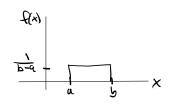
## Stat 134 lec 26

### Warmon: 11:00-11:10

Recall that the commulative abstribution function (CDF) for a RV X is  $F(x) = P(X \le x)$ 

Dran the CDF for each of the distributions below?

生 X へ Un H (a,b)



P(x)

A

B

A

B

A

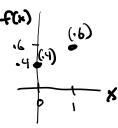
B

A

B

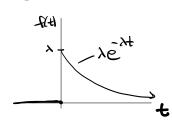
A

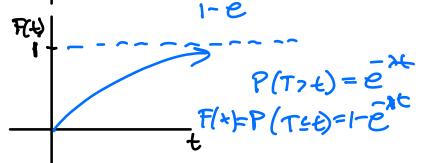
Ex XV Bernoull (6=19)



F(x)

STN EWW





Today

- Drewlen MGF E) Sec 4.5 Find CDF of a wixed distribution
- 3 Sec 4.5 Using CDF to find E(x)

$$f_{(x)} = \frac{1}{1} \chi_{(x)} = \frac{1}{2} \chi_{(x)} =$$

$$M_X(t) = \left(\frac{\lambda}{\lambda - t}\right), t < \lambda$$

Property of WGF:

of zero, iff x = y (i.e. x and y have the same distribution

Knowing the distribution uniquely specifies the MGF

And

Knowing the MGF uniquely specifies the distribution

#### **Stat 134**

### Monday April 1 339

1. Let X have density  $f(x) = xe^{-x}$  for x > 0. X ~ 69mma (2,1) The MGF is?

$$\mathbf{a} M_{\mathbf{X}}(\mathbf{t}) = \frac{1}{1-\mathbf{t}} \text{ for } t < 1$$

$$\mathbf{a} \ \mathrm{M}_{\mathrm{X}}(\mathrm{t}) = \frac{1}{1-\mathrm{t}} \ \mathrm{for} \ t < 1$$

$$\mathbf{b} \ \mathrm{M}_{\mathrm{X}}(\mathrm{t}) = \frac{1}{(1-\mathrm{t})^2} \ \mathrm{for} \ t < 1$$

$$\mathbf{a} \ \mathrm{M}_{\mathrm{Y}}(\mathrm{t}) = \frac{1}{(1-\mathrm{t})^2} \ \mathrm{for} \ t < 1$$

$$\mathbf{a} \ \mathrm{M}_{\mathrm{Y}}(\mathrm{t}) = \frac{1}{(1-\mathrm{t})^2} \ \mathrm{for} \ t < 1$$

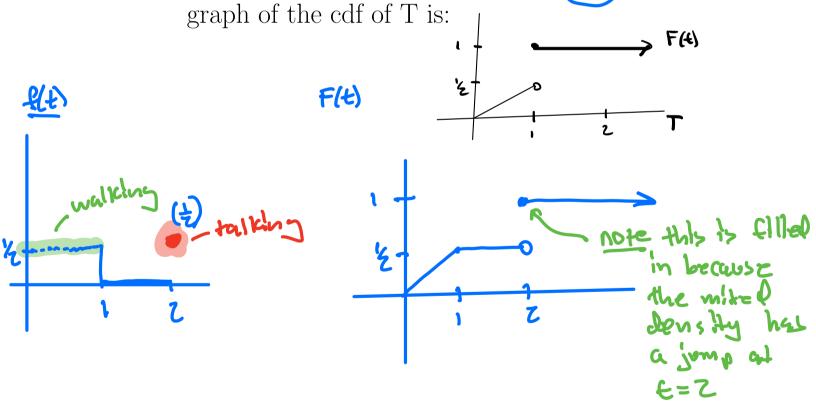
$$\mathbf{c} \ M_{X}(t) = \frac{1}{(1+t)^{2}} \text{ for } t > -1$$

d none of the above

# (2) SEC 4.5 CDF of whee distributions

## EK EK

Suppose you are trying to discretly leave a party. Your time to leave is uniform from 0 to 2 minutes. However, if your walk to the exit takes more than 1 minute, you run into a friend at the door and and must spend the full 2 minutes to leave. Let T represent the time it takes you to leave. True or false the

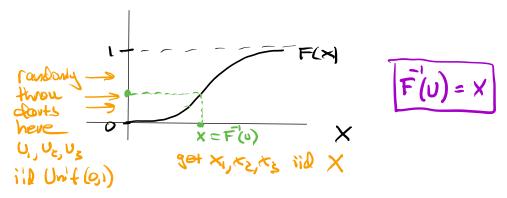


see #9 P324

(3) Sec 4.5 Using CDF to that E(X) for X>0

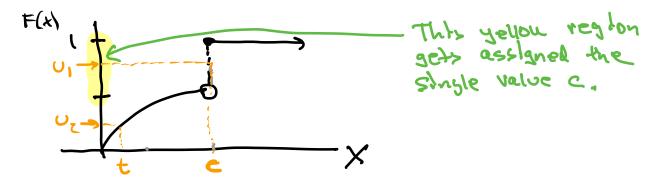
# Inverse abstribution function, F'(u)

Let X have CDF F(X)



Note: doesn't have to be continuous RV.

EX=min(Ic), Tr Exp()



Thun (1522) - Proot at end of lecture.

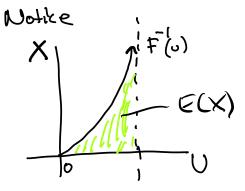
Let X have CDF F.

Then the RV F'(U) = X

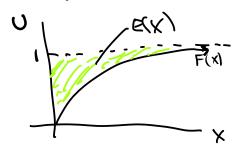


How is this useful to us finding E(x)?

 $E(X) = E(F'(U)) = \int_{F(U)}^{1} f(u) du$ 



Now reflect
the above graph
about the
diagonal y=x



we can find the shaded region by integrating 1- F(x) with respect to x:

The Let X be a pos. roulon voviable, ust CDF F. (continuos, obserte, mixed),  $E(X) = \int_{-\infty}^{\infty} (1 - F(x)) dx$ FCK

= T~ expon (k)

F (1) = 1- = >=

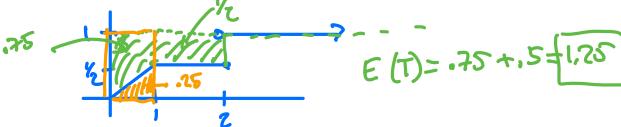
the second has earlier to calculate

E(X) using the case (avoid doing the arts):

E(T) = [the de



Suppose you are trying to discretly leave a party. Your time to leave is uniform from 0 to 2 minutes. However, if your walk to the exit takes more than 1 minute, you run into a friend at the door and and must spend the full 2 minutes to leave. Let T represent the time it takes you to leave. True or false, the graph of the cdf of T is: F : A E(T)



## Appendix

/ See P 322 in book

Claim for any CDF F

$$X = F^{-1}(U) \text{ is a RV with cdf } F$$

Proof/ let  $X = F^{-1}(U)$ 

$$F(x) = P(X \le x) \text{ we will show } F_{X} = F$$

$$= P(F^{-1}(U) \le x)$$

$$= P(F F^{-1}(U) \le F(x)) \text{ increasing } F(U \le F(x))$$

$$= F(x) \text{ share } P(U \le u) = u$$