

Physical Problem Solving

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Question 1

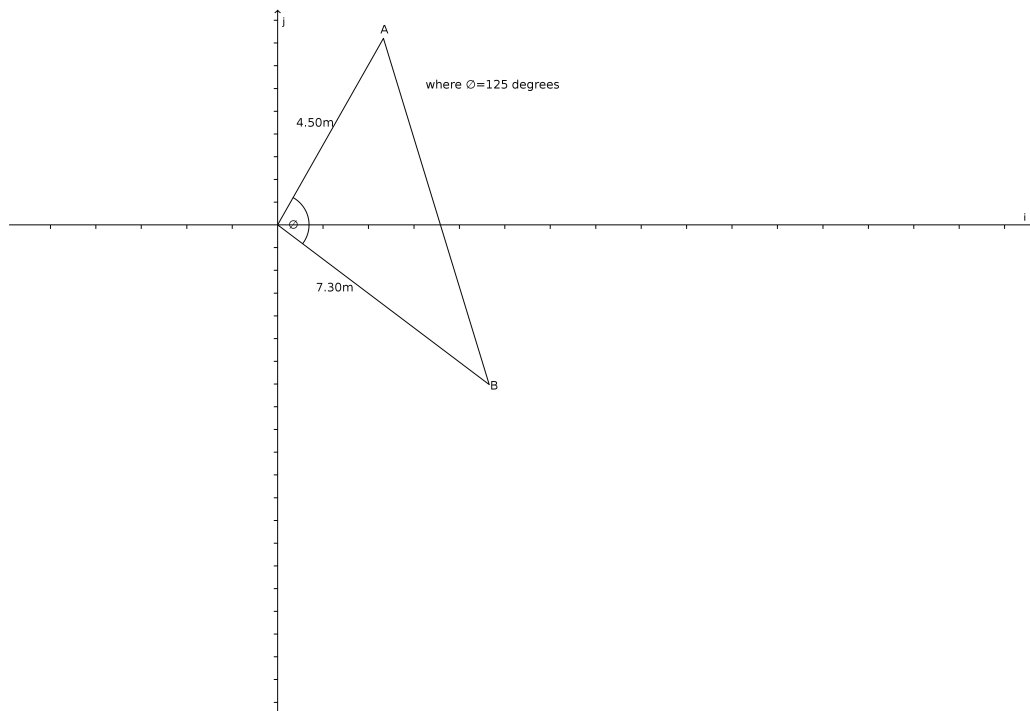


Figure 1: Vector Diagram

a $\vec{A} \cdot \vec{B}$

The scalar product of the vectors is obtained by multiplying the magnitude of the vectors by the cosine of their angle.

$$\vec{A} \cdot \vec{B} = |\vec{A}| |\vec{B}| \cos \theta$$

$$\vec{A} \cdot \vec{B} = 4.50 \times 7.30 \cos (125^\circ)$$

$$\therefore \vec{A} \cdot \vec{B} = -18.84$$

b $\vec{A} \times \vec{B}$

Observe that the two vectors \vec{A} and \vec{B} have both i and j components, so we have to resolve these vectors both horizontally and vertically, we can write the vectors component-wise as;

$$\vec{A} = |\vec{A}| \cos (40^\circ) \hat{i} - |\vec{A}| \sin (40^\circ) \hat{j}$$

$$\vec{B} = |\vec{B}| \cos (85^\circ) \hat{i} + |\vec{B}| \sin (85^\circ) \hat{j}$$

We can now find the cross product of these two vectors by computing their determinant.

$$\begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ |\vec{A}| \cos(40^\circ) & -|\vec{A}| \sin(40^\circ) & 0 \\ |\vec{B}| \cos(85^\circ) & |\vec{B}| \sin(85^\circ) & 0 \end{vmatrix} \quad (1)$$

$$\therefore \vec{A} \times \vec{B} = (|\vec{A}||\vec{B}| \sin(85^\circ) \cos(40^\circ) + |\vec{A}||\vec{B}| \cos(85^\circ) \sin(40^\circ)) \hat{k}$$

$$\vec{A} \times \vec{B} = |\vec{A}||\vec{B}| \sin(85^\circ + 40^\circ) \hat{k}$$

$$\vec{A} \times \vec{B} = 4.50 \times 7.30 \sin(125^\circ) \hat{k} = 26.90 \hat{k}$$

We therefore conclude that the cross product of vector A and B produces a vector with magnitude 26.90 in the \hat{k} -direction.

Question 2

From the pieces of information given in the question, we have that; The horizontal distance between the boy and the middle of the basket is D , D can also be referred to as the range of the projectile motion, the angle of inclination is 55° , substituting these values into our range equation for the projectile motion, we shall obtain the initial velocity of the ball.

$$Range = \frac{U^2 \sin 2\theta}{g}$$

where $\theta = 55^\circ$, Range = 4.20m and $g = 9.8 \text{ ms}^{-2}$

$$U = \left(\frac{9.8 \times 4.2}{\sin(110^\circ)} \right)^{\frac{1}{2}}$$

$$U = 6.618 \text{ ms}^{-1}$$

Question 3

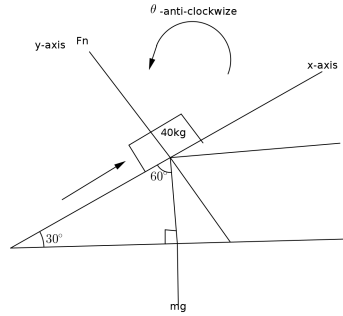


Figure 2: Force Diagram

Considering the force diagram of the box moving along an inclined plane as shown above, we can resolve the forces into their respective x and y components

| Force | x-components | y-components |
|-------------|----------------|----------------|
| \vec{F}_n | $F_n \cos 90$ | $F_n \sin 90$ |
| mg | $mg \cos(240)$ | $mg \sin(240)$ |
| \vec{F} | $F \cos(330)$ | $F \sin(330)$ |

Now let's resolve the forces to their respective components, starting with the x-component R_x .

$$R_x = F_n \cos 90 + mg \cos 240 + F \cos 330 = ma$$

Since the body is moving at a constant speed, acceleration $a = 0$, so that the right hand part of the equation turns to zero.

$$R_x = F_n \cos 90 + mg \cos 240 + F \cos 330 = 0$$

Where $m=40\text{kg}$ and $g=9.8\text{ms}^{-2}$

$$R_x = 0 - 196 + 0.866F = 0$$

$$F = \frac{-196}{-0.866} = 226.32\text{N}$$

Therefore the force required to sustain the motion is 226.32N.

Now let's consider the y-axis, we take a similar approach as we did for the x-axis.

$$R_y = F_n \sin 90 + mg \sin 240 + F \sin 330 = ma.$$

Acceleration = 0, $F = 226.32N$, $ma = 0$, $\sin 90 = 1$, $m = 40kg$, $g = 9.8ms^{-1}$.

$$Fn - 339.481 - (226.32)(-0.5) = 0$$

$$\therefore Fn = 451.641N$$

The force exerted on the ramp by the crate is $451.641N$.