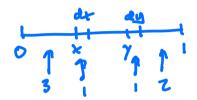
Stat 134 Lec 36 (MTZ review)

Warmun 11:00-11:10

Let (X, Y) have joint density $f_{X,Y}(x, y) = 420x^3(1 - y)^2$ for 0 < x < y < 1.

(a)

Fill in the blanks: X and Y represent the _____ smallest and ____ smallest of i.i.d. Unif (0,1) random variables, respectively.



To And marying!

X~ U(4) out at 7 ~ Betr (4,4)

Let (X, Y) have joint density $f_{X,Y}(x, y) = 420x^3(1 - y)^2$ for 0 < x < y < 1.

(a) Find P(3X < Y);

$$= \frac{A^{1} \cdot 2}{A^{2}} \left\{ \begin{array}{c} 0 \\ 1 - 0 \\ 1 \end{array} \right\} \left\{ \begin{array}{c} 0 \\ 1 - 0$$

By Method Z (uniform specing) P(X/3)

$$f_{X,Y}(x,y) = \frac{\lambda}{y} e^{-\lambda y}, \quad 0 < x < y.$$

Find the marginal distribution of Y.

$$= \frac{1}{\sqrt{3}} = \frac$$

- (Change of variables, order statistics) Let $X \sim \text{Uniform } (-1,1)$ (this is a continuous uniform random variable).
 - (a) Compute the density of $Y = e^X$.

Change of variables
$$X = ln(4) \qquad \frac{d9(x)}{dx} = e^{x}$$

$$f_{y}(y) = \frac{f_{x}(ln(y))}{e^{ln(y)}} = \frac{1}{e^{y}} \quad \text{for } e^{y} \leq (4 < e^{x})$$
Share $-1 \leq ln(y) \leq 1 \leq e^{x}$

(b) Let now X_1 , X_2 be i.i.d. uniform random variables, and for each i = 1, 2, let $Y_i = e^{X_i}$. What is the joint density of $Y_{(1)}$ and $Y_{(2)}$, the minimum and the maximum of the Y_i 's?

$$f(x,y) = \begin{pmatrix} 2 \\ 1/1 \end{pmatrix} \cdot 2x \cdot 2y = \begin{cases} 2xy \\ 2xy \end{cases}$$

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Review M6F Mx 41= E(exx)

Main properties

(2)
$$M_{\alpha X}(t) = M_{X}(\alpha t)$$

3)
$$M(0) = E(x)$$

 $M'(0) = E(x)$
 X
 $M(0) = E(x)$
 X

$$M$$
 It $\times_{1}...,\times_{n}$ are independent then
$$M_{X_{1}+...+}\times_{n}(+)=M_{X_{1}}(+)...M_{X_{n}}(+)$$

(5) M (4) is unique for t in a neighborhood of 0. So if Mx(t) = e^{xx}, for t around 0, then x N(0,1).

$$\frac{S_n-nu}{\sqrt{n}\sigma} \rightarrow \frac{2}{\sqrt{N(0,1)}} as n \rightarrow \infty$$

We will show that for N longe,

EY: and Z have the some MOF

Note that

$$E(Y_{i}) = E(X_{i}^{2} - M) = \frac{1}{\sigma} E(X_{i}^{2} - M) = 0$$

$$Ver(Y_{i}^{2}) = \frac{1}{\sigma^{2}} Ver(X_{i}^{2} - M) = \frac{1}{\sigma^{2}} \cdot \sigma^{2} = 1$$

$$So E^{2}(Y_{i}^{2}) = Ver(Y_{i}^{2}) + E(Y_{i}^{2})^{2} = 1$$

Make a Taylor sorber of M, th available 0;

$$M_{\chi}(t) = M(t) = M_{\chi}(0) + M_$$

& Gamma

- 5. Travelers arrive at an airport Information desk according to a Poisson process at the rate of 15 per hour. Assume that each traveler arriving at the desk has a 60% chance of being male and a 40% chance of being female, independent of all other travelers.
- a) Fill in the blank with a number: The fifth male traveler is expected to arrive at the desk minutes after the first male traveler.

The Pois (15.
$$\frac{1}{60}$$
)

M N Pois (14. (16)) = Pois (9/60)

F Nois (14. (14)) = Pois (6/60)

To = world three of 5th male ~ Gamma (5, 9/60)

The in the pois (1, 9/60)

E(To - The E(To) - E(The) = 41.60 = 4/9/60

The interpretation of the pois of the possible integers. The obtherence of the possible integers. The obtherence

- 5. Travelers arrive at an airport Information desk according to a Poisson process at the rate of 15 per hour. Assume that each traveler arriving at the desk has a 60% chance of being male and a 40% chance of being female, independent of all other travelers.
- **b)** Find the chance that the fifth male traveler arrives at the desk more than 30 minutes after the first male traveler.