

GU TECH, AL GHAZALI UNIVERSITY



FALL-2024 CS-Department Assignment 1

Course Code: CS101 | Course Name: Discrete Structures

Instructions:

You must submit the **scanned copy** of your own handwritten assignment on google classroom within the due date, strong action would be taken on plagiarism cases from straight **ZERO** in assignment to **Grade F** in course.

1. Suppose the following two propositions are both False.

[10 points]

- If the student has passed Calculus, then he is registered for Discrete Math.
- The student has not passed Programming.

Determine the truth value of the following propositions. Just list the truth value.

- (a) The student has passed Programming and he is registered for Discrete Math.
- (b) The student has passed Calculus and he has passed Programming.
- (c) The student is not registered for Discrete Math or he has passed Programming.
- (d) If the student is not registered for Disc. Math, then the student has not passed Calc..
- (e) If the student is registered for Discrete Math, then he has passed Programming.
- (f) If the student has not passed Calculus, then he is not registered for Discrete Math.
- (g) If the student is registered for Discrete Math, then he has passed Calculus.
- (h) The student has passed Programming if and only if he has passed Calculus.
- (i) The student has passed Programming or he has passed Calculus but not both
- (j) The student has passed Programming or he has passed Calculus or he is registered for Discrete Math.
- 2. Show the following equivalences using using logical equivalence laws.

[10 points]

- (a) Show that $(P \rightarrow R) \lor (Q \rightarrow R) \equiv (P \land Q) \rightarrow R$
- (b) Show that $P \wedge (Q \vee R) \equiv (P \wedge Q) \vee (P \wedge R)$.
- (c) Show that $\neg[\neg[(P \lor Q) \land R] \lor \neg Q] \equiv Q \land R$
- (d) Show that $(P \lor Q \lor R) \land (P \lor T \lor \neg Q) \land (P \lor \neg T \lor R) \equiv P \lor [R \land (T \lor \neg Q)]$

3. Let A, B and C be propositions. Using truth table show that the following is a logical equivalence.

[10 points]

$$(\neg A \lor B) \land (\neg B \lor C) \land (\neg C \lor A) \land (\neg A \lor \neg B \lor \neg C) \equiv (\neg A \land \neg B \land \neg C).$$

A	B	C			LHS	RHS

4. Use Truth tables to see if the following statements are true:

[10 points]

(a)
$$P \rightarrow (Q \land R) \equiv (Q \rightarrow P) \land (P \rightarrow R)$$

(b)
$$(P \lor Q) \rightarrow R \equiv [(P \rightarrow R) \land (Q \rightarrow R)]$$

(c)
$$[P \rightarrow (Q \lor R)] \equiv [\neg R \rightarrow (P \rightarrow Q)]$$

(d)
$$(P \land Q) \rightarrow R \equiv (\neg R \lor P) \rightarrow Q$$

5. Complete the following truth table:

[10 points]

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p	q	r	$\overbrace{p \to (q \to r)}$	$\overbrace{(p \to q) \to (p \to r)}$	$s \to t$