

# Final Project

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In our dataset, a number of smoke or non-smoke data is missing. So our goal is to find whether the data is come from smoke or non-smoke and their parameters  $\mu$  and  $\sigma$ . Assume Smoker  $\sim N(\mu_1, \sigma_1^2)$ , Non-Smoke  $\sim N(\mu_2, \sigma_2^2)$   $\theta_1 = [\mu_1, \sigma_1]^T$   $\theta_2 = [\mu_2, \sigma_2]^T$   $\theta = [\theta_1, \theta_2]$   $\rightarrow$  the parameter need to be estimate. Let  $Z$  be the missing data, and set when  $z = 1$ , the data comes from smoke, else when  $z = 0$  comes from non-smoke.

set initial parameters:  $\mu_1 = 2000, \mu_2 = 1000, \sigma_1 = 100, \sigma_2 = 100$ .

We need to design a cut-off point  $C$ , based on the normal graph, to determine  $x_i$  belongs to which group, smoker or non-smoker.

After grouping our initial data, we can calculate the MLE of  $\mu$  and  $\sigma$  for both group.

Then we use  $\hat{\mu}$  and  $\hat{\sigma}$  to re-select group. We use Newton iteration method until  $\hat{\mu} = \mu$  and  $\hat{\sigma} = \sigma$ .

Finally, we will have mean cost and variance for smoker and non-smoker.