



模式识别与机器学习 (12)

卷积神经网络-1

左旺孟

综合楼712

视觉感知与认知组

哈尔滨工业大学计算机学院

cswmzuo@gmail.com

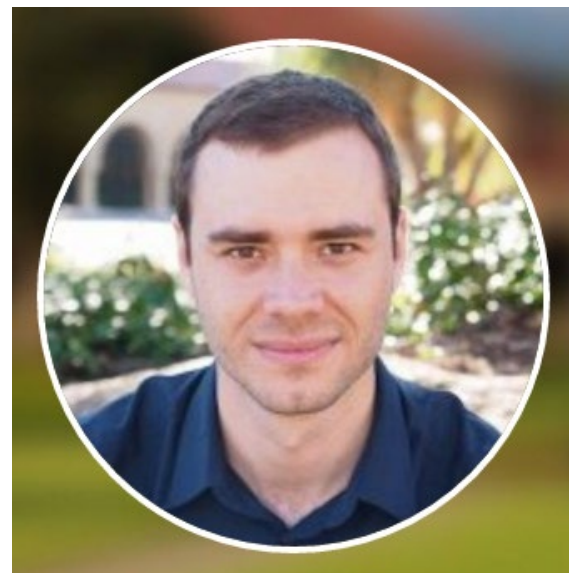
13134506692

卷积神经网络

- 历史和动机
- 基本操作
 - 卷积、池化、归一化、卷积神经网络
- 新进展
 - 3x3、Dilated Convolution
- 典型网络架构
 - LeNet、AlexNet、VGGNet、Inception
 - ResNet、SENet、DenseNet、Attention

Why Deep CNNs

“在使用RNN之前，一定要先尝试CNN。
你会惊讶于你能走多远”。——
Andrej Karpathy （特斯拉人工智能主管
-> OpenAI ）



Why Deep CNNs (vs RNN)

- Facebook: A novel convolutional neural network (CNN) approach for language translation that achieves state-of-the-art accuracy at nine times the speed of recurrent neural systems.
- <https://code.fb.com/ml-applications/a-novel-approach-to-neural-machine-translation/>

Jonas Gehring, Michael Auli, David Grangier, Denis Yarats, Yann N. Dauphin. Convolutional Sequence to Sequence Learning. ArXiv, 2017

Why Deep CNNs (vs Transformer)

- Large Kernel
- Layer Norm
- Nonlinear Activations
- Optimization: AdamW、LAMB
- ConvNeXts compete favorably with Transformers in terms of accuracy and scalability

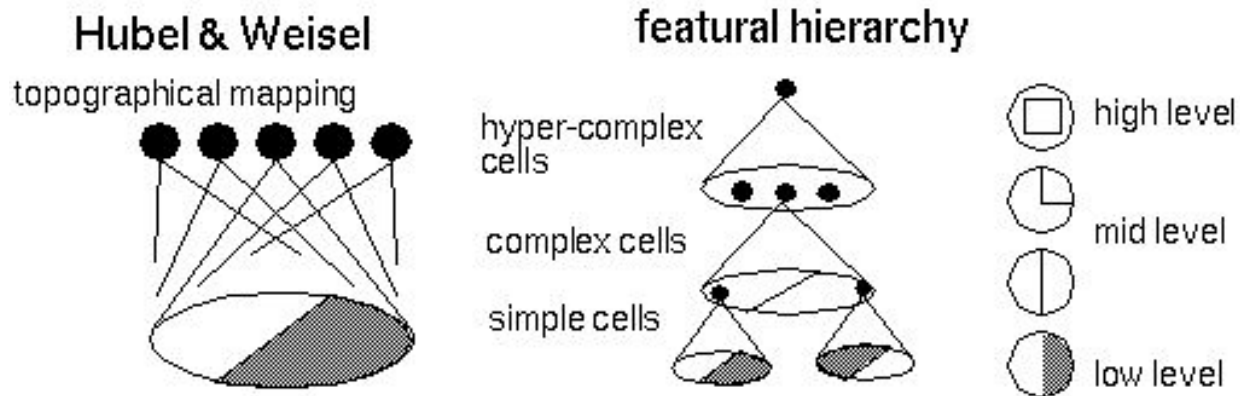
Simple Baselines for Image Restoration, Arxiv 2022

A ConvNet for the 2020s, Arxiv 2022

Scaling Up Your Kernels to 31x31: Revisiting Large Kernel Design in CNNs , Arxiv 2022

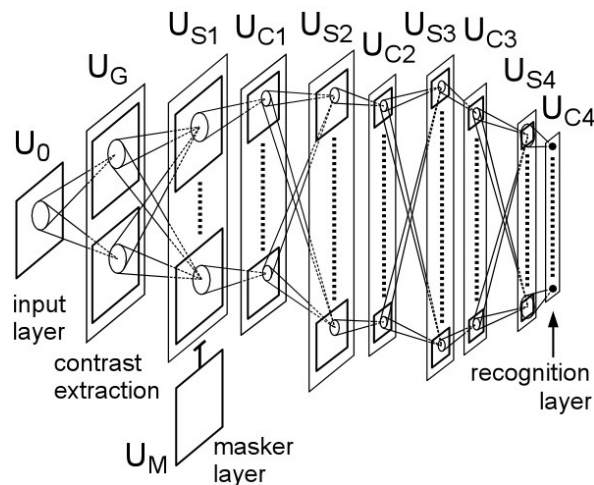
Hubel/Wiesel架构

- D. Hubel and T. Wiesel (1959, 1962, Nobel Prize 1981)
 - 视觉皮层：包括 *simple*, *complex*, and *hyper-complex* 细胞

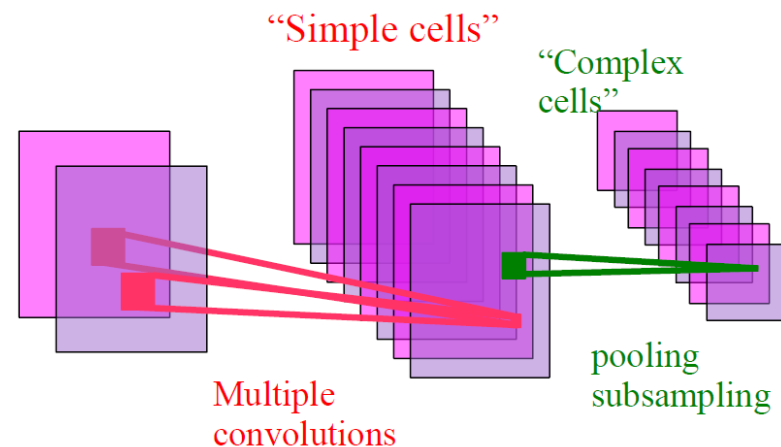


Neocognitron

- **[Hubel & Wiesel 1962]:**
 - 简单细胞：局部特征检测
 - 复杂细胞：简单特征输出的聚合



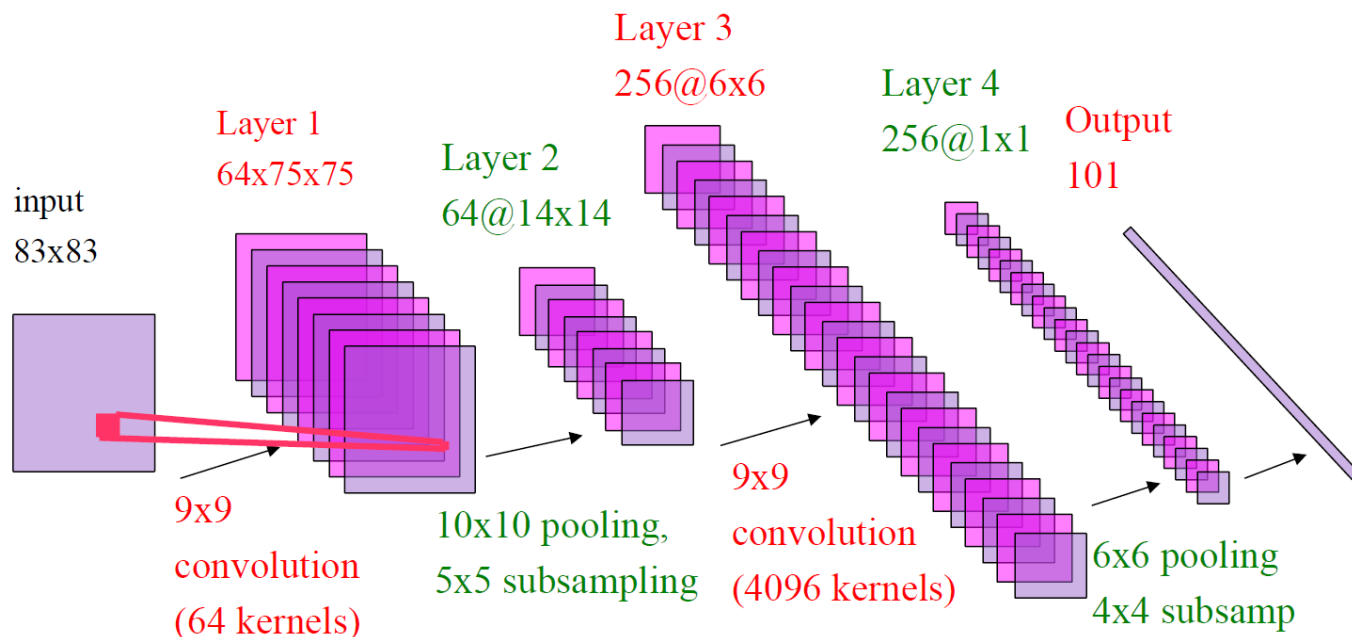
Cognitron & Neocognitron
[Fukushima 1974-1982]



卷积神经网络

卷积神经网络（上半场）

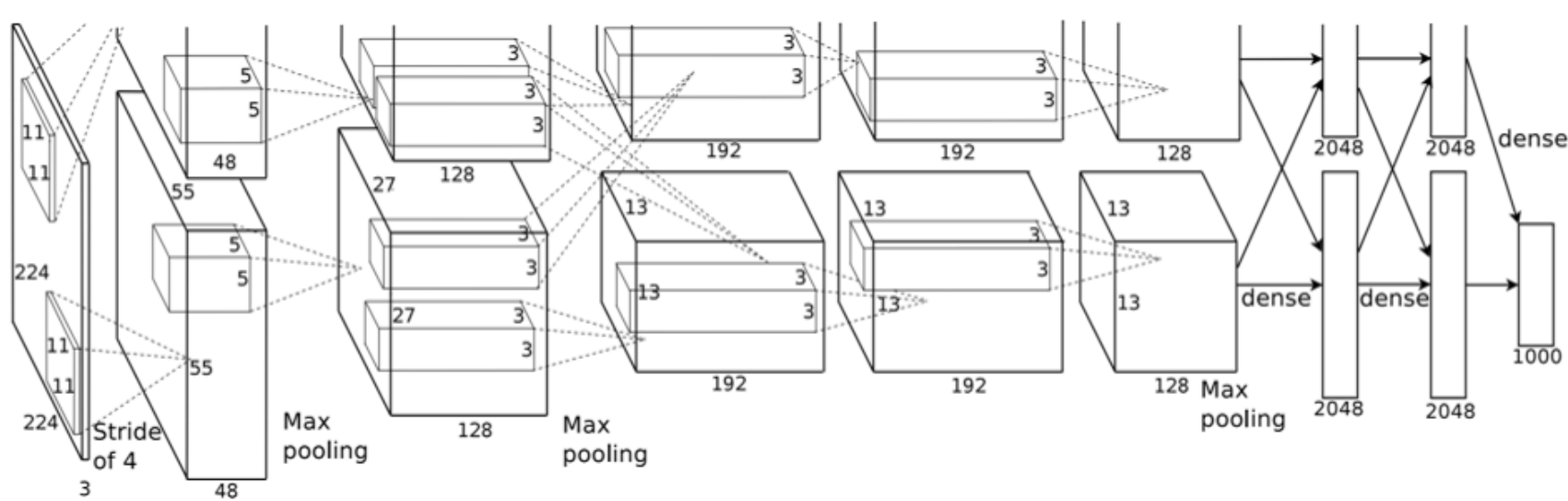
- LeCun et al., NIPS 1989



- 2个卷积层一个全连接层

深度卷积神经网络（下半场）

- Krizhevsky et al. NIPS 2012

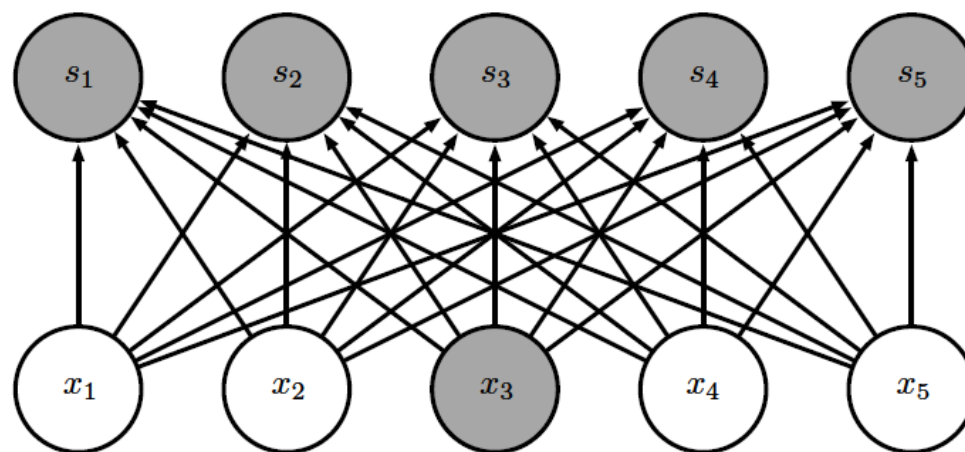
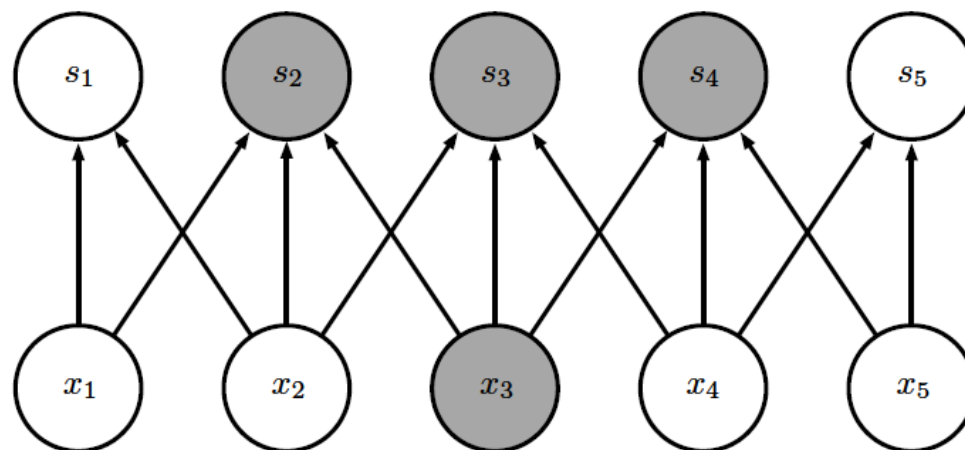


- 5个卷积层、3个全连接层

动机:

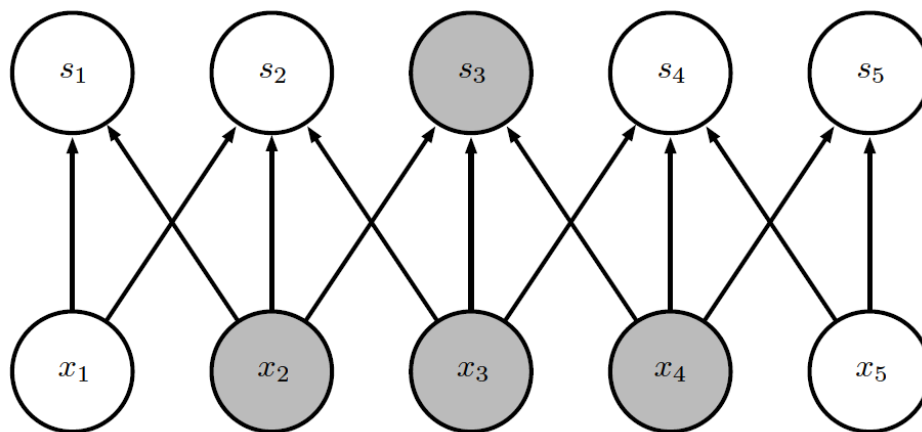
- 稀疏交互 (sparse interactions)
- 参数共享 (parameter sharing)
- 等变表示 (equivariant representation)
 - 不变表示 (invariant representation)

稀疏交互（稀疏连接）

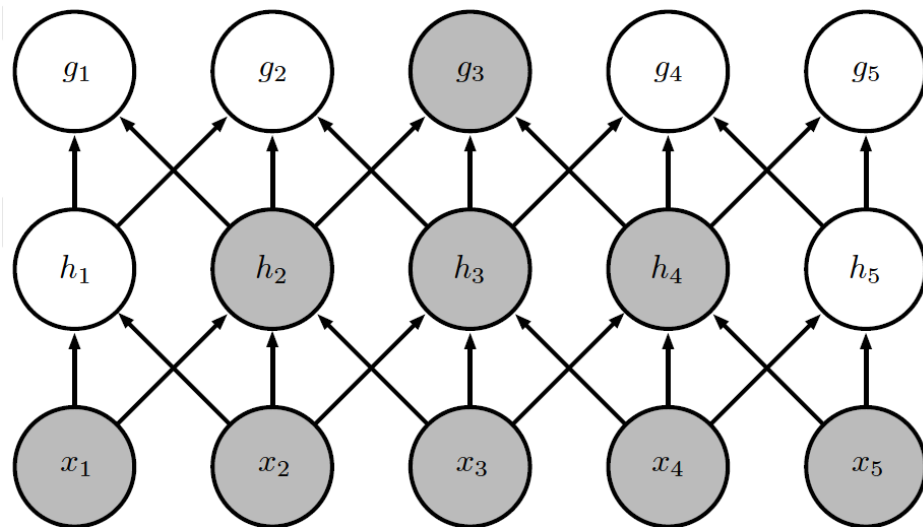


感受野 (Receptive Field)

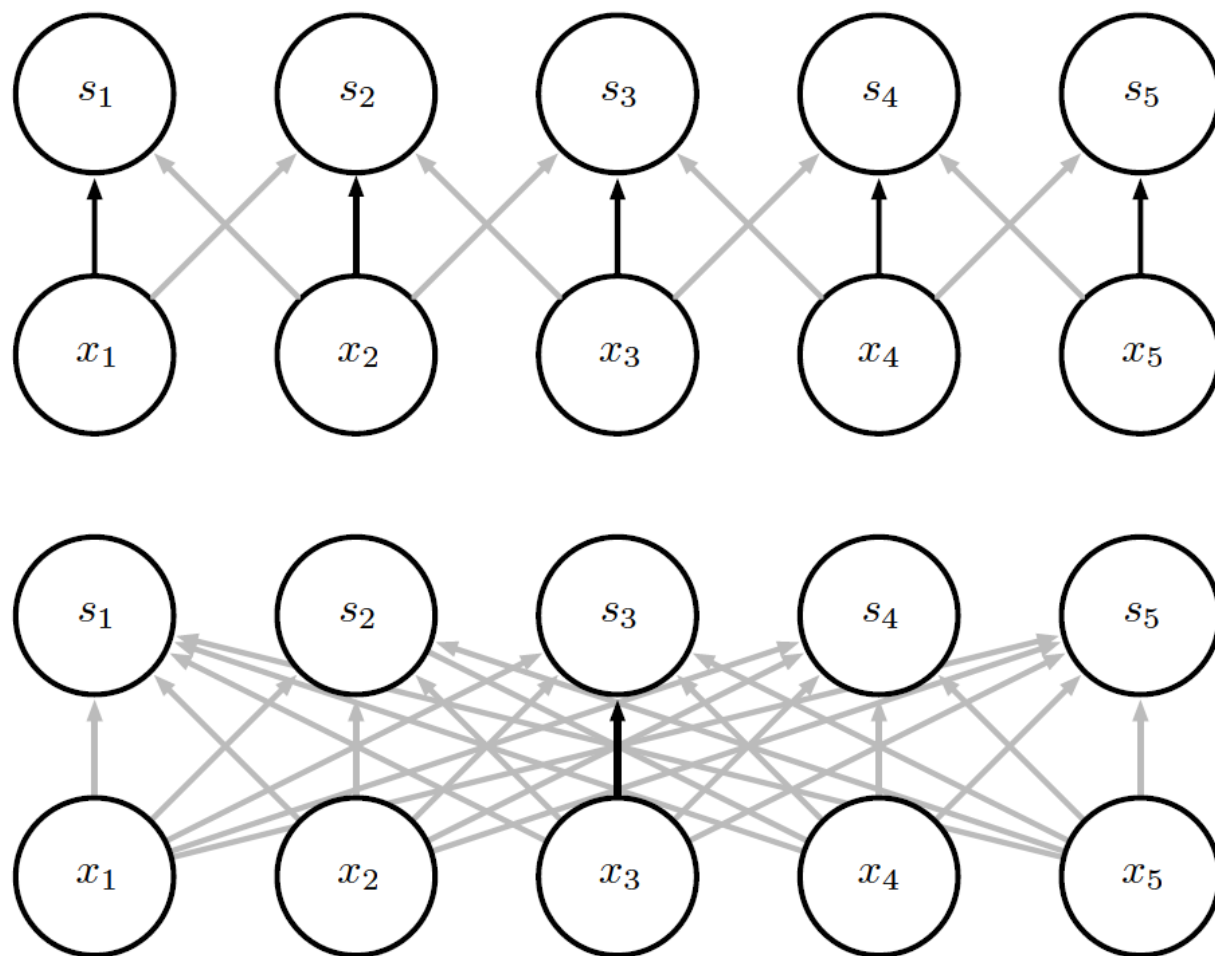
• 层1:



• 层2:



参数共享



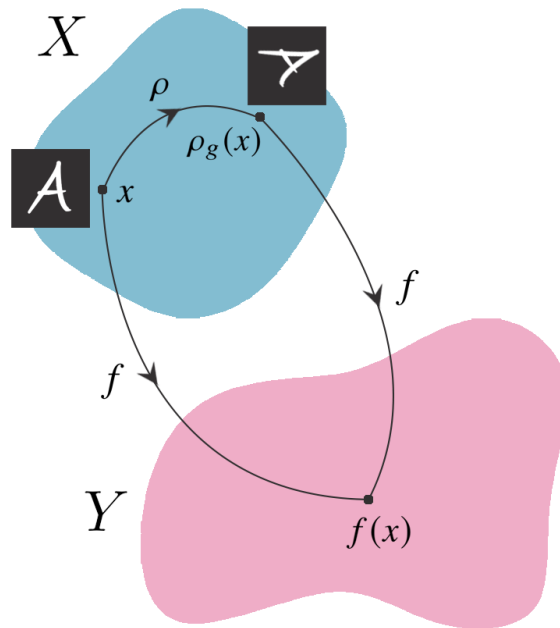
等变表示 (Equivariant Representation)

- 如果一个函数满足输入改变，输出也以同样方式进行改变的话，我们称它是**等变的**
- 卷积： 平移等变
- 不变表示 (Transform-invariant)

等变与不变表示 (Equivariant/Invariant)

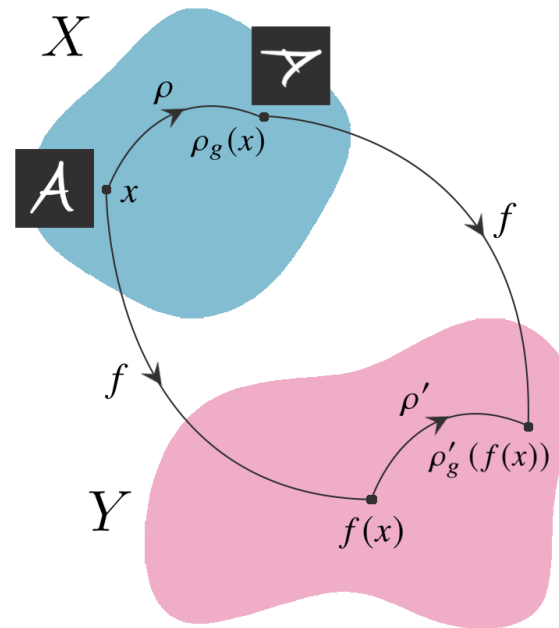
Invariance

$$f(\rho_g(x)) = f(x)$$

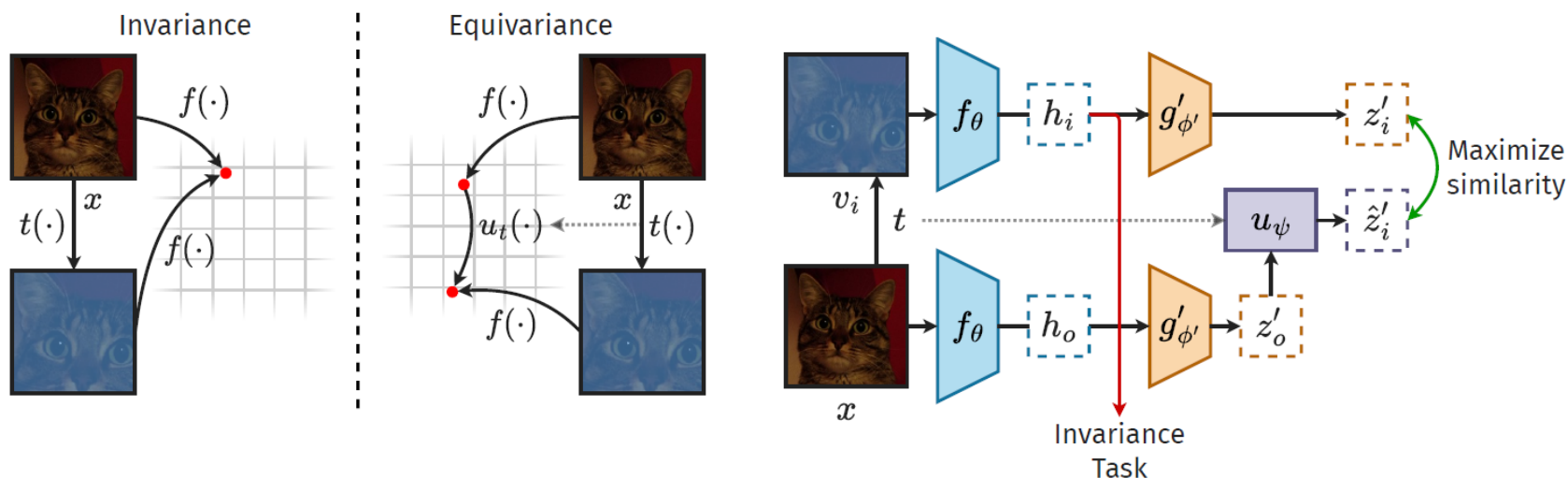


Equivariance

$$f(\rho_g(x)) = \rho'_g(f(x))$$



等变性与不变性的结合



$$\mathcal{L} = \mathcal{L}_{Invariance} + \lambda \mathcal{L}_{EquiMod}$$

- 尽可能保持不变性，但差别仍可以利用等性进一步建模

EquiMod: An Equivariance Module to Improve Visual Instance Discrimination, ICLR 2023.

卷积神经网络

- 历史和动机
- 基本操作
 - 卷积、池化、归一化、卷积神经网络
- 新进展
 - 3x3、空洞卷积（dilated convolution）
- 典型网络架构
 - LeNet、AlexNet、VGGNet、Inception
 - ResNet、SENet、DenseNet、Attention

卷积：参数共享和稀疏连接

- 连续卷积

$$s(t) = \int x(a)w(t-a)da$$

$$s(t) = (x * w)(t).$$

- 输入、核函数

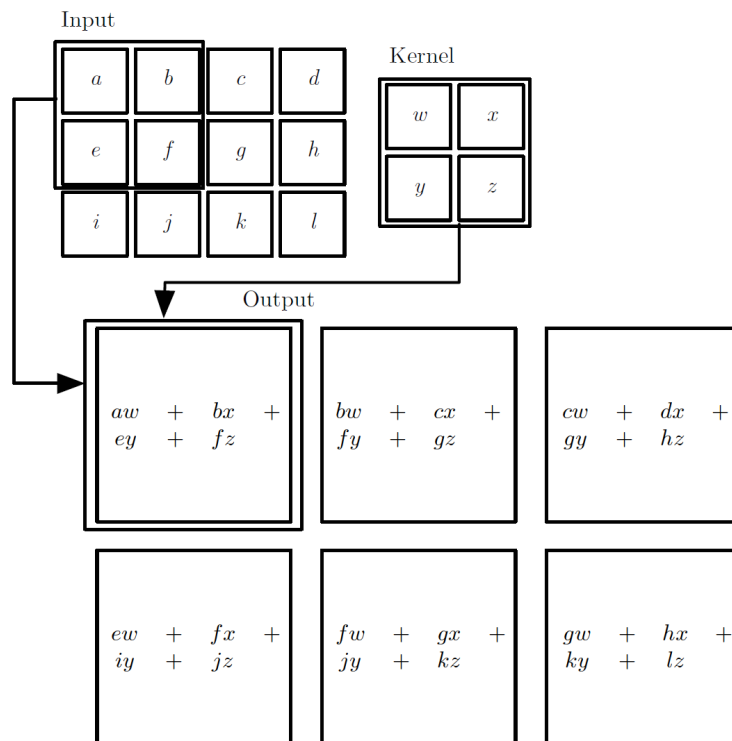
- 离散卷积

$$s(t) = (x * w)(t) = \sum_{a=-\infty}^{\infty} x(a)w(t-a)$$

二维卷积

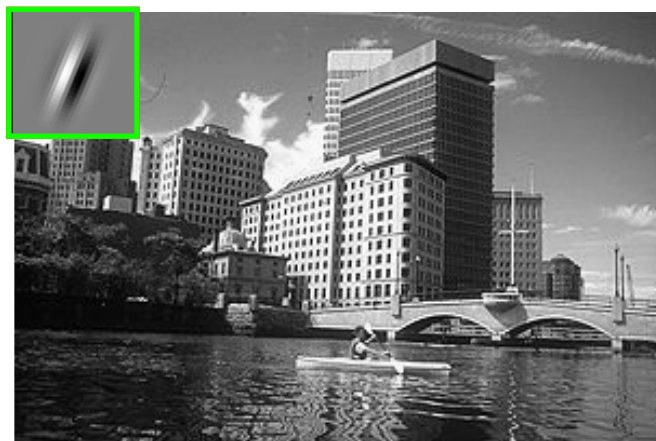
- 二维卷积

$$S(i, j) = (I * K)(i, j) = \sum_m \sum_n I(m, n) K(i - m, j - n)$$

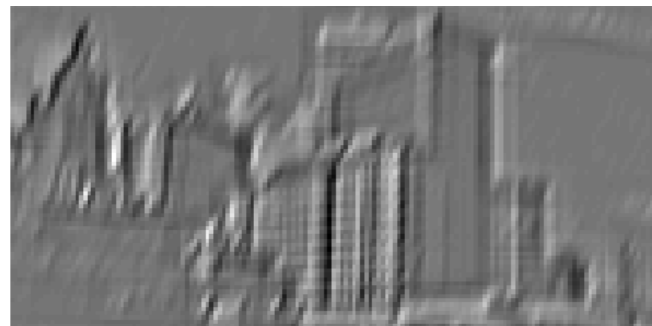


直观展示

- 卷积核(Conv. Kernel)
- 特征图(Feature Map)



Input

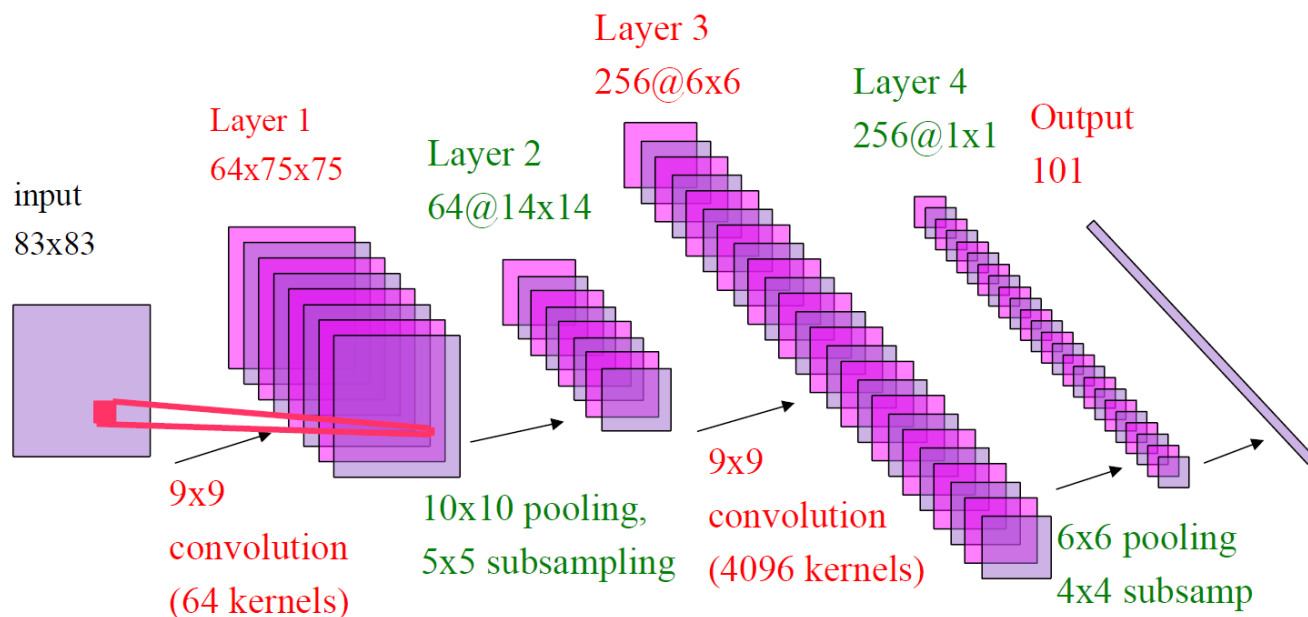


Feature Map

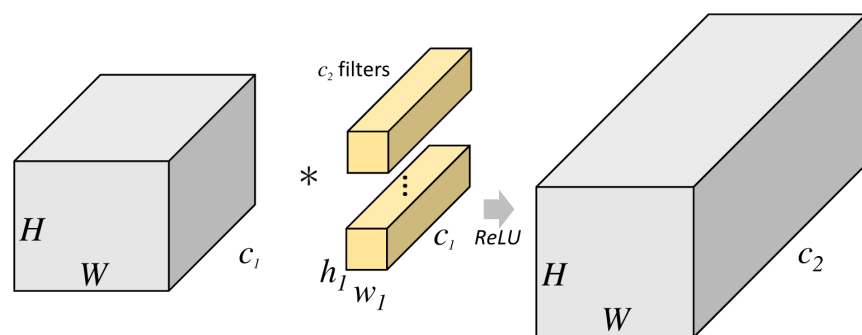
拓展：多通道卷积

- 多通道卷积

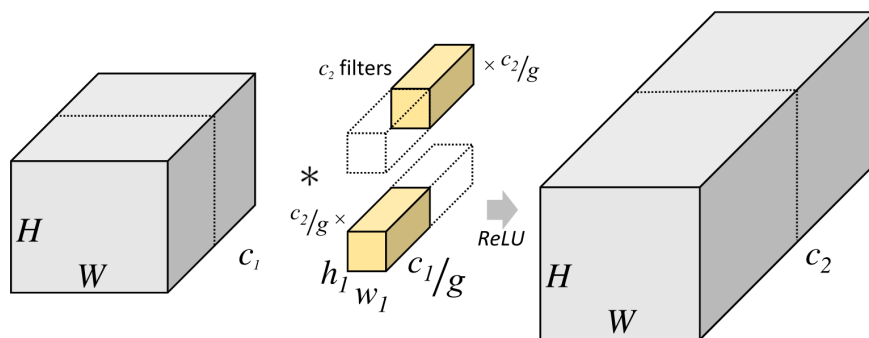
$$F_i = \sum_{j=1}^C w_{j,i} * x_j$$



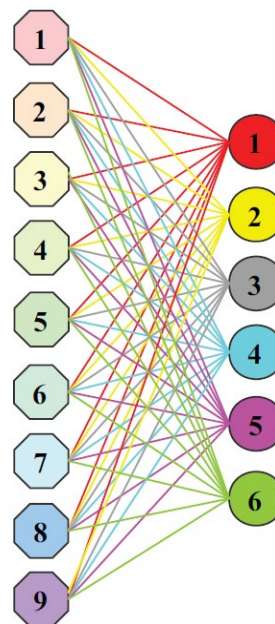
拓展: Grouped Convolution



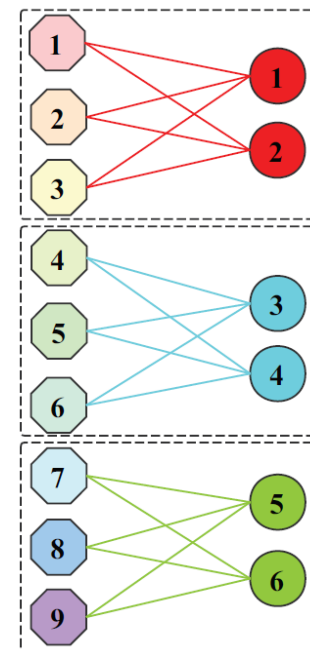
标准卷积



Grouped Convolution



标准卷积



Grouped Convolution

拓展：步幅（Stride）

• 步幅为1

$$\begin{array}{|c|c|c|c|c|} \hline a_{11} & a_{12} & a_{13} & a_{14} & \\ \hline a_{21} & a_{22} & a_{23} & a_{24} & \\ \hline a_{31} & a_{32} & a_{33} & a_{34} & \\ \hline a_{41} & a_{42} & a_{43} & a_{44} & \\ \hline & & & & \\ \hline \end{array}
 \quad * \quad
 \begin{array}{|c|c|c|} \hline k_{11} & k_{12} & k_{13} \\ \hline k_{21} & k_{22} & k_{23} \\ \hline k_{31} & k_{32} & k_{33} \\ \hline \end{array}
 \quad = \quad
 \begin{array}{|c|c|} \hline a_{11}k_{11}+a_{12}k_{12}+a_{13}k_{13} & a_{12}k_{11}+a_{13}k_{12}+a_{14}k_{13} \\ \hline + & + \\ a_{21}k_{21}+a_{22}k_{22}+a_{23}k_{23} & a_{22}k_{21}+a_{23}k_{22}+a_{24}k_{23} \\ \hline + & + \\ a_{31}k_{31}+a_{32}k_{32}+a_{33}k_{33} & a_{32}k_{31}+a_{33}k_{32}+a_{34}k_{33} \\ \hline \end{array}
 \quad \dots$$

I K S

• 步幅为2

$$\begin{array}{|c|c|c|c|c|c|} \hline a_{11} & a_{12} & a_{13} & a_{14} & a_{15} & \\ \hline a_{21} & a_{22} & a_{23} & a_{24} & a_{25} & \\ \hline a_{31} & a_{32} & a_{33} & a_{34} & a_{35} & \\ \hline a_{41} & a_{42} & a_{43} & a_{44} & & \\ \hline & & & & & \\ \hline \end{array}
 \quad * \quad
 \begin{array}{|c|c|c|} \hline k_{11} & k_{12} & k_{13} \\ \hline k_{21} & k_{22} & k_{23} \\ \hline k_{31} & k_{32} & k_{33} \\ \hline \end{array}
 \quad = \quad
 \begin{array}{|c|c|} \hline a_{11}k_{11}+a_{12}k_{12}+a_{13}k_{13} & a_{13}k_{11}+a_{14}k_{12}+a_{15}k_{13} \\ \hline + & + \\ a_{21}k_{21}+a_{22}k_{22}+a_{23}k_{23} & a_{23}k_{21}+a_{24}k_{22}+a_{25}k_{23} \\ \hline + & + \\ a_{31}k_{31}+a_{32}k_{32}+a_{33}k_{33} & a_{33}k_{31}+a_{34}k_{32}+a_{35}k_{33} \\ \hline \end{array}
 \quad \dots$$

I K S

拓展：边界条件

- 特征图尺寸逐渐减小
- 零填充（ Zero Padding ）、镜像填充
- 其他方式： Partial Conv.

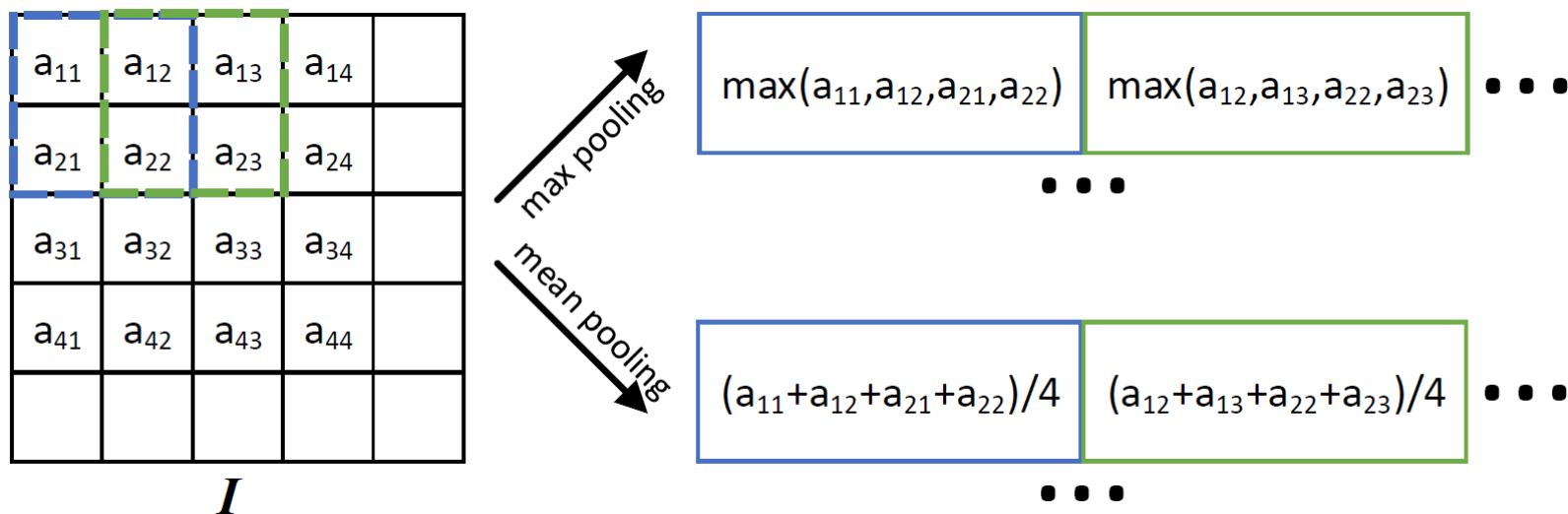
Guilin Liu, Kevin J. Shih, Ting-Chun Wang, Fitsum A. Reda, Karan Sapra, Zhiding Yu, Andrew Tao, Bryan Catanzaro, [Partial Convolution based Padding](#), arXiv:1811.11718 .

卷积神经网络

- 历史和动机
- 基本操作
 - 卷积、池化、归一化、卷积神经网络
- 新进展
 - 3x3、空洞卷积（dilated convolution）
- 典型网络架构
 - LeNet、AlexNet、VGGNet、Inception
 - ResNet、SENet、DenseNet、Attention

池化：形变不敏感

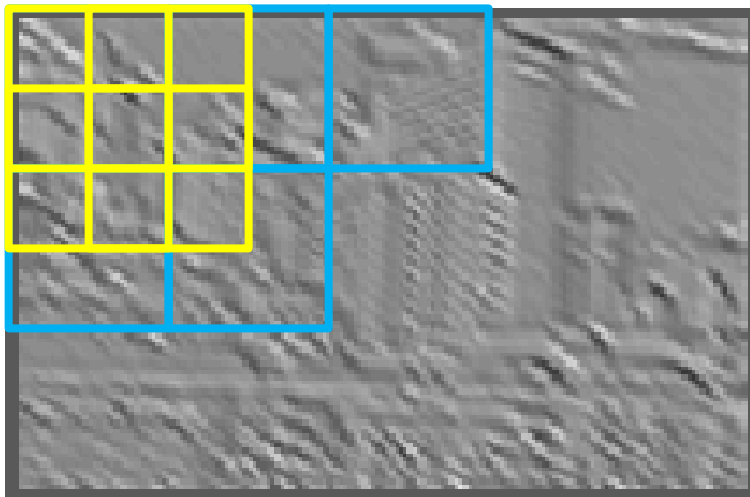
• 池化



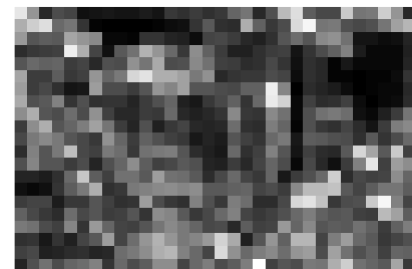
• 下采样

直观展示

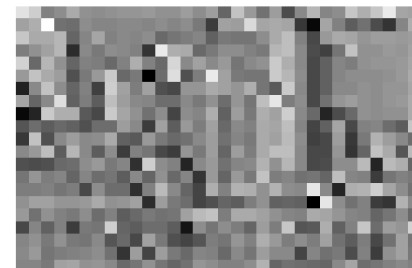
- Max Pooling
- Average Pooling



Max



Sum

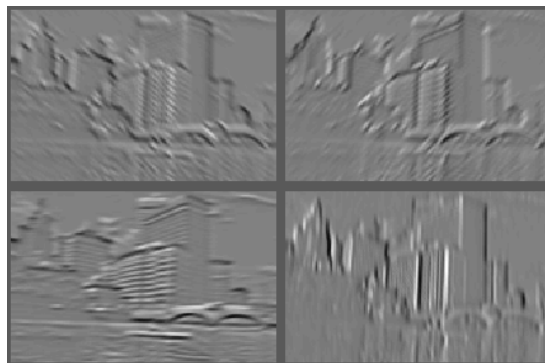


池化: Comment

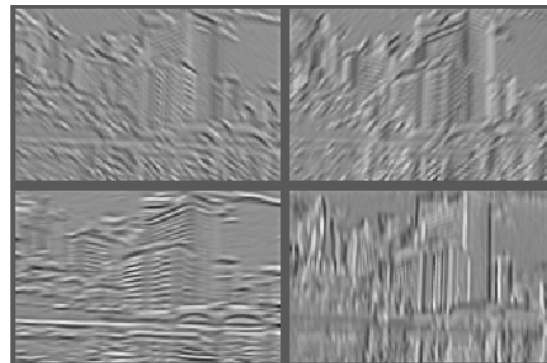
- 作用: 增大感受野、形变不敏感
- Hinton (reddit, 2014): The pooling operation used in convolutional neural networks is a big mistake and the fact that it works so well is a disaster.
- <https://mirror2image.wordpress.com/2014/11/11/geoffrey-hinton-on-max-pooling-reddit-ama/>
- 思考: 如何去掉池化但仍保持感受野和不敏感性特性?
 - Pooling / Downsampling / Conv with Larger Stride

归一化：光照不敏感

- 每个channel或所有channel归一化
- 池化前或池化后归一化



Feature Maps

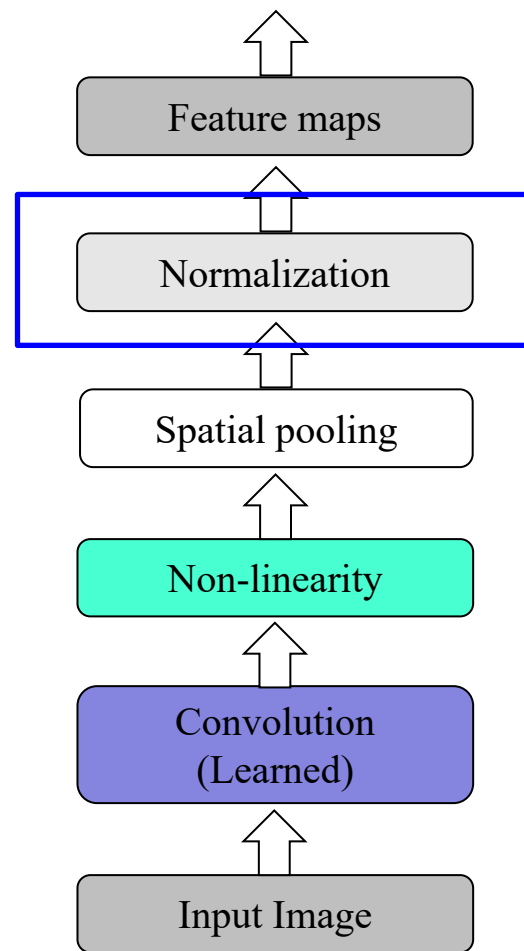


Feature Maps
After Contrast Normalization

- 已不太常用或结合Batch Normalization

总结：CNN网络层

1. 卷积
2. 非线性激活函数
3. 池化
4. 归一化

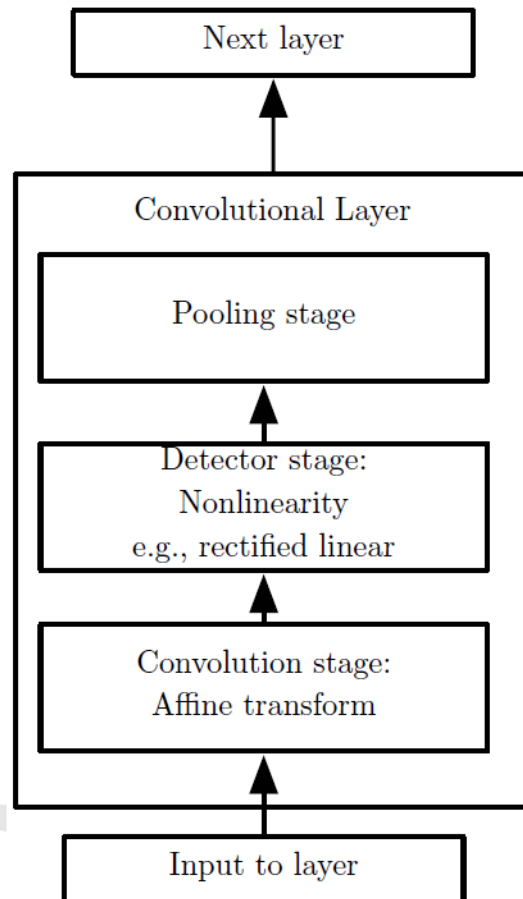


卷积神经网络

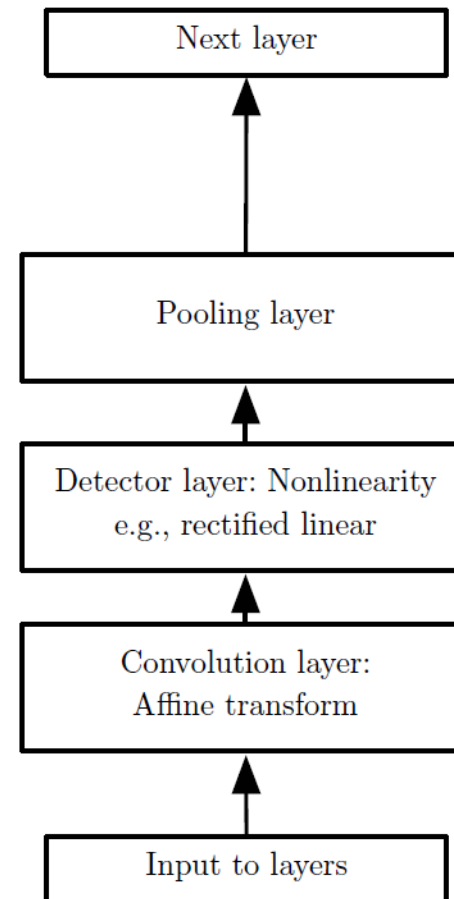
- 历史和动机
- 基本操作
 - 卷积、池化、 归一化、 卷积神经网络
- 新进展
 - 3x3、空洞卷积 (dilated convolution)
- 典型网络架构
 - LeNet、 AlexNet、 VGGNet、 Inception
 - ResNet、 SENet、 DenseNet、 Attention

典型的卷积神经网络层

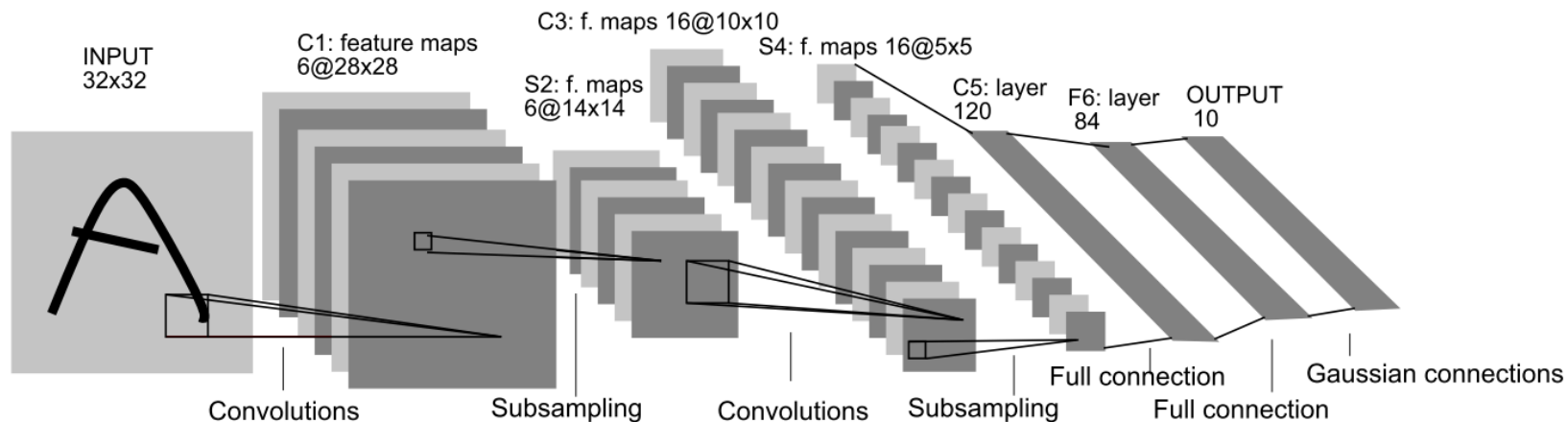
Complex layer terminology



Simple layer terminology

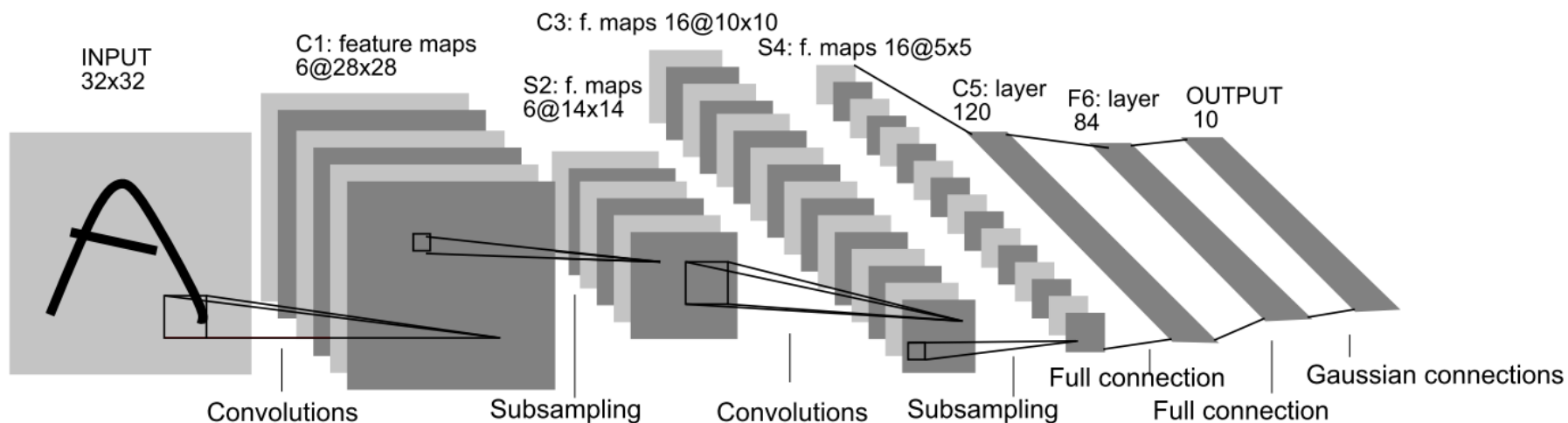


卷积神经网络示例：LeNet5（1998）



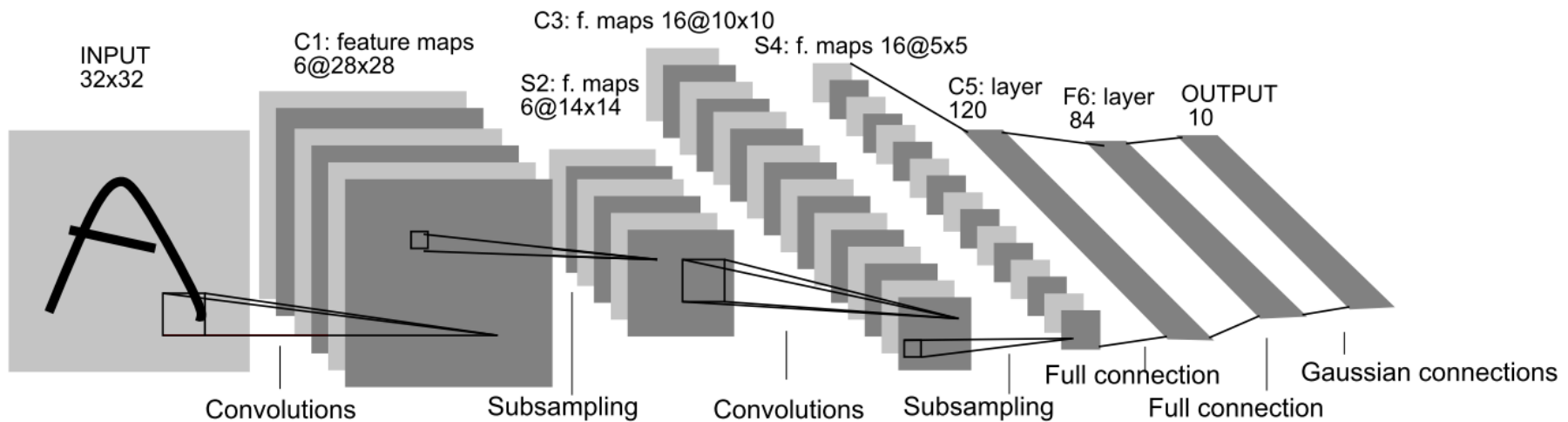
- 输入: 32x32图像
- C_x: 卷积层
- S_x: 下采样层
- F_x: 全连接层

LeNet 5, Layer C1



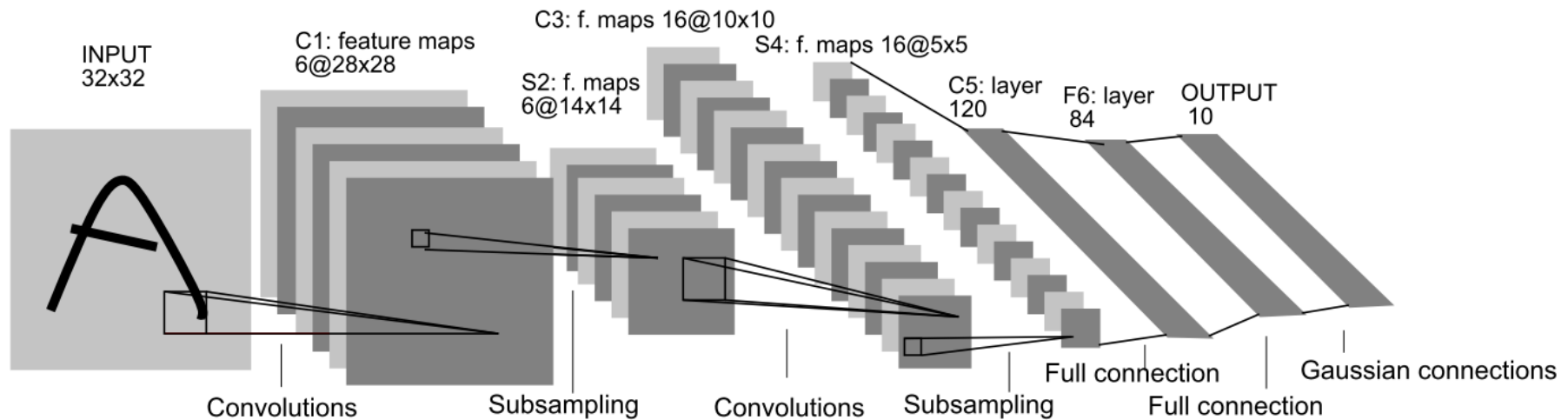
- C1: 卷积层，通道数为6，特征图大小 28x28. 卷积核 5x5.
 - 稀疏连接
 - 参数共享：参数量： $(5*5+1)*6=156$
非参数共享： $28*28*(5*5+1)*6=122304$
全连接： $(32*32+1)*(28*28)*6$ parameters

LeNet 5, Layer S2



- S2: 下采样层，6通道，特征图大小14x14
- 2x2 感受野
- 学习参数: $6 * 2 = 12$.
- 全连接: $14 * 14 * (2 * 2 + 1) * 6 = 5880$

LeNet 5, Layer C3



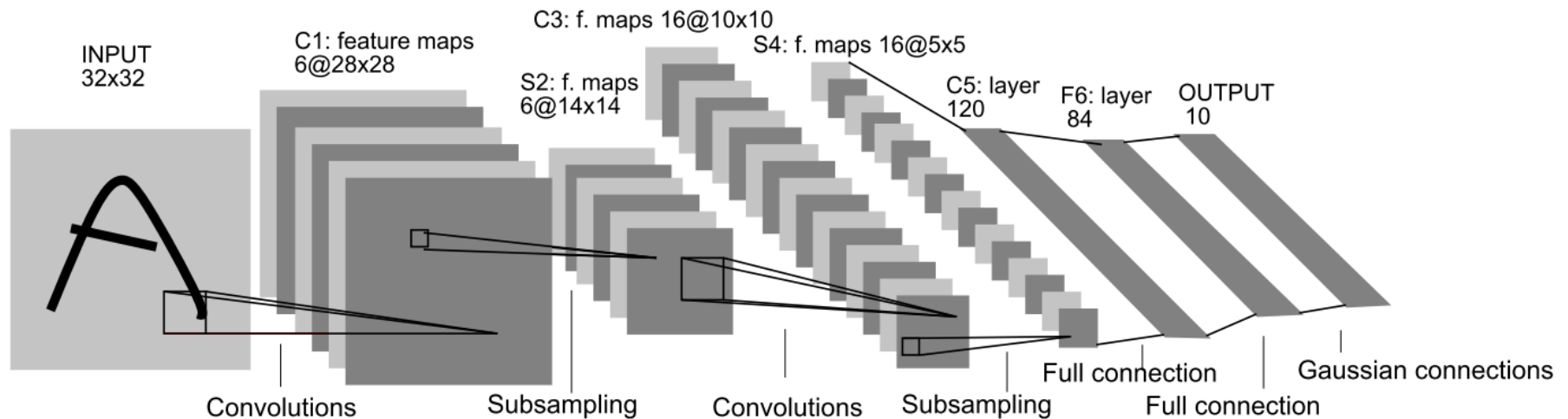
- C3: 卷积层，通道数16，特征图大小 10x10
- Each unit in C3 is connected to several! 5x5 receptive fields at identical locations in S2
- 参数量: 1516.
- 全连接: 151600

	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
0	X				X	X	X			X	X	X	X		X	X
1	X	X				X	X	X			X	X	X	X		X
2	X	X	X				X	X	X			X		X	X	X
3			X	X	X			X	X	X	X		X		X	X
4				X	X	X			X	X	X	X		X	X	X
5					X	X	X			X	X	X	X		X	X

TABLE I

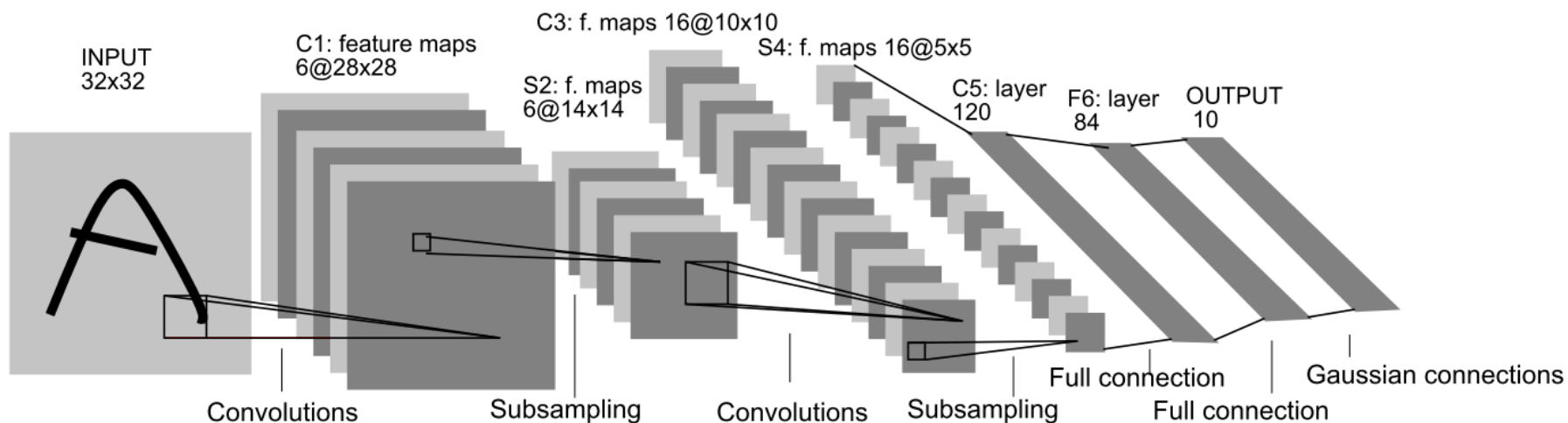
EACH COLUMN INDICATES WHICH FEATURE MAP IN S2 ARE COMBINED BY THE UNITS IN A PARTICULAR FEATURE MAP OF C3.

LeNet 5, Layer S4



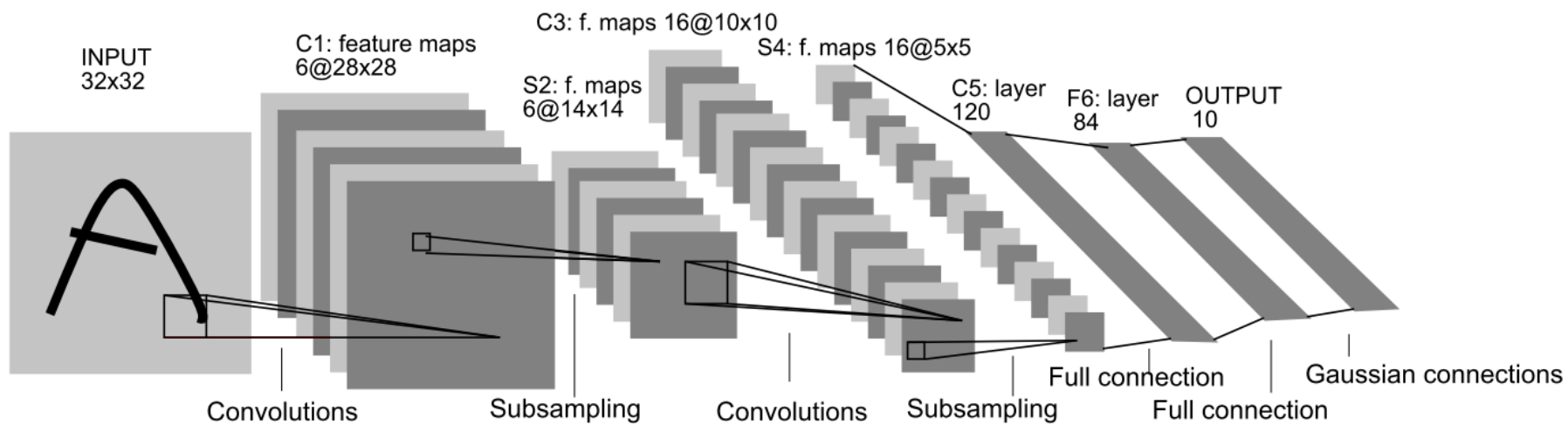
- S4: 下采样层, with 16 feature maps of size 5x5
- 感受野: 2x2
- 参数量: $16 * 2 = 32$.
- 全连接: $5 * 5 * (2 * 2 + 1) * 16 = 2000$

LeNet 5, Layer C5



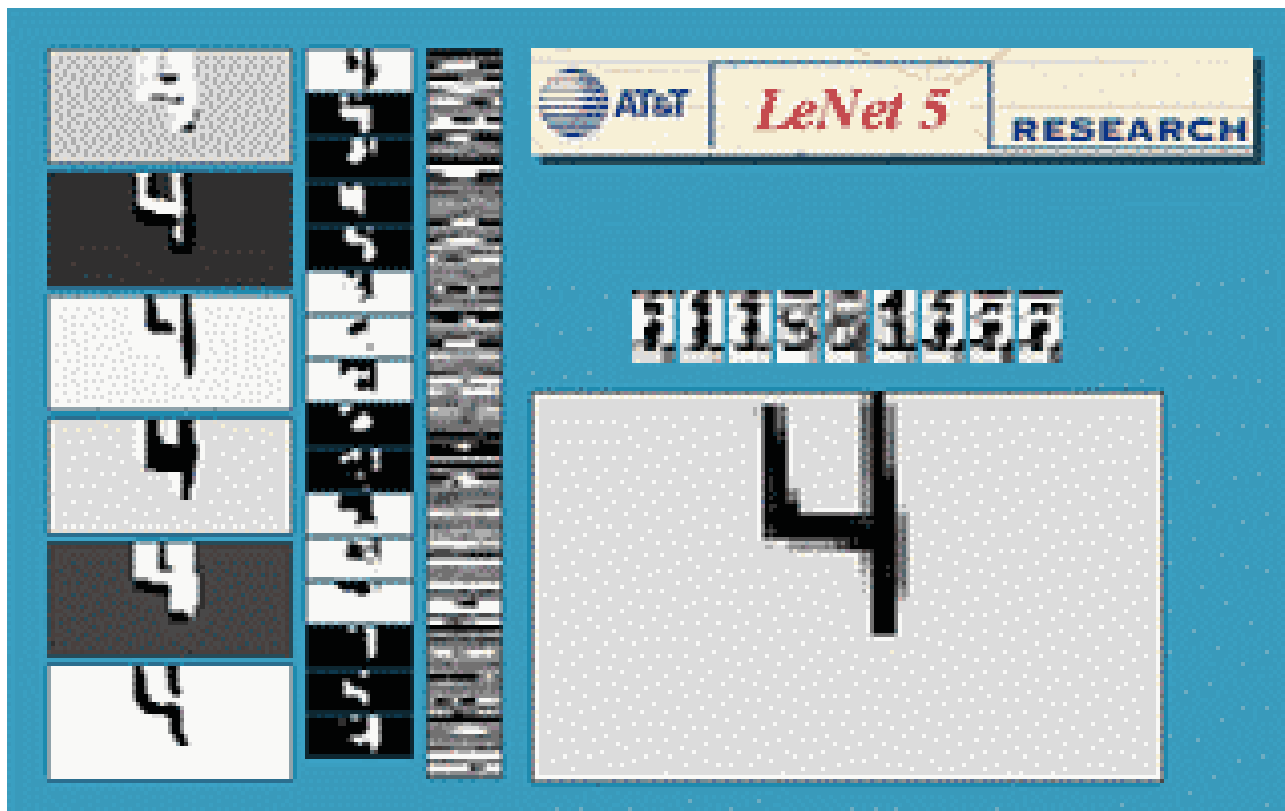
- C5: 卷积层，通道数120，特征图大小1x1
- 感受野 5x5
- 参数量: $120 \times (16 \times 25 + 1) = 48120$

LeNet 5, Layer F6

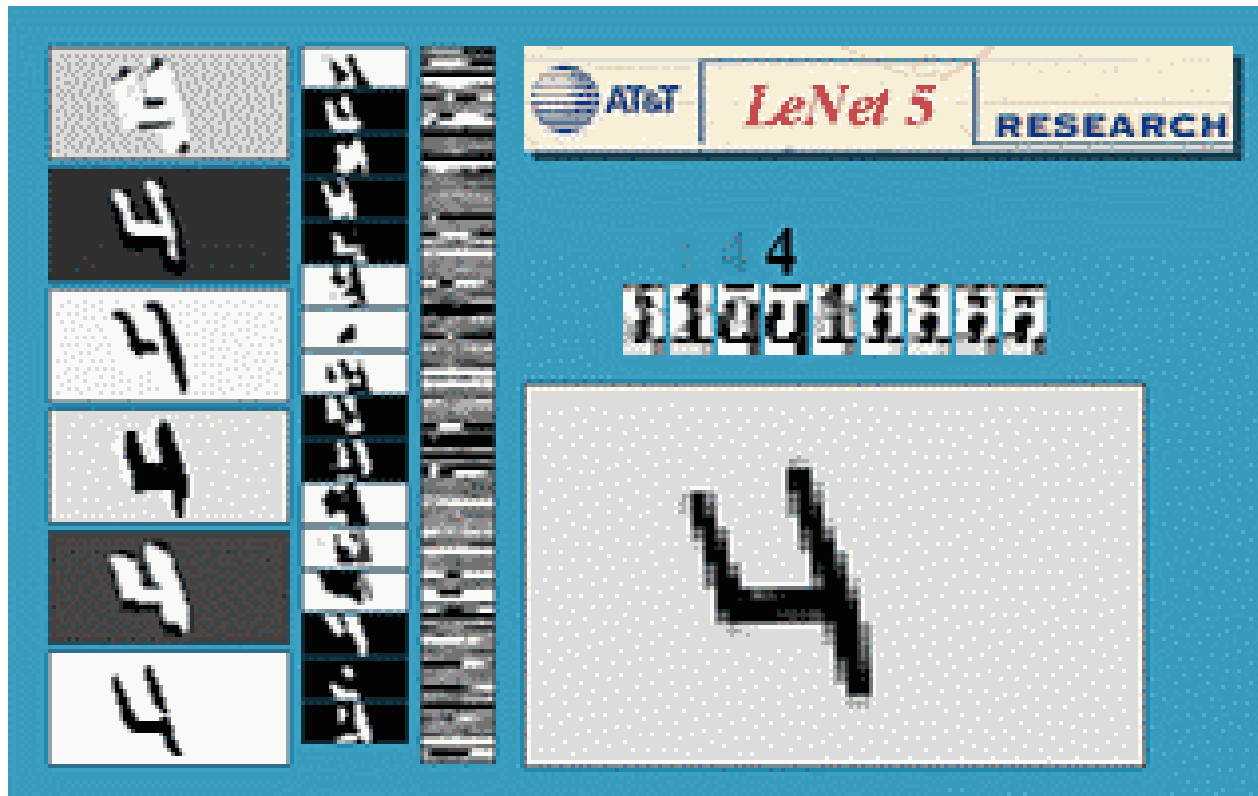


- Layer F6: 全连接层，特征位数84
- 参数量: $84 \times (120 + 1) = 10164$.
- 输出: 10 RBF (One for each digit)
- 学习算法: BP

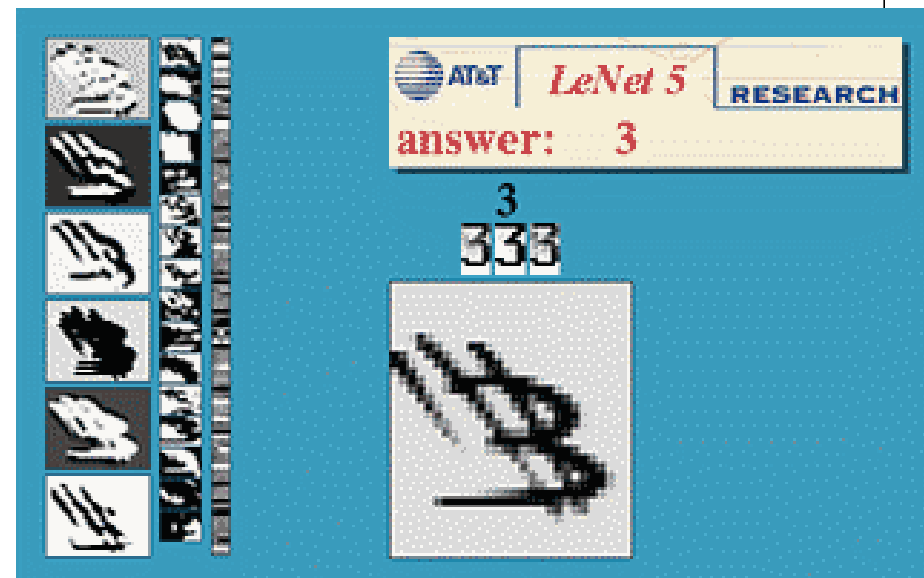
LeNet 5, Shift invariance



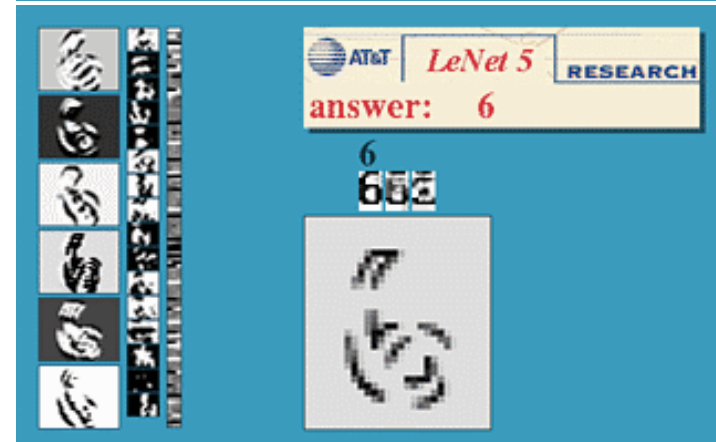
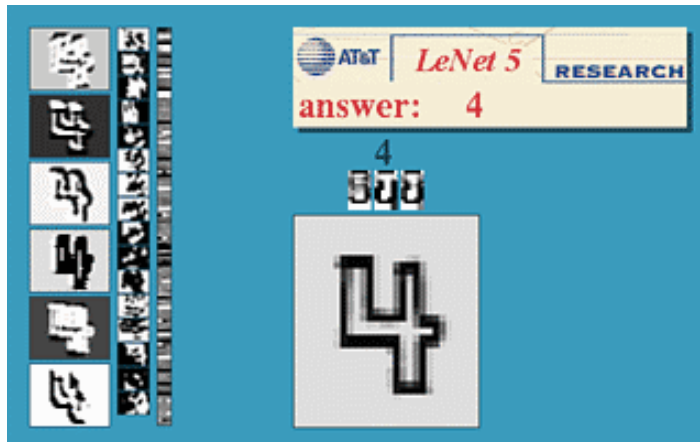
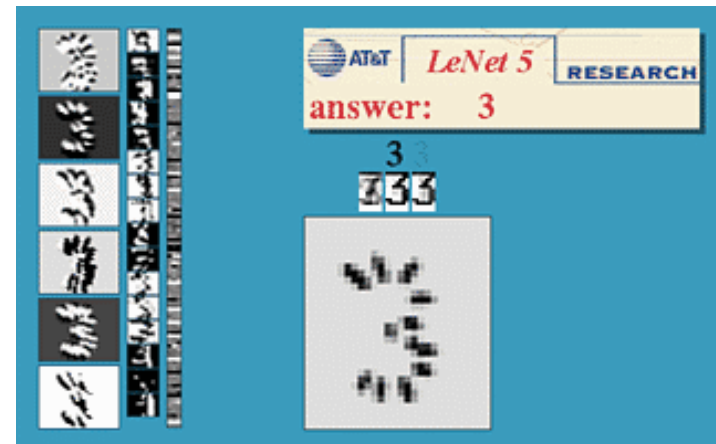
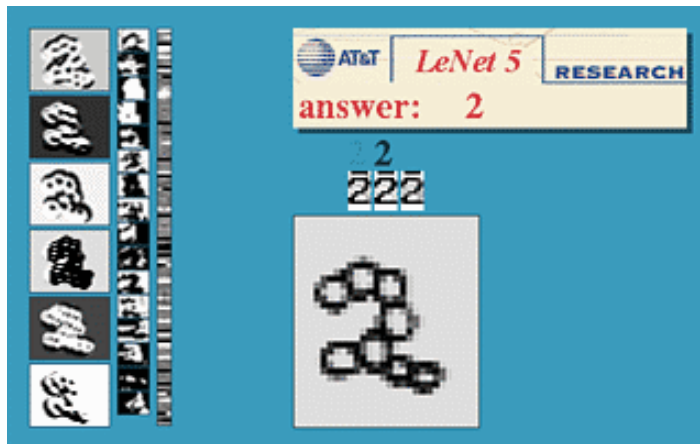
LeNet 5, Rotation invariance



LeNet 5, Noise resistance



LeNet 5, Unusual Patterns



卷积神经网络

- 历史和动机
- 基本操作
 - 卷积、池化、归一化、卷积神经网络
- 新进展：操作
 - 3x3、dilated convolution
- 典型网络架构：思想和网络结构
 - LeNet、AlexNet、VGGNet、Inception
 - ResNet、SENet、DenseNet、Attention