stat 134 lec 9

01:P-00:P homes

stat 134 concept test

September $12\ 2022$

The joint distribution of X and Y is drawn below:

	3/8	1/2	1/8	P(x)
l	4	1/3	1/z	7/5
0	1/8	Ye	1/24	1/3
XX	0	١	2	

- a) X and Y are independent
- b) If we divide both rows by their marginal probability we get the same answer.

c)
$$P(X = x|Y = 0) = P(X = x|Y = 1)$$

d) All of the above

re call	P(X== Y=0)
6 (X= * () = 0)	= P(X=x, Y=0) P(Y=0)
P(K2x(1) =	P(t= 1, Y=1)
	P(7=1)

Last time

Sec 3.1 Randon Vailables

The event (x=x, Y=y) is the intersection of events
X=x and Y=y. Sometimes written (x,y)

the Probability X and Y satisfies some condition (i.e P(X+Y=s) is the som of P(X,Y) that satisfy that condition.

P(X+Y=s) = P(x,y) = P(x,s-x) $(x,y): x+y=s \qquad q | x$

Independence of (x, Y, Z) means $P(x=x, Y=y, Z=z) = P(x=x)P(Y=y)P(Z=z) \quad \text{for all } x=X, Z=Z.$ Today

(2) Sec 3.1 Sums of independent Polsons b Address
(2) Sec 3.2 Expectation of a RV.

(1) Sum at independent Poisson is Poisson

informal arguenent; Rob(1)

X₁ ~ Bin (1000, 1000)

X₂ ~ Bin (2000, 1000)

X₁ + ×₂ ~ ? Bin (3000, 1000) ~ Poly (3)

proven in amount to these

Claim It X ~ Pols (M) and Yn Pols (X)

are independent then

S=X+1~Pb(n+x).

$$E(x) = \sum_{x \in X} x \cdot P(x = x)$$

Proporties of Expectation - P167 Pitman

$$E(C) = E(X) + E(Y) \qquad (X, Y \text{ dont need to be independent})$$

$$E(X+Y) = E(X) + E(Y) \qquad (X, Y \text{ dont need to be independent})$$

$$E(X+Y) = G(X) + G(X) + G(X) + G(X) = G(X) + G(X)$$

$$E(X+Y) = G(X) + G(X$$

Inducators

+ E(X)

An indicator is a RV that has only Z values I (u/probp) and O(nith prob 1-p)

RV that are Counts an other be written as a sum of indigetors.

EX X~ Bln(n,p)

Successed in a Bernoull p trials, X = H heads in a film of P commentation is heads $X = T_1 + T_2 + \dots + T_n$ $T_2 = \{0, p\} \text{ ever}$ Where Is= > if it it trial
Success

indicators are independent since trials are indep.

X= # aces in a porev hand from a deck X~ H6(5,52,4)

a) what are the range of values of X?
0,1,2,3,4

b) unite x as a sum of indicators, X=I,+I2+I3+Iy+I5.

c) How 12 Iz defined?

Te = 91 it 2nd and is are

Te = 90 else

d) Find E(Iz) = 4/52

e) Find E(X) = 5, 4 5

Another more complicated solution?

Note

You may define
$$T_z = \begin{cases} 1 & \text{if } 2d \\ 0 & \text{else} \end{cases}$$

So

 $X = T_1 + 2T_2 + 3T_3 + 4T_4$

This is also correct but more

Complicated.

 $E(T_1) = \frac{(4)(48)}{(52)}$
 $E(T_2) = \frac{(4)(48)}{(52)}$
 $E(T_3) = \frac{(4)(48)}{(52)}$
 $E(T_4) = \frac{(4)(48)}{(52)}$
 $E(T_4) = \frac{(4)(48)}{(52)}$
 $E(T_4) = \frac{(4)(48)}{(52)}$

Appendit

Claim It X ~ Pois (M) and Yn Pols (X)

are independent them

S=X+1~Bb(m+x)

To prove this you need to know 2 facts:

Recall bironial theorem

Recoll X~ Pols (M)

PE/P(S=s) = P(X=0, Y=s) + P(X=1, Y=S-1) +

Summathen notation ... P(X=S,Y=0) $= \sum_{k=1}^{\infty} P(X=K,Y=S-K)$

=
$$\sum_{x=0}^{k-0} P(x=x)P(y=s-x)$$