

## *Stat 134: Section 17*

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### *Conceptual Review*

Please discuss these short questions with those around you in section. These problems are intended to highlight concepts that will be relevant for today's problems.

- a. What is a joint distribution? Can you come up with examples where the joint distribution is jointly independent and dependent?
- b. What is the joint density function and marginal density?
- c. Describe the joint uniform distribution.

### *Problem 1*

Let  $X, Y$  be independently distributed and uniform on  $(0, 1)$ . Find:

$$P\left(Y \geq \frac{1}{2} \mid Y \geq 1 - 2X\right).$$

*Ex 5.1.3 in Pitman's Probability*

*Problem 2*

For a straight stick, we pick two points uniformly and independently. What is the probability that the three parts can form a triangle? Ex 5.1.9 in *Pitman's Probability*

*Problem 3*

Suppose  $X_1, X_2, X_3$  are independent exponential distributions with  $\lambda_1, \lambda_2, \lambda_3$ . Find  $P(X_1 < X_2 < X_3)$ . Ex 5.2.16 in *Pitman's Probability*