

Introduction to RNA-seq sequencing: Preprocessing

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1 The study of gene expression

- The first part of this course focussed on proteomics, studying the concentration of proteins in biological samples. We have seen that identification of proteins and measuring their respective concentrations are extremely challenging, leading to many technological and statistical challenges in order to interpret these data.
- In the second part of the course, we will focus on measuring gene expression, i.e., measuring the concentration of mRNA molecules, that may eventually be translated into proteins, but may also have functions on their own.

```
include_graphics("./images_sequencing/centralParadigm.png")
```



Figure 1: Central Paradigm of Biology: a gene, a specific region in the DNA, is first transcribed into RNA and then into proteins. Note, that for RNA-genes the RNA molecule is the end product itself, which is referred to as non-coding RNA (ncRNA) (Source: Wikipedia)

1.1 Alternative splicing

```
include_graphics("./images_sequencing/alternative_splicing.png")
```

2 Sequencing technology

- Measuring mRNA molecules typically happens through sequencing.
- The technology continues to evolve at an incredible speed. The data output of so-called ‘next generation’ sequencing machines has more than doubled each year! Simultaneously, the cost of sequencing (in terms of \$ per Gigabase) is dropping. Each year, we’re able to sequence more for less money, providing more information, as well as also computational and statistical challenges.
- This tremendous technological revolution has revolutionized biology, and genomic sequencing is now a core component of the modern-day biologist’s toolkit.
- The large majority of sequencing data is generated using sequencing-by-synthesis using machines produced by the company Illumina. While new players such as Pacific Biosciences and Oxford Nanopore have entered the scene, these are typically most useful for (but not limited to) DNA sequencing rather than gene expression studies, owing to their capability of sequencing long molecules.

2.1 From sample to data analysis

2.2 Illumina Sequencing

2.3 Single vs paired end

2.4 The sequencing workflow with Details

Library preparation steps

1. First, the biological **samples of interest are collected**. Owing to the maturity of different protocols for sequencing, several types of biological input samples are amenable to sequencing, such as frozen tissues or FFPE-preserved samples.
2. The **mRNA molecules from our sample are captured**. This typically involves cell lysis in order to release the mRNA molecules from within the cells. The mRNA molecules are most often captured using (i) polyA-capture to select for polyadenylated RNA, or (ii) ribosomal depletion, where ribosomal and transfer RNAs are depleted, and so also non-polyA-mRNA molecules may be captured, such as long non-coding RNAs. In the case of ‘targeted sequencing’, where relevant molecules are of main interest (e.g., a gene panel), these targets can be specifically targeted in this step.
3. **Fragmentation** of captured molecules. The captured molecules are fragmented, either chemically or mechanically. The appropriate size of fragments depends on the sequencing machines, but is often in the range of 300 - 500bp.
4. **Reverse transcription**. Current dominant sequencing machines only sequence double-stranded DNA molecules. Therefore, in order to measure single-stranded mRNA, we must first reverse transcribe these molecules to a double-stranded complementary (cDNA) molecule.
5. **Adapter ligation**. Adapters are oligonucleotides (short sequences of nucleotides) that are platform-specific sequences for fragment recognition by the sequencing machines. These are added either to the 3' or 5' end of the cDNA molecules or used as primers in the reverse transcription reaction. The final cDNA library consists of cDNA inserts flanked by an adapter sequence on each end.
6. **PCR amplification**. To increase concentration, several PCR reactions are performed.



Figure 2: Alternative splicing allows a single gene in Eucaryotes to code for multiple proteins. During alternative splicing particular exons of a gene may be included or excluded from the premature messenger RNA when producing the messenger RNA (mRNA) from that gene. Hence exons can be joined in different combinations, leading to different (alternative) mRNA strands. The proteins translated from alternatively spliced mRNAs thus differ in their amino acid sequence and, often, in their biological functions (Source: Wikipedia)

Human Genomes Sequenced Annually

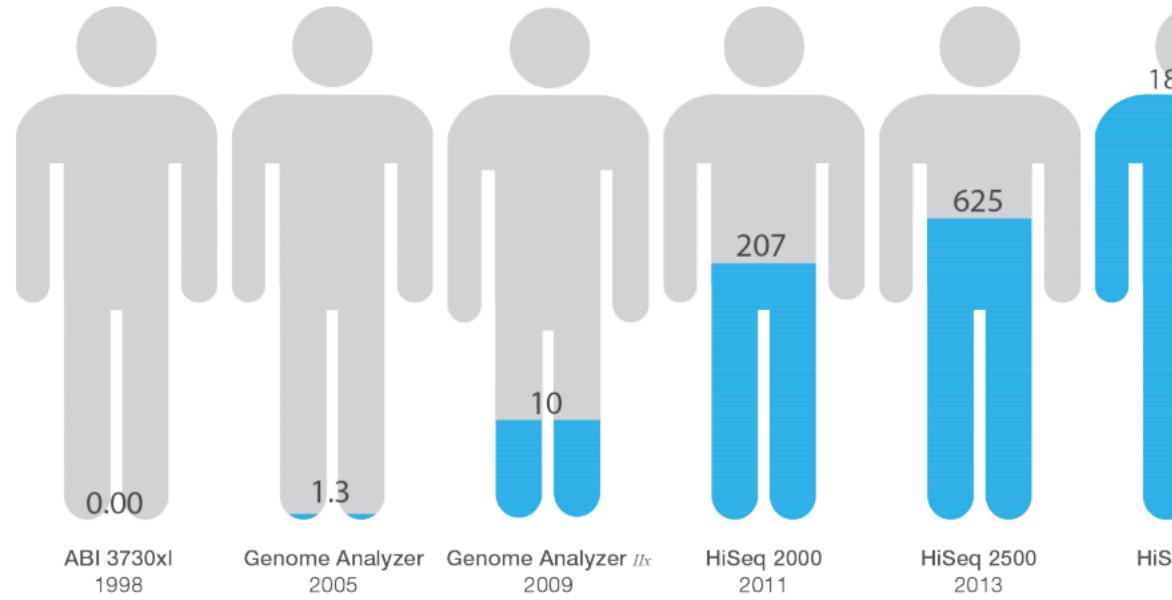


Figure 2: Human Genome Sequencing Over the Decades—The capacity to sequence all 3.2 billion bases of the human genome (at 30x coverage) has exponentially increased since the 1990s. In 2005, with the introduction of the Illumina Genome Analyzer System, 1.3 human genomes could be sequenced annually. Later, with the Illumina HiSeq X Ten fleet of sequencing systems, the number has climbed to 18,000 human genomes a year.

Figure 3: Figure: The data output revolution of sequencing machines. Image from Illumina documentation.



Figure 4: Figure: The sequencing workflow. Image adapted from Van den Berge et al. (2019).



Figure 5: Figure: Illumina sequencing steps 1-6 (Source: Illumina)



Figure 6: Figure: Illumina sequencing steps 1-6 (Source: Illumina)

Single-end

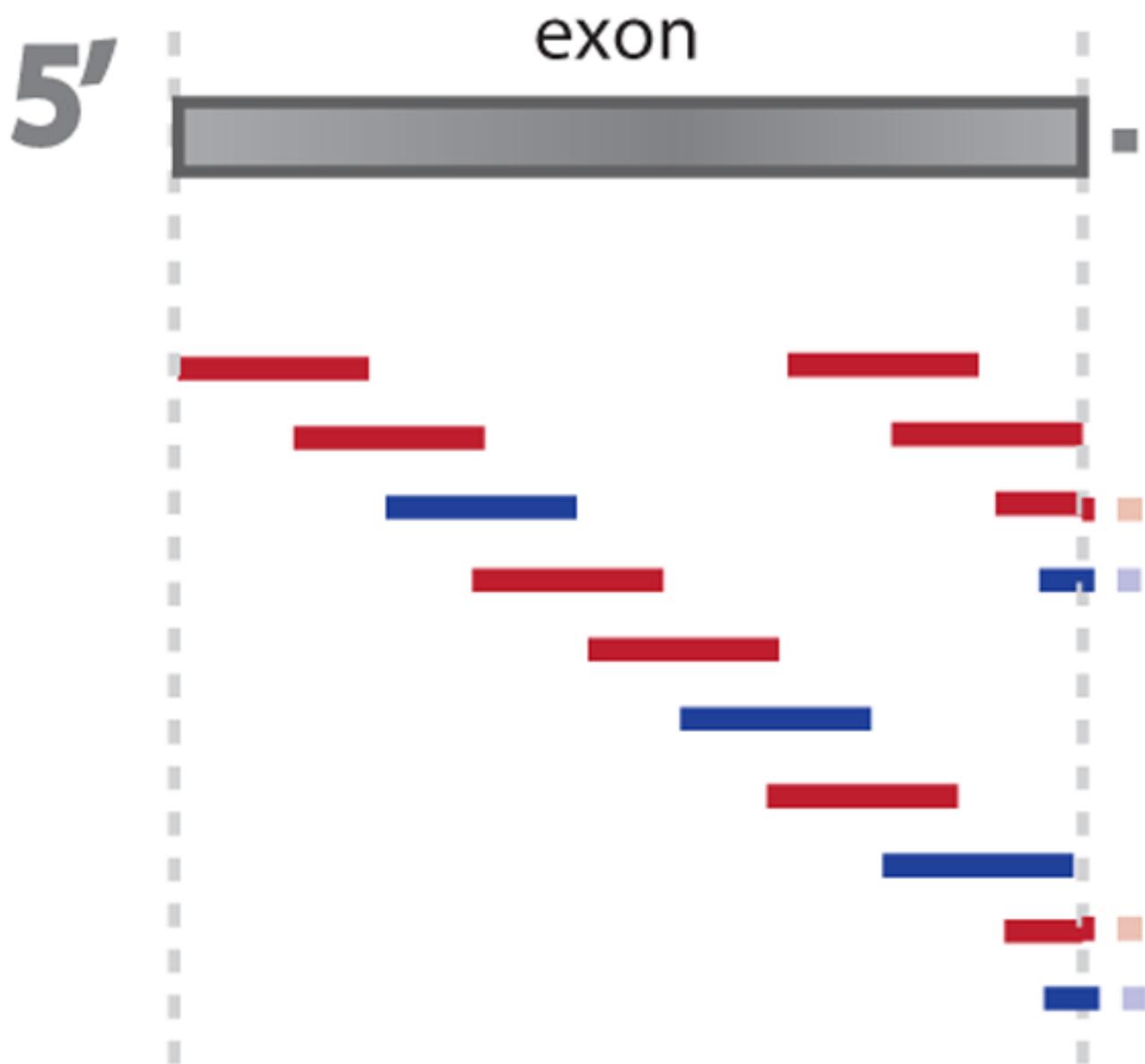


Figure 7: Figure: Single vs paired end sequencing. In contrast to single-end sequencing, paired-end sequencing allows users to sequence both ends of a fragment (Image adopted from Zhernakova et al., 2013, doi.org/10.1371/journal.pgen.1003594).

7. Loading the amplified cDNA library on the **sequencing** machine. Find out how sequencing-by-synthesis works through this video. Note that the video shows paired-end sequencing, where a number of basepairs are sequenced at each end of the fragment. All previous steps together are described as ‘sample prep’ in that video.



Figure 8: Figure: The sequencing workflow. Image adapted from Van den Berge et al. (2019).

Note that several variants of library preparation protocols are available. The most important ones are:

- Single-end vs paired-end sequencing: In single-end sequencing, a single end (3' or 5') of the cDNA fragment is sequenced. In paired-end sequencing, both ends are sequenced, and depending on the size of the fragment, the reads may or may not overlap.
- Strand-specific protocols: Some library preparation protocols allow measuring strand specificity, where the strand information (i.e., sense/antisense) of each read can be preserved.

2.5 The sequencing output files

- The typical output of a sequencing machine we will be working with are FASTA or FASTQ files for each sample. Each of these files are several gigabases large and contain millions of sequences, which we will call **reads**. For paired-end sequencing, there are two files for each sample, one for each end of the sequenced fragments.
- The difference between a FASTA file and a FASTQ file, is that while FASTA files only store the results of base calls (sequences), FASTQ files also store the quality score of each base call (i.e., each called nucleotide), which can be useful in downstream analyses such as mapping or variant calling.
- A FASTQ file contains four lines for each sequenced read:
 1. Sequence identifier line, starting with @.
 2. The sequence.
 3. Another sequence identifier line, now starting with +.
 4. Quality scores.

FASTQ format

- D7MHBFI - unique instrument name
 - 202 - run ID
 - D1BUDACXX - flowcell ID
 - 4 - flowcell lane
 - 1101 - tile number within lane
 - 1340 - x-coordinate of cluster within tile
 - 1967 - y-coordinate of cluster within tile

Figure 9: Figure: One read in a FASTQ file. Slide courtesy by Charlotte Soneson.

As you'll have noticed, the base call quality scores are encoded as ASCII characters for efficient storage. These ASCII characters can be converted into integers called Phred scores, which are logarithmically related to the probability of an erroneous base call.

2.5.1 Quality score

The Phred Score is a quality score

$$Q = -10 \log_{10} p$$

, with p the probability on an incorrect base call

Phred Score	Probability on incorrect base call	Base call accuracy
10	1/10	90%
20	1/100	99%
30	1/1000	99.9%
40	1/10000	99.99%
50	1/10000	99.999%

Phred score encoded as an ASCII letter. E.g. Phred+33:

Phredl	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40
Ph33B4	35	36	37	38	39	40	41	42	43	44	45	46	47	48	49	50	51	52	53	54	55	56	57	58	59	60	61	62	63	64	65	66	67	68	69	70	71	72	73
+																																							
33																																							
ASCII	#	\$	%	&	'	()	*	+	,	-	.	/	0	1	2	3	4	5	6	7	8	9	:	;	<	=	>	?	@	A	B	C	D	E	F	G	H	I

3 Preprocessing of raw sequencing data

After sequencing, we typically do a quality control (QC) check to verify the quality of the samples. During QC check, aberrant samples due to e.g. degraded mRNA can be detected.

The sequencing reads on their own contain a lot of information, but are most useful if we would be able to assign sequencing reads to genomic features (genes, exons, transcripts, etc.), i.e., for each sequencing read we will try to derive the (set of) feature(s) that could have plausibly produced the fragment through the process of gene expression. This process is called **mapping**. Most often we map reads to genes.

3.1 Quality control

During quality control, diagnostic plots are created for each sample in order to determine its quality. The most popular QC tool for bulk RNA-seq data is FastQC. If many samples are sequenced, then MultiQC can be used to aggregate the QC checks across samples in a conveniently organized overview.

The FastQC website provides interesting example reports for us to look at and compare against. Here are example reports of high-quality Illumina data and low-quality Illumina data.



Figure 10: Figure: An updated sequencing workflow, including sequencing and mapping. Image adapted from Van den Berge et al. (2019).

3.2 Read Trimming

- Read Trimming
 - Adaptor sequence
 - Bar code
 - (deteriorating bases at the end of reads)
 - often already done by the sequencing provider.
 - remaining polyA tails
- Read filtering
 - low quality reads
 - PhiX reads (should be removed already by sequence provider) in
 - RNA-seq never remove duplicates because they can occur for highly expressed transcripts
- Perform fastQC again

3.3 Mapping

- Mapping is a critical step in the interpretation of RNA-seq data, where we are attributing reads to genomic features.
- Allows us to measure how strong a feature such as a gene is expressed: the number of reads mapping to a gene serve as a proxy for how high that gene has been expressed in the sample.
- While this opens the door to many opportunities, mapping is hard.
- We are **typically unable to assign each individual read uniquely** to one specific gene; some reads cannot be unambiguously mapped and are compatible with multiple genes. These reads are said to be ‘multi-mapping’.

Finally, a note on terminology. In this text we will use the words ‘read’ or ‘fragment’ (referring to the fragmented mRNA molecule being sequenced) to designate a datum, note that this could be either a single read (in single-end sequencing) or a read pair (in paired-end sequencing). The literature may also use these words interchangeably, although ‘fragment’ seems better at avoiding ambiguity between single-end reads and paired-end read pairs.

3.3.1 Reference files

- The alignment most often relies on a **reference genome** of the species, which can be considered a ‘representative example’ of the genome sequence of that species. Reference genomes are continuously updated and released periodically.
- Reference genomes can be freely downloaded from several providers, for example Ensembl or Gencode.
- Along with a reference genome, an annotation GFF or GTf file defines the coordinates of specific genomic features.
- While here we will focus on reference-based alignment, i.e., alignment where a reference genome or transcriptome is available, note that a *de novo* construction of a reference transcriptome is also possible, where the reference may be constructed from the observed sequencing reads.

The human reference genome

www.ensembl.org/info/data/ftp/index.html

Single species data

Popular species are listed first. You can customise this list via our [home page](#)

★ Species	DNA (FASTA)	cDNA (FASTA)	CDS (FASTA)	ncRNA (FASTA)	Protein sequence (FASTA)
	FASTA				
Y Human <i>Homo sapiens</i>	FASTA				
Y Mouse <i>Mus musculus</i>	FASTA				
Y Zebrafish <i>Danio rerio</i>	FASTA				

[Homo_sapiens.GRCh38.dna.primary_assembly.fa.gz](#) 840 MB

<https://www.gencodegenes.org/human/>

Fasta files

Content	Regions	Description	Download
Transcript sequences	CHR	• Nucleotide sequences of all transcripts on the reference chromosomes	Fasta
Protein-coding transcript sequences	CHR	• Nucleotide sequences of coding transcripts on the reference chromosomes • Transcript biotypes: protein_coding, nonsense-mediated_decay, non_stop_decay, IG_-, gene, TR_-, gene, polymorphic_pseudogene	Fasta
Protein-coding transcript translation sequences	CHR	• Amino acid sequences of coding transcript translations on the reference chromosomes • Transcript biotypes: protein_coding, nonsense-mediated_decay, non_stop_decay, IG_-, gene, TR_-, gene, polymorphic_pseudogene	Fasta
Long non-coding RNA transcript sequences	CHR	• Nucleotide sequences of long non-coding RNA transcripts on the reference chromosomes	Fasta
Genome sequence (GRCh38.p12)	ALL	• Nucleotide sequence of the GRCh38.p12 genome assembly version on all regions, including reference chromosomes, scaffolds, assembly patches and haplotypes • The sequence region names are the same as in the GTf/GFF3 files	Fasta
Genome sequence, primary assembly (GRCh38)	PRI	• Nucleotide sequence of the GRCh38 primary genome assembly (chromosomes and scaffolds) • The sequence region names are the same as in the GTf/GFF3 files	Fasta

Figure 11: slide courtesy Charlotte Soneson

- More recently, mapping of RNA-seq data occurs more often against a **reference transcriptome**, which is a reference file containing the sequences all known isoforms of a particular species, e.g., using kallisto or Salmon.
- The set of spliced transcripts is much smaller than the entire genome, and therefore mapping against a reference transcriptome is typically **fast and memory efficient**.
- However, it has been noted that mapping against a reference transcriptome may also introduce spurious expression for genes that are not expressed. These observations can be explained by **intronic reads** that share some sequence similarity with transcripts, and could map to spliced transcript sequences. Recent methods, such as alevin-fry, avoid this by expanding the reference transcriptome to also include intronic sequences.

Figure 12: Figure: A reference sequence of human chr1.

www.ensembl.org/info/data/ftp/index.html

<https://www.gencodegenes.org/human/>

ie this list via our [home page](#).

GTF / GFF3 files									
		Content		Regions		Description		Download	
DS	ncRNA (FASTA)	Protein sequence (FASTA)	Annotated sequence (EMBL)	Annotated sequence (GenBank)	Gene sets	Whole databases	Vari-		
STA	FASTA	FASTA	FASTA	EMBL	GenBank	GTF	MySQL	G'	GTF GFF3
					GFF3				
TA	FASTA	FASTA	FASTA	EMBL	GenBank	GTF	MySQL	G'	GTF GFF3
					GFF3				
TA	FASTA	FASTA	FASTA	EMBL	GenBank	GTF	MySQL	G'	GTF GFF3
					GFF3				

Figure 13: slide courtesy Charlotte Soneson

3.3.2 Alignment-based workflows

- Traditionally, alignment-based workflows have been used to map reads, where one tries to find the exact coordinates a read maps to on the reference genome or the reference transcriptome.
- Note that due to alternative splicing, reads do not necessarily map contiguously on a reference genome, as a read can overlap with a splicing junction, where an intron has been excised. When mapping against a transcriptome, however, reads should be mapping contiguously.
- A main challenge in spliced alignment against a reference genome is the proper alignment of reads that span a splice junction, especially when these junctions are not annotated a priori. Indeed, in spliced alignment reads can be split at any nucleotide, and the corresponding subsequences can map several thousands of basepairs apart. Meanwhile, the main challenge in unspliced alignment to a transcriptome is the redundant sequence among related transcripts in the transcriptome, which often leads to a high multi-mapping rate (i.e., reads that cannot be unambiguously assigned to a single transcript).
- Spliced alignment against a genome is therefore computationally a much harder task. Since the transcript sequences are already spliced when aligning to a reference transcriptome, reads should align contiguously, and many of the computationally expensive steps and heuristics can be avoided, there.

3.3.3 Alignment-free workflows

- Modern approaches avoid mapping each fragment individually (i.e., do not attempt to find the exact coordinates of a read's origin), and instead posit a probabilistic model where transcript abundances are typically defined using its constituent k -mers. These methods are sometimes referred to as *lightweight*.
- A k -mer is a short sequence of nucleotides of length k . The space of possible k -mers and the corresponding transcripts can be precomputed in advance using the reference transcriptome, providing a computational advantage as it only needs to be computed once.
- For each fragment, the transcripts its k -mers are compatible with is searched for using an indexed (efficiently searchable) transcriptome. The set of compatible transcripts is called the ' k -compatibility class', 'equivalence class' or 'transcript compatibility class' of the fragment.

3.4 Abundance quantification

Given a set of mappings, using either alignment-based or alignment-free workflows, the estimation of expression of a gene/transcript/exon may occur in several ways.

Counting:

```

(base) Koen-MacBook-Pro:gtf koenvandenberge$ cat test_ensemble_chr22.gtf
22     protein_coding  UTR      12791    14009    .        +        .        ccds_
e_name "EP300"; gene_source "ensembl_havana"; p_id "P5137"; tag "CCDS"; trans
nsembl_havana"; tss_id "TSS138009";
22     protein_coding  exon     12791    14103    .        +        .        ccds_
tein_coding"; gene_id "ENSG00000100393"; gene_name "EP300"; gene_source "ense
cript_name "EP300-001"; transcript_source "ensembl_havana"; tss_id "TSS138009";
22     protein_coding  transcript 12791    101082   .        +        .        .
93"; gene_name "EP300"; gene_source "ensembl_havana"; p_id "P5137"; tag "CCDS"
ource "ensembl_havana"; tss_id "TSS138009";
22     miRNA    exon     13518    13571    .        +        .        exon_id "ENSE
"; gene_name "MIR1281"; gene_source "ensembl"; transcript_id "ENST00000408233
801";
22     miRNA    transcript  13518    13571    .        +        .        gene_
"ensembl"; transcript_id "ENST00000408233"; transcript_name "MIR1281-201"; tr
22     protein_coding CDS      14010    14103    .        +        0        ccds_
00000100393"; gene_name "EP300"; gene_source "ensembl_havana"; p_id "P5137";
anscript_name "EP300-001"; transcript_source "ensembl_havana"; tss_id "TSS138
22     protein_coding start_codon 14010    14012    .        +        0
id "ENSG00000100393"; gene_name "EP300"; gene_source "ensembl_havana"; p_id "
01"; transcript_source "ensembl_havana"; tss_id "TSS138009";
22     protein_coding CDS      38192    38826    .        +        2        ccds_
00000100393"; gene_name "EP300"; gene_source "ensembl_havana"; p_id "P5137";
anscript_name "EP300-001"; transcript_source "ensembl_havana"; tss_id "TSS138
22     protein_coding exon     38192    38826    .        +        .        ccds_
tein_coding"; gene_id "ENSG00000100393"; gene_name "EP300"; gene_source "ense
cript_name "EP300-001"; transcript_source "ensembl_havana"; tss_id "TSS138009";
22     protein_coding CDS      46869    47045    .        +        0        ccds_
00000100393"; gene_name "EP300"; gene_source "ensembl_havana"; p_id "P5137";
anscript_name "EP300-001"; transcript_source "ensembl_havana"; tss_id "TSS138
22     protein_coding exon     46869    47045    .        +        .        ccds_
tein_coding"; gene_id "ENSG00000100393"; gene_name "EP300"; gene_source "ense
cript_name "EP300-001"; transcript_source "ensembl_havana"; tss_id "TSS138009";
22     protein_coding CDS      48492    48753    .        +        0        ccds_
00000100393"; gene_name "EP300"; gene_source "ensembl_havana"; p_id "P5137";
anscript_name "EP300-001"; transcript_source "ensembl_havana"; tss_id "TSS138
22     protein_coding exon     48492    48753    .        +        .        ccds_
tein_coding"; gene_id "ENSG00000100393"; gene_name "EP300"; gene_source "ense
cript_name "EP300-001"; transcript_source "ensembl_havana"; tss_id "TSS138009";
22     protein_coding CDS      50895    51008    .        +        2        ccds_
00000100393"; gene_name "EP300"; gene_source "ensembl_havana"; p_id "P5137";
anscript_name "EP300-001"; transcript_source "ensembl_havana"; tss_id "TSS138

```

Figure 14: Figure: An example GTF file.

a Spliced alignment against genome



b Unspliced alignment against transcriptome



Figure 4

An illustration of spliced alignment of RNA sequencing (RNA-seq) fragments to a transcriptome (*b*). Reads are designated by thick solid lines, pairing relationship between paired-end reads. This illustration depicts alignment to a transcriptome consisting of three distinct transcripts. In the spliced alignment (*a*), the leftmost read aligns to the blue exon, and the rightmost read aligns to the green exon, spanning the junction between the blue and green exons. In the direct alignment (*b*), one observes how the same alignment (e.g., the alignment to the blue exon) can be observed across different transcripts.

Figure 15: Figure: Unspliced and spliced alignment. Figure from Van den Berge et al. (2019).



Figure 16: Figure: Overview of kallisto, image from Bray et al. (2016).

Figure 1 Overview of kallisto. The input consists of a reference transcriptome and reads from an RNA-seq experiment. **(a)** An example of a read (in black) and three overlapping transcripts with exonic regions as shown. **(b)** An index is constructed by creating the transcriptome de Bruijn Graph (T-DBG) where nodes (v_1, v_2, v_3, \dots) are k -mers, each transcript corresponds to a colored path as shown and the path cover of the transcriptome induces a k -compatibility class for each k -mer. **(c)** Conceptually, the k -mers of a read are hashed (black nodes) to find the k -compatibility class of a read. **(d)** Skipping (black dashed lines) uses the information stored in the T-DBG to skip k -mers that are redundant because they have the same k -compatibility class. **(e)** The k -compatibility class of the read is determined by taking the intersection of the k -compatibility classes of its constituent k -mers.

Figure 17: Figure: Overview of kallisto, image from Bray et al. (2016).

- In alignment-based workflows, one could do a direct counting of fragments at the gene-level, counting the number fragments mapping to each gene. This has been the dominant approach for the first decade of RNA-seq data, often obtained using reference genome alignments.
- Many heuristic choices need to be made: Do we count a fragment as soon as it intersects with the gene's coordinates, or do we require the full fragment to map to the gene? Do we count intronic reads? Do we count multi-mapping reads?

Estimation:

- Abundance quantification is more recently starting to shift from counting towards using statistical models to estimate the expression counts for a feature, which in this case is typically a transcript.
- This approach is amenable to alignment-free workflows, since the number of fragments in each equivalence class are sufficient statistics for the abundance quantification, meaning that they contain all information needed to estimate the parameters of the statistical model, and hence the feature-level abundances. Since the expression counts in this case are estimated, they are not necessarily integer counts, and will be referred to as 'estimated counts'.
- In order to derive these, the EM-algorithm is often used, although other approaches have been used by tools like Salmon. A big advantage of the estimation approach is that it probabilistically assigns fragments to transcripts, thereby automatically dealing with multi-mapping reads. The total number of fragments mapping to each transcript is then the sum of all fragment-level probabilities to be assigned to that respective transcript.

3.4.1 Abundance metrics

- For simplicity, we have only been talking about feature-level counts as in sums of fragments. However, this is merely one metric that can be used as a proxy for expression, and several others exist.
- Most of these were introduced to attempt to make the abundances more comparable across samples or features, as compared to the simple counts. These mainly serve to correct for technical biases such as transcript length and sequencing depth, both of which have significant impact on the observed counts.

Gene and transcripts



Gene-level quantification:



Exon-level quantification:

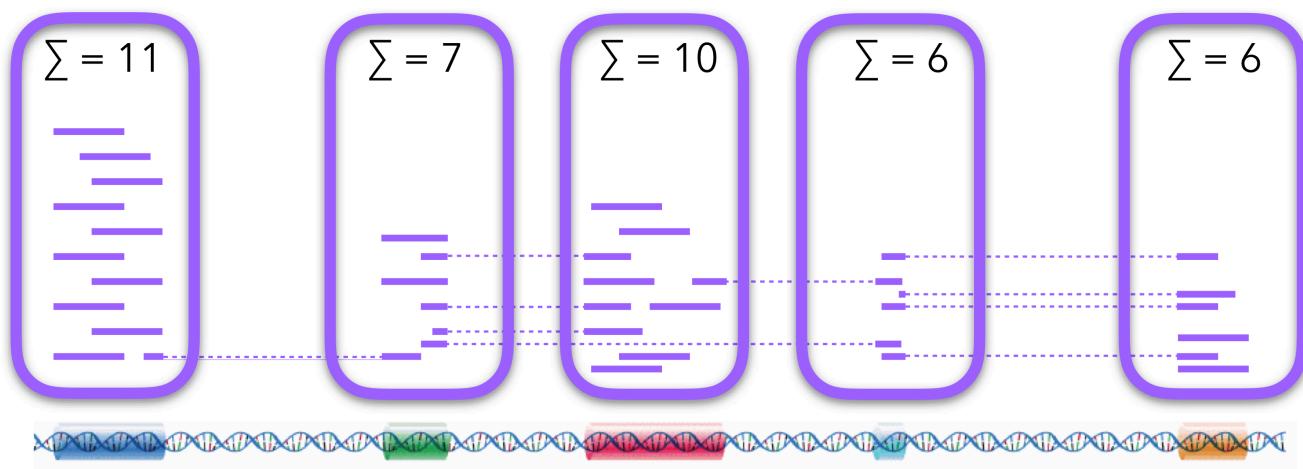


Figure 18: Figure: Gene- and exon-level read counting. Image adapted from Charlotte Soneson.
20



Figure 5

An illustration of the alignment of various reads to a gene with three isoforms: blue (B), green (G), and red (R). In this example, we wish to estimate the abundances of these isoforms, but most reads have ambiguous origins and need to be probabilistically assigned to the transcripts (relative probabilities for each read are shown by the magnitudes of the three colors). Some reads are consistent only with the B and G transcripts, and a few reads uniquely align to a single transcript (single color). In the expectation-maximization (or related) algorithm, given the current abundance estimates, fragments are probabilistically assigned to transcripts, and then estimated abundances are updated by summarizing the (proportional) allocations over all fragments; transcript abundance estimates are determined by iterating the procedure until convergence.

Figure 19: Figure: Abundance quantification using the EM algorithm. Figure from Van den Berge et al. (2019).

- Indeed, for a gene with the same mRNA concentration in two samples, sequencing one sample deeper, will on average result in a higher count.
- Likewise, for two transcripts with the same mRNA concentration but different transcript lengths, one will tend to observe more fragments from the longer transcript due to the fragmentation step in the RNA-seq protocol, where longer transcripts can be split into more fragments of appropriate length.

Below we introduce several relevant abundance metrics, but note that most data analysis methods we will discuss in this course will work with (estimated) counts. In what follows, let Y_{fi} denote the random variable representing the expression counts of feature f in sample i (obtained either as a simple sum of fragments or estimated using lightweight approaches), and let $N_i = \sum_f Y_{fi}$ denote the sequencing depth of sample i .

- **Counts per million (CPM)** are the counts one could expect to observe if the sample was sequenced to a depth of one million.

$$CPM_{fi} = \frac{Y_{fi}}{N_i} 10^6$$

- **Transcripts per million (TPM)** refers to the concentration or proportion of your feature in the sample. TPMs take into account the length of the feature, which is often reformulated into an *effective length* $l_{fi}^{(eff)}$, relating to the number of possible start sites that a feature may have in order to generate fragments of a typical length observed in your dataset. This typical length is often calculated using the observed fragment length distribution from the data and defined as

$$l_{fi}^{(eff)} = l_f - \hat{F}_i + 1,$$

where l_f is the total length of a feature in terms of number of nucleotides, and \hat{F}_i is the estimated average fragment length in sample i . We can use this to define

$$TPM_{fi} = \frac{Y_{fi}}{l_{fi}^{(eff)}} \left(\frac{1}{\sum_f \frac{Y_{fi}}{l_{fi}^{(eff)}}} \right) 10^6.$$

Note that the first part of the right-hand-side (RHS), $\frac{Y_{fi}}{l_{fi}^{(eff)}}$ is the expression counts normalized for the length of the feature. This measure, however, is still affected by the sequencing depth, which is then alleviated by dividing by the sum of the length-normalized counts across all features, i.e., $\sum_f \frac{Y_{fi}}{l_{fi}^{(eff)}}$. TPMs hence normalize for the feature length as well as sequencing depth.

3.4.2 The final countdown

Once abundances have been quantified, the (estimated) counts are typically stored in a count matrix, with genes spanning the rows and samples spanning the columns. This count matrix forms the basis of most downstream analyses to interpret RNA-seq data, and it will be the main object we will be working with in the following lectures.

4 References



Figure 20: Figure: An updated sequencing workflow. Image adapted from Van den Berge et al. (2019).