

Physics Notes

Stasya

Fall 2024 & Spring 2025

Contents

1	Section 1	3
1.1	Powers of Ten. Units, Dimensions, Measurements, Uncertainties, Dimensional Analysis, Scaling Arguments	3
1.2	1D Kinematics, Speed, Velocity, Acceleration	3
1.3	Vectors, Dot Products, Cross Products, 3D Kinematics	3
1.4	3D Kinematics, Free Falling Reference Frames	3
1.5	Circular Motion, Centrifuges Moving, Reference Frames, Perceived Gravity	3
1.6	Newton's Laws	3
1.7	Weight, Perceived Gravity, Weightlessness Free Fall, Zero Gravity in Orbit (Misnomer)	3
1.8	Friction	3
1.9	Part 1 Summary	3
2	Section 2	4
2.1	Hooke's Law, Springs, Simple Harmonic Motion, Pendulum, Small Angle Approximation	4
2.2	Work, Kinetic Energy, Potential Energy, Conservative Forces, Conservation of Mechanical Energy, Newton's Laws of Universal Gravitation	4
2.3	Non-Conservative Forces, Resistive Forces, Air Drag, Terminal Velocity	4
2.4	Potential Energy, Energy Considerations to Derive Simple Harmonic Motion	4
2.5	Escape Velocities, Bound and Unbound Orbits, Circular Orbits, Various Forms of Energy, Power	4
2.6	Momentum, Conservation of Momentum, Center of Mass	4
2.7	Collisions, Elastic and Inelastic, Center of Mass Frame of Reference	4
2.8	Impulse, Rockets	4
2.9	Part 2 Summary	4
3	Section 3	5
3.1	Rotating Rigid Bodies, Moment of Inertia, Parallel and Perpendicular Axis Theorem, Rotational KE, Fly Wheels, Neutron Stars, Pulsars	5
3.2	Angular Momentum, Torques, Conservation of Angular Momentum, Spinning Neutron Stars, Stellar Collapse	5
3.3	Torques, Oscillating Bodies, Hoops	5
3.4	Kepler's Laws, Elliptical Orbits, Satellites, Change of Orbits, Ham Sandwich	5
3.5	Doppler Effect, Binary Stars, Neutron Stars and Black Holes	5
3.6	Rolling Motion, Gyroscopes, Very Non-intuitive	5
3.7	Static Equilibrium, Stability, Rope Walker	5
3.8	Elasticity, Young's Modulus	5
3.9	Fluid Mechanics, Pascal's Principle, Hydrostatics, Atmospheric Pressure, Over Pressure in Lungs and Tires	5
3.10	Hydrostatics, Archimedes' Principle, Fluid Dynamics, What Makes Your Boat Float?, Bernoulli's Equation	5
3.11	Part 3 Summary	5
4	Section 4	6
4.1	Simple Harmonic Oscillations, Energy Considerations, Torsional Pendulum	6
4.2	Forced Oscillations, Normal Modes, Resonance, Natural Frequencies, Musical Instruments	6
4.3	Heat, Thermal Expansion	6
4.4	Kinetic Gas Theory, Ideal Gas Law, Isothermal Atmosphere, Phase Diagrams, Phase Transitions	6
4.5	The Wonderful Quantum World, Breakdown of Classical Mechanics	6
5	Section 5	7
5.1	Electric Charges and Forces, Coulomb's Law, Polarization	7
5.2	Electric Field Lines, Superposition, Inductive Charging, Induced Dipoles	7
5.3	Electric Flux, Gauss' Law, Examples	9
5.4	Electrostatic Potential, Electric Energy, Equipotential Surfaces	10
5.5	$E = -\text{grad } V$, Conductors, Electrostatic Shielding (Faraday Cage)	10
5.6	High-voltage Breakdown, Lightning, Sparks, St-Elmo's Fire	10

5.7	Capacitance, Electric Field Energy	10
5.8	Polarization, Dielectrics, Van de Graaff Generator, Capacitors	10
5.9	Electric Currents, Resistivity, Conductivity, Ohm's Law	10
5.10	Batteries, Power, Kirchhoff's Rules, Circuits, Kelvin Water Dropper	10
5.11	Magnetic Fields, Lorentz Force, Torques, Electric Motors (DC)	10
5.12	Section 5 Review	10
6	Section 6	11
6.1	Moving charges in B-fields, Cyclotrons, Mass Spectrometers, LHC	11
6.2	Biot-Savart, $\text{div } \mathbf{B} = 0$, High-voltage Power Lines, Leyden Jar revisited	11
6.3	Ampere's Law, Solenoids, Kelvin Water Dropper (revisited)	11
6.4	Electromagnetic Induction, Faraday's Law, Lenz Law, SUPER DEMO	11
6.5	Motional EMF, Dynamos, Eddy Currents, Magnetic Braking	11
6.6	Displacement Current, Synchronous Motors, Explanation Secret Top	11
6.7	Magnetic Levitation, Human, Superconductivity, Aurora Borealis	11
6.8	Inductance, RL Circuits, Magnetic Field Energy	11
6.9	Magnetic Materials, Dia- Para-, Ferromagnetism	11
6.10	Maxwell's Equations, 600 Daffodil Ceremony	11
6.11	Section 6 Review	11
7	Section 7	12
7.1	Transformers, Car Coils, RC Circuits	12
7.2	Driven LRC Circuits, Metal Detectors	12
7.3	Traveling Waves, Standing Waves, Musical Instruments	12
7.4	Destructive Resonance, Electromagnetic Waves, Speed of Light	12
7.5	Poynting Vector, Oscillating Charges, Polarization, Radiation Pressure	12
7.6	Snell's Law, Index of Refraction, Huygen's Principle, Illusion of Color	12
7.7	Polarizers, Malus' Law, Light Scattering, Blue Skies, Red Sunsets	12
7.8	Rainbows, Fog Bows, Haloes, Glories, Sun Dogs	12
7.9	Section 7 Review	12
8	Section 8	13
8.1	Double-slit Interference, Interferometers	13
8.2	Diffraction, Gratings, Resolving Power, Angular Resolution	13
8.3	Doppler Effect, Big Bang, Cosmology	13

1 Section 1

- 1.1 Powers of Ten. Units, Dimensions, Measurements, Uncertainties, Dimensional Analysis, Scaling Arguments**
- 1.2 1D Kinematics, Speed, Velocity, Acceleration**
- 1.3 Vectors, Dot Products, Cross Products, 3D Kinematics**
- 1.4 3D Kinematics, Free Falling Reference Frames**
- 1.5 Circular Motion, Centrifuges Moving, Reference Frames, Perceived Gravity**
- 1.6 Newton's Laws**
- 1.7 Weight, Perceived Gravity, Weightlessness Free Fall, Zero Gravity in Orbit (Misnomer)**
- 1.8 Friction**
- 1.9 Part 1 Summary**

2 Section 2

- 2.1 Hooke's Law, Springs, Simple Harmonic Motion, Pendulum, Small Angle Approximation**
- 2.2 Work, Kinetic Energy, Potential Energy, Conservative Forces, Conservation of Mechanical Energy, Newton's Laws of Universal Gravitation**
- 2.3 Non-Conservative Forces, Resistive Forces, Air Drag, Terminal Velocity**
- 2.4 Potential Energy, Energy Considerations to Derive Simple Harmonic Motion**
- 2.5 Escape Velocities, Bound and Unbound Orbits, Circular Orbits, Various Forms of Energy, Power**
- 2.6 Momentum, Conservation of Momentum, Center of Mass**
- 2.7 Collisions, Elastic and Inelastic, Center of Mass Frame of Reference**
- 2.8 Impulse, Rockets**
- 2.9 Part 2 Summary**

3 Section 3

- 3.1 Rotating Rigid Bodies, Moment of Inertia, Parallel and Perpendicular Axis Theorem, Rotational KE, Fly Wheels, Neutron Stars, Pulsars**
- 3.2 Angular Momentum, Torques, Conservation of Angular Momentum, Spinning Neutron Stars, Stellar Collapse**
- 3.3 Torques, Oscillating Bodies, Hoops**
- 3.4 Kepler's Laws, Elliptical Orbits, Satellites, Change of Orbits, Ham Sandwich**
- 3.5 Doppler Effect, Binary Stars, Neutron Stars and Black Holes**
- 3.6 Rolling Motion, Gyroscopes, Very Non-intuitive**
- 3.7 Static Equilibrium, Stability, Rope Walker**
- 3.8 Elasticity, Young's Modulus**
- 3.9 Fluid Mechanics, Pascal's Principle, Hydrostatics, Atmospheric Pressure, Over Pressure in Lungs and Tires**
- 3.10 Hydrostatics, Archimedes' Principle, Fluid Dynamics, What Makes Your Boat Float?, Bernoulli's Equation**
- 3.11 Part 3 Summary**

4 Section 4

- 4.1 Simple Harmonic Oscillations, Energy Considerations, Torsional Pendulum**
- 4.2 Forced Oscillations, Normal Modes, Resonance, Natural Frequencies, Musical Instruments**
- 4.3 Heat, Thermal Expansion**
- 4.4 Kinetic Gas Theory, Ideal Gas Law, Isothermal Atmosphere, Phase Diagrams, Phase Transitions**
- 4.5 The Wonderful Quantum World, Breakdown of Classical Mechanics**

5 Section 5

5.1 Electric Charges and Forces, Coulomb's Law, Polarization

A property of matter is electric charge. There is a negative and positive electric charge. Like charges will repel, and opposite charges will attract.

The law of conservation of electric charge states that the total charge of the universe remains unchanged in all observed processes. If $+Q$ is created somewhere, $-Q$ is also created.

Atoms have generally been considered positively charged. Negatively charged electrons orbit around the nucleus. Atoms can lose or gain electrons and have a net electric charge. These are called ions. We call a molecule with asymmetrical distribution of charges polar.

Materials in which electric charge is easily transported are called conductors. Insulators are the opposite. Semiconductors are in the middle.

Charge can be transferred through direct contact from one electrically charged object to another. Conductors can also be charged without direct contact. We can charge by induction - firstly there will be a pair of consecutive bodies that has no net electric charge. Then, a positive charged object is brought near one of the objects, then the wire is cut and will leave one side positive charged and the other negatively charged. Electroscopes and electrometers are used to measure electric charge.

Coulomb's Law is the relationship between the size of the force between charges to the amount of charge and distance separating the charges. We write this as:

$$F = k \frac{Q_1 Q_2}{r^2}$$

Note that the charge of an electron is 1.602×10^{-19} C and the value of k is 8.988×10^9 N·m²/C².

Sometimes k is written as

$$k = \frac{1}{4\pi\epsilon_0}$$

where $\epsilon_0 = 8.85 \times 10^{-12}$ C²/N·m².

We can also rewrite Coulomb's Law in a vector expression that includes the information about the direction of the force:

$$\mathbf{F}_{12} = k \frac{Q_1 Q_2}{r_{21}^2} \hat{\mathbf{r}}_{21}$$

Note that in this expression Q_1 and Q_2 will bear the signs of the charges, where the above equation will be the magnitude. $\hat{\mathbf{r}}_{21}$ is the unit vector that points in the direction from charge Q_2 to charge Q_1 .

5.2 Electric Field Lines, Superposition, Inductive Charging, Induced Dipoles

The electric field \mathbf{E} , at a given point in space is defined as the electric force \mathbf{F} , on a small test charge, q , divided by the charge:

$$\mathbf{E} = \frac{\mathbf{F}}{q}$$

A small test charge is a charge small enough to not change the distribution of charge that cause the force on the test charge.

The electric field created by a point charge Q is:

$$\mathbf{E} = \frac{\mathbf{F}}{q} = k \frac{Qq}{qr^2} \hat{\mathbf{r}} = k \frac{Q}{r^2} \hat{\mathbf{r}}$$

where r is the distance from charge Q to the point at which the electric field is being evaluated and $\hat{\mathbf{r}}$ is the unit vector that points from the charge Q to the point at which the electric field is evaluated.

Electric fields can add to each other like vectors do:

$$\mathbf{E} = \mathbf{E}_1 + \mathbf{E}_2 + \mathbf{E}_3 + \cdots$$

This is called the principle of superposition for electric fields.

In many cases, there it is impossible to sum the electric field from each of the individual charges, but it can be treated by a continuous charge density.

For each infinitesimal charge element dq in the distribution of charge, there is an infinitesimal contribution to the net electric field $d\mathbf{E}$, where:

$$d\mathbf{E} = k \frac{\hat{\mathbf{r}}}{r^2} dq$$

The distance from the charge element to the point at which the field is being evaluated is r and the unit vector in the direction from the charge element to the point being evaluated is $\hat{\mathbf{r}}$.

To determine the electric field at a given point, we integrate over all of the infinitesimal charge elements:

$$\mathbf{E} = \int d\mathbf{E} = \int k \frac{\hat{\mathbf{r}}}{r^2} dq$$

Because charge distribution is often a known function of spatial location, we almost always will change variables in the integral and write charge density as a function of position.

For a linear charge density, we write:

$$dq = \lambda dl$$

where λ is the linear charge density (charge per unit length) and dl is an infinitesimal line element along the charge distribution.

If the charge distribution is a surface charge density, we write:

$$dq = \sigma dA$$

where σ is the surface charge density and dA is an infinitesimal area element of the charge distribution.

If the charge is three-dimensional, we write:

$$dq = \rho dV$$

where ρ is the volume charge density, and dV is an infinitesimal volume element.

A type of diagram that is used to help visualize the electric field is a diagram of electric field lines. An electric field line only gives information about the direction of an electric field.

Electric field lines only begin on positive charges and end on negative charges. The number of lines starting or ending on a given charge is proportional to the magnitude of the charge.

A given line has its tangent at a given point in the direction of the electric field at that point.

The magnitude of the electric field is proportional to the density of the electric field lines passing through a plane perpendicular to the direction of the electric field.

There will be no electric field inside a conductor. The electric field at the surface just external to the conductor must be perpendicular to the conductor under static conditions.

The force of an object with charge q in an electric field \mathbf{E} is given by:

$$\mathbf{F} = q\mathbf{E}$$

A particular distribution of charge that is often a good approximation to many physical situations is the electric dipole.

An electric dipole is two charges of equal magnitude but opposite sign separated by a displacement \mathbf{d} . This displacement is the displacement of the positive charge from the negative charge, basically it points from the location of the negative charge to the location of the positive charge.

The electric dipole moment \mathbf{p} is a vector given by:

$$\mathbf{p} = Q\mathbf{d}$$

If l is the length of the displacement vector \mathbf{d} we can write the magnitude of the dipole moment $p = Ql$.

In an electric field, a dipole experiences a torque:

$$\boldsymbol{\tau} = \mathbf{p} \times \mathbf{E}$$

As the dipole is rotated by the electric field, work is done on the dipole by the torque. The potential energy associated with the orientation of the dipole moment in the electric field is given by:

$$U = -\mathbf{p} \cdot \mathbf{E}$$

A dipole in a uniform electric field feels no net electric force. In a uniform electric field, the positive charge and the negative charge of the dipole experience equal magnitude and opposite direction forces. An electric dipole in a non-uniform electric field can experience a net electric force because the electric field can be different at the locations of the positive and negative charges.

5.3 Electric Flux, Gauss' Law, Examples

The electric flux ϕ_E passing through a planar surface of area A that lies in a plane perpendicular to a uniform electric field of magnitude E is defined to be:

$$\phi_E = EA$$

If the plane of the area A is not perpendicular to the electric field, the electric flux instead is:

$$\phi_E = EA_{\perp} \cos \theta$$

where A_{\perp} is the area of the projection of the area A onto a plane perpendicular to the electric field and θ is the angle between the electric field and the direction of the perpendicular to the area.

If we define a vector \mathbf{A} that has magnitude A and a direction of the perpendicular to the area, the electric flux is written as:

$$\phi_E = EA$$

If the electric field is non-uniform and a general surface, we can consider the flux through infinitesimal areas dA and integrate the flux over the surface:

$$\phi_E = \int E \cdot d\mathbf{A}$$

When the surface is a closed surface, a surface that separates space into an interior and exterior, we write it as:

$$\phi_E = \oint E \cdot d\mathbf{A}$$

A closed surface has a definite inside and outside. The area vector $d\mathbf{A}$ always points outward for a closed volume. Electric field entering a closed surface contributes to negative flux and electric field leaving a closed surface contributes to positive flux.

The electric flux through a closed surface is proportional to the charge within the closed surface:

$$\oint E \cdot d\mathbf{A} = \frac{Q_{encl}}{\epsilon_0}$$

This is called Gauss's Law. Gauss's Law is more general than Coulomb's Law in that it applies to situations where there is an electric field that is not produced by a charge distribution.

We can use Gauss's Law to determine an unknown electric field from a given charge distribution using a surface with correct symmetry.

Experimentally, Gauss's Law and Coulomb's Law are in agreement to very high amounts of precision. If we wanted to measure deviation we would have:

$$F = k \frac{Q_1 Q_2}{r^{2+\delta}}$$

where δ is $(2.7 \pm 3.1) \times 10^{-16}$.

- 5.4 Electrostatic Potential, Electric Energy, Equipotential Surfaces**
- 5.5 $E = -\text{grad } V$, Conductors, Electrostatic Shielding (Faraday Cage)**
- 5.6 High-voltage Breakdown, Lightning, Sparks, St-Elmo's Fire**
- 5.7 Capacitance, Electric Field Energy**
- 5.8 Polarization, Dielectrics, Van de Graaff Generator, Capacitors**
- 5.9 Electric Currents, Resistivity, Conductivity, Ohm's Law**
- 5.10 Batteries, Power, Kirchhoff's Rules, Circuits, Kelvin Water Dropper**
- 5.11 Magnetic Fields, Lorentz Force, Torques, Electric Motors (DC)**
- 5.12 Section 5 Review**

6 Section 6

- 6.1 Moving charges in B-fields, Cyclotrons, Mass Spectrometers, LHC**
- 6.2 Biot-Savart, $\text{div } \mathbf{B} = 0$, High-voltage Power Lines, Leyden Jar revisited**
- 6.3 Ampere's Law, Solenoids, Kelvin Water Dropper (revisited)**
- 6.4 Electromagnetic Induction, Faraday's Law, Lenz Law, SUPER DEMO**
- 6.5 Motional EMF, Dynamos, Eddy Currents, Magnetic Braking**
- 6.6 Displacement Current, Synchronous Motors, Explanation Secret Top**
- 6.7 Magnetic Levitation, Human, Superconductivity, Aurora Borealis**
- 6.8 Inductance, RL Circuits, Magnetic Field Energy**
- 6.9 Magnetic Materials, Dia- Para-, Ferromagnetism**
- 6.10 Maxwell's Equations, 600 Daffodil Ceremony**
- 6.11 Section 6 Review**

7 Section 7

- 7.1 Transformers, Car Coils, RC Circuits**
- 7.2 Driven LRC Circuits, Metal Detectors**
- 7.3 Traveling Waves, Standing Waves, Musical Instruments**
- 7.4 Destructive Resonance, Electromagnetic Waves, Speed of Light**
- 7.5 Poynting Vector, Oscillating Charges, Polarization, Radiation Pressure**
- 7.6 Snell's Law, Index of Refraction, Huygen's Principle, Illusion of Color**
- 7.7 Polarizers, Malus' Law, Light Scattering, Blue Skies, Red Sunsets**
- 7.8 Rainbows, Fog Bows, Haloes, Glories, Sun Dogs**
- 7.9 Section 7 Review**

8 Section 8

8.1 Double-slit Interference, Interferometers

8.2 Diffraction, Gratings, Resolving Power, Angular Resolution

8.3 Doppler Effect, Big Bang, Cosmology