

Homework 3

Name_____

Problem 1 (10 Points): Given a relation with five attributes $R(A,B,C,D,E)$ and functional dependencies,

$AB \rightarrow C$, $BD \rightarrow E$, $C \rightarrow D$

which of the following does not functionally determine E.

- A. BCD
- B. BE
- C. ABC
- D. AC

Problem 2(25 Points): Consider a relation $R(A,B,C)$ with functional dependencies $A \rightarrow B$, $B \rightarrow C$. Suppose R already has a tuple $(1,1,2)$, can we insert new tuples $(1,1,3)$, $(0,3,3)$? Why?

$(1,1,3)$ can not be inserted because it's A is the same as the one already there and its B is all the same as the existing one.

$(0,3,3)$ can be inserted because is A is different then the existing one and also its B.

Problem 3 (30 points): Decompose the relation $R(A,B,C,D, E)$ using BCNF. R has the following functional dependencies:

$A \rightarrow B$, $C \rightarrow D$, $AC \rightarrow E$

$A \rightarrow B$ violates BCNF because A is not superkey

(a,b) and (a,c,d,e)

$C \rightarrow D$ violates BCNF because is not superkey

(c, d) and (a, c, e)

$AC \rightarrow E$ is good

Problem4 (35 Points): Consider a relation $R(A,B,C,D, E)$ with functional dependencies $BDE \rightarrow A$, $AC \rightarrow E$, $B \rightarrow C$, $DE \rightarrow A$. Does any of these FD violate BCNF? why?

Merged cover

$AC \rightarrow E$

$B \rightarrow c$

$DE \rightarrow A$

$AC \rightarrow E$ violates BCNF because AC is not superkey

(a, c, e) and (a, b, c, d)

$B \rightarrow C$ violates BCNF because B is not superkey

(b, c) and (a, b, d)

If we change R 's functional dependencies to $BCD \rightarrow E$, $BDE \rightarrow C$, $BE \rightarrow D$, $BE \rightarrow A$, does any of these FD violate BCNF? why?

Merged cover

$BCD \rightarrow E$

$BE \rightarrow CDA$

Already in BCNF form