NYCU Introduction to Machine Learning, Homework 4

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**Part. 1, Coding (50%)**:

**(50%) Support Vector Machine**

1. (10%) Show the accuracy score of the testing data using linear\_kernel. Your accuracy score should be higher than 0.8.



1. (20%) Tune the hyperparameters of the polynomial\_kernel. Show the accuracy score of the testing data using polynomial\_kernel and the hyperparameters you used.



1. (20%) Tune the hyperparameters of the rbf\_kernel. Show the accuracy score of the testing data using rbf\_kernel and the hyperparameters you used. 

**Part. 2, Questions (50%):**

1. (20%) Given a valid kernel 𝑘1(𝑥, 𝑥'), prove that the following proposed functions are or are not valid kernels. If one is not a valid kernel, give an example of 𝑘(𝑥, 𝑥') that the corresponding 𝐾 is not positive semidefinite and shows its eigenvalues.

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自動產生的描述

Ans: with the following rules

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1. (15%) One way to construct kernels is to build them from simpler ones. Given three possible “construction rules”: assuming K1(x, x’) and K2(x, x’) are kernels, then so are

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Use the construction rules to build a normalized cubic polynomial kernel:



You can assume that you already have a constant kernel K0 = 1 and a linear kernel K1(x, x’). Identify which rules you are employing at each step.

Ans:

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Then K(x, x’) is constructed.

1. (15%) A social media platform has posts with text and images spanning multiple topics like news, entertainment, tech, etc. They want to categorize posts into these topics using SVMs. Discuss two multi-class SVM formulations: `one-versus-one` and `One-versus-the-rest` for this task.
   1. The formulation of the method [how many classifiers are required.
   2. Key trade offs involved (such as complexity and robustness)
   3. If the platform has limited computing resources for the application in the inference phase and requires a faster method for the service, which method is better.

Ans:

* + - * 1. Let the number of categories equal to n, n\*(n-1)/2 classifiers are required when using one-versus-one method, and n-1 classifiers are required when using one-versus-the-rest method.
        2. The space & training time complexity of one-versus-one method is higher than the one-versus-the-rest method because the model is number of model is higher (when n is big enough), so it requires more time and space to train and store them. As for the performance, one-versus-one is generally higher. Considering an imbalanced dataset with class A, B, C having 98% of A, 1% of B and 1% of C. Since SVM will accept some data point misclassified during training (depend on C), when you are training B v.s. the rest, the C might also be included, causing B and C unable to correctly classified. However, when using one-versus-one, we will train a classifier of B and C, so there won’t be any problem classifying B and C when using one-versus-one in this case, and that is why I think one-versus-one generally perform better.
        3. One-versus-the-rest is better in this case. Since you have limited computation resource, you would better choose the one with the lower memory requirement, which is one-versus-the-rest. As for running time, if you use one-versus-one, you may run the n\*(n-1)/2 classifiers and do voting, which more time-consuming than running a maximum of n-1 classifiers when using one-versus-the-rest.