

# < STAT-5361 > HW#2-Exercises 3

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Explain how `.Machinedouble.xmax`, `.Machinedouble.xmin`, `.Machinedouble.eps`, and `.Machinedouble.neg.eps` are defined using the 64-bit double precision floating point arithmetic.

## 1) Description

- (a) `Machine()` returns information on numeric characteristics of the machine R is running on, such as the largest double or integer and the machine's precision.
  - (b) `.Machine` is a variable holding this information.
- 2) `.Machine$double.xmax` <- the largest finite floating-point number. Typically, it is equal to  $(1 - \text{neg.eps}) * \text{base}^{\text{max.exp}}$ , but on some machines it is only the second, or perhaps third, largest number, being too small by 1 or 2 units in the last digit of the significand.

```
.Machine$double.xmax
```

```
## [1] 1.797693e+308
```

- 3) `.Machine$double.xmin` <- the smallest non-vanishing normalized floating-point power of the radix, i.e.,  $\text{base}^{\text{min.exp}}$ .

```
.Machine$double.xmin
```

```
## [1] 2.225074e-308
```

- 4) `.Machine$double.eps` <- the smallest positive floating-point number  $x$  such that  $1 + x \neq 1$ . It equals  $\text{base}^{\text{ulp.digits}}$  if either base is 2 or rounding is 0; otherwise, it is  $(\text{base}^{\text{ulp.digits}}) / 2$

```
.Machine$double.eps
```

```
## [1] 2.220446e-16
```

- 5) `.Machine$double.neg.eps` <- a small positive floating-point number  $x$  such that  $1 - x \neq 1$ . It equals  $\text{base}^{\text{neg.ulp.digits}}$  if base is 2 or round is 0; otherwise, it is  $(\text{base}^{\text{neg.ulp.digits}}) / 2$ . As `neg.ulp.digits` is bounded below by  $-(\text{digits} + 3)$ , `neg.eps` may not be the smallest number that can alter 1 by subtraction.

```
.Machine$double.neg.eps
```

```
## [1] 1.110223e-16
```