

Stat 134: Change of Variable/Operations Review Session

December 5th, 2018

Conceptual Review

- a. Write out the five steps for computing a change of variable density.
- b. What is the formula for $Z = X + Y$, where X, Y are continuous random variables?
- c. What is the formula for $Z = X/Y$ where X, Y are non-negative continuous random variables?

Problem 1: Properties of Exponentials

Suppose X is an $\text{Exponential}(\lambda)$ and Y is a $\text{Gamma}(n, \lambda)$. Let $W = X/Y$.

- a. Find the distribution of cX
- b. Find the distribution of cY
- c. Use the above parts to find the CDF of W

Problem 2

Let X be the minimum of 6 independent $\text{Uniform}(0,1)$ distributions and Y be the maximum. Find the distribution of $Z = X/Y$ and $Z = Y - X$

Problem 3

Let U_1, U_2, \dots, U_n be independent $\text{Uniform}(0,1)$ random variables.

- a. Find the distribution of $-\log(U_1 U_2 \dots U_n)$
- b. Use the above to find the probability $-\log(U_1 U_2 \dots U_{10}) > 8$