

## *Stat 134: Section 23*

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### ***Conceptual Review***

Please discuss these short questions with those around you in section. These problems are intended to highlight concepts from lecture that will be relevant for today's problems.

- a. Suppose  $X_1 + X_2 + \dots + X_k$  is a constant, where  $X_i$ 's are identically distributed. What is  $\text{Corr}(X_i, X_j)$ ,  $0 < i < j < k$ ?

### *Problem 1*

Let  $Y$  have exponential distribution with mean 0.5. Let  $X$  be such that, conditional on  $Y = y$ ,  $X$  has exponential distribution with mean  $y$ . Find:

- a.  $\mathbb{E}(X)$ ;  
b.  $\text{Corr}(X, Y)$ .

*Ex 6.rev.8 in Pitman's Probability*

*Problem 2*

Let  $X$  and  $Y$  be the minimum and maximum of 8 independent uniform  $(0, 1)$  random variables respectively. Find  $\text{Corr}(X, Y)$ .