Workout 03: R Package binomial

Stat 133, Spring 2019

The purpose of this assignment is to create an R package that implements functions for calculating probabilities of a Binomial random variable, and related calculations such as the probability distribution, the expected value, variance, etc.

Here's a list of resources that may help you complete this assignment:

• Pack YouR Code: www.gastonsanchez.com/packyourcode

• Example package "cointoss": github.com/gastonstat/cointoss

• Package development cheat-sheet: packages-cheatsheet.pdf

• R Packages: r-pkgs.had.co.nz

Binomial Distribution

The Binomial distribution is perhaps the most famous probability distribution among discrete random variables. This is the theoretical probability model that we use when calculating probabilities about the number of successes in a fixed number of random trials performed under identical conditions (assuming a constant probability of success on each trial).

A classic example of a binomial random variable X involves the number of Heads (or Tails) that you get when tossing a coin $n \ge 0$ times. Say you are interested in finding the probability of getting three heads in four tosses of a fair coin: P(X = 3 heads in 4 tosses). To find the answer, we use the formula of the binomial probability:

$$Pr(X = k) = \binom{n}{k} p^k (1 - p)^{n-k}$$

where:

- n is the number of (fixed) trials ($n \ge 0$)
- p is the probability of success on each trial $(0 \le p \le 1)$
- 1-p is the probability of failure on each trial
- k is a variable that represents the number of successes out of n trials $(0 \le k \le n)$
- the first term in parenthesis is NOT a fraction, it is the number of combinations in which k success can occur in n trials

So, what is the probability of three heads in four tosses? Assuming that we flip a fair coin (50% chance of heads), P(X = 3) is:

$$Pr(X=3) = {4 \choose 3} 0.5^3 (1-0.5)^{4-3} = 0.25$$

If, instead of a fair coin, you have a loaded coin with a 75% chance of heads, then P(X = 3) is:

$$Pr(X=3) = {4 \choose 3} 0.75^3 (1 - 0.75)^{4-3} \approx 0.4218$$

Mean and Variance

When X is a random variable that has a binomial distribution with n trials and probability of success p, we write $X \sim Bin(n, p)$. As with most random variables, it is useful to know about the various summary measures of X.

The expected value or mean of a binomial distribution is: np. This is the expected number of successes in n trials.

The variance is given by: np(1-p). Consequently, the standard deviation is simply the square root of the variance, that is: $\sqrt{np(1-p)}$

Mode

For 0 , the most likely number of success in <math>n independent trials with probability p of success on each trial is m, the greater integer less than or equal to np + p:

how to know check if it is an integer or not

$$m = int(np + p)$$

where int denotes the integer part function. If np + p is an integer, as in the case p = 0.5 and n odd, then there are two most likely numbers, m and m - 1. Otherwise, there is a unique mode.

Skewness and Kurtosis

Other two additional measures are skewness and kurtosis. Skewness is a measure of the asymmetry of the probability distribution of a random variable about its mean. The skewness value can be positive or negative, or undefined. The skewness of a binomial random variable can be calculated as:

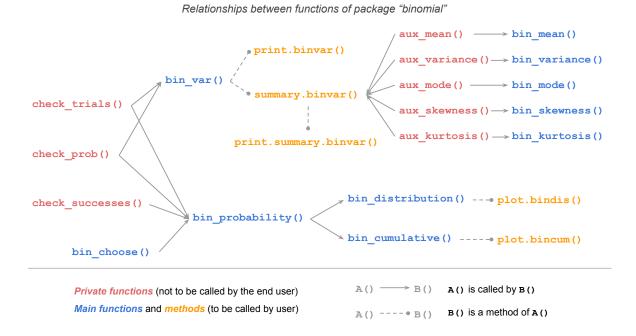
skewness =
$$\frac{1 - 2p}{\sqrt{np(1 - p)}}$$

The Kurtosis (from greek *kurtos*, meaning "curved, arching") is a measure of the "tailedness" of the probability distribution of a random variable. In a similar way to the concept of skewness, kurtosis is a descriptor of the shape of a probability distribution. For a binomial random variable, its kurtosis can be obtained as:

$$kurtosis = \frac{1 - 6p(1 - p)}{np(1 - p)}$$

1) R Functions

In order to create the package "binomial", the first stage involves writing all the functions depicted in the following diagram (more explanations below):



As you can tell from the diagram above, there are three types of functions:

- **private**: these are auxiliary functions not intended to be called by the user (in red color).
- main: these are the main functions that the user is expected to invoke (in blue color).
- **methods**: these are also public functions (in yellow color) that support classes of objects generated by some of the *main* functions.

More details about these functions is given in the following section.

Some Restrictions

R comes with built-in functions that allow you to compute binomial probabilities, as well as factorial, and combinations. However, we want to make things a bit challenging and interesting. Therefore, you are **NOT allowed** to use base R functions such as:

- choose()
- dbinom()
- pbinom()
- qbinom()
- rbinom()

Checklist

Here's a list for each of the mandatory functions in your "binomial" package.

- private checker functions:
 - check_prob()
 - check trials()
 - check_success()
- private auxiliary functions for summary measures:
 - aux mean()
 - aux_variance()
 - aux mode()
 - aux skewness()
 - aux kurtosis()
- main functions; and methods:
 - bin_choose()
 - bin probability()
 - bin distribution(); and plot.bindis()
 - bin_cumulative(); and plot.bincum()
 - bin var(); and print.binvar(), summary.binvar(), print.summary.binvar()
 - bin_mean(), bin_variance(), bin_mode(), bin_skewness(), bin_kurtosis()

1.1) Private Checker Functions

Function check_prob()

Write a *private* auxiliary function check_prob() to test if an input prob is a valid probability value (i.e. $0 \le p \le 1$).

- check_prob() takes one input: prob.
- If prob is valid, then check prob() should return TRUE.

- If prob is invalid, then check_prob() should stop() execution with an error—e.g. something like 'invalid prob value', or 'p has to be a number betwen 0 and 1'.
- Since this is a *private* function, use simple R comments to write its documentation (don't use Roxygen comments).

Function check_trials()

Write a *private* auxiliary function check_trials() to test if an input trials is a valid value for number of trials (i.e. n is a non-negative integer).

how to check if it is an integer or not

- check_trials() takes one input: trials.
- If trials is valid, then check_trials() should return TRUE.
- If trials is invalid, then check_trials() should stop() execution with an error—e.g. something like 'invalid trials value'.
- Since this is a *private* function, use simple R comments to write its documentation (don't use Roxygen comments).

Function check_success()

Write a *private* auxiliary function check_success() to test if an input success is a valid value for number of successes (i.e. $0 \le k \le n$).

- check success() takes two inputs: success and trials.
- success should be a vector of non-negative integer(s) less than or equal to trials.
- Notice that success can be of length greater than 1 (i.e. multiple successes).
- If success is valid, then check success() should return TRUE.
- If success is invalid, then check_success() should stop() execution with an error—e.g. something like 'invalid success value' or if k > n then 'success cannot be greater than trials'.
- Since this is a *private* function, use simple R comments to write its documentation (don't use Roxygen comments).

1.2) Private Auxiliary Functions

Write the following *private* auxiliary functions:

- aux mean()
- aux_variance()
- aux mode()
- aux skewness()
- aux_kurtosis()

All these functions take two arguments: **trials** and **prob**. And return the corresponding value from the computed summary measure (formulas provided in the introduction of this

document).

- Because these are *private* functions, there's no need to use the *checker* functions check_trials() and check_prob() inside the auxiliary functions.
- Each of these functions will be invoked by their corresponding *main* functions e.g. bin_mean(), bin_variance(), etc.
- Since these are *private* functions, use simple R comments to write the documentation (don't use Roxygen comments).

Here's how you should be able to invoke these functions:

```
aux_mean(10, 0.3)
## [1] 3
aux_variance(10, 0.3)
## [1] 2.1
aux_mode(10, 0.3)
## [1] 3
aux_skewness(10, 0.3)
## [1] 0.2760262
aux_kurtosis(10, 0.3)
## [1] -0.1238095
```

1.3) Function bin_choose()

Use factorial() to write a main function bin_choose() that calculates the number of combinations in which k successes can occur in n trials.

Recall that the number of combinations "n choose k" is given by:

$$\binom{n}{k} = \frac{n!}{k!(n-k)!}$$

For instance, the number of combinations in which k=2 successes can occur in n=5 trials is:

$$\binom{n=5}{k=2} = \frac{5!}{2!(5-2)!} = 10$$

- Your function should have arguments n and k.
- Try to write bin_choose() with vectorized code (i.e. avoid loops).
- If k > n, then bin_choose() should stop() execution returning an error message like "k cannot be greater than n"
- Keep in mind that you are NOT allowed to use the R function choose().
- Document your function with roxygen comments: (e.g. @title, @description, @param, @return, @export, @examples).

Here's how you should be able to invoke bin_choose()

```
bin_choose(n = 5, k = 2)
bin_choose(5, 0)
bin_choose(5, 1:3)
```

1.4) Function bin_probability()

Use bin_choose() to create a main function bin_probability().

- bin_probability() should take three arguments: success, trials, and prob.
- Use check trials() to check that trials is valid
- Use check prob() to check that prob is valid
- Use check_success() to check that success is valid
- If any of trials, prob or success is invalid, then bin_probability() should raise an error—triggered by stop()—e.g. something like 'invalid trials value' or 'invalid success value'.
- Document your function with roxygen comments: (e.g. @title, @description, @param, @return, @export, @examples).

Here's how you should be able to invoke bin_probability():

```
# probability of getting 2 successes in 5 trials
# (assuming prob of success = 0.5)
bin_probability(success = 2, trials = 5, prob = 0.5)

## [1] 0.3125

# probabilities of getting 2 or less successes in 5 trials
# (assuming prob of success = 0.5)
bin_probability(success = 0:2, trials = 5, prob = 0.5)

## [1] 0.03125 0.15625 0.31250
```

```
# 55 heads in 100 tosses of a loaded coin with 45% chance of heads bin_probability(success = 55, trials = 100, prob = 0.45)
```

```
## [1] 0.01075277
```

1.5) Function bin_distribution()

Use bin_probability() to create a main function bin_distribution().

- Your function should have two arguments trials, and prob.
- The returned output should be a data.frame with two classes: c("bindis", "data.frame")
- In other words, the primary class is "bindis" indicating that this is an object of class binomial distribution. Additionally, to keep this object as a data frame, we still need to include a class "data.frame".
- This function should return a data frame with the probability distribution: sucesses in the first column, probability in the second column.
- Document your function with roxygen comments: (e.g. @title, @description, @param, @return, @export, @examples).

Here's how you should be able to invoke bin_distribution()

```
# binomial probability distribution
bin_distribution(trials = 5, prob = 0.5)
```

```
##
     success probability
## 1
            0
                  0.03125
## 2
            1
                  0.15625
## 3
            2
                  0.31250
            3
## 4
                  0.31250
## 5
            4
                  0.15625
## 6
            5
                  0.03125
```

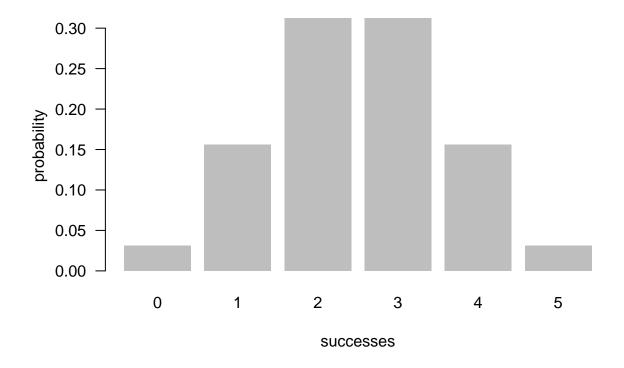
Function plot.bindis()

Write a plotting method (i.e. a function) plot.bindis() that graphs a barplot to display the probability histogram of a binomial distribution object "bindis".

• Since this is a method, you just need to document your function with the roxygen comment: @export.

Here's an example of how to invoke the plot method. You are welcome to plot a graph with more visual appeal than the image depicted below.

```
# plotting binomial probability distribution
dis1 <- bin_distribution(trials = 5, prob = 0.5)
plot(dis1)</pre>
```



1.6) Function bin_cumulative()

Use bin_cumulative() to create a main function bin_cumulative().

- Your function should have two arguments trials, and prob.
- The returned output should be a data.frame with two classes: c("bincum", "data.frame")
- In other words, the primary class is "bincum" indicating that this is an object of class binomial cumulative distribution. Additionally, to keep this object as a data frame, we still need to include a class "data.frame".
- This function should return a data frame with both the probability distribution and the cumulative probabilities: sucesses in the first column, probability in the second column, and cumulative in the third column.
- Document your function with roxygen comments: (e.g. @title, @description, @param, @return, @export, @examples).

Here's how you should be able to invoke bin cumulative()

```
# binomial cumulative distribution
bin_cumulative(trials = 5, prob = 0.5)
##
     success probability cumulative
## 1
           0
                 0.03125
                             0.03125
## 2
           1
                 0.15625
                             0.18750
           2
                 0.31250
                             0.50000
## 3
```

```
## 4 3 0.31250 0.81250
## 5 4 0.15625 0.96875
## 6 5 0.03125 1.00000
```

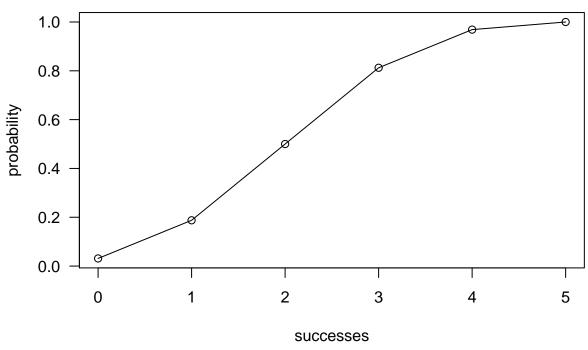
Function plot.bincum()

Write a plotting method (i.e. a function) plot.bincum() that graphs the cumulative distribution in ab object "bincum".

• Since this is a method, you just need to document your function with the roxygen comment: @export.

Here's an example of how to invoke the plot method. You are welcome to plot a graph with more visual appeal than the image depicted below.

```
# plotting binomial cumulative distribution
dis2 <- bin_cumulative(trials = 5, prob = 0.5)
plot(dis2)</pre>
```



1.7) Function bin_variable()

Another function to include in your "binomial" package is bin variable().

- This is a *main* function that takes two arguments: trials and prob
- This function should return an object of class "binvar", that is, a binomial random variable object.

- This function should invoke check trials() and <a href="mailto:check prob()
- The returned object should be a list with named elements:
 - trials: number of trials
 - prob: probability of success
- Document your function with roxygen comments: (e.g. @title, @description, @param, @return, @export, @examples).

Because bin_variable() will return an object of class "binvar", you will also need to implement methods: print.binvar(), summary.binvar(), and print.summary.binvar().

Method print.binvar()

Create a method function print.binvar() to be able to nicely print the content of an object "binvar". See example below.

• Since this is a method, you just need to document your function with the roxygen comment: @export.

Here's an example of how you should be able to invoke bin_variable(), and its printed output:

```
bin1 <- bin_variable(trials = 10, p = 0.3)
bin1</pre>
```

"Binomial variable"

Paramaters

- number of trials: 10
- prob of success : 0.3

Methods summary.binvar() and print.summary.binvar()

To get a full summary description of an object "binvar", you need to create a function summary.binvar().

- This function takes an object of class "binvar"
- The returned output is a list of class "summary.binvar" containing named elements:
 - trials: number of trials
 - prob: probability of success
 - mean: mean or expected value
 - variance: variance
 - mode: mode
 - skewness: skewness
 - kurtosis: kurtosis

- Use the *private* auxiliary functions: aux_mean(), aux_variance(), etc. to compute the summary measures.
- Since this is a method, you just need to document your function with the roxygen comment: @export.

In order to nicely print the contents of an object "summary.binvar", you also need to write a print method: print.summary.binvar(). See example below:

```
bin1 <- bin_variable(trials = 10, p = 0.3)
binsum1 <- summary(bin1)
binsum1</pre>
```

"Summary Binomial"

Paramaters

- number of trials: 10
- prob of success : 0.3

Measures

- mean : 3 - variance: 2.1 - mode : 3

- skewness: 0.2760262 - kurtosis: -0.1238095

1.8) Functions of measures

Finally, your "binomial" package should also contain *main* functions for each of the summary measures: e.g. bin_mean(), bin_variance(), etc.

- These are *main* functions that take two arguments: trials and prob
- Use check_trials() to check that trials is valid
- Use check_prob() to check that prob is valid
- Invoke your *auxiliary* functions to do the corresponding calculation. For instance: aux_mean() gets called by bin_mean().

Here's how you should be able to invoke these functions:

```
bin_mean(10, 0.3)
## [1] 3
bin_variance(10, 0.3)
## [1] 2.1
```

```
bin_mode(10, 0.3)

## [1] 3

bin_skewness(10, 0.3)

## [1] 0.2760262

bin_kurtosis(10, 0.3)

## [1] -0.1238095
```

2) Tests

Your "binomial" package should include tests—via the package "testthat"—for the following functions, and their *contexts*:

- Context for checkers:
 - check prob()
 - check_trials()
 - check_success()
- Context for summary measures:
 - aux_mean()
 - aux_variance()
 - aux_mode()
 - aux skewness()
 - aux kurtosis()
- Context for binomial:
 - bin choose()
 - bin probability()
 - bin distribution()
 - bin cumulative()

You will need to come up with at least three *expectations* for each of the above functions. For example, say you are testing <code>check_prob()</code>, you may want to use expectations to confirm that:

- prob is a number between 0 and 1
- prob is of length 1
- getting an error if prob is invalid

Recall that, when writing test for functions of an R package, you need to create a subdirectory tests/ containing a subdirectory testthat/ which will contain the R scripts for each *context*.

3) Package Creation

Carefully check the example package "cointoss" to get some hints and inspiration. We expect that you write your own code, with your consistent style (avoid the temptation of copy/plagiarism):

https://github.com/gastonstat/cointoss

Vignette

Your package should also include an introductory vignette that shows the user how to utilize the various functionalities of the "binomial" package.

Package Structure

After completion, your package "binomial" should have the following filestructure:

```
binomial/
.Rbuildignore
binomial.Rproj
devtools-flow.R
DESCRIPTION
NAMESPACE
README.md
R/
man/
tests/
```

Submission

vignettes/

- Create a folder (i.e. subdirectory) binomial/ in your github classroom repository. This will be the folder of your package.
- The due date is May-01 (before midnight). You will have to show your package to your GSI during lab, either May-02 or May-03. We will only grade committed work pushed to your classroom repo before the deadline.