
7:             op ← top(s)
8:             if (op has higher precedence than or equal to data)
9:                 op ← pop(s)
10:                print(op)
11:            else
12:                break
13:        push(s, data)
14:
15: while (!is_empty(s))
16:     op ← pop(s)
17:     print(op)
```



Application: Infix to Postfix Conversion

10 + 6 * 5 / 2 - 4

Input	Stack	Output
10 + 6 * 5 / 2 - 4		10
10 + 6 * 5 / 2 - 4	+	10
10 + 6 * 5 / 2 - 4	+	10 6
10 + 6 * 5 / 2 - 4	+	10 6
10 + 6 * 5 / 2 - 4	+	10 6 5
10 + 6 * 5 / 2 - 4	+	10 6 5 *
10 + 6 * 5 / 2 - 4	+	10 6 5 * 2
10 + 6 * 5 / 2 - 4	+	10 6 5 * 2 /
10 + 6 * 5 / 2 - 4	+	10 6 5 * 2 / +
10 + 6 * 5 / 2 - 4	+	10 6 5 * 2 / + 4
10 + 6 * 5 / 2 - 4	-	10 6 5 * 2 / + 4 -

Other Applications of Stack

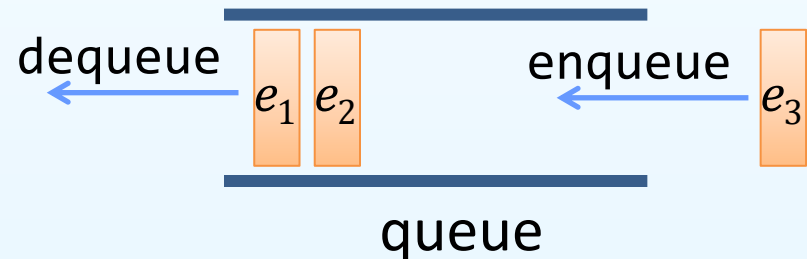
- Backtracking
 - A recursive algorithm which is used for solving the optimization problem
- Function calls
 - Whenever you invoke a function, the address of the calling function gets stored in the stack. This helps in going back when the called function is terminated
- Memory management
 - The stack segment of memory
- Depth-first search

Queue ADT



What is a Queue ADT?

- Data:
 - Elements stored in a list linearly, but are allowed insertion at **one end** and deletion at **the other end**
 - This mechanism is called **FIFO** – First in, First out
- Common operations:
 - `enqueue(queue, value)`
 - `dequeue(queue)`
 - `is_empty(queue)`
 - `is_full(queue)`
 - ...



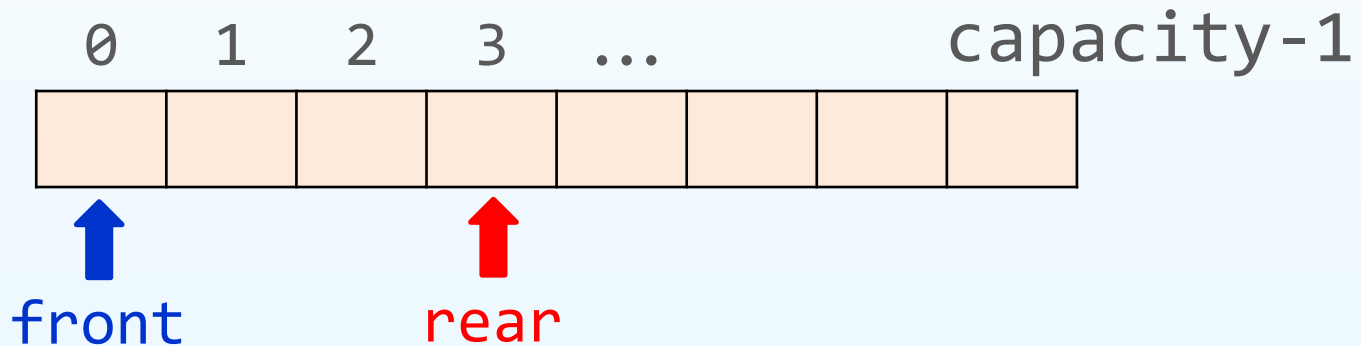
Queue Implementations

- Two types of implementation
 - Array-based queue
 - Pointer-based queue

Queue: Array Implementation

Basic idea:

- **Allocate** a big array (of size capacity)
- **Keep track** two ends (using variables front and rear)

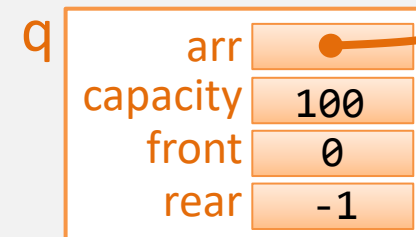
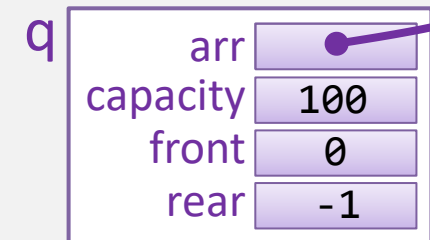
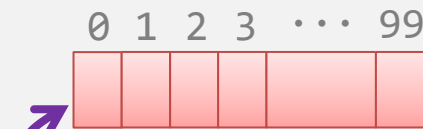


How should we initialize both variables?

Queue: Array-based Construction

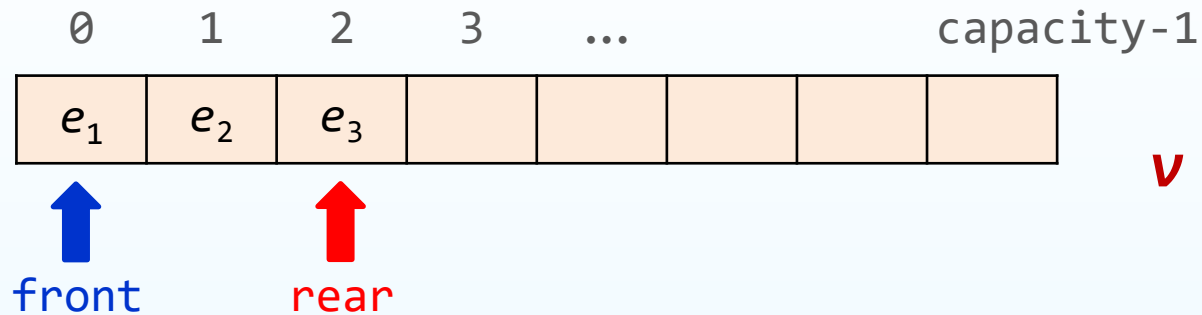
Assume that all data are positive integer

```
1: #include <stdio.h>
2: #include <stdlib.h>
3:
4: typedef struct queue {
5:     int *arr;        // array-based queue
6:     int capacity;    // size of queue
7:     int front;       // position of front
8:     int rear;        // position of rear
9: } queue_t;
10:
11: queue_t create(int size) {
12:     queue_t q = {NULL, size, 0, -1};
13:     q.arr = (int *)malloc(sizeof (int) * size);
14:     return q;
15: }
16: int main(void) {
17:     queue_t q = create(100);
18:     return 0;
19: }
```



Array-based Queue: enqueue() Operation

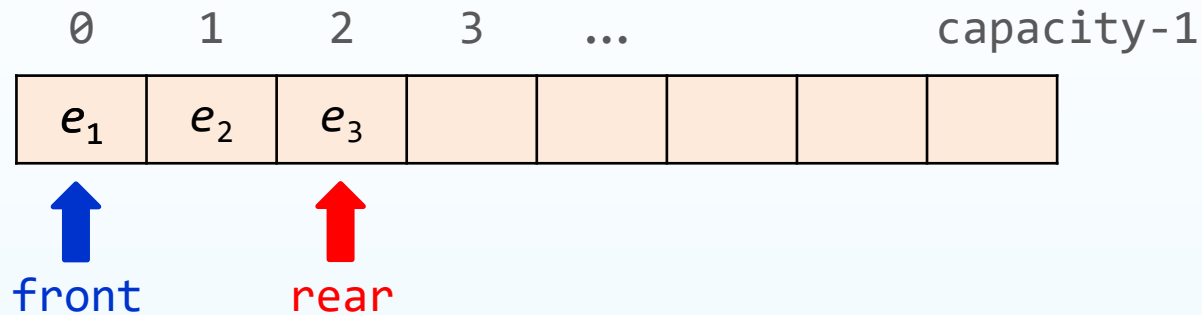
Insert a value v into queue q



```
1: int enqueue(queue_t *q, int v) {
2:     if (q->rear == q->capacity-1) // queue is full
3:         return 0;
4:
5:     q->rear++; // enqueue normally
6:     q->arr[q->rear] = v;
7:     return 1;
8: }
```

Array-based Queue: dequeue() Operation

Remove a value from queue q and return it



```
1: int dequeue(queue_t *q) {  
2:     int v;  
3:  
4:     if (q->front > q->rear)           // queue is empty  
5:         return 0;  
6:  
7:     v = q->arr[q->front];             // dequeue normally  
8:     q->front++;  
9:     return v;  
10: }
```

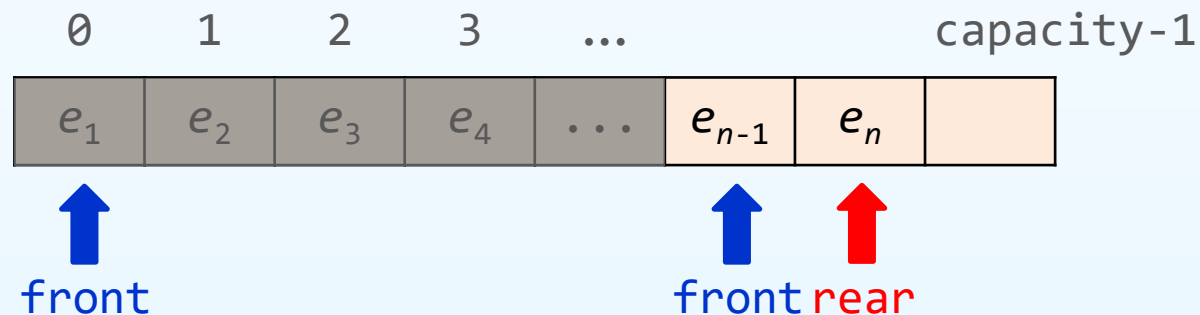
Array-based Queue: Running Time

Operation	Running Time
create()	$O(1)$
enqueue()	$O(1)$
dequeue()	$O(1)$
is_empty()	$O(1)$
make_empty()	$O(1)$
is_full()	$O(1)$
destroy()	$O(1)$



Limitation of Array-based queue

- If the queue is **full**, **reallocate** a huge new array and **move** everything over
- A simple implementation of `dequeue()` can lead to a lot of unused spaces

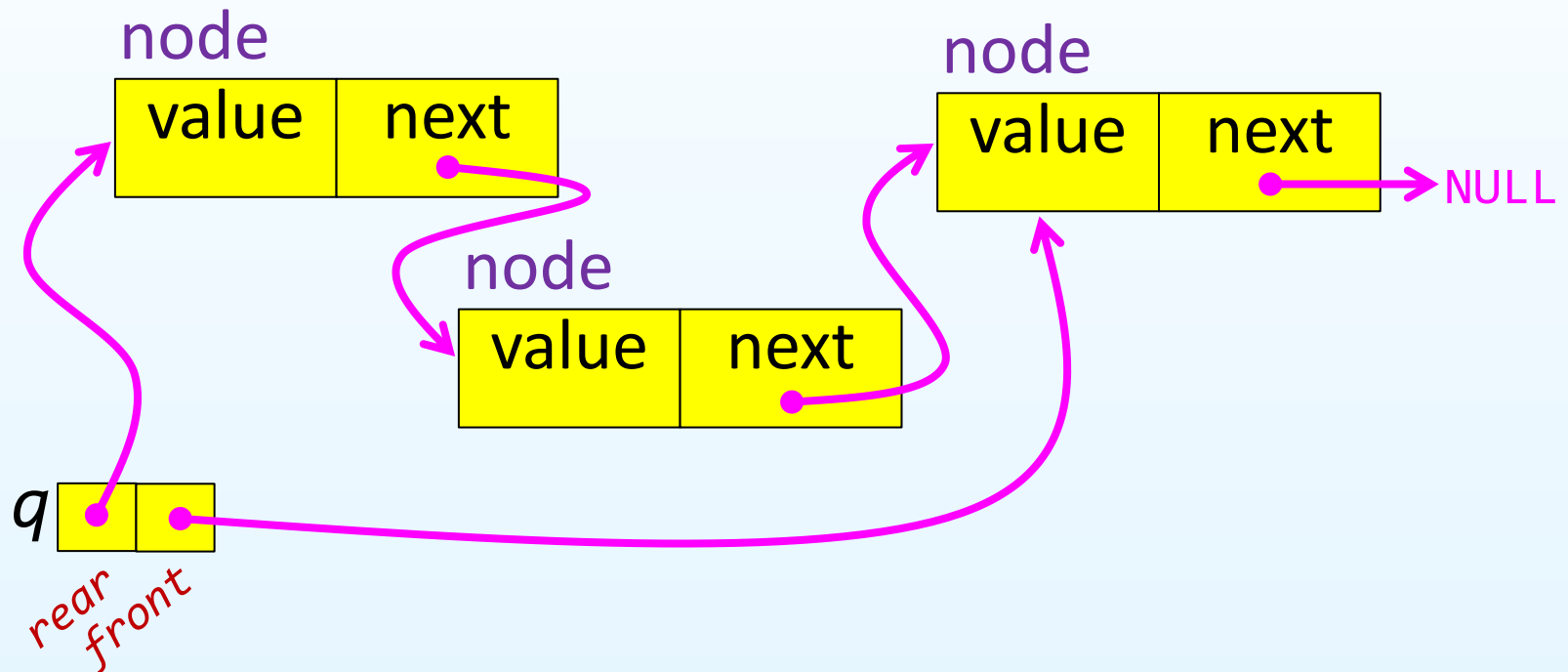


How can you solve this problem?

Queue: Pointer Implementation

Basic idea:

- Allocate **nodes** for elements, and link them as a list
- Form a queue with front and rear pointers

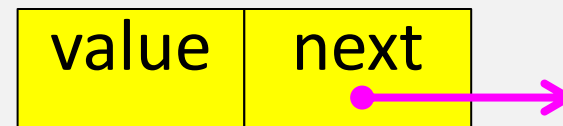


List-based Stack: Construction

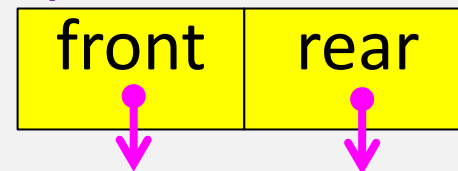
Assume that all data are positive integer

```
1: #include <stdio.h>
2: #include <stdlib.h>
3:
4: typedef struct node {
5:     int value;
6:     struct node *next;
7: } node_t;
8:
9: typedef struct queue {
10:     node_t *front;
11:     node_t *rear;
12: } queue_t;
13:
14: int main(void) {
15:     queue_t q = {NULL, NULL};
16:     return 0;
17: }
```

node



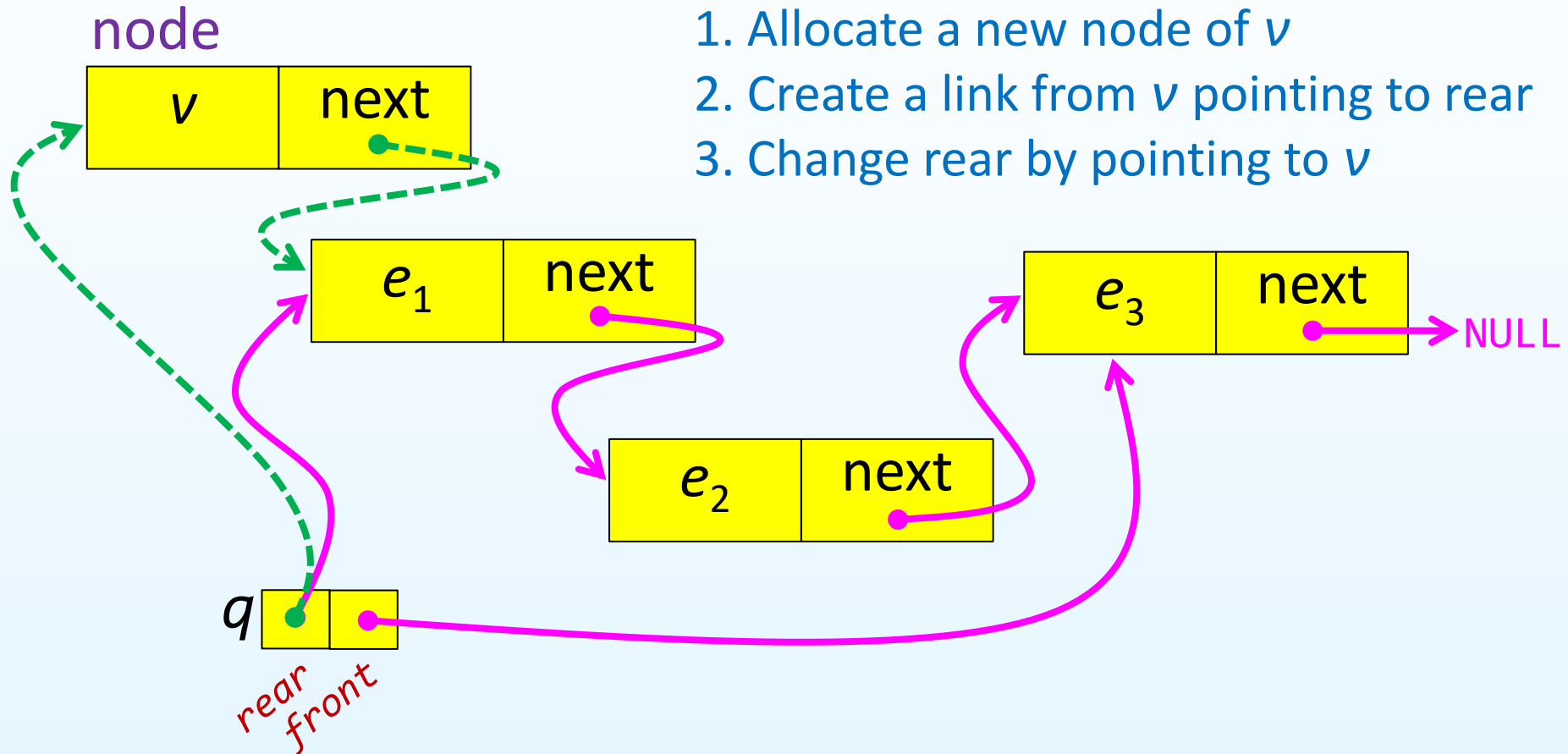
queue



List-based Queue: enqueue() Operation

Insert a value v into queue q

1. Allocate a new node of v
2. Create a link from v pointing to rear
3. Change rear by pointing to v



List-based Queue: enqueue() Operation

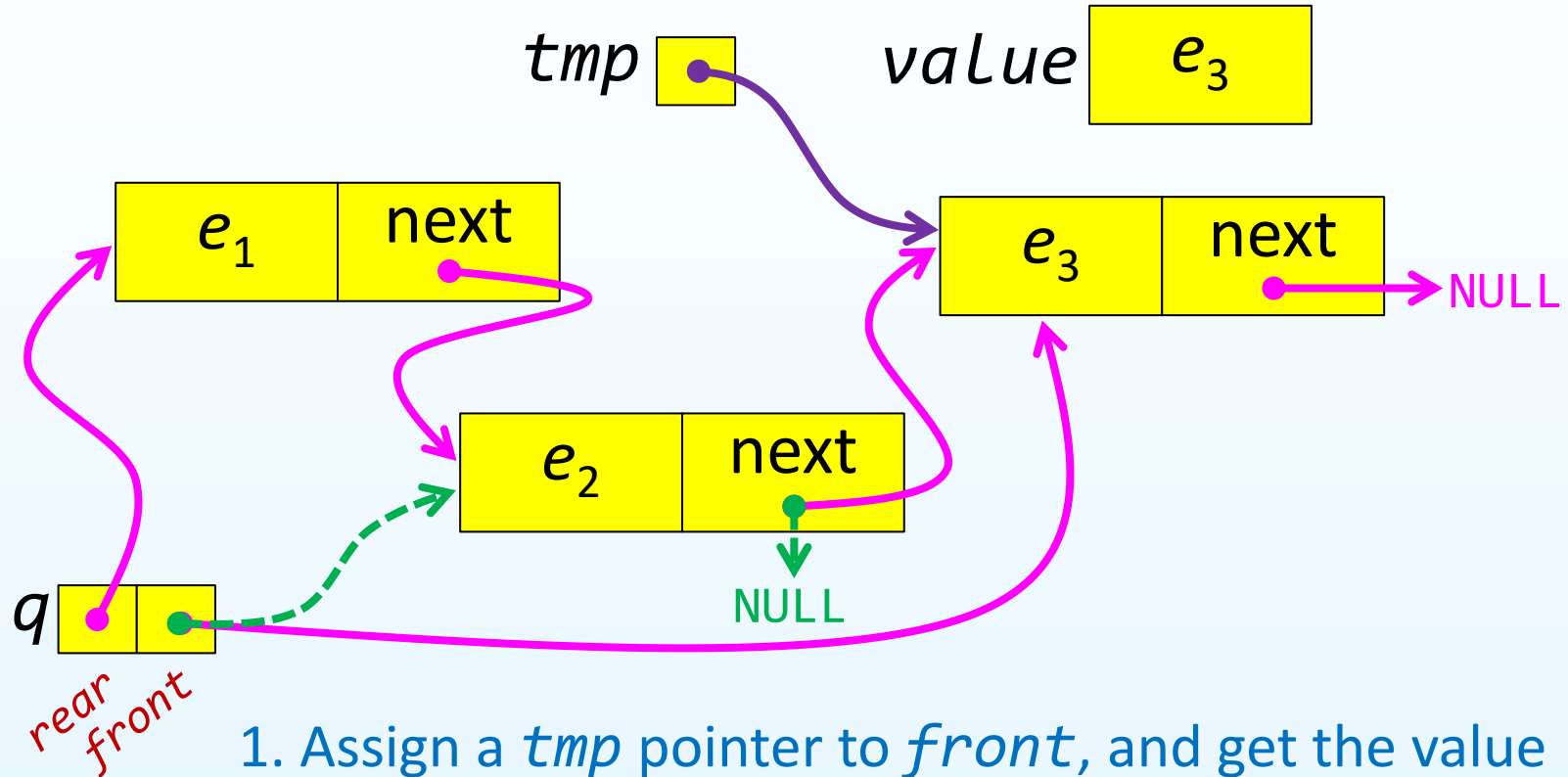
Insert a value v into queue q

```
1: void enqueue(queue_t *q, int v) {  
2:     node_t *node = (node_t *)malloc(sizeof (node_t));  
3:     node->value = v;  
4:     node->next = NULL;  
5:  
6:     node->next = q->rear;  
7:     q->rear = node;  
8:  
9:     if (q->front == NULL)  
10:         q->front = node;  
11: }
```

1. Allocate a new node of v
2. Create a link from v pointing to rear
3. Change rear by pointing to v

List-based Queue: dequeue() Operation

Remove a value from queue q and return it



1. Assign a tmp pointer to $front$, and get the value
2. Change $front$ pointing to the 2nd last node of list
3. Change next of 2nd last node pointing to NULL
4. Free the node pointing by tmp

List-based Queue: dequeue() Operation

Remove a value from queue q and return it

```
1: int dequeue(queue_t *q) {
2:     node_t *tmp = NULL;
3:     int value = 0;
4:
5:     if (q->front == NULL)           // queue is empty
6:         return -1;
7:
8:     tmp = q->front;
9:     value = q->front->value;
10:
11:    if (q->front == q->rear) {        // queue has only one node
12:        q->front = NULL;
13:        q->rear = NULL;
14:    } else {
15:        q->front = q->rear;           // find 2nd last node
16:        while (q->front->next != tmp)
17:            q->front = q->front->next;
18:        q->front->next = NULL;        // set 2nd last node pointing to NULL
19:    }
20:    free(tmp);
21:    return value;
22: }
```

List-based Queue: Running Time

Operation	Running Time
enqueue()	$O(1)$
dequeue()	$O(n)$
is_empty()	$O(1)$
make_empty()	$O(n)$



Limitation of List-based Queue

- Potentially **a lot of calls** to `malloc()` and `free()` if the queue is actively used
 - In practice, memory allocation and release require **expensive** trips through the operating system

How can you solve this problem?

Applications of Queue

- Printer queue
- Web server queue
- Call Center phone system
- Breadth-first search

Any Question?

