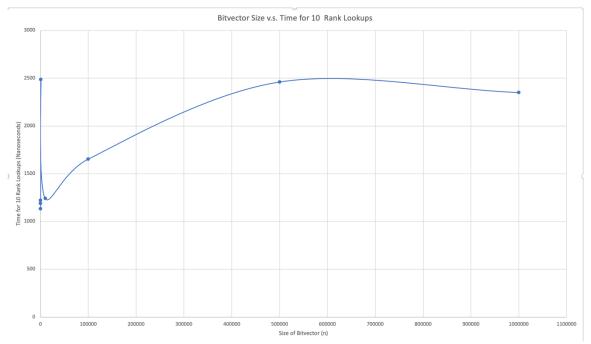
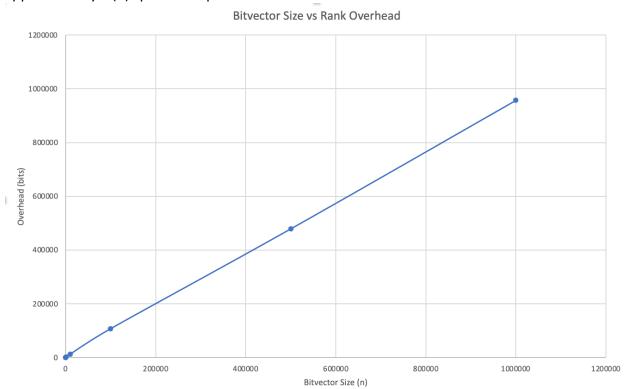
# Link to Public Github Repo: https://github.com/stang10/CMSC701\_HW2 Task 1:

- 1) My task, one implementation is based on Jacobson's rank. When a rank support object is initialized, it takes in a bitvector pointer, which it stores as a local variable. At this point a number of calculations are done. First, the size of the bitvector is calculated. Then, in order to create an int vector object to store the relative cumulative rank of the chunks of a bitvector, calculations are done. Such calculations include the bits needed to represent a number for the value of the relative cumulative rank of each chunk, the length of a chunk, and the number of chunks needed for the expression of this bitvector. Similarly, calculations are done as well to create an int vector object to store the relative cumulative rank of the subchunks of a bitvector. We need the bits needed to express the value of the relative cumulative rank of each subchunk, the number of subchunks per chunk, and the length of those subchunks. An int vector is created for the chunks representation with size and bit length as calculated above, and similarly for an int vector for subchunks. These values are created and stored as local variables. The rank function takes advantage of these vectors, and uses the value stored within each appropriate chunk and subchunk along with population count performed on and the get int() function for the SDSL int vectors to determine the rank. Overhead uses the SDSL size in bytes() function for the chunks and subchunks int vectors, adds the two values, multiplies the values by 8 to get bits and returns it. Save prints the number of bits used by a vector, the size of that vector, and then each element of the vector on all separated by new lines for the bitvector, then the chunks vector, followed by the subchunks vector. The load function reads each of these values in and creates new int vector objects to account for these values for the chunks and subchunks local variables.
- 2) For task one, the most difficult implementation was the rank1() function. This was due to the fact I had to determine the correct calculations for each chunk and sub chunk that an index would fall into. This also required that I did the correct building of the chunk and subchunk int\_vector objects in the initialization of the rank support structure to make sure that I would get approximately O(1) time for determining the rank. Besides this, before I had switched to using the SDSL library from compact::vector objects, the load and save functions were particularly difficult, mostly because compact::vector objects did not allow for resizing a bit length.
- 3) The image below is a graph of the size of a bitvector versus the time needed to complete 10 rank1() function calls. Though there is some variation across sizes, it appears to me that the run time does not rely heavily on the size of the bitvector as bitvectors of exponentially larger sizes only appear to have runtimes very close to those of much smaller bitvectors. I would say, accounting to variations in my system, that there is an approximate O(1) runtime as we would expect.

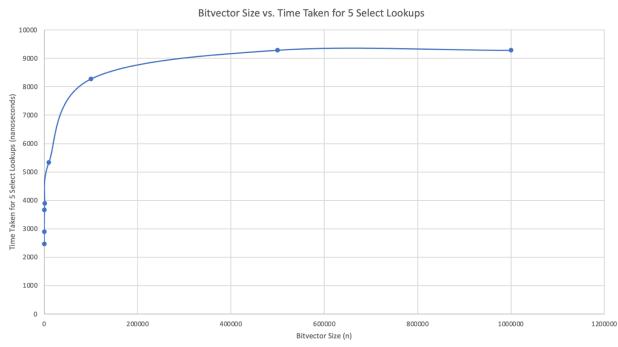


The image below is a graph of the size of a bitvector versus the overhead bits necessary to create a rank\_support structure for the bitvector. As you can see, there very clearly appears to be a linear relationship between these two variables. As such, we see this is approximately O(n) space as expected.

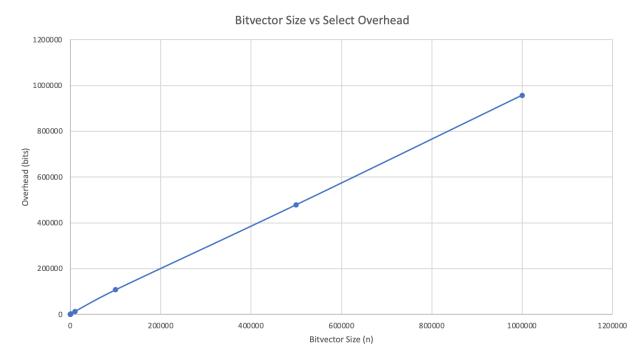


#### Task 2:

- 1) My task 2 implementation is heavily based upon the task 1 implementation. When a select support object is initialized, it takes in a pointer to a rank support object which contains the bitvector pointer, the chunks int\_vector, and subchunks int\_vector that were created previously. Upon initialization just the local variable for the rank support object pointer is set to the parameter passed in. The select1() function takes advantage of binary search, and the rank function. The binary search functionality is specialized so that it will continue to search for further left indices after an index is found that contains the correct rank being searched for. This leftmost value is then returned. The overhead function, since I chose not to implement Clark's select, simply returns the result of calling overhead on the rank support object pointed to by the local variable stored. Save and load simply call the save and load functions on the rank support object pointed to by the local variable stored.
- 2) For task two, the most difficult implementation was the select1() function. This difficulty lied within the binary search portion. For this part of the select function, I had to determine the leftmost index that carried the correct rank value. As such this required additional thought, unlike the other functions that I could make use of the previous definitions in the rank support class. Again, I still had some difficulties initially when using compact::vector for load and save as explained above. After switching to SDSL those became much easier to handle.
- 3) The image below is a graph of the size of a bitvector versus the time needed to complete 5 select1() function calls. As you can see, there very clearly appears to be a logarithmic relationship between these two variables. As such, we see this runs in approximately O(log(n)) time as expected of the non-Clark select implementation.



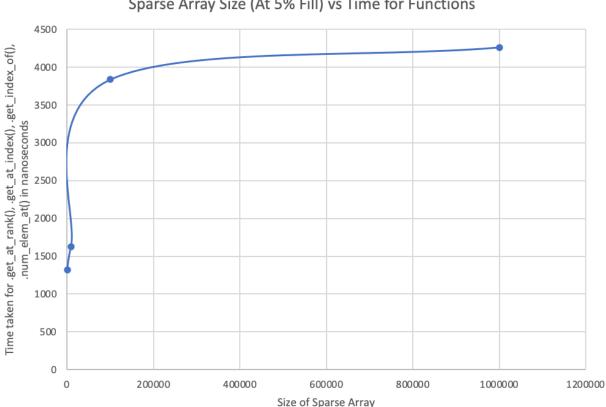
The image below is a graph of the size of a bitvector versus the overhead bits necessary to create a select\_support structure for the bitvector which is simply the overhead bits necessary to create a rank\_support structure for the bitvector. As you can see, there very clearly appears to be a linear relationship between these two variables. As such, we see this is approximately O(n) space as expected.



#### Task 3:

1) Within the sparse array class, there are a few local variables needed. There is a bitvector and a standard vector of strings created to hold the indices of the non-empty values for the sparse array and the values themselves, respectively. Additionally, a rank support and a select support structure are needed as well. There is also a Boolean value to mark whether a sparse array is finalized or not. Initialization of an object in this class establishes a dummy bitvector to be replaced later from the create() function. The rank support and select support structures are initialized using this dummy bitvector, again with the intention to be changed later. Also, the finalized variable is set to false. The create() function reinitializes the local bitvector variable to a bitvector object of the specified size. The append() function adds the specified string to the end of the strings vector and sets the specified index in the bitvector to 1. Each of get\_at\_rank(), get at index(), get index of(), and num elem at() leverage the results of the rank1() and select1() functions along with simple calculations to return the desired results. The size() function returns the size of the bitvector and the num elem() function returns the size of the strings vector. The save and load functions simply run the select support save and load functions (which run those of the rank support class as specified above) with the addition of the value of the finalized Boolean value printed on a newline at the end of the file and read in at the end of the load function.

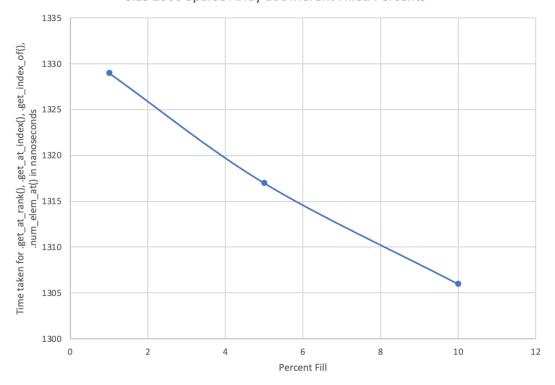
- 2) For task three, the implementations in my opinion were much easier to handle due to the completeness of tasks one and two. I did not struggle too much beyond dealing with the issue of inclusive versus exclusive rank values. Overall, there was not one particular function that I struggled with, more so, I needed extra effort to determine which rank I should be using, which index I should be using, etc. Again, due to the fact that the descriptions for the functions were written using inclusive rank and our tasks one and two were done with exclusive rank.
- 3) The image below is a graph of the size of a sparse array (that is 5% filled) versus the time needed to complete one call to each of .get at rank(), .get at index(), .get index of(), and .num elem at(). There appears to be an approximately logarithmic relationship between the size of the sparse array and the time needed to complete these calls.



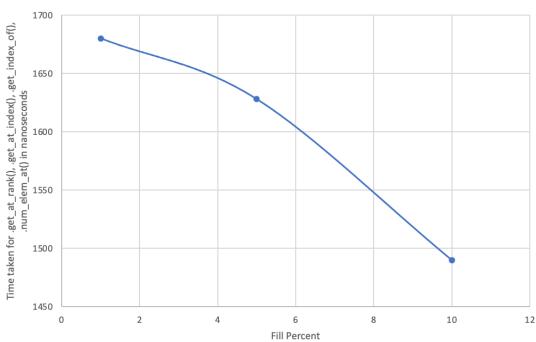
Sparse Array Size (At 5% Fill) vs Time for Functions

The next series of images shows the percent fill of a sparse array versus the time needed to complete one call to each of .get\_at\_rank(), .get\_at\_index(), .get\_index\_of(), and .num elem at() for various sizes of sparse arrays.

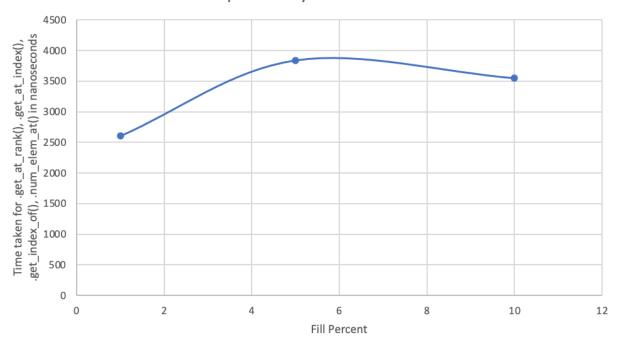
### Size 1000 Sparse Array at Different Filled Percents



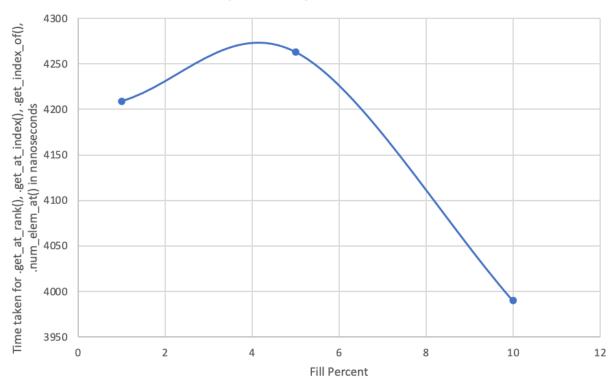
## Size 10000 Sparse Array At Different Fill Percents



### Size 100000 Sparse Array At Different Fill Percents



## Size 1000000 Sparse Array At Different Fill Percents



Though there appears to be some variation across the various sparse array sizes, there generally appears to be a decrease in time needed to carry out the function calls as the sparse array becomes more full.