Bootstrap aggregated sparse FPCA for classification

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Simulation

- 2 different simulations
 - The classifiers applied sparse FPCA for 1st simulated data
 - The classifiers with bootstrap aggregating for 1st simulated data
- The number of FPCs are selected by the proportion of variance explained(PVE) with over 99%.

Simulation results

Table 1: The accuracy of classifiers after FPCA

Logistic	SVM	SVM	SVM				Naive
Regression	(Linear)	(Gaussian)		KNN	LDA	QDA	Bayes
0.700	0.700	0.690	0.610	0.880	0.680	0.700	0.650
0.740	0.750	0.750	0.740	0.810	0.730	0.690	0.720
0.770	0.750	0.740	0.740	0.780	0.760	0.730	0.720
0.710	0.700	0.710	0.740	0.810	0.750	0.770	0.700
0.770	0.780	0.790	0.770	0.810	0.780	0.740	0.740
0.830	0.840	0.840	0.850	0.820	0.830	0.850	0.780
0.770	0.760	0.820	0.780	0.870	0.780	0.810	0.770
0.790	0.830	0.770	0.820	0.850	0.790	0.820	0.760
0.810	0.840	0.820	0.840	0.860	0.830	0.840	0.800
0.860	0.850	0.830	0.880	0.870	0.870	0.880	0.750
0.840	0.850	0.820	0.820	0.860	0.840	0.860	0.780
0.810	0.830	0.810	0.830	0.850	0.810	0.850	0.800
0.820	0.790	0.820	0.820	0.860	0.830	0.870	0.780
0.800	0.810	0.800	0.760	0.880	0.810	0.840	0.760
0.800	0.770	0.800	0.800	0.860	0.810	0.840	0.770
0.810	0.770	0.800	0.770	0.850	0.810	0.860	0.770
0.800	0.810	0.810	0.810	0.860	0.800	0.860	0.770
0.790	0.790	0.789	0.787	0.846	0.795	0.812	0.754
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0.780 0.810 0.790 0.830 0.770 0.820 0.850 0.790 0.820 0.810 0.840 0.820 0.840 0.860 0.830 0.840 0.840

Simulation results

Table 2: The accuracy with bootstrap aggregated curves

No.	Logistic	SVM	SVM	SVM				Naive
of obs	Regression	(Linear)	(Gaussian)	(Sigmoid)	KNN	LDA	QDA	Bayes
2	0.750	0.740	0.740	0.740	0.920	0.750	0.730	0.730
3	0.740	0.730	0.730	0.730	0.850	0.740	0.720	0.710
4	0.770	0.780	0.760	0.780	0.940	0.780	0.790	0.740
5	0.710	0.680	0.710	0.690	0.860	0.690	0.710	0.720
6	0.760	0.760	0.760	0.770	0.900	0.760	0.760	0.740
7	0.860	0.840	0.810	0.850	0.890	0.860	0.860	0.780
8	0.770	0.780	0.820	0.780	0.890	0.760	0.810	0.790
9	0.780	0.790	0.790	0.780	0.860	0.780	0.820	0.760
10	0.810	0.820	0.800	0.810	0.880	0.820	0.830	0.760
11	0.860	0.850	0.840	0.850	0.880	0.870	0.870	0.760
12	0.840	0.840	0.820	0.830	0.880	0.850	0.860	0.780
13	0.800	0.810	0.810	0.810	0.900	0.820	0.830	0.790
14	0.820	0.810	0.820	0.840	0.870	0.830	0.860	0.770
15	0.800	0.800	0.820	0.800	0.910	0.800	0.840	0.740
16	0.800	0.790	0.800	0.790	0.880	0.810	0.830	0.760
17	0.810	0.800	0.810	0.810	0.890	0.810	0.840	0.760
18	0.800	0.810	0.820	0.790	0.880	0.800	0.850	0.760
Average	0.793	0.790	0.792	0.791	0.887	0.796	0.812	0.756

Simulation

- 5 different aggregation methods
 - Majority vote
 - LSE-based weighting(2003, Kim et al.)
 - Training accuracy
 - Out-of-bag accuracy
 - The proportion of response class(P(Y=1))
- The data has different sparsity with 6~12 time points randomly from 1st simulated data.
- The number of FPCs are selected by the proportion of variance explained(PVE) with over 99%.

Simulation results

Table 3: The accuracy of classifiers between different aggregation methods

Aggregation	Logistic	SVM	SVM	SVM				Naive
method	Regression	(Linear)	(Gaussian)	(Sigmoid)	KNN	LDA	QDA	Bayes
Majority vote	0.80	0.78	0.77	0.77	0.87	0.78	0.80	0.76
LSE(-1 vs 1)	0.22	0.23	0.24	0.24	0.20	0.21	0.22	0.27
LSE(0 vs 1)	0.77	0.84	0.80	0.81	0.88	0.81	0.86	0.76
LSE(1 vs 2)	0.77	0.84	0.80	0.82	0.89	0.81	0.85	0.76
Train accuracy	0.80	0.78	0.79	0.77	0.87	0.79	0.80	0.75
OOB accuracy	0.80	0.79	0.80	0.78	0.87	0.79	0.81	0.75
P(Y = 1)	0.79	0.78	0.73	0.77	0.71	0.82	0.82	0.74
Bagging X	0.81	0.79	0.78	0.79	0.86	0.78	0.81	0.74