

OnRamps PreCalculus Notes

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OnRamps Precalculus works through a dual-enrollment model with the University of Texas at Austin. Through a creative and connected approach, students deepen and extend their knowledge of functions, graphs, and equations from their high school Algebra and Geometry courses so that they can successfully work with the concepts in a rigorous university-level calculus course. This course is designed to push students well beyond “drill and kill” exercises, emphasizing conceptual understanding of mathematical definitions and developing logical arguments with peers.

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1.5 Functions Defined by Patterns

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