

# Blur

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An R package for finding convolution for subsets of large rasters (to determine effective spatial scales).

## Introduction

Consider the linear predictor at location  $\mathbf{s}_i$ :

$$\mu(\mathbf{s}_i) = \beta_1 x_1(\mathbf{s}_i) + \dots + \beta_P x_P(\mathbf{s}_i) + \gamma_1 y_1 + \dots + \gamma_Q y_Q + z_1(\mathbf{s}_i) + \dots + z_R(\mathbf{s}_i) \quad (1)$$

where  $x_1 \dots x_P$  are spatial covariates with corresponding unknown effective spatial scales  $\sigma_1 \dots \sigma_P$ ,  $\beta$ s are unknown weights and  $y_1 \dots y_Q$  are other terms such as non-spatial fixed effects with unknown weights  $\gamma$  and  $z_1(\mathbf{s}_i) \dots z_R(\mathbf{s}_i)$  are spatial and non-spatial random effects.

The spatial covariates are defined such that

$$x(\mathbf{s}_i) = \frac{\sum_{\mathbf{s}_j \in \Omega} K(\sigma^{-1} \|\mathbf{s}_i - \mathbf{s}_j\|) 1_{x=X(\mathbf{s}_j)}}{\sum_{\mathbf{s}_j \in \Omega} K(\sigma^{-1} \|\mathbf{s}_i - \mathbf{s}_j\|)} \quad (2),$$

where the indicator function  $1_{x=X(\mathbf{s}_j)}$  returns 1 if the map  $X(\mathbf{s}_j)$  contains the variable  $x$  at the location  $\mathbf{s}_j$ , or 0 otherwise. The equation (2) produces a subset of convolution and applying it over all locations in  $\Omega$  generates visually a blur effect (hence the name of the package), where the blur is stronger for larger scales (see figure 1).

Such construct captures spatial variation surrounding the covariate (eg. habitat type, population density, elevation) at location  $\mathbf{s}_i$  and typically the kernel function  $K$  assigns more weight on the nearby locations than distant. There are two unknowns to be determined: 1) strength of the effect, i.e.  $\beta$  and 2) scale of the effect, i.e.  $\sigma$ . The latter is the radius of the kernel and distances longer than that do not practically contribute to the result. (The kernel function  $K$  is unknown also, but we assume it to be known.)

In practice, models (1) cannot be estimated directly due to the heavy computation of the  $x(\mathbf{s}_i)$ s and, instead, multiple  $x(\mathbf{s}_i)$ s at  $\Sigma$  different fixed scales  $\sigma \in \{\sigma_1 \dots \sigma_\Sigma\}$  are precomputed. From those, the effective scale and magnitude of the effect are found via variable selection.

This R package provides tools for finding convolution  $x(\mathbf{s}_i)$  between map  $X$  and kernel  $K$  at each location  $\mathbf{s}_i$  for each scale  $\sigma_1 \dots \sigma_\Sigma$ . It is left to the user to determine which scales are relevant depending on the nature of the generating spatial processes. Once the covariates  $x_1(\mathbf{s}_i) \dots x_P(\mathbf{s}_i)$  are computed, they are included in the model such as (1) and selected using WAIC or other variable selection method. The R package [SpaceTimeModels](#) provides spatial and spatio-temporal model fitting, which may be helpful for the selection.

## Installation

The package is available in Github and can be installed with the following commands:

```
library(devtools)
install.github("statguy/Blur")
```

The `devtools` package is needed to be installed first. The package can be loaded with

```
library(Blur)
```

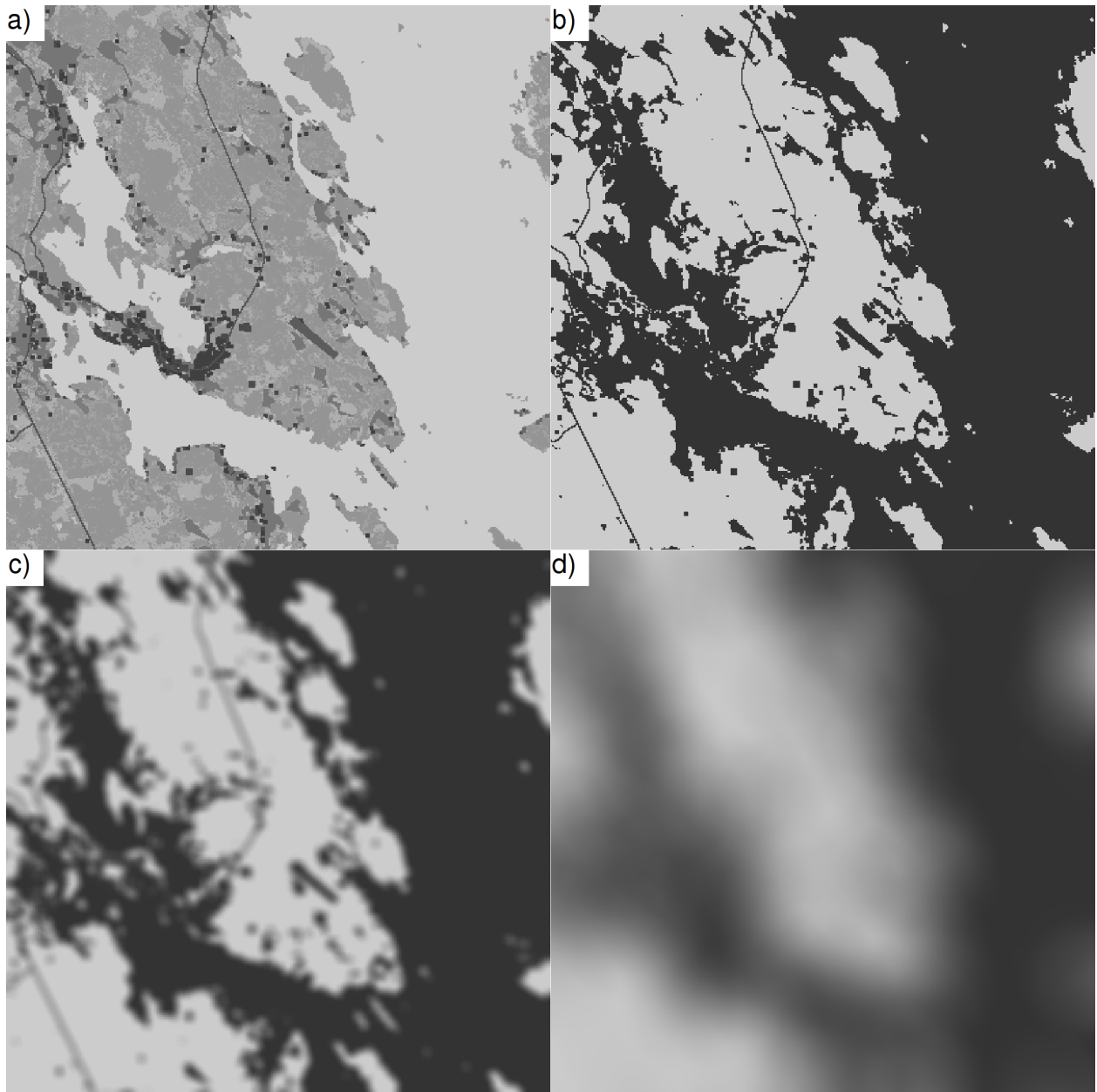


Figure 1: Panel a) Landscape classified to various habitat types. b) Only forest habitat. c) Forest habitat convolution at the scale of 125 meters. d) Forest habitat convolution at the scale of 1 km.

## Kernels

The following kernels are currently implemented in the package:

- `ExponentialKernel` for exponential smoothing and
- `GaussianKernel` for Gaussian smoothing.

Kernel objects are created with the `new` constructor, eg.

```
kernel <- ExponentialKernel$new()
```

User may specify custom kernels as well by inheriting from the `Kernel` class and implementing the `constructKernelInternal` abstract method. See the [source code](#) for examples.

## Convolution

Convolution for the locations specified by x and y coordinates is performed with the functions

- `smoothContinuousSubsets` for continuous data and
- `smoothDiscreteSubsets` for discrete data with multiple classes.

Say that we have locations of the measurements in the variable `coords` (as `data.frame`, `matrix` or `SpatialPoints` (of the `sp` package) class) and the continuous covariate raster (map) in `r` as the `RasterLayer` object of the `raster` package. Using

```
x <- Blur::smoothContinuousSubsets(r=r, coords=coords, kernel=kernel,
  scales=c(1000,2000,4000))
```

the convolution is found for the scales 1000, 2000 and 4000 in the coordinate units defined by the raster map `r`.

Edge values that should be ignored are specified with the `edgeValues` argument as a `numeric` vector. By default no values in `r` are ignored except `NA`.

For a multivalued discrete raster, the corresponding call is

```
x <- Blur::smoothDiscreteSubsets(r=r, coords=coords, kernel=kernel,
  scales=c(1000,2000,4000), smoothValues=c(1,2,3))
```

where `smoothValues` argument specifies a vector of the values to be smoothed.

The covariates are returned in wide format, but can be returned in the long format with the `wide=FALSE` argument.

By default, the convolution is performed in parallel taking advantage of the multicore/multiprocessor environment if available, but can be turned off by setting the `.parallel=FALSE` argument. The parallel computation is enabled by installing the `doMC` package and issuing the following commands first:

```
library(parallel)
library(doMC)
registerDoMC(cores=detectCores())
```

## Additional remarks

Convolution may produce undesired effects near the edges of the covariate raster if not properly handled. The smoothing functions cut the kernel  $K$  if outside the raster  $X$  and rescales it so that the kernel matrix values sum to unity. This ensures that no artifacts are generated near the edges.

Note that the convolution is performed only at the measurement and prediction locations, which is usually much smaller number than the data available in the covariate raster (denoted with  $X$ ) files. There are faster ways to perform the convolution over the whole study area, but working with large raster files may lead to memory issues.

The functions `smoothContinuousSubsets` and `smoothDiscreteSubsets` are the same except the latter creates a binary mask of a subset of the raster where the convolution is applied on. The same result is achieved by masking the whole raster and supplying it to `smoothContinuousSubsets`. However, the use of subsets saves memory.

## Feedback

For feedback, please contact Jussi Jousimo at [jvj@iki.fi](mailto:jvj@iki.fi).