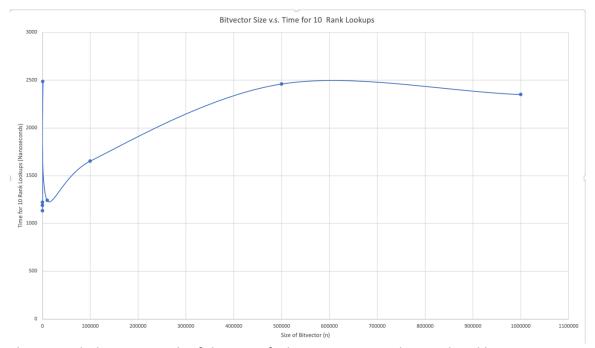
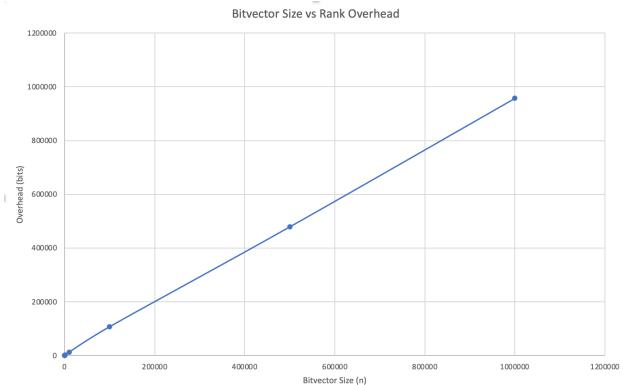
Task 1:

- 1) My task, one implementation is based on Jacobson's rank. When a rank support object is initialized, it takes in a bitvector pointer, which it stores as a local variable. At this point a number of calculations are done. First, the size of the bitvector is calculated. Then, in order to create an int vector object to store the relative cumulative rank of the chunks of a bitvector, calculations are done. Such calculations include the bits needed to represent a number for the value of the relative cumulative rank of each chunk, the length of a chunk, and the number of chunks needed for the expression of this bitvector. Similarly, calculations are done as well to create an int vector object to store the relative cumulative rank of the subchunks of a bitvector. We need the bits needed to express the value of the relative cumulative rank of each subchunk, the number of subchunks per chunk, and the length of those subchunks. An int vector is created for the chunks representation with size and bit length as calculated above, and similarly for an int vector for subchunks. These values are created and stored as local variables. The rank function takes advantage of these vectors, and uses the value stored within each appropriate chunk and subchunk along with population count performed on and the get int() function for the SDSL int vectors to determine the rank. Overhead uses the SDSL size in bytes() function for the chunks and subchunks int vectors, adds the two values, multiplies the values by 8 to get bits and returns it. Save prints the number of bits used by a vector, the size of that vector, and then each element of the vector on all separated by new lines for the bitvector, then the chunks vector, followed by the subchunks vector. The load function reads each of these values in and creates new int vector objects to account for these values for the chunks and subchunks local variables.
- 2) For task one, the most difficult implementation was the rank1() function. This was due to the fact I had to determine the correct calculations for each chunk and sub chunk that an index would fall into. This also required that I did the correct building of the chunk and subchunk int_vector objects in the initialization of the rank support structure to make sure that I would get approximately O(1) time for determining the rank. Besides this, before I had switched to using the SDSL library from compact::vector objects, the load and save functions were particularly difficult, mostly because compact::vector objects did not allow for resizing a bit length.
- 3) The image below is a graph of the size of a bitvector versus the time needed to complete 10 rank1() function calls. Though there is some variation across sizes, it appears to me that the run time does not rely heavily on the size of the bitvector as bitvectors of exponentially larger sizes only appear to have runtimes very close to those of much smaller bitvectors. I would say, accounting to variations in my system, that there is an approximate O(1) runtime as we would expect.

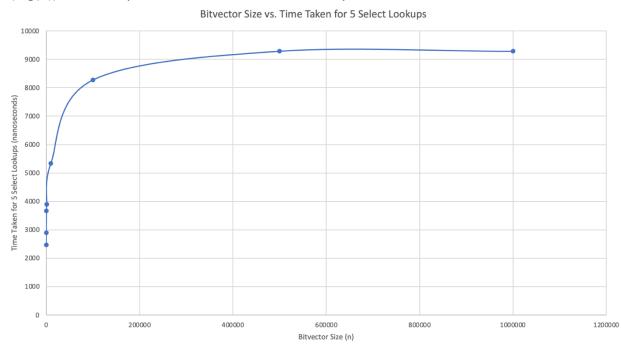


The image below is a graph of the size of a bitvector versus the overhead bits necessary to create a rank_support structure for the bitvector. As you can see, there very clearly appears to be a linear relationship between these two variables. As such, we see this is approximately O(n) space as expected.



Task 2:

- 1) My task 2 implementation is heavily based upon the task 1 implementation. When a select support object is initialized, it takes in a pointer to a rank support object which contains the bitvector pointer, the chunks int_vector, and subchunks int_vector that were created previously. Upon initialization just the local variable for the rank support object pointer is set to the parameter passed in. The select1() function takes advantage of binary search, and the rank function. The binary search functionality is specialized so that it will continue to search for further left indices after an index is found that contains the correct rank being searched for. This leftmost value is then returned. The overhead function, since I chose not to implement Clark's select, simply returns the result of calling overhead on the rank support object pointed to by the local variable stored. Save and load simply call the save and load functions on the rank support object pointed to by the local variable stored.
- 2) For task two, the most difficult implementation was the select1() function. This difficulty lied within the binary search portion. For this part of the select function, I had to determine the leftmost index that carried the correct rank value. As such this required additional thought, unlike the other functions that I could make use of the previous definitions in the rank support class. Again, I still had some difficulties initially when using compact::vector for load and save as explained above. After switching to SDSL those became much easier to handle.
- 3) The image below is a graph of the size of a bitvector versus the time needed to complete 5 select1() function calls. As you can see, there very clearly appears to be a logarithmic relationship between these two variables. As such, we see this runs in approximately O(log(n)) time as expected of the non-Clark select implementation.



The image below is a graph of the size of a bitvector versus the overhead bits necessary to create a select_support structure for the bitvector which is simply the overhead bits necessary to create a rank_support structure for the bitvector. As you can see, there very clearly appears to be a linear relationship between these two variables. As such, we see this is approximately O(n) space as expected.

