

**Difference of cubes:**  $A^3 - B^3 = (A - B)(A^2 + AB + B^2)$

**Law of trigonometric limit**  $\lim_{x \rightarrow 0} \frac{x}{\sin(x)} = 1$  so  $\lim_{x \rightarrow 0} \frac{\tan(x)}{x} = 1$

**Limits.**

1. Try plugging indirectory, make sure limit exists from both sides.
2. Factor and simplify, try plugging value in again.
3. Multiply by the conjugate to rationalize if there is a denominator
4. Multiply by GCD of any complex fractions

**Product Rule:**  $h(x) = f(x)g(x)$  then  $h'(x) = f'(x)g(x) + f(x)g'(x)$

**Quotient Rule:**  $h(x) = \frac{f(x)}{g(x)}$  then  $h'(x) = \frac{f'(x)g(x) - f(x)g'(x)}{g(x)^2}$

**Chain Rule:**  $h(x) = f(g(x))$  then  $h' = f'(g(x))g'(x)$

**Trig Derivatives:**

- $f(x) = \sin(x)$  then  $f'(x) = \cos(x)$
- $f(x) = \cos(x)$  then  $f'(x) = -\sin(x)$
- $f(x) = \tan(x)$  then  $f'(x) = \sec^2(x)$
- $f(x) = \sec(x)$  then  $f'(x) = \sec(x)\tan(x)$
- $f(x) = \csc(x)$  then  $f'(x) = -\csc^2(x)$
- $f(x) = \cot(x)$  then  $f'(x) = -\csc(x)\cot(x)$

**General trig identities:**

- $\tan \theta = \frac{\sin \theta}{\cos \theta}$
- $\cot \theta = \frac{1}{\tan \theta} = \frac{\cos \theta}{\sin \theta}$
- $\sec \theta = \frac{1}{\cos \theta}$
- $\csc \theta = \frac{1}{\sin \theta}$
- $1 + \cot^2 x = \csc^2 x$
- $1 - \cos^2 a = \sin^2 a$
- $1 + \tan^2 x = \sec^2 x$
- $\sin(\theta + \phi) = \sin \theta \cos \phi + \cos \theta \sin \phi$
- $\cos(\theta + \phi) = \cos \theta \cos \phi - \sin \theta \sin \phi$

$\theta$		$\sin \theta$	$\cos \theta$	$\tan \theta$	$\csc \theta$	$\sec \theta$	$\cot \theta$
Rad	Deg						
0	0	0	1	0	Undef	1	Undef
$\pi/6$	30	$1/2$	$\sqrt{3}/2$	$\sqrt{3}/3$	2	$2\sqrt{3}/3$	$\sqrt{3}$
$\pi/4$	45	$\sqrt{2}/2$	$\sqrt{2}/2$	1	$\sqrt{2}$	$\sqrt{2}$	1
$\pi/3$	60	$\sqrt{3}/2$	$1/2$	$\sqrt{3}$	$2\sqrt{3}/3$	2	$\sqrt{3}/3$
$\pi/2$	90	1	0	Undef	1	Undef	0