# Package 'SDRcausal'

November 30, 2020

140Velliber 50, 2020
Version 0.3.0
<b>Date</b> 2020-06-11
Title SDRcausal
Author Filip Edstrom [aut, cre]
Maintainer Mohammad Ghasempour < mohammad.ghasempour@umu.se>
<b>Description</b> Provides two semiparametric estimators, imp.ate and ipw.ate.
Encoding UTF-8
Imports stats, ggplot2
Suggests nloptr
LazyData true
License GPL (>= 2)
RoxygenNote 7.1.0
NeedsCompilation yes

# R topics documented:

Index

aipw.ate .																					2
aipw.var .																					3
aipw2.ate																					2
b10_fun .																					4
b_fun																					(
cms.ps.sem	i.																				- 7
cms.semi																					8
example_da	ıta																				10
imp.ate .																					1
imp.val .																					13
imp.var .																					15
imp2.var .																					16
inf.ate																					18
ipw.ate																					
ipw.var																					23
nw_kernel_	reg	res	S																		25
plot.imp .																					20
plot.ipw .																					2
ps.semi .												•			•				•		28
																					3(

2 aipw.ate

aipw.ate

Combines IPW and IMP estimators to form the augmented IPW, AIPW

# **Description**

Augmented IPW (AIPW) as in Ghosh, Ma, & De Luna (2020).

### Usage

```
aipw.ate(y, treated, imp, ipw)
```

### **Arguments**

У	Observed response
treated	A binary vetor indicating treatment
imp	imp output object from imp.ate
ipw	ipw output object from ipw.ate

# Value

The AIPW estimation (AIPW) of the average treatment effect (ATE).

#### References

Ghosh, T., Ma, Y., & De Luna, X. (2020). Sufficient dimension reduction for feasible and robust estimation of average causal effect. Statistica Sinica, accepted.

```
# Using example data from package SDRcausal
library(SDRcausal)
# Import example data
x <- SDRcausal::covariates
y <- SDRcausal::outcomes
trt <- SDRcausal::treated</pre>
b1 <- SDRcausal::beta1_guess</pre>
b0 <- SDRcausal::beta0_guess</pre>
alp <- SDRcausal::alpha_guess</pre>
# Perform semiparametric imputation
imp <- SDRcausal::imp.ate(x, y, trt, b1, b0,</pre>
           explicit_bandwidth = TRUE, bwc_dim_red1 = 1, bwc_impute1 = 1,
           bwc_dim_red0 = 1, bwc_impute0 = 1)
# Perform semiparametric inverse probability weighting
ipw <- SDRcausal::ipw.ate(x, y, trt, alp, bwc_dim_red = 8,</pre>
           bwc_prop_score = 8)
# Calculate the Augmented IPW (AIPW)
aipw <- SDRcausal::aipw.ate(y, trt, imp, ipw)</pre>
```

aipw.var 3

aipw.var

Estimates Augmented Inverse Probability variance

### **Description**

Variance of the Augmented IPW as in Ghosh, Ma, & De Luna (2020).

# Usage

```
aipw.var(
   x,
   y,
   treated,
   imp,
   ipw,
   bandwidth_scale1 = imp$bw1,
   bandwidth_scale0 = imp$bw0,
   bandwidth_scale_pr = ipw$bw_dr,
   kernel = "EPAN",
   explicit_bandwidth = TRUE,
   gauss_cutoff = 0.001,
   num_deriv_h = 1e-08,
   verbose = FALSE
)
```

# **Arguments**

x Covariate matrixy Response vectortreated Binary vetor indicating treatment

bandwidth\_scale1

Scaling of the calculated bandwidth, or in case of explicit\_bandwidth = TRUE, the actual bandwidth for the estimations of  $E(\cdot|\beta_1^TX)$ . The default value is imp\$bw1. If this default value is used, one should use the default value TRUE for explicit\_bandwidth.

bandwidth\_scale0

Scaling of the calculated bandwidth, or in case of explicit\_bandwidth = TRUE, the actual bandwidth for the estimations of  $E(\cdot|\beta_0^TX)$ . The default value is imp\$bw0. If this default value is used, one should use the default value TRUE for explicit\_bandwidth.

bandwidth\_scale\_pr

Scaling of the calculated bandwidth, or in case of explicit\_bandwidth = TRUE, the actual bandwidth for the estimations of  $E(\cdot|\alpha^TX)$ . The default value is ipw\$bw\_dr. If this default value is used, one should use the default value TRUE for explicit\_bandwidth.

kernel Specifies which kernel function to be used. The default is "EPAN".

4 aipw2.ate

```
explicit_bandwidth
```

Specifies if bandwidth\_scale will be used as the bandwidth or if it will be calculated as bandwidth\_scale \*  $sd(\beta^T x)$  \*  $n^{(1/5)}$ . The default value is TRUE.

gauss\_cutoff Cutoff value for Gaussian kernel. The default value is 1e-3.

num\_deriv\_h Step size of numerical derivative. The default value is 1e-6.

verbose Specifies if the program should print output while running. The default value is

FALSE.

#### Value

The variance of Augmented IPW estimator.

#### References

Ghosh, T., Ma, Y., & De Luna, X. (2020). Sufficient dimension reduction for feasible and robust estimation of average causal effect. Statistica Sinica, accepted.

# **Examples**

```
# Using example data from package SDRcausal
library(SDRcausal)
# Import example data
x <- SDRcausal::covariates
y <- SDRcausal::outcomes</pre>
trt <- SDRcausal::treated</pre>
b1 <- SDRcausal::beta1_guess</pre>
b0 <- SDRcausal::beta0_guess</pre>
alp <- SDRcausal::alpha_guess</pre>
# Perform semiparametric imputation
imp <- SDRcausal::imp.ate(x, y, trt, b1, b0,</pre>
           explicit_bandwidth = TRUE, bwc_dim_red1 = 1, bwc_impute1 = 1,
           bwc_dim_red0 = 1, bwc_impute0 = 1)
# Perform semiparametric inverse probability weighting
ipw <- SDRcausal::ipw.ate(x, y, trt, alp, bwc_dim_red = 10,</pre>
           bwc_prop_score = 18)
# Calculate the variance of the Augmented IPW (AIPW)
var <- SDRcausal::aipw.var(x, y, trt, imp, ipw,</pre>
           bandwidth_scale1 = imp$bw1, bandwidth_scale0 = imp$bw0,
           bandwidth_scale_pr = ipw$bw_pr)
```

aipw2.ate

Improved Augmented IPW (AIPW2)

# **Description**

Combines IPW and IMP estimators to form the improved augmented IPW, AIPW2 as in Ghosh, Ma, & De Luna (2020).

*b*10\_fun 5

# Usage

```
aipw2.ate(y, treated, imp, ipw)
```

## **Arguments**

У	Observed response
treated	A binary vetor indicating treatment
imp	imp output object from imp.ate
ipw	ipw output object from ipw.ate

#### Value

The improved augmented IPW estimation (AIPW2) of the average treatment effect (ATE).

### References

Ghosh, T., Ma, Y., & De Luna, X. (2020). Sufficient dimension reduction for feasible and robust estimation of average causal effect. Statistica Sinica, accepted.

# **Examples**

```
# Using example data from package SDRcausal
library(SDRcausal)
# Import example data
x <- SDRcausal::covariates
y <- SDRcausal::outcomes
trt <- SDRcausal::treated</pre>
b1 <- SDRcausal::beta1_guess</pre>
b0 <- SDRcausal::beta0_guess</pre>
alp <- SDRcausal::alpha_guess</pre>
# Perform semiparametric imputation
imp <- SDRcausal::imp.ate(x, y, trt, b1, b0,</pre>
           explicit_bandwidth = TRUE, bwc_dim_red1 = 1, bwc_impute1 = 1,
           bwc_dim_red0 = 1, bwc_impute0 = 1)
# Perform semiparametric inverse probability weighting
ipw <- SDRcausal::ipw.ate(x, y, trt, alp, bwc_dim_red = 10,</pre>
           bwc_prop_score = 18)
# Calculate the Improved Augmented IPW (AIPW2)
aipw2 <- SDRcausal::aipw2.ate(y, trt, imp, ipw)</pre>
```

b10\_fun

Calculates B1/0

# **Description**

Calculates Eq 2.8 or 2.10 in Ghosh, Ma, & De Luna (2020).

6 b\_fun

# Usage

b10\_fun(x, treated, dm, beta, kernel, bandwidth, gauss\_cutoff)

# **Arguments**

x Projection of covariate matrix on CMStreated Binary vector indicating treatment.

dm Derivative of imputed values

beta CMS

kernel Specifies which kernel function to be used bandwidth Specifies if bandwidth\_scale will be used as the

gauss\_cutoff Cutoff value for Gaussian kernel

### Value

B1/0 matrix

b\_fun Calculates B1/0

# **Description**

Calculates Eq 2.8 or 2.10 in Ghosh, Ma, & De Luna (2020).

# Usage

b\_fun(x, treated, alpha\_hat, h, kernel, bandwidth, bandwidth\_pr, verbose)

# **Arguments**

x Projection of covariate matrix on CMS

treated Treated

alpha\_hat Derivative of imputed values

h CMS

kernel Specifies which kernel function to be used

bandwidth Kernel bandwidth

bandwidth\_pr Kernel bandwidth for probability

verbose Specifies if the program should print output while running.

# Value

B1/0 matrix

cms.ps.semi 7

cms.ps.semi

Estimates the Central Mean Space (CMS)

# Description

Semiparametric estimation of the Central Mean Space (CMS) as in Ghosh, Ma, & De Luna (2020). To be used with SDRcausal::ps.semi().

# Usage

```
cms.ps.semi(
    x,
    treated,
    alpha_initial,
    solver = "optim",
    kernel = "EPAN",
    explicit_bandwidth = FALSE,
    bandwidth_scale = 1,
    gauss_cutoff = 0.001,
    penalty = 10,
    n_before_pen = 5,
    root_tol = 0.001,
    n_threads = 1,
    verbose = FALSE,
    ...
)
```

# **Arguments**

X	Covariate matrix	ĸ

treated Binary vetor indicating treatment

alpha\_initial Initial guess of CMS

solver Specifies which solver to be used. Current options optim and cobyla (from nloptr

package).

kernel Specifies which kernel function to be used, current options are: "EPAN", "QUAR-

TIC", and "GAUSSIAN".

explicit\_bandwidth

Specifies if bandwidth\_scale will be used explicitly as the bandwidth.

bandwidth\_scale

Scaling of the calculated bandwidth, or in case of explicit\_bandwidth = TRUE

the bandwidth.

gauss\_cutoff cutoff value for Gaussian kernel

penalty Penalty for the optimizer if a probability is outside (0, 1). Added to the function

value in optim as: penalty^(n), where n is the number of probabilities outside

(0, 1).

n\_before\_pen Number of probabilities outside the range (0, 1) to accept during dimension

reduction.

root\_tol Tolerance which makes the program warn if optim stops at at a value higher than

root\_tol.

8 cms.semi

 $n\_threads \hspace{1cm} Sets \hspace{0.1cm} number \hspace{0.1cm} of \hspace{0.1cm} threads \hspace{0.1cm} for \hspace{0.1cm} parallel \hspace{0.1cm} run. \hspace{0.1cm} Set \hspace{0.1cm} to \hspace{0.1cm} 0 \hspace{0.1cm} serial. \hspace{0.1cm} If \hspace{0.1cm} n\_threads \hspace{0.1cm} exceeds \hspace{0.1cm} max-$ 

imum number of threads, sets n\_threads to max\_threads - 1. To use max\_threads,

set to n\_threads to max\_threads of system.

verbose Specifies if the program should print output while running.

... Additional parameters passed to solver.

#### Value

A list containing the final alpha, bandwwidth used, and the output of optim

### References

Ghosh, T., Ma, Y., & De Luna, X. (2020). Sufficient dimension reduction for feasible and robust estimation of average causal effect. Statistica Sinica, accepted.

#### See Also

```
[stats::optim]
```

# **Examples**

cms.semi

Estimates the Central Mean Space (CMS)

# Description

Semiparametric estimation of the Central Mean Space (CMS) as in Ghosh, Ma, & De Luna (2020). To be used with SDRcausal::imp.val().

# Usage

```
cms.semi(
   x,
   y,
   treated,
   beta_initial,
   solver = "optim",
   kernel = "EPAN",
```

cms.semi 9

```
explicit_bandwidth = FALSE,
bandwidth_scale = 1,
gauss_cutoff = 0.001,
penalty = 10,
n_before_pen = 1,
root_tol = 0.001,
n_threads = 1,
verbose = FALSE,
...
)
```

# **Arguments**

x Covariate matrixy Response vector

treated Binary vetor indicating treatment

beta\_initial Initial guess of CMS

solver Specifies which solver to be used. Current options optim and cobyla (from nloptr

package).

kernel Specifies which kernel function to be used, current options are: "EPAN", "QUAR-

TIC", and "GAUSSIAN".

explicit\_bandwidth

Specifies if bandwidth\_scale will be used as the bandwidth or if it will be calcu-

lated as bw = bandwidth\_scale \*  $sd(x * beta) * n^{(1/5)}$ 

bandwidth\_scale

Scaling of the bandwidth or the actual bandwidth if explicit bandwidth.

gauss\_cutoff cutoff value for Gaussian kernel

penalty Penalty for the optimizer if local linear regression fails. Added to the function

value in solver as: penalty^(n - n before pen), where n is the number of llr fails.

n\_before\_pen Number of probabilities outside the range (0, 1) to accept during dimension

reduction.

root\_tol Tolerance which makes the program warn if optim stops at at a value higher than

root tol.

n\_threads Sets number of threads for parallel run. Set to 0 serial. If n\_threads exceeds max-

imum number of threads, sets n\_threads to max\_threads - 1. To use max\_threads,

set to n\_threads to max\_threads of system.

verbose Specifies if the program should print output while running.

... Additional parameters passed to optim.

#### Value

A list containing the final beta, the bandwidth used, a warning if optim does not converge or converges to a value that is larger than root\_tol, and the output of optim.

### References

Ghosh, T., Ma, Y., & De Luna, X. (2020). Sufficient dimension reduction for feasible and robust estimation of average causal effect. Statistica Sinica, accepted.

10 example\_data

### See Also

```
[stats::optim]
```

# **Examples**

example\_data

Example data

# **Description**

Data generated as in paper, study 1. Using the betas in betas data. Use beta1/0 for imputation as the initial guess of the central mean space (CMS) and alpha as the initial guess of the CMS for IPW.

# **Format**

Data used in examples of the SDRcausal package

covariates covariate matrix

outcomes observed outcome vector

treated binary treatment vector

beta1\_guess Starting guess for CMS for treated

beta0\_guess Starting guess for CMS for untreated

alpha\_guess Starting guess for CMS for propensity score

imp.ate 11

imp.ate

Estimates Average Treatment Effect (ATE) by imputation (IMP)

# **Description**

Semiparametric estimation of the average treatment effect based on the imputation method described in Ghosh, Ma, & De Luna (2020).

# Usage

```
imp.ate(
 х,
 у,
  treated1,
 beta_guess1,
 beta_guess0,
  solver = "optim",
  kernel = "EPAN",
  explicit_bandwidth = FALSE,
  recalc_bandwidth = TRUE,
 bwc_dim_red1 = 1,
 bwc_impute1 = 1.25,
 bwc_dim_red0 = 1,
 bwc_impute0 = 1.25,
 gauss_cutoff = 0.001,
 penalty = 10,
 n_before_pen = 5,
  to_extrapolate = TRUE,
  to_truncate = TRUE,
 extrapolation_basis = 5,
 n_{threads} = 1,
 verbose = TRUE,
)
```

Covariate matrix

# **Arguments**

Χ

y Response vector treated1 A binary vector indicating treatment. beta\_guess1 Initial guess for  $\beta_1$  beta\_guess0 Initial guess for  $\beta_0$  solver Specifies which solver is to be used. Current options are optim and cobyla (from nloptr package). The diffault value is "optim". kernel Specifies which kernel function is to be used, current options are: "EPAN",

"QUARTIC", and "GAUSSIAN". The default value is "EPAN".

explicit\_bandwidth

Specifies if bandwidth\_scale will be used as the bandwidth or if it will be calculated as bandwidth\_scale \*  $\operatorname{sd}(\beta^T x)$  \*  $n^{(1/5)}$ . The default value is FALSE.

12 imp.ate

recalc\_bandwidth

Specifies whether the bandwidth should be recalculated after the first stage (the estimations of dimension reduction step). If explicit\_bandwidth is TRUE, recalc\_bandwidth is not used, but if explicit\_bandwidth is FALSE, then if recalc\_bandwidth is TRUE, bandwidths are recalculated at the beginning of the second step based on bwc\_impute0 and bwc\_impute1. If recalc\_bandwidth is FALSE, the first step bandwidths are used. The default value is FALSE.

bwc\_dim\_red1

Scaling of calculated bandwidth, or if explicit\_bandwidth = TRUE used as the bandwidth. It is used in the dimension reduction step for  $\hat{m}_1(\beta_1^T x)$ . The default value is 1

bwc\_impute1

Scaling of calculated bandwidth, or if explicit\_bandwidth = TRUE used as the bandwidth. It is used in the imputation step for  $\hat{m}_1(\beta_1^T x)$ . The default value is 1.25.

bwc\_dim\_red0

Scaling of calculated bandwidth, or if explicit\_bandwidth = TRUE used as the bandwidth. It is used in the dimension reduction step for  $\hat{m}_0(\beta_0^T x)$ . The default value is 1.

bwc\_impute0

Scaling of calculated bandwidth, or if explicit\_bandwidth = TRUE used as the bandwidth. It is used in the imputation step for  $\hat{m}_0(\beta_0^T x)$ . The default value is 1.25.

gauss\_cutoff

The cutoff value for Gaussian kernel. The default value is 1e-3.

penalty

Penalty for the optimizer if local linear regression fails. Added to the function value in solver as penalty $^(n - n_before_pen)$ , where n is the number of times local linear regression fails. The default value is 10.

n\_before\_pen

The number of acceptable local linear regression failures during the estimation of  $\beta_0$  and  $\beta_1$  phase. The default value is 5.

to\_extrapolate

Specifies whether to extrapolate or not. Since in  $\hat{m}_0(\beta_0^Tx)$  and  $\hat{m}_1(\beta_1^Tx)$  estimates in terms of  $\beta_0$  and  $\beta_1$ , local linear regression at the boundaries of  $\beta_0^Tx$  and  $\beta_1^Tx$  can be very volatile, it is recommended to use extrapolation on those points instead of local linear regression. The default value is TRUE.

to\_truncate

Specifies whether to truncate  $\hat{m}_0(\beta_0^T x)$  and  $\hat{m}_1(\beta_1^T x)$  or not. After estimating  $\hat{m}_0(\beta_0^T x)$  and  $\hat{m}_1(\beta_1^T x)$ , if they are outside the range of observed outputs, they are replaced with the minimum and maximum observed outputs. The default value is TRUE.

extrapolation\_basis

The number of data points to base extrapolation on. Extrapolation at border points can be done based on a different number of neighborhood points. extrapolation\_basis is how many neighborhood points are used. The default value is 5.

n\_threads

Sets the number of threads for parallel computing. Set to 1 serial. If n\_threads exceeds the maximum number of threads, sets n\_threads to max\_threads - 1. To use max\_threads, set to n\_threads to max\_threads of system. The default value is 1.

verbose

Specifies if the program should print output while running. The default value is TRUE.

1110

. Additional parameters passed to optim or cobyla.

# Value

A list containing the average treatment effect of the combination of observed and imputed values (ate), the average treatment effect based on the imputed values only (ate2), the imputed values for treated (m1) and untreated treated (m0), the and the output from optim (op).

imp.val

### References

Ghosh, T., Ma, Y., & De Luna, X. (2020). Sufficient dimension reduction for feasible and robust estimation of average causal effect. Statistica Sinica, accepted.

### See Also

```
[stats::optim]
```

### **Examples**

imp.val

Estimates imputed values based on CMS

# **Description**

Performs semiparametric imputation based on the CMS calculated by cms.semi, as in Ghosh, Ma, & De Luna (2020).

# Usage

```
imp.val(
    x,
    y,
    treated,
    beta_hat,
    kernel = "EPAN",
    explicit_bandwidth = FALSE,
    bandwidth_scale = 1,
    gauss_cutoff = 0.001,
    to_extrapolate = TRUE,
    to_truncate = TRUE,
    extrapolation_basis = as.integer(5),
    verbose = FALSE
)
```

14 imp.val

#### **Arguments**

x Covariate matrixy Response vector

treated Binary vetor indicating treatment

beta\_hat Locally efficient CMS

kernel Specifies which kernel function to be used

explicit\_bandwidth

Specifies if bandwidth\_scale will be used as the bandwidth or if it will be calcu-

lated as bw = bandwidth\_scale \*  $sd(x * beta) * n^{(1/3)}$ 

bandwidth\_scale

Kernel bandwidth

gauss\_cutoff Cutoff value for Gaussian kernel
to\_extrapolate Specifies wheter to extrapolate or not
to\_truncate Specifies wheter to extrapolate or not
extrapolation\_basis

Number of data point to base extrapolation on.

verbose Specifies if the program should print output while running

#### Value

A list containing the reduced space xb, the imputed values and their derivatives.

### References

Ghosh, T., Ma, Y., & De Luna, X. (2020). Sufficient dimension reduction for feasible and robust estimation of average causal effect. Statistica Sinica, accepted.

```
# Using example data from package SDRcausal
library(SDRcausal)
# Import example data
x <- SDRcausal::covariates
y <- SDRcausal::outcomes</pre>
trt <- SDRcausal::treated</pre>
b1 <- SDRcausal::beta1_guess</pre>
b0 <- SDRcausal::beta0_guess</pre>
# Using example data from package SDRcausal
library(SDRcausal)
# Import example data
x <- SDRcausal::covariates
y <- SDRcausal::outcomes</pre>
trt1 <- SDRcausal::treated</pre>
n <- as.integer(dim(x)[1])</pre>
trt0 <- as.integer(rep(1, times = n) - trt1)</pre>
b1 <- SDRcausal::beta1_guess</pre>
b0 <- SDRcausal::beta0_guess</pre>
```

imp.var

imp.var

Estimates IMP variance

#### **Description**

Variance of the IMP as in Ghosh, Ma, & De Luna (2020).

# Usage

```
imp.var(
    x,
    y,
    treated,
    imp,
    ipw,
    bandwidth_scale1 = imp$bw1,
    bandwidth_scale0 = imp$bw0,
    kernel = "EPAN",
    explicit_bandwidth = TRUE,
    gauss_cutoff = 0.001
)
```

# **Arguments**

x Covariate matrix
y Response vector
treated A binary vetor indicating treatment
imp imp output object from imp.ate
ipw ipw output object from ipw.ate
bandwidth\_scale1

Scaling of the calculated bandwidth, or in case of explicit\_bandwidth = TRUE, the actual bandwidth for the estimation of  $E(\cdot|\beta_1^TX)$ . The default value is imp\$bw1. If this default value is used, one should use the default value TRUE for explicit\_bandwidth.

16 imp2.var

bandwidth\_scale0

Scaling of the calculated bandwidth, or in case of explicit\_bandwidth = TRUE, the actual bandwidth for the estimation of  $E(\cdot|\beta_0^TX)$ . The default value is imp\$bw0. If this default value is used, one should use the default value TRUE for explicit\_bandwidth.

kernel

Specifies which kernel function to be used. The default is "EPAN".

explicit\_bandwidth

Specifies if bandwidth\_scale will be used as the bandwidth or if it will be calculated as bandwidth\_scale \*  $\operatorname{sd}(\beta_t^T x)$  \*  $n^{(1/5)}$ . The default value is TRUE.

gauss\_cutoff

The cutoff value for Gaussian kernel. The default value is 1e-3.

## Value

Variance of IMP estimator

#### References

Ghosh, T., Ma, Y., & De Luna, X. (2020). Sufficient dimension reduction for feasible and robust estimation of average causal effect. Statistica Sinica, accepted.

# **Examples**

```
# Using example data from package SDRcausal
library(SDRcausal)
# Import example data
x <- SDRcausal::covariates
y <- SDRcausal::outcomes
trt <- SDRcausal::treated</pre>
b1 <- SDRcausal::beta1_guess
b0 <- SDRcausal::beta0_guess</pre>
alp <- SDRcausal::alpha_guess</pre>
# Perform semiparametric imputation
imp <- SDRcausal::imp.ate(x, y, trt, b1, b0,</pre>
           explicit_bandwidth = TRUE, bwc_dim_red1 = 1, bwc_impute1 = 1,
           bwc_dim_red0 = 1, bwc_impute0 = 1)
# Perform semiparametric inverse probability weighting
ipw <- SDRcausal::ipw.ate(x, y, trt, alp, bwc_dim_red = 10,</pre>
           bwc_prop_score = 18)
# Calculate the variance of the IMP estimator.
var <- SDRcausal::imp.var(x, y, trt, imp, ipw,</pre>
           bandwidth_scale1 = imp$bw1, bandwidth_scale0 = imp$bw0)
```

imp2.var

Estimates IMP2 variance

# **Description**

Variance of IMP2 as in Ghosh, Ma, & De Luna (2020).

imp2.var

#### Usage

```
imp2.var(
    x,
    y,
    treated,
    imp,
    ipw,
    bandwidth_scale1 = imp$bw1,
    bandwidth_scale0 = imp$bw0,
    kernel = "EPAN",
    explicit_bandwidth = TRUE,
    gauss_cutoff = 0.001
)
```

# **Arguments**

x Covariate matrixy Response vector

treated A binary vetor indicating treatment imp imp output object from imp.ate ipw output object from ipw.ate

bandwidth\_scale1

Scaling of the calculated bandwidth, or in case of explicit\_bandwidth = TRUE, the actual bandwidth for the estimation of  $E(.|\beta_1^TX)$ . The default value is imp\$bw1. If this default value is used, one should use the default value TRUE for explicit\_bandwidth.

bandwidth\_scale0

Scaling of the calculated bandwidth, or in case of explicit\_bandwidth = TRUE, the actual bandwidth for the estimation of  $E(.|\beta_0^TX)$ . The default value is imp\$bw0. If this default value is used, one should use the default value TRUE for explicit\_bandwidth.

kernel Specifies which kernel function to be used. The default is "EPAN". explicit\_bandwidth

Specifies if bandwidth\_scale will be used as the bandwidth or if it will be calculated as bandwidth\_scale \*  $\operatorname{sd}(\beta_t^T x)$  \*  $n^{(1/5)}$ . The default value is TRUE.

gauss\_cutoff The cutoff value for Gaussian kernel. The default value is 1e-3.

# Value

Variance of IMP2

### References

Ghosh, T., Ma, Y., & De Luna, X. (2020). Sufficient dimension reduction for feasible and robust estimation of average causal effect. Statistica Sinica, accepted.

```
# Using example data from package SDRcausal
library(SDRcausal)
```

inf.ate

```
# Import example data
x <- SDRcausal::covariates
y <- SDRcausal::outcomes</pre>
trt <- SDRcausal::treated</pre>
b1 <- SDRcausal::beta1_guess</pre>
b0 <- SDRcausal::beta0_guess</pre>
alp <- SDRcausal::alpha_guess</pre>
# Perform semiparametric imputation
imp <- SDRcausal::imp.ate(x, y, trt, b1, b0,</pre>
           explicit_bandwidth = TRUE, bwc_dim_red1 = 1, bwc_impute1 = 1,
           bwc_dim_red0 = 1, bwc_impute0 = 1)
# Perform semiparametric inverse probability weighting
ipw <- SDRcausal::ipw.ate(x, y, trt, alp, bwc_dim_red = 10,</pre>
           bwc_prop_score = 18)
# Calculate the variance of the IMP2 estimator.
var <- SDRcausal::imp2.var(x, y, trt, imp, ipw,</pre>
           bandwidth_scale1 = imp$bw1, bandwidth_scale0 = imp$bw0)
```

inf.ate

Performs Estimations of Average Treatment Effect and Infrences

# **Description**

Semiparametric estimation of the average treatment effect based on the all methods described in Ghosh, Ma, & De Luna (2020) and all infrences.

## Usage

```
inf.ate(
 Х,
 у,
  treated.
 beta_guess1,
 beta_guess0,
  imp.solver = "optim",
  imp.kernel = "EPAN",
  imp.explicit_bandwidth = FALSE,
  imp.recalc_bandwidth = TRUE,
 bwc_dim_red1 = 1,
 bwc_impute1 = 1.25,
 bwc_dim_red0 = 1,
 bwc_impute0 = 1.25,
  imp.gauss_cutoff = 0.001,
  imp.penalty = 10,
  imp.n_before_pen = 5,
  imp.to_extrapolate = TRUE,
  imp.to_truncate = TRUE,
  imp.extrapolation_basis = 5,
  alpha_initial,
```

inf.ate 19

```
ipw.solver = "optim",
ipw.kernel = "EPAN",
ipw.explicit_bandwidth = FALSE,
ipw.recalc_bandwidth = TRUE,
bwc_dim_red = 1,
bwc_prop_score = 10,
ipw.gauss_cutoff = 0.001,
ipw.penalty = 10,
ipw.n_before_pen = 1,
n_threads = 1,
verbose = TRUE,
imp.solver.options = NA,
ipw.solver.options = NA
```

#### Arguments

x Covariate matrixy Response vector

treated A binary vector indicating treatment status

beta\_guess1 Initial guess for  $\beta_1$ beta\_guess0 Initial guess for  $\beta_0$ 

imp.solver Specifies which solver is to be used. Current options are optim and cobyla

(from nloptr package). The diffault value is "optim".

imp.kernel Specifies which kernel function is to be used, current options are: "EPAN",

"QUARTIC", and "GAUSSIAN". The default value is "EPAN".

imp.explicit\_bandwidth

Specifies if bandwidth\_scale will be used as the bandwidth or if it will be calculated as bandwidth\_scale \*  $sd(\beta^T x)$  \*  $n^{(1/5)}$ . The default value is FALSE.

imp.recalc\_bandwidth

Specifies whether the bandwidth should be recalculated after the first stage (the estimations of dimension reduction step). If explicit\_bandwidth is TRUE, recalc\_bandwidth is not used, but if explicit\_bandwidth is FALSE, then if recalc\_bandwidth is TRUE, bandwidths are recalculated at the beginning of the second step based on bwc\_impute0 and bwc\_impute1. If recalc\_bandwidth is FALSE, the first step bandwidths are used. The default value is FALSE.

bwc\_dim\_red1 Scaling of calculated bandwidth, or if explicit\_bandwidth = TRUE used as the bandwidth. It is used in the dimension reduction step for  $\hat{m}_1(\beta_1^T x)$ . The default

value is 1.

bwc\_impute1 Scaling of calculated bandwidth, or if explicit\_bandwidth = TRUE used as the

bandwidth. It is used in the imputation step for  $\hat{m}_1(\beta_1^T x)$ . The default value is

1.25.

bwc\_dim\_red0 Scaling of calculated bandwidth, or if explicit\_bandwidth = TRUE used as the

bandwidth. It is used in the dimension reduction step for  $\hat{m}_0(\beta_0^T x)$ . The default

value is 1.

 $\label{eq:bwc_impute0} \textbf{Scaling of calculated bandwidth, or if explicit\_bandwidth} = \textbf{TRUE used as the}$ 

bandwidth. It is used in the imputation step for  $\hat{m}_0(\beta_0^T x)$ . The default value is

1.25.

imp.gauss\_cutoff

The cutoff value for Gaussian kernel. The default value is 1e-3.

20 inf.ate

Penalty Penalty Penalty for the optimizer if local linear regression fails. Added to the function value in solver as penalty^(n - n\_before\_pen), where n is the number of times

local linear regression fails. The default value is 10.

imp.n\_before\_pen

The number of acceptable local linear regression failures during the estimation of  $\beta_0$  and  $\beta_1$  phase. The default value is 5.

imp.to\_extrapolate

Specifies whether to extrapolate or not. Since in  $\hat{m}_0(\beta_0^T x)$  and  $\hat{m}_1(\beta_1^T x)$  estimates in terms of  $\beta_0$  and  $\beta_1$ , local linear regression at the boundaries of  $\beta_0^T x$  and  $\beta_1^T x$  can be very volatile, it is recommended to use extrapolation on those points instead of local linear regression. The default value is TRUE.

imp.to\_truncate

Specifies whether to truncate  $\hat{m}_0(\beta_0^T x)$  and  $\hat{m}_1(\beta_1^T x)$  or not. After estimating  $\hat{m}_0(\beta_0^T x)$  and  $\hat{m}_1(\beta_1^T x)$ , if they are outside the range of observed outputs, they are replaced with the minimum and maximum observed outputs. The default value is TRUE.

imp.extrapolation\_basis

The number of data points to base extrapolation on. Extrapolation at border points can be done based on a different number of neighborhood points. extrapolation\_basis is how many neighborhood points are used. The default value is 5.

alpha\_initial Initial guess for  $\alpha$ 

ipw.solver Specifies which solver is to be used. Current options are optim and cobyla (from nloptr package). The diffault value is "optim".

ipw.kernel Specifies which kernel function is to be used, current options are: "EPAN", "QUARTIC", and "GAUSSIAN". The default value is "EPAN".

ipw.explicit\_bandwidth

Specifies if bandwidth\_scale will be used as the bandwidth or if it will be calculated as bandwidth\_scale \*  $\operatorname{sd}(\alpha^T x)$  \*  $n^{(1/5)}$ . The default value is FALSE.

ipw.recalc\_bandwidth

Specifies whether the bandwidth should be recalculated after the estimations of  $\alpha$ . If explicit\_bandwidth is TRUE, recalc\_bandwidth is not used, but if explicit\_bandwidth is FALSE, then if recalc\_bandwidth is TRUE, bandwidths are recalculated at the beginning of the second step based on bwc\_prop\_score. If recalc\_bandwidth is FALSE, the first step bandwidths are used. The default value is FALSE.

bwc\_dim\_red Scaling of calculated bandwidth, or if explicit\_bandwidth = TRUE used as the bandwidth. It is used in the dimension reduction step for  $\alpha^T x$ . The default value is 1

bwc\_prop\_score Scaling of calculated bandwidth, or if explicit\_bandwidth = TRUE used as the bandwidth. It is used for the estimation of the propensity score. The default value is 10.

ipw.gauss\_cutoff

The cutoff value for Gaussian kernel. The default value is 1e-3.

ipw.penalty Penalty for the optimizer if a probability is outside (0, 1) during the estimation of  $\alpha$  phase. Added to the function value in solver as penalty^(n - n\_before\_pen), where n is the number of probabilities outside (0, 1). The default value is 10.

ipw.n\_before\_pen

The number of probabilities outside the range (0, 1) to accept during the estimation of  $\alpha$  phase. The default value is 1.

ipw.ate 21

n\_threads Sets the number of threads for parallel computing. Set to 1 serial. If n\_threads

exceeds the maximum number of threads, sets  $n_{threads}$  to  $max_{threads}$  - 1. To use  $max_{threads}$ , set to  $n_{threads}$  to  $max_{threads}$  of system. The default

value is 1.

verbose Specifies if the program should print output while running. The default value is

TRUE.

imp.solver.options

Additional parameters passed to optim or cobyla for imp.ate.

ipw.solver.options

Additional parameters passed to optim or cobyla for ipw.ate.

#### Value

A list containing the average treatment effect of the combination of observed and imputed values (ate), the average treatment effect based on the imputed values only (ate2), the imputed values for treated (m1) and untreated treated (m0), the and the output from optim (op).

#### References

Ghosh, T., Ma, Y., & De Luna, X. (2020). Sufficient dimension reduction for feasible and robust estimation of average causal effect. Statistica Sinica, accepted.

#### See Also

[stats::optim]

# **Examples**

```
# Using example data from package SDRcausal
library(SDRcausal)

# Import example data
x <- SDRcausal::covariates
y <- SDRcausal::outcomes
trt <- SDRcausal::treated
b1 <- SDRcausal::beta1_guess
b0 <- SDRcausal::beta0_guess
a <- SDRcausal::alpha_guess
# Perform semiparametric imputation
inf.ate <- SDRcausal::inf.ate(x, y, trt, b1, b0, alpha_initial = a)</pre>
```

ipw.ate

Estimates average treatment effect through IPW

# **Description**

Semiparametric estimation of the average treatment effect based on the IPW method described in Ghosh, Ma, & De Luna (2020).

ipw.ate

#### Usage

```
ipw.ate(
 Х,
 у,
  treated,
  alpha_initial,
  solver = "optim",
  kernel = "EPAN",
  explicit_bandwidth = FALSE,
  recalc_bandwidth = TRUE,
  bwc_dim_red = 1,
  bwc_prop_score = 10,
  gauss_cutoff = 0.001,
  penalty = 10,
 n_before_pen = 1,
 n_{threads} = 1,
 verbose = TRUE,
)
```

### **Arguments**

x Covariate matrixy Response vector

treated A binary vector indicating treatment.

alpha\_initial Initial guess for  $\alpha$ 

solver Specifies which solver is to be used. Current options are optim and cobyla

(from nloptr package). The diffault value is "optim".

kernel Specifies which kernel function is to be used, current options are: "EPAN",

"QUARTIC", and "GAUSSIAN". The default value is "EPAN".

explicit\_bandwidth

Specifies if bandwidth\_scale will be used as the bandwidth or if it will be calculated as bandwidth\_scale \*  $\operatorname{sd}(\alpha^T x)$  \*  $n^{(1/5)}$ . The default value is FALSE.

recalc\_bandwidth

Specifies whether the bandwidth should be recalculated after the estimations of  $\alpha$ . If explicit\_bandwidth is TRUE, recalc\_bandwidth is not used, but if explicit\_bandwidth is FALSE, then if recalc\_bandwidth is TRUE, bandwidths are recalculated at the beginning of the second step based on bwc\_prop\_score. If recalc\_bandwidth is FALSE, the first step bandwidth is used. The default value is TRUE.

bwc\_dim\_red

Scaling of calculated bandwidth, or if explicit\_bandwidth = TRUE used as the bandwidth. It is used in the dimension reduction step for  $\alpha^T x$ . The default value is 1.

bwc\_prop\_score

Scaling of calculated bandwidth, or if explicit\_bandwidth = TRUE used as the bandwidth. It is used for the estimation of the propensity score. The default value is 10.

gauss\_cutoff

The cutoff value for Gaussian kernel. The default value is 1e-3.

penalty

Penalty for the optimizer if a probability is outside (0, 1) during the estimation of  $\alpha$  phase. Added to the function value in solver as penalty^(n - n\_before\_pen), where n is the number of probabilities outside (0, 1). The default value is 10.

ipw.var 23

n_before_pen	The number of probabilities outside the range $(0, 1)$ to accept during the estimation of $\alpha$ phase. The default value is 1.
n_threads	Sets the number of threads for parallel computing. Set to 1 serial. If n_threads exceeds the maximum number of threads, sets n_threads to max_threads - 1. To use max_threads, set to n_threads to max_threads of system. The default value is 1.
verbose	Specifies if the program should print output while running. The default value is FALSE.
	Additional parameters passed to optim or cobyla.

# Value

A list containing the average treatment effect (ate), the propensity score (pr), the final alpha (fa), and the output from optim (op).

# References

Ghosh, T., Ma, Y., & De Luna, X. (2020). Sufficient dimension reduction for feasible and robust estimation of average causal effect. Statistica Sinica, accepted.

# See Also

```
[stats::optim]
```

# **Examples**

```
# Using example data from package SDRcausal
library(SDRcausal)

# Import example data
x <- SDRcausal::covariates
y <- SDRcausal::outcomes
trt <- SDRcausal::treated
alp <- SDRcausal::alpha_guess

# Perform semiparametric inverse probability weighting
ipw <- SDRcausal::ipw.ate(x, y, trt, alp)</pre>
```

ipw.var

Estimates IPW variance

# Description

Variance of the IPW as in Ghosh, Ma, & De Luna (2020).

24 ipw.var

#### Usage

```
ipw.var(
    x,
    y,
    treated,
    imp,
    ipw,
    bandwidth_scale = ipw$bw_dr,
    kernel = "EPAN",
    explicit_bandwidth = TRUE,
    gauss_cutoff = 0.001,
    num_deriv_h = 1e-06,
    verbose = FALSE
)
```

# **Arguments**

x Covariate matrix y Response vector

treated A binary vetor indicating treatment imp imp output object from imp.ate ipw output object from ipw.ate

bandwidth\_scale

Scaling of the calculated bandwidth, or in case of explicit\_bandwidth = TRUE, the actual bandwidth for the estimation of  $E(\cdot|\alpha^TX)$ . The default value is ipw\$bw\_dr. If this default value is used, one should use the default value TRUE

for explicit\_bandwidth.

kernel Specifies which kernel function to be used. The default is "EPAN".

explicit\_bandwidth

Specifies if bandwidth\_scale will be used as the bandwidth or if it will be calculated as bandwidth\_scale \*  $sd(\alpha^T x)$  \*  $n^{(1/5)}$ . The default value is TRUE.

gauss\_cutoff The cutoff value for Gaussian kernel. The default value is 1e-3.

num\_deriv\_h Step size of numerical derivative. The default value is 1e-6.

verbose Specifies if the program should print output while running. The default value if

FALSE.

#### Value

The variance of IPW

### References

Ghosh, T., Ma, Y., & De Luna, X. (2020). Sufficient dimension reduction for feasible and robust estimation of average causal effect. Statistica Sinica, accepted.

```
# Using example data from package SDRcausal
library(SDRcausal)
```

nw\_kernel\_regress 25

```
# Import example data
x <- SDRcausal::covariates
y <- SDRcausal::outcomes</pre>
trt <- SDRcausal::treated</pre>
b1 <- SDRcausal::beta1_guess</pre>
b0 <- SDRcausal::beta0_guess</pre>
alp <- SDRcausal::alpha_guess</pre>
# Perform semiparametric imputation
imp <- SDRcausal::imp.ate(x, y, trt, b1, b0,</pre>
            explicit_bandwidth = TRUE, bwc_dim_red1 = 1, bwc_impute1 = 1,
            bwc_dim_red0 = 1, bwc_impute0 = 1)
# Perform semiparametric inverse probability weighting
ipw <- SDRcausal::ipw.ate(x, y, trt, alp, bwc_dim_red = 10,</pre>
           bwc_prop_score = 18)
# Calculate the variance of the Augmented IPW (AIPW)
var <- SDRcausal::ipw.var(x, y, trt, imp, ipw,</pre>
            bandwidth_scale = ipw$bw_dr)
```

nw\_kernel\_regress

The Nadaraya-Watson kernel estimator

# **Description**

Gives the expected value of Y given X = x by kernel regression according to the Nadaraya-Watson kernel estimator to get E(Y|X). Note that y and x may be vectors or matrices, as long as dim(x)[1] = dim(y)[1].

### Usage

```
nw_kernel_regress(
   y,
   x,
   bandwidth = 1,
   kernel = "EPAN",
   gauss_cutoff = 0.001,
   verbose = FALSE
)
```

# **Arguments**

 $\begin{array}{ll} y & Y \text{ in } E(Y|X) \\ x & X \text{ in } E(Y|X) \\ \text{bandwidth} & \text{Kernel bandwidth} \end{array}$ 

kernel Indicates which kernel function to be used

gauss\_cutoff Cutoff value for Gaussian kernel

verbose Specifies if the program should print output while running.

26 plot.imp

### Value

Value of kernel regression

#### References

Ghosh, T., Ma, Y., & De Luna, X. (2020). Sufficient dimension reduction for feasible and robust estimation of average causal effect. Statistica Sinica, accepted.

# **Examples**

```
# Using example data from package SDRcausal
library(SDRcausal)

# Import example data
x <- SDRcausal::covariates
y <- SDRcausal::outcomes

# Extimating y given x, E(y | x)
k <- nw_kernel_regress(y, x, bandwidth = 1)</pre>
```

plot.imp

Plots imputation output

# Description

Plot function for visualisation of imputation output from imp.ate. Note: The function requires ggplot2.

# Usage

```
## S3 method for class 'imp'
plot(x, ..., covariates, y, treated)
```

# **Arguments**

x imp\_output object from imp.ate()

Other parameterscovariatesCovariate matrixResponse vector

treated Binary vetor indicating treatment

# Value

A list of ggplot plots of observed and imputed values (pl\_imp), imputed treated values vs CMS (pl\_m1), and imputed untreated values vs CMS (pl\_m0).

plot.ipw 27

# **Examples**

plot.ipw

Plots IPW output

# **Description**

Plot function for visualisation of IPW output from ipw.ate. Note: The function requires ggplot2.

# Usage

```
## S3 method for class 'ipw'
plot(x, ..., treated, covariates)
```

# **Arguments**

x ipw\_output object from ipw.ate()
... Other parameters

treated Binary vetor indicating treatment

covariates Covariate matrix

# Value

ggplot plot of the propensity score vs CMS.

```
# Using example data from package SDRcausal
library(SDRcausal)

# Import example data
covariates <- SDRcausal::covariates
y <- SDRcausal::outcomes</pre>
```

28 ps.semi

ps.semi

Estimates propensity score

# **Description**

Semiparametric estimation of the propensity score as in Ghosh, Ma, & De Luna (2020). To be used with SDRcausal::cms.ps.semi().

# Usage

```
ps.semi(
    x,
    treated,
    alpha_hat,
    kernel = "EPAN",
    explicit_bandwidth = FALSE,
    bandwidth_scale = 1,
    verbose = FALSE
)
```

# Arguments

x Covariate matrix

treated Binary vetor indicating treatment

alpha\_hat Locally efficient CMS kernel Kernel specification explicit\_bandwidth

Specifies if bandwidth\_scale will be used as the bandwidth or if it will be calculated as  $bw = bandwidth_scale * sd(x * beta) * n^(1/3)$ .

bandwidth\_scale

Scaling of calculated bandwidth, or if explicit\_bandwidth = TRUE used as the

banddwidth.

verbose Specifies if the program should print output while running.

# Value

A list containing the estimated propensity scores values and their derivatives, and the bandwidth used.

ps.semi 29

### References

Ghosh, T., Ma, Y., & De Luna, X. (2020). Sufficient dimension reduction for feasible and robust estimation of average causal effect. Statistica Sinica, accepted.

# **Index**

```
*Topic data
      example_data, 10
aipw.ate, 2
aipw.var, 3
aipw2.ate, 4
b10_fun, 5
b_fun, 6
{\sf cms.ps.semi}, 7
{\sf cms.semi}, 8
\verb|example_data|, 10
imp.ate, 11
\texttt{imp.val}, \textcolor{red}{13}
imp.var, 15
imp2.var, 16
\quad \text{inf.ate, } 18 \\
\texttt{ipw.ate}, \textcolor{red}{21}
ipw.var, 23
nw_kernel_regress, 25
plot.imp, 26
plot.ipw, 27
\texttt{ps.semi}, \textcolor{red}{28}
```