A drawer contains s black socks and s white socks (s> 0). I pull two socks out at random without replacement and call that my first pair. Then I pull out two socks at random without replacement and call that my second pair. I proceed in this way until I have s pairs and the drawer is empty. Find the expected number of pairs in which two socks are different colors.

$$X = \text{Number of pairs}$$
 (out of S) of unismetches.

 $T_2 = \{1 \text{ if } 2^{nQ} \text{ pqi/is mismetch} \}$
 $\{0 \text{ elso}\}$
 $P = 2.5 \cdot 5 \text{ elso}$
 $\{1 \cdot (5) \cdot ($

Last time sec 3.2 Expectation $E(x) = \{x \in X \mid x = x\}$

If X is a count, X can be withen as a sum of indicators

Sum of indicators $X = I_1 + I_2 + \cdots + I_n, \quad I_s = \begin{cases} 1 & \text{Prob } p \\ 0 & \text{prob } 1-p \end{cases}$

E(I) = 1.P + 0. (1-P) = P.

Idea Even it indicators are dependent the Expedation of each indicator is an unconditional Probability.

Try Choosing indicators such that all indicates have the some expectation P.

then E(x) = n.P

we howed it X~Bin (np) => E(x) =np

if X~ HG(1,N,6) => E(X)=nG

X= # aces in a porer hand from a deck

 $\times \wedge HG(n, N, G) = 4$

X= I, +I2+ I3+ I4+ T5

Iz={1 It zwe could be on ace / P= 452

 $E(x) \approx 5 \cdot E(\Sigma_1) = 5 \cdot \left(\frac{4}{5}\right)$

(1) SEC 3.2 More expectation with indicator examples

U sec 3.2 talksom formula

(1) Sec 3.2 more expectation/indicator examples

ex Consider a 5 card deck consisting of 2,2,3,4,5

should the cards.

Let X = number of cards before the first 2.

a) what are the range of values of X.

O, 1,2,3

b) write X as a Sum of indicators

 $X = I_3 + I_4 + I_5$ C) How is an indicator defined. $I_3 = \begin{cases} 1 & \text{if 3 before Close 2} \\ 0 & \text{eve} \end{cases}$

d) Find $E(I_3)$ six on here have I_3 I_4 I_5 I_5 I_6 I_7 I_8 I_8

e) Find E(x) you can not 3

E(x) = E(Iz) + E(Ii) + E(Is) = (1)

1/3

1/3

Stat 134

- 1. Consider a well shuffled deck of cards. The expected number of cards before the first ace is?
 - a 52/5
 - **b** 48/5
 - c 48/4
 - d none of the above

$$X = I_1 + I_2 + \dots + I_{48}$$

$$I_2 = \begin{cases} 1 & \text{if } 2^{48} \\ \text{order} \end{cases}$$

$$V = I_1 + I_2 + \dots + I_{48}$$

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$$V = I_1 + \dots + I_{48}$$

$$\frac{\text{ec 3.2 Tall Sum Countable for expectation}}{\text{Soffore } \times \text{is a count } 0,1,7,3...}$$

$$E(x) = 0.R(x=0) + 1.R(x=1) + 2.R(x=2) + \dots$$

$$= \frac{1.R(x=1) + 2.R(x=2) + \dots}{P_2}$$

$$= \frac{P_1}{P_2} \frac{P_2}{P_3} \frac{P_4}{P_4}$$

$$= \frac{P_4}{P_4} \frac{P_4}{P_4} \frac{P_4}{P_4}$$

$$= \frac{P(x=1) + P(x=2) + P(x=3) + \dots}{P_4} \frac{P_4}{P_4}$$

$$= \frac{P(x=1) + P(x=2) + P(x=3) + \dots}{P_4} \frac{P_4}{P_4}$$

This is weth when it is easy to find P(XZK)

ez A fair die is rolled 10 thmes.

Let X=max(X1,...,X10)

Find P(XZK)

$$P(x \le k) = 1 - P(x < k)$$

$$= 1 - P(x_1 < k) P(x_2 < k) ... P(x_0 < k)$$

$$= 1 - P(x_1 < k) P(x_2 < k) ... P(x_0 < k)$$

$$= 1 - P(x_1 < k) P(x_2 < k) ... P(x_0 < k)$$

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$$= 1 - P(x_1 < k) P(x_2 < k) ... P(x_0 < k)$$

$$= Q - \left(\frac{P}{T}\right)_{10} \left[l_{10} + S_{10} + 3_{10} + l_{10} + 2_{10} \right] = \underbrace{2.85}_{10}$$

$$= \left[l_{10} \left(\frac{P}{T}\right)_{10} + \left(\frac{P}{T}\right)_{10} + \left(\frac{P}{T}\right)_{10} + \left(\frac{P}{T}\right)_{10} \right] = \underbrace{2.85}_{10}$$

$$= \left[(x) = b(x51) + b(x55) + \dots + b(x59) + b(x53) + \dots + b(x5) + \dots + b$$

EX A fair die is rolled 3 times,
$$X_1, X_2, X_3$$
.
Let Y be the sum of the largest Z numbers,
Wotice that $Y = X_1 + X_2 + X_3 - min(X_1, X_2, X_3)$

a) Find
$$P(m)n(X_1,X_2,X_3) \geq 2$$
) Pleture

=
$$P(x_1 \ge 2)^3 = (\frac{5}{6})^3$$

(b) Find E (min (x, x, x, x))

P(min 21) + P(min 22) + ... + V(min 26)

P(x, 21)³ (x, 22)³ (26)³

=
$$\frac{1}{3}$$
 + $(\frac{5}{6})^3$ + $(\frac{4}{6})^3$ + ... + $(\frac{1}{6})^3$ = $\frac{1}{6}$ (6+5+...+)

Extra Practice

. (3 pts) On a telephone wire, n birds sit arranged in a line. A noise startles them, causing each bird to look left or right at random. Calculate the expected number of birds which are not seen by an adjacent bird.

$$X = \# \text{ bluds not seen by an adjacent blud}$$

$$X = T, + T_z + ... + T_n$$

$$T_1 = \begin{cases} 1 & \text{if } 1^{\text{st}} \text{ blud not seen} \\ 0 & \text{else} \end{cases}$$

$$T_2 = \begin{cases} 1 & \text{if } 2^{\text{nd}} \text{ blud not seen} \\ 0 & \text{else} \end{cases}$$

$$T_2 = \begin{cases} 1 & \text{if } 2^{\text{nd}} \text{ blud not seen} \\ 0 & \text{else} \end{cases}$$

$$E(x) = 2 \cdot 1/2 + (n-2) \cdot 1/4$$