Optimization

February 10, 2021

0.1 Optimization for Fully Connected Networks

In this notebook, we will implement different optimization rules for gradient descent. We have provided starter code; however, you will need to copy and paste your code from your implementation of the modular fully connected nets in HW #3 to build upon this.

CS231n has built a solid API for building these modular frameworks and training them, and we will use their very well implemented framework as opposed to "reinventing the wheel." This includes using their Solver, various utility functions, and their layer structure. This also includes nndl.fc_net, nndl.layers, and nndl.layer_utils. As in prior assignments, we thank Serena Yeung & Justin Johnson for permission to use code written for the CS 231n class (cs231n.stanford.edu).

```
In [1]: ## Import and setups
        import time
        import numpy as np
        import matplotlib.pyplot as plt
        from nndl.fc_net import *
        from cs231n.data_utils import get_CIFAR10_data
        from cs231n.gradient_check import eval_numerical_gradient, eval_numerical_gradient_arra
        from cs231n.solver import Solver
        %matplotlib inline
        plt.rcParams['figure.figsize'] = (10.0, 8.0) # set default size of plots
        plt.rcParams['image.interpolation'] = 'nearest'
        plt.rcParams['image.cmap'] = 'gray'
        # for auto-reloading external modules
        # see http://stackoverflow.com/questions/1907993/autoreload-of-modules-in-ipython
        %load ext autoreload
        %autoreload 2
        def rel_error(x, y):
          """ returns relative error """
          return np.max(np.abs(x - y) / (np.maximum(1e-8, np.abs(x) + np.abs(y))))
In [2]: # Load the (preprocessed) CIFAR10 data.
        data = get_CIFAR10_data()
```

```
for k in data.keys():
    print('{}: {} '.format(k, data[k].shape))

X_train: (49000, 3, 32, 32)
y_train: (49000,)

X_val: (1000, 3, 32, 32)
y_val: (1000,)

X_test: (1000, 3, 32, 32)
y_test: (1000,)
```

0.2 Building upon your HW #3 implementation

Copy and paste the following functions from your HW #3 implementation of a modular FC net:

- affine_forward in nndl/layers.py
- affine_backward in nndl/layers.py
- relu_forward in nndl/layers.py
- relu_backward in nndl/layers.py
- affine_relu_forward in nndl/layer_utils.py
- affine_relu_backward in nndl/layer_utils.py
- The FullyConnectedNet class in nndl/fc_net.py

0.2.1 Test all functions you copy and pasted

```
In [9]: from nndl.layer_tests import *
        affine_forward_test(); print('\n')
        affine_backward_test(); print('\n')
        relu_forward_test(); print('\n')
       relu_backward_test(); print('\n')
        affine_relu_test(); print('\n')
        fc_net_test()
If affine_forward function is working, difference should be less than 1e-9:
difference: 9.7698500479884e-10
If affine_backward is working, error should be less than 1e-9::
dx error: 2.5674880320599406e-10
dw error: 1.1072649924956976e-10
db error: 6.34992930063245e-11
If relu_forward function is working, difference should be around 1e-8:
difference: 4.999999798022158e-08
If relu_forward function is working, error should be less than 1e-9:
```

```
If affine_relu_forward and affine_relu_backward are working, error should be less than 1e-9::
dx error: 2.3621210601547635e-11
dw error: 1.1156063849734917e-09
db error: 7.826664541496885e-12
Running check with reg = 0
Initial loss: 2.3017421779580767
W1 relative error: 1.5084400200498516e-06
W2 relative error: 1.3775224757147523e-06
W3 relative error: 8.909682200725716e-08
b1 relative error: 8.609616513959897e-08
b2 relative error: 1.5413886482138335e-08
b3 relative error: 1.347783721628031e-10
Running check with reg = 3.14
Initial loss: 6.682355902315649
W1 relative error: 4.924156166497565e-08
W2 relative error: 3.9030799191168844e-08
W3 relative error: 1.6484914722565553e-08
b1 relative error: 2.4823367993673714e-08
b2 relative error: 2.46596419476167e-08
b3 relative error: 2.67837965759578e-10
```

1 Training a larger model

In general, proceeding with vanilla stochastic gradient descent to optimize models may be fraught with problems and limitations, as discussed in class. Thus, we implement optimizers that improve on SGD.

1.1 SGD + momentum

In the following section, implement SGD with momentum. Read the nndl/optim.py API, which is provided by CS231n, and be sure you understand it. After, implement sgd_momentum in nndl/optim.py. Test your implementation of sgd_momentum by running the cell below.

```
In [15]: from nndl.optim import sgd_momentum

N, D = 4, 5
w = np.linspace(-0.4, 0.6, num=N*D).reshape(N, D)
dw = np.linspace(-0.6, 0.4, num=N*D).reshape(N, D)
v = np.linspace(0.6, 0.9, num=N*D).reshape(N, D)

config = {'learning_rate': 1e-3, 'velocity': v}
next_w, _ = sgd_momentum(w, dw, config=config)
```

```
expected_next_w = np.asarray([
            0.20738947, 0.27417895, 0.34096842, 0.40775789],
  0.1406,
  [0.47454737, 0.54133684, 0.60812632, 0.67491579, 0.74170526],
  [ 0.80849474, 0.87528421, 0.94207368, 1.00886316, 1.07565263],
  [1.14244211, 1.20923158, 1.27602105, 1.34281053, 1.4096
                                                               11)
expected velocity = np.asarray([
            0.55475789, 0.56891579, 0.58307368, 0.59723158],
  [0.5406,
  [ 0.61138947, 0.62554737, 0.63970526, 0.65386316, 0.66802105],
  [0.68217895, 0.69633684, 0.71049474, 0.72465263, 0.73881053],
  [ 0.75296842, 0.76712632, 0.78128421, 0.79544211, 0.8096
                                                               ]])
print('next_w error: {}'.format(rel_error(next_w, expected_next_w)))
print('velocity error: {}'.format(rel_error(expected_velocity, config['velocity'])))
```

0.9 0.001

next_w error: 8.882347033505819e-09 velocity error: 4.269287743278663e-09

1.2 SGD + Nesterov momentum

Implement sgd_nesterov_momentum in ndl/optim.py.

```
In [17]: from nndl.optim import sgd_nesterov_momentum
        N, D = 4, 5
        w = np.linspace(-0.4, 0.6, num=N*D).reshape(N, D)
        dw = np.linspace(-0.6, 0.4, num=N*D).reshape(N, D)
        v = np.linspace(0.6, 0.9, num=N*D).reshape(N, D)
        config = {'learning_rate': 1e-3, 'velocity': v}
        next_w, _ = sgd_nesterov_momentum(w, dw, config=config)
        expected_next_w = np.asarray([
          [0.08714, 0.15246105, 0.21778211, 0.28310316, 0.34842421],
          [0.41374526, 0.47906632, 0.54438737, 0.60970842, 0.67502947],
          [0.74035053, 0.80567158, 0.87099263, 0.93631368, 1.00163474],
          [1.06695579, 1.13227684, 1.19759789, 1.26291895, 1.32824 ]])
        expected_velocity = np.asarray([
          [0.5406, 0.55475789, 0.56891579, 0.58307368, 0.59723158],
          [ 0.61138947, 0.62554737, 0.63970526, 0.65386316, 0.66802105],
          [0.68217895, 0.69633684, 0.71049474, 0.72465263, 0.73881053],
          [ 0.75296842, 0.76712632, 0.78128421, 0.79544211, 0.8096
                                                                        11)
        print('next_w error: {}'.format(rel_error(next_w, expected_next_w)))
        print('velocity error: {}'.format(rel_error(expected_velocity, config['velocity'])))
```

```
next_w error: 1.0875186845081027e-08 velocity error: 4.269287743278663e-09
```

1.3 Evaluating SGD, SGD+Momentum, and SGD+NesterovMomentum

Run the following cell to train a 6 layer FC net with SGD, SGD+momentum, and SGD+Nesterov momentum. You should see that SGD+momentum achieves a better loss than SGD, and that SGD+Nesterov momentum achieves a slightly better loss (and training accuracy) than SGD+momentum.

```
In [20]: num_train = 4000
         small data = {
           'X_train': data['X_train'][:num_train],
           'y_train': data['y_train'][:num_train],
           'X_val': data['X_val'],
           'y_val': data['y_val'],
         }
         solvers = {}
         for update_rule in ['sgd', 'sgd_momentum', 'sgd_nesterov_momentum']:
           print('Optimizing with {}'.format(update_rule))
           model = FullyConnectedNet([100, 100, 100, 100, 100], weight scale=5e-2)
           solver = Solver(model, small data,
                           num_epochs=5, batch_size=100,
                           update_rule=update_rule,
                           optim_config={
                              'learning_rate': 1e-2,
                           verbose=False)
           solvers[update_rule] = solver
           solver.train()
           print
         plt.subplot(3, 1, 1)
         plt.title('Training loss')
         plt.xlabel('Iteration')
         plt.subplot(3, 1, 2)
         plt.title('Training accuracy')
         plt.xlabel('Epoch')
         plt.subplot(3, 1, 3)
         plt.title('Validation accuracy')
         plt.xlabel('Epoch')
```

```
for update_rule, solver in solvers.items():
    plt.subplot(3, 1, 1)
    plt.plot(solver.loss_history, 'o', label=update_rule)

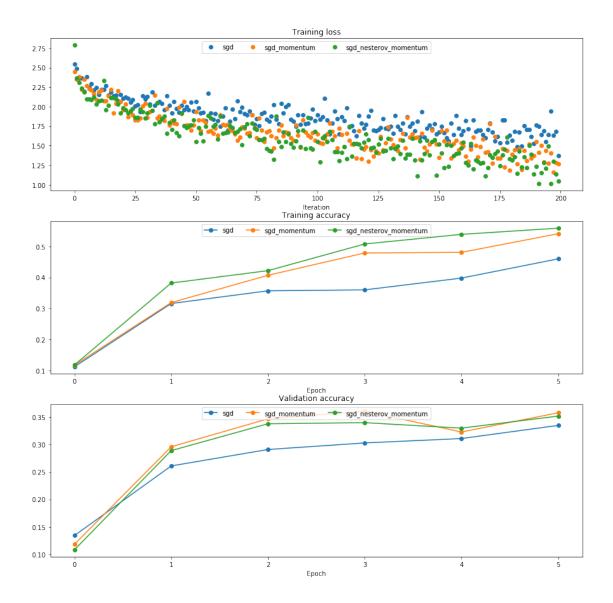
    plt.subplot(3, 1, 2)
    plt.plot(solver.train_acc_history, '-o', label=update_rule)

    plt.subplot(3, 1, 3)
    plt.plot(solver.val_acc_history, '-o', label=update_rule)

for i in [1, 2, 3]:
    plt.subplot(3, 1, i)
    plt.legend(loc='upper center', ncol=4)
    plt.gcf().set_size_inches(15, 15)
    plt.show()

Optimizing with sgd
Optimizing with sgd_momentum
Optimizing with sgd_nesterov_momentum
```

/Users/stathismegas/opt/anaconda3/envs/nndl/lib/python3.6/site-packages/matplotlib/cbook/deprewarnings.warn(message, mplDeprecation, stacklevel=1)



1.4 RMSProp

Now we go to techniques that adapt the gradient. Implement rmsprop in nndl/optim.py. Test your implementation by running the cell below.

```
In [23]: from nndl.optim import rmsprop

N, D = 4, 5
w = np.linspace(-0.4, 0.6, num=N*D).reshape(N, D)
dw = np.linspace(-0.6, 0.4, num=N*D).reshape(N, D)
a = np.linspace(0.6, 0.9, num=N*D).reshape(N, D)

config = {'learning_rate': 1e-2, 'a': a}
```

```
next_w, _ = rmsprop(w, dw, config=config)
        expected_next_w = np.asarray([
          [-0.39223849, -0.34037513, -0.28849239, -0.23659121, -0.18467247],
          [-0.132737, -0.08078555, -0.02881884, 0.02316247, 0.07515774],
          [ 0.12716641, 0.17918792, 0.23122175, 0.28326742, 0.33532447],
          [ 0.38739248, 0.43947102, 0.49155973, 0.54365823, 0.59576619]])
        expected_cache = np.asarray([
                    0.6126277, 0.6277108, 0.64284931, 0.65804321],
          [ 0.5976,
          [0.67329252, 0.68859723, 0.70395734, 0.71937285, 0.73484377],
          [0.75037008, 0.7659518, 0.78158892, 0.79728144, 0.81302936],
          [ 0.82883269, 0.84469141, 0.86060554, 0.87657507, 0.8926
                                                                        ]])
        print('next_w error: {}'.format(rel_error(expected_next_w, next_w)))
        print('cache error: {}'.format(rel_error(expected_cache, config['a'])))
next_w error: 9.502645229894295e-08
cache error: 2.6477955807156126e-09
```

1.5 Adaptive moments

Now, implement adam in nndl/optim.py. Test your implementation by running the cell below.

```
In [28]: # Test Adam implementation; you should see errors around 1e-7 or less
        from nndl.optim import adam
        N, D = 4, 5
        w = np.linspace(-0.4, 0.6, num=N*D).reshape(N, D)
        dw = np.linspace(-0.6, 0.4, num=N*D).reshape(N, D)
        v = np.linspace(0.6, 0.9, num=N*D).reshape(N, D)
        a = np.linspace(0.7, 0.5, num=N*D).reshape(N, D)
        config = {'learning_rate': 1e-2, 'v': v, 'a': a, 't': 5}
        next_w, _ = adam(w, dw, config=config)
        expected_next_w = np.asarray([
          [-0.40094747, -0.34836187, -0.29577703, -0.24319299, -0.19060977],
          [-0.1380274, -0.08544591, -0.03286534, 0.01971428, 0.0722929],
          [0.1248705, 0.17744702, 0.23002243, 0.28259667, 0.33516969],
          [ 0.38774145, 0.44031188, 0.49288093, 0.54544852, 0.59801459]])
        expected_a = np.asarray([
          [0.69966, 0.68908382, 0.67851319, 0.66794809, 0.65738853,],
          [0.64683452, 0.63628604, 0.6257431, 0.61520571, 0.60467385,],
          [0.59414753, 0.58362676, 0.57311152, 0.56260183, 0.55209767,],
          [ 0.54159906, 0.53110598, 0.52061845, 0.51013645, 0.49966, ]])
        expected_v = np.asarray([
                   0.49947368, 0.51894737, 0.53842105, 0.55789474],
          [ 0.48,
```

```
[ 0.57736842, 0.59684211, 0.61631579, 0.63578947, 0.65526316],
        [ 0.67473684, 0.69421053, 0.71368421, 0.73315789, 0.75263158],
        [ 0.77210526, 0.79157895, 0.81105263, 0.83052632, 0.85 ]])

        print('next_w error: {}'.format(rel_error(expected_next_w, next_w)))
        print('a error: {}'.format(rel_error(expected_a, config['a'])))
        print('v error: {}'.format(rel_error(expected_v, config['v'])))

next_w error: 1.1395691798535431e-07
a error: 4.208314038113071e-09
v error: 4.214963193114416e-09
```

1.6 Comparing SGD, SGD+NesterovMomentum, RMSProp, and Adam

The following code will compare optimization with SGD, Momentum, Nesterov Momentum, RM-SProp and Adam. In our code, we find that RMSProp, Adam, and SGD + Nesterov Momentum achieve approximately the same training error after a few training epochs.

```
In [29]: learning_rates = {'rmsprop': 2e-4, 'adam': 1e-3}
         for update_rule in ['adam', 'rmsprop']:
           print('Optimizing with {}'.format(update_rule))
           model = FullyConnectedNet([100, 100, 100, 100, 100], weight_scale=5e-2)
           solver = Solver(model, small_data,
                           num_epochs=5, batch_size=100,
                           update_rule=update_rule,
                           optim_config={
                              'learning_rate': learning_rates[update_rule]
                           },
                           verbose=False)
           solvers[update_rule] = solver
           solver.train()
           print
         plt.subplot(3, 1, 1)
         plt.title('Training loss')
         plt.xlabel('Iteration')
         plt.subplot(3, 1, 2)
         plt.title('Training accuracy')
         plt.xlabel('Epoch')
         plt.subplot(3, 1, 3)
         plt.title('Validation accuracy')
         plt.xlabel('Epoch')
```

```
for update_rule, solver in solvers.items():
    plt.subplot(3, 1, 1)
    plt.plot(solver.loss_history, 'o', label=update_rule)

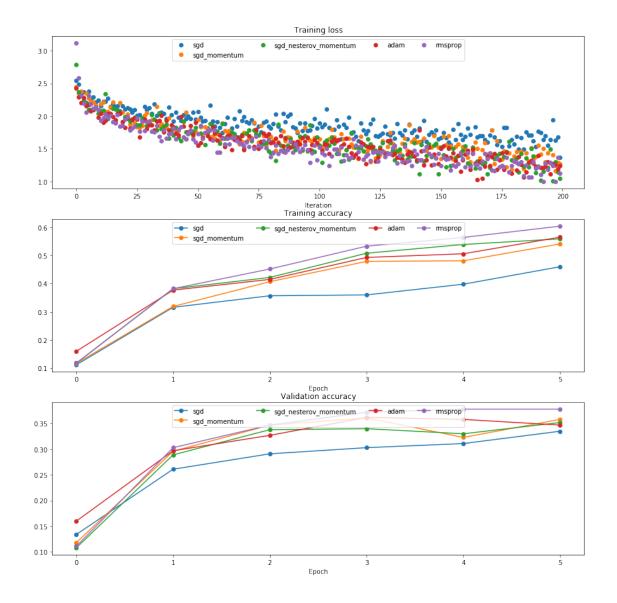
    plt.subplot(3, 1, 2)
    plt.plot(solver.train_acc_history, '-o', label=update_rule)

    plt.subplot(3, 1, 3)
    plt.plot(solver.val_acc_history, '-o', label=update_rule)

for i in [1, 2, 3]:
    plt.subplot(3, 1, i)
    plt.legend(loc='upper center', ncol=4)
    plt.gcf().set_size_inches(15, 15)
    plt.show()

Optimizing with adam
Optimizing with rmsprop
```

/Users/stathismegas/opt/anaconda3/envs/nndl/lib/python3.6/site-packages/matplotlib/cbook/deprewarnings.warn(message, mplDeprecation, stacklevel=1)



1.7 Easier optimization

In the following cell, we'll train a 4 layer neural network having 500 units in each hidden layer with the different optimizers, and find that it is far easier to get up to 50+% performance on CIFAR-10. After we implement batchnorm and dropout, we'll ask you to get 55+% on CIFAR-10.

```
In [30]: optimizer = 'adam'
    best_model = None

layer_dims = [500, 500, 500]
  weight_scale = 0.01
  learning_rate = 1e-3
  lr_decay = 0.9
```

```
model = FullyConnectedNet(layer_dims, weight_scale=weight_scale,
                                   use_batchnorm=True)
         solver = Solver(model, data,
                         num_epochs=10, batch_size=100,
                         update rule=optimizer,
                         optim_config={
                           'learning_rate': learning_rate,
                         },
                         lr_decay=lr_decay,
                         verbose=True, print_every=50)
         solver.train()
(Iteration 1 / 4900) loss: 2.323014
(Epoch 0 / 10) train acc: 0.215000; val_acc: 0.219000
(Iteration 51 / 4900) loss: 1.623141
(Iteration 101 / 4900) loss: 1.767984
(Iteration 151 / 4900) loss: 1.399408
(Iteration 201 / 4900) loss: 1.465321
(Iteration 251 / 4900) loss: 1.569343
(Iteration 301 / 4900) loss: 1.520545
(Iteration 351 / 4900) loss: 1.659743
(Iteration 401 / 4900) loss: 1.441347
(Iteration 451 / 4900) loss: 1.382932
(Epoch 1 / 10) train acc: 0.504000; val acc: 0.460000
(Iteration 501 / 4900) loss: 1.139995
(Iteration 551 / 4900) loss: 1.306148
(Iteration 601 / 4900) loss: 1.356901
(Iteration 651 / 4900) loss: 1.339270
(Iteration 701 / 4900) loss: 1.408049
(Iteration 751 / 4900) loss: 1.289504
(Iteration 801 / 4900) loss: 1.428854
(Iteration 851 / 4900) loss: 1.269246
(Iteration 901 / 4900) loss: 1.133099
(Iteration 951 / 4900) loss: 1.144630
(Epoch 2 / 10) train acc: 0.560000; val_acc: 0.540000
(Iteration 1001 / 4900) loss: 1.292918
(Iteration 1051 / 4900) loss: 1.205553
(Iteration 1101 / 4900) loss: 1.087161
(Iteration 1151 / 4900) loss: 1.260181
(Iteration 1201 / 4900) loss: 1.134963
(Iteration 1251 / 4900) loss: 1.105680
(Iteration 1301 / 4900) loss: 1.152940
(Iteration 1351 / 4900) loss: 1.161172
(Iteration 1401 / 4900) loss: 1.147134
(Iteration 1451 / 4900) loss: 0.999926
(Epoch 3 / 10) train acc: 0.607000; val_acc: 0.554000
```

```
(Iteration 1501 / 4900) loss: 0.965714
(Iteration 1551 / 4900) loss: 1.167281
(Iteration 1601 / 4900) loss: 1.376391
(Iteration 1651 / 4900) loss: 0.979931
(Iteration 1701 / 4900) loss: 1.196980
(Iteration 1751 / 4900) loss: 1.020352
(Iteration 1801 / 4900) loss: 1.196114
(Iteration 1851 / 4900) loss: 0.985472
(Iteration 1901 / 4900) loss: 1.168343
(Iteration 1951 / 4900) loss: 1.162383
(Epoch 4 / 10) train acc: 0.620000; val_acc: 0.557000
(Iteration 2001 / 4900) loss: 0.948648
(Iteration 2051 / 4900) loss: 0.891093
(Iteration 2101 / 4900) loss: 1.109773
(Iteration 2151 / 4900) loss: 0.992742
(Iteration 2201 / 4900) loss: 1.037180
(Iteration 2251 / 4900) loss: 1.000976
(Iteration 2301 / 4900) loss: 0.813562
(Iteration 2351 / 4900) loss: 1.075664
(Iteration 2401 / 4900) loss: 1.146494
(Epoch 5 / 10) train acc: 0.654000; val acc: 0.563000
(Iteration 2451 / 4900) loss: 0.905896
(Iteration 2501 / 4900) loss: 0.767075
(Iteration 2551 / 4900) loss: 1.098396
(Iteration 2601 / 4900) loss: 0.805684
(Iteration 2651 / 4900) loss: 0.856237
(Iteration 2701 / 4900) loss: 1.057827
(Iteration 2751 / 4900) loss: 1.077589
(Iteration 2801 / 4900) loss: 0.883959
(Iteration 2851 / 4900) loss: 0.924040
(Iteration 2901 / 4900) loss: 0.743116
(Epoch 6 / 10) train acc: 0.675000; val_acc: 0.549000
(Iteration 2951 / 4900) loss: 0.875558
(Iteration 3001 / 4900) loss: 0.793751
(Iteration 3051 / 4900) loss: 0.942932
(Iteration 3101 / 4900) loss: 0.767934
(Iteration 3151 / 4900) loss: 0.769317
(Iteration 3201 / 4900) loss: 0.672196
(Iteration 3251 / 4900) loss: 0.700567
(Iteration 3301 / 4900) loss: 0.827174
(Iteration 3351 / 4900) loss: 0.890606
(Iteration 3401 / 4900) loss: 0.705535
(Epoch 7 / 10) train acc: 0.750000; val_acc: 0.556000
(Iteration 3451 / 4900) loss: 0.942096
(Iteration 3501 / 4900) loss: 0.673768
(Iteration 3551 / 4900) loss: 0.958750
(Iteration 3601 / 4900) loss: 0.714521
(Iteration 3651 / 4900) loss: 0.630136
```

```
(Iteration 3701 / 4900) loss: 0.717633
(Iteration 3751 / 4900) loss: 1.065947
(Iteration 3801 / 4900) loss: 0.766535
(Iteration 3851 / 4900) loss: 0.655765
(Iteration 3901 / 4900) loss: 0.634796
(Epoch 8 / 10) train acc: 0.745000; val acc: 0.566000
(Iteration 3951 / 4900) loss: 0.604901
(Iteration 4001 / 4900) loss: 0.671123
(Iteration 4051 / 4900) loss: 0.675287
(Iteration 4101 / 4900) loss: 0.657262
(Iteration 4151 / 4900) loss: 0.859105
(Iteration 4201 / 4900) loss: 0.658996
(Iteration 4251 / 4900) loss: 0.727481
(Iteration 4301 / 4900) loss: 0.568398
(Iteration 4351 / 4900) loss: 0.440338
(Iteration 4401 / 4900) loss: 0.630017
(Epoch 9 / 10) train acc: 0.802000; val_acc: 0.554000
(Iteration 4451 / 4900) loss: 0.648635
(Iteration 4501 / 4900) loss: 0.611868
(Iteration 4551 / 4900) loss: 0.765228
(Iteration 4601 / 4900) loss: 0.752633
(Iteration 4651 / 4900) loss: 0.453143
(Iteration 4701 / 4900) loss: 0.557257
(Iteration 4751 / 4900) loss: 0.536190
(Iteration 4801 / 4900) loss: 0.532417
(Iteration 4851 / 4900) loss: 0.568353
(Epoch 10 / 10) train acc: 0.824000; val_acc: 0.553000
In [31]: y_test_pred = np.argmax(model.loss(data['X_test']), axis=1)
         y_val_pred = np.argmax(model.loss(data['X_val']), axis=1)
         print('Validation set accuracy: {}'.format(np.mean(y_val_pred == data['y_val'])))
         print('Test set accuracy: {}'.format(np.mean(y_test_pred == data['y_test'])))
Validation set accuracy: 0.572
Test set accuracy: 0.55
```

optim

February 10, 2021

In []: import numpy as np

HHHH

This code was originally written for CS 231n at Stanford University (cs231n.stanford.edu). It has been modified in various areas for use in the ECE 239AS class at UCLA. This includes the descriptions of what code to implement as well as some slight potential changes in variable names to be consistent with class nomenclature. We thank Justin Johnson & Serena Yeung for permission to use this code. To see the original version, please visit cs231n.stanford.edu.

" " "

11 11 11

This file implements various first-order update rules that are commonly used for training neural networks. Each update rule accepts current weights and the gradient of the loss with respect to those weights and produces the next set of weights. Each update rule has the same interface:

def update(w, dw, config=None):

Inputs:

- w: A numpy array giving the current weights.
- dw: A numpy array of the same shape as w giving the gradient of the loss with respect to w.
- config: A dictionary containing hyperparameter values such as learning rate, momentum, etc. If the update rule requires caching values over many iterations, then config will also hold these cached values.

Returns:

- $next_w$: The next point after the update.
- config: The config dictionary to be passed to the next iteration of the update rule.

NOTE: For most update rules, the default learning rate will probably not perform well; however the default values of the other hyperparameters should work well for a variety of different problems.

```
For efficiency, update rules may perform in-place updates, mutating w and
setting next_w equal to w.
11 11 11
def sgd(w, dw, config=None):
 Performs vanilla stochastic gradient descent.
 config format:
  - learning_rate: Scalar learning rate.
 if config is None: config = {}
 config.setdefault('learning_rate', 1e-2)
 w -= config['learning_rate'] * dw
 return w, config
def sgd_momentum(w, dw, config=None):
 Performs stochastic gradient descent with momentum.
 config format:
 - learning_rate: Scalar learning rate.
 - momentum: Scalar between 0 and 1 giving the momentum value.
   Setting momentum = 0 reduces to sqd.
  - velocity: A numpy array of the same shape as w and dw used to store a moving
   average of the gradients.
 if config is None: config = {}
 config.setdefault('learning_rate', 1e-2)
 config.setdefault('momentum', 0.9) # set momentum to 0.9 if it wasn't there
 v = config.get('velocity', np.zeros_like(w))
                                                 # gets velocity, else sets it t
  # ------ #
  # YOUR CODE HERE:
     Implement the momentum update formula. Return the updated weights
     as next_w, and the updated velocity as v.
  # ----- #
 next_w = np.zeros_like(w)
 alpha = config.get('momentum')
 eps = config.get('learning_rate')
 #print(alpha, eps)
 v = alpha * v - eps * dw
 next_w = w + v
```

```
# ----- #
 # END YOUR CODE HERE
 # ------ #
 config['velocity'] = v
 return next w, config
def sgd_nesterov_momentum(w, dw, config=None):
 Performs stochastic gradient descent with Nesterov momentum.
 config format:
 - learning_rate: Scalar learning rate.
 - momentum: Scalar between 0 and 1 giving the momentum value.
  Setting momentum = 0 reduces to sgd.
 - velocity: A numpy array of the same shape as w and dw used to store a moving
   average of the gradients.
 11 11 11
 if config is None: config = {}
 config.setdefault('learning_rate', 1e-2)
 config.setdefault('momentum', 0.9) # set momentum to 0.9 if it wasn't there
 v = config.get('velocity', np.zeros_like(w))
                                         # gets velocity, else sets it t
 # ------ #
 # YOUR CODE HERE:
    Implement the momentum update formula. Return the updated weights
    as next_w, and the updated velocity as v.
 # ------ #
 alpha = config['momentum']
 eps = config['learning_rate']
 old_v = v
 next_v = alpha * v - eps * dw
 next_w = w + next_v + alpha * (next_v - old_v)
 v = next v
 # ------ #
 # END YOUR CODE HERE
 # ----- #
 config['velocity'] = v
 return next_w, config
def rmsprop(w, dw, config=None):
 11 11 11
```

Uses the RMSProp update rule, which uses a moving average of squared gradient values to set adaptive per-parameter learning rates.

```
config format:
 - learning_rate: Scalar learning rate.
 - decay_rate: Scalar between 0 and 1 giving the decay rate for the squared
   gradient cache.
 - epsilon: Small scalar used for smoothing to avoid dividing by zero.
 - beta: Moving average of second moments of gradients.
 if config is None: config = {}
 config.setdefault('learning_rate', 1e-2)
 config.setdefault('decay_rate', 0.99)
 config.setdefault('epsilon', 1e-8)
 config.setdefault('a', np.zeros_like(w))
 next_w = None
 # ------ #
 # YOUR CODE HERE:
 # Implement RMSProp. Store the next value of w as next_w. You need
   to also store in config['a'] the moving average of the second
 # moment gradients, so they can be used for future gradients. Concretely,
     config['a'] corresponds to "a" in the lecture notes.
 a = config['a']
 beta = config['decay_rate']
 lr = config['learning_rate']
 nu = config['epsilon']
 a = beta * a + (1-beta) * dw * dw
 next_w = w - lr * dw / (np.sqrt(a+ nu))
 config['a'] = a
 # ------ #
 # END YOUR CODE HERE
 # ------ #
 return next_w, config
def adam(w, dw, config=None):
 Uses the Adam update rule, which incorporates moving averages of both the
 gradient and its square and a bias correction term.
 confiq format:
```

```
- learning_rate: Scalar learning rate.
- beta1: Decay rate for moving average of first moment of gradient.
- beta2: Decay rate for moving average of second moment of gradient.
- epsilon: Small scalar used for smoothing to avoid dividing by zero.
- m: Moving average of gradient.
- v: Moving average of squared gradient.
- t: Iteration number.
if config is None: config = {}
config.setdefault('learning_rate', 1e-3)
config.setdefault('beta1', 0.9)
config.setdefault('beta2', 0.999)
config.setdefault('epsilon', 1e-8)
config.setdefault('v', np.zeros_like(w))
config.setdefault('a', np.zeros_like(w))
config.setdefault('t', 0)
next_w = None
# YOUR CODE HERE:
  Implement Adam. Store the next value of w as next_w. You need
# to also store in config['a'] the moving average of the second
  moment gradients, and in config['v'] the moving average of the
   first moments. Finally, store in config['t'] the increasing time.
# ------ #
lr = config['learning_rate']
beta1 = config['beta1']
beta2 = config['beta2']
nu = config['epsilon']
p = config['v']
a = config['a']
t = config['t']
g = dw
t+=1
p = beta1 * p + (1-beta1) * g
a = beta2 * a + (1-beta2) * g * g
p_u = p / (1-beta1**t)
a_u = a / (1-beta2**t)
next_w = w - lr * p_u / (np.sqrt(a_u) + nu)
config['a'] = a
config['v'] = p
config['t'] = t
# ------ #
```

Batch-Normalization

February 10, 2021

1 Batch Normalization

%reload_ext autoreload

In this notebook, you will implement the batch normalization layers of a neural network to increase its performance. Please review the details of batch normalization from the lecture notes.

CS231n has built a solid API for building these modular frameworks and training them, and we will use their very well implemented framework as opposed to "reinventing the wheel." This includes using their Solver, various utility functions, and their layer structure. This also includes nndl.fc_net, nndl.layers, and nndl.layer_utils. As in prior assignments, we thank Serena Yeung & Justin Johnson for permission to use code written for the CS 231n class (cs231n.stanford.edu).

```
In [41]: ## Import and setups
         import time
         import numpy as np
         import matplotlib.pyplot as plt
         from nndl.fc_net import *
         from nndl.layers import *
         from cs231n.data_utils import get_CIFAR10_data
         from cs231n.gradient_check import eval_numerical_gradient, eval_numerical_gradient_ar
         from cs231n.solver import Solver
         %matplotlib inline
         plt.rcParams['figure.figsize'] = (10.0, 8.0) # set default size of plots
         plt.rcParams['image.interpolation'] = 'nearest'
         plt.rcParams['image.cmap'] = 'gray'
         # for auto-reloading external modules
         # see http://stackoverflow.com/questions/1907993/autoreload-of-modules-in-ipython
         %load ext autoreload
         %autoreload 2
         def rel_error(x, y):
           """ returns relative error """
           return np.max(np.abs(x - y) / (np.maximum(1e-8, np.abs(x) + np.abs(y))))
The autoreload extension is already loaded. To reload it, use:
```

1.1 Batchnorm forward pass

Implement the training time batchnorm forward pass, batchnorm_forward, in nndl/layers.py. After that, test your implementation by running the following cell.

```
In [43]: # Check the training-time forward pass by checking means and variances
         # of features both before and after batch normalization
         # Simulate the forward pass for a two-layer network
        N, D1, D2, D3 = 200, 50, 60, 3
        X = np.random.randn(N, D1)
        W1 = np.random.randn(D1, D2)
        W2 = np.random.randn(D2, D3)
        a = np.maximum(0, X.dot(W1)).dot(W2)
        print('Before batch normalization:')
        print(' means: ', a.mean(axis=0))
        print(' stds: ', a.std(axis=0))
         # Means should be close to zero and stds close to one
        print('After batch normalization (gamma=1, beta=0)')
         a_norm, _ = batchnorm_forward(a, np.ones(D3), np.zeros(D3), {'mode': 'train'})
        print(' mean: ', a_norm.mean(axis=0))
        print(' std: ', a_norm.std(axis=0))
         # Now means should be close to beta and stds close to gamma
         gamma = np.asarray([1.0, 2.0, 3.0])
        beta = np.asarray([11.0, 12.0, 13.0])
         a_norm, _ = batchnorm_forward(a, gamma, beta, {'mode': 'train'})
        print('After batch normalization (nontrivial gamma, beta)')
        print(' means: ', a_norm.mean(axis=0))
        print(' stds: ', a_norm.std(axis=0))
Before batch normalization:
 means: [-10.72317378 -23.96027117 -28.21227696]
```

Implement the testing time batchnorm forward pass, batchnorm_forward, in nndl/layers.py. After that, test your implementation by running the following cell.

```
In [44]: # Check the test-time forward pass by running the training-time
         # forward pass many times to warm up the running averages, and then
         # checking the means and variances of activations after a test-time
         # forward pass.
         N, D1, D2, D3 = 200, 50, 60, 3
         W1 = np.random.randn(D1, D2)
         W2 = np.random.randn(D2, D3)
         bn_param = {'mode': 'train'}
         gamma = np.ones(D3)
         beta = np.zeros(D3)
         for t in np.arange(50):
          X = np.random.randn(N, D1)
           a = np.maximum(0, X.dot(W1)).dot(W2)
           batchnorm_forward(a, gamma, beta, bn_param)
         bn_param['mode'] = 'test'
         X = np.random.randn(N, D1)
         a = np.maximum(0, X.dot(W1)).dot(W2)
         a_norm, _ = batchnorm_forward(a, gamma, beta, bn_param)
         # Means should be close to zero and stds close to one, but will be
         # noisier than training-time forward passes.
         print('After batch normalization (test-time):')
         print(' means: ', a_norm.mean(axis=0))
         print(' stds: ', a_norm.std(axis=0))
After batch normalization (test-time):
 means: [-0.01574468 0.05018803 -0.04722696]
  stds: [ 0.97146815  0.9448945  1.03960547]
```

1.2 Batchnorm backward pass

Implement the backward pass for the batchnorm layer, batchnorm_backward in nndl/layers.py. Check your implementation by running the following cell.

In [45]: # Gradient check batchnorm backward pass N, D = 4, 5x = 5 * np.random.randn(N, D) + 12gamma = np.random.randn(D)beta = np.random.randn(D) dout = np.random.randn(N, D) bn param = {'mode': 'train'} fx = lambda x: batchnorm_forward(x, gamma, beta, bn_param)[0] fg = lambda a: batchnorm_forward(x, gamma, beta, bn_param)[0] fb = lambda b: batchnorm_forward(x, gamma, beta, bn_param)[0] dx_num = eval_numerical_gradient_array(fx, x, dout) da_num = eval_numerical_gradient_array(fg, gamma, dout) db_num = eval_numerical_gradient_array(fb, beta, dout) _, cache = batchnorm_forward(x, gamma, beta, bn_param) dx, dgamma, dbeta = batchnorm_backward(dout, cache) print('dx error: ', rel_error(dx_num, dx)) print('dgamma error: ', rel_error(da_num, dgamma)) print('dbeta error: ', rel_error(db_num, dbeta)) dx error: 2.76131460647e-09 dgamma error: 5.28501631015e-12

1.3 Implement a fully connected neural network with batchnorm layers

Modify the FullyConnectedNet() class in nndl/fc_net.py to incorporate batchnorm layers. You will need to modify the class in the following areas:

- (1) The gammas and betas need to be initialized to 1's and 0's respectively in __init__.
- (2) The batchnorm_forward layer needs to be inserted between each affine and relu layer (except in the output layer) in a forward pass computation in loss. You may find it helpful to write an affine_batchnorm_relu() layer in nndl/layer_utils.py although this is not necessary.
- (3) The batchnorm backward layer has to be appropriately inserted when calculating gradients.

After you have done the appropriate modifications, check your implementation by running the following cell.

Note, while the relative error for W3 should be small, as we backprop gradients more, you may find the relative error increases. Our relative error for W1 is on the order of 1e-4.

```
In [50]: N, D, H1, H2, C = 2, 15, 20, 30, 10
    X = np.random.randn(N, D)
```

dbeta error: 3.27557685192e-12

```
y = np.random.randint(C, size=(N,))
         for reg in [0, 3.14]:
           print('Running check with reg = ', reg)
           model = FullyConnectedNet([H1, H2], input_dim=D, num_classes=C,
                                     reg=reg, weight_scale=5e-2, dtype=np.float64,
                                     use batchnorm=True)
           loss, grads = model.loss(X, y)
           print('Initial loss: ', loss)
           for name in sorted(grads):
             f = lambda _: model.loss(X, y)[0]
             grad_num = eval_numerical_gradient(f, model.params[name], verbose=False, h=1e-5)
             print('{} relative error: {}'.format(name, rel_error(grad_num, grads[name])))
           if reg == 0: print('\n')
Running check with reg = 0
Initial loss: 2.41650020747
W1 relative error: 5.985749731163056e-05
W2 relative error: 2.7451619993354665e-05
W3 relative error: 1.62647725491626e-09
b1 relative error: 0.0
b2 relative error: 0.0
b3 relative error: 1.2573369412722414e-10
beta1 relative error: 4.596102177627084e-09
beta2 relative error: 2.9270384543944824e-09
gamma1 relative error: 4.550901225892006e-09
gamma2 relative error: 3.6685936695841338e-09
Running check with reg = 3.14
Initial loss: 6.74771978744
W1 relative error: 6.139323185925442e-05
W2 relative error: 3.571174504398055e-06
W3 relative error: 3.528833394780356e-08
b1 relative error: 0.004440892098500625
b2 relative error: 0.004440892098500625
b3 relative error: 2.7546031757937963e-10
beta1 relative error: 9.208007229374668e-08
beta2 relative error: 3.1981564030343375e-08
gamma1 relative error: 4.064932024614984e-08
gamma2 relative error: 7.047072535184226e-08
```

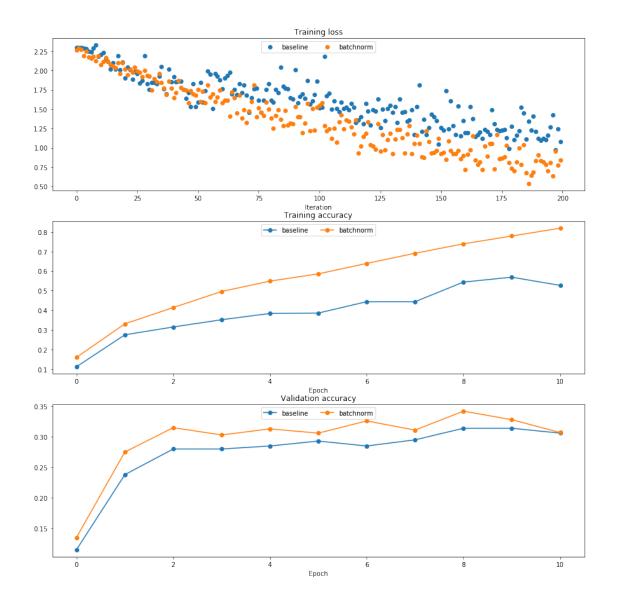
1.4 Training a deep fully connected network with batch normalization.

To see if batchnorm helps, let's train a deep neural network with and without batch normalization.

```
In [51]: # Try training a very deep net with batchnorm
         hidden_dims = [100, 100, 100, 100, 100]
         num_train = 1000
         small data = {
           'X_train': data['X_train'][:num_train],
           'y_train': data['y_train'][:num_train],
           'X_val': data['X_val'],
           'y_val': data['y_val'],
         weight_scale = 2e-2
         bn_model = FullyConnectedNet(hidden_dims, weight_scale=weight_scale, use_batchnorm=Tr
         model = FullyConnectedNet(hidden_dims, weight_scale=weight_scale, use_batchnorm=False
         print('defined the models')
         bn_solver = Solver(bn_model, small_data,
                         num_epochs=10, batch_size=50,
                         update_rule='adam',
                         optim_config={
                           'learning_rate': 1e-3,
                         verbose=True, print_every=200)
         print('now let us train')
         bn_solver.train()
         solver = Solver(model, small_data,
                         num_epochs=10, batch_size=50,
                         update_rule='adam',
                         optim_config={
                           'learning_rate': 1e-3,
                         },
                         verbose=True, print_every=200)
         solver.train()
defined the models
now let us train
(Iteration 1 / 200) loss: 2.266888
(Epoch 0 / 10) train acc: 0.160000; val acc: 0.135000
(Epoch 1 / 10) train acc: 0.331000; val_acc: 0.275000
(Epoch 2 / 10) train acc: 0.414000; val_acc: 0.315000
(Epoch 3 / 10) train acc: 0.496000; val_acc: 0.303000
(Epoch 4 / 10) train acc: 0.549000; val_acc: 0.313000
(Epoch 5 / 10) train acc: 0.586000; val_acc: 0.306000
(Epoch 6 / 10) train acc: 0.639000; val_acc: 0.326000
(Epoch 7 / 10) train acc: 0.691000; val_acc: 0.311000
(Epoch 8 / 10) train acc: 0.739000; val_acc: 0.342000
```

```
(Epoch 9 / 10) train acc: 0.779000; val_acc: 0.328000
(Epoch 10 / 10) train acc: 0.819000; val_acc: 0.307000
(Iteration 1 / 200) loss: 2.302211
(Epoch 0 / 10) train acc: 0.112000; val_acc: 0.115000
(Epoch 1 / 10) train acc: 0.275000; val_acc: 0.238000
(Epoch 2 / 10) train acc: 0.315000; val_acc: 0.280000
(Epoch 3 / 10) train acc: 0.352000; val_acc: 0.280000
(Epoch 4 / 10) train acc: 0.384000; val_acc: 0.285000
(Epoch 5 / 10) train acc: 0.386000; val_acc: 0.293000
(Epoch 6 / 10) train acc: 0.444000; val_acc: 0.285000
(Epoch 7 / 10) train acc: 0.444000; val_acc: 0.295000
(Epoch 8 / 10) train acc: 0.544000; val_acc: 0.314000
(Epoch 9 / 10) train acc: 0.569000; val_acc: 0.314000
(Epoch 10 / 10) train acc: 0.527000; val_acc: 0.306000
In [52]: plt.subplot(3, 1, 1)
        plt.title('Training loss')
         plt.xlabel('Iteration')
         plt.subplot(3, 1, 2)
         plt.title('Training accuracy')
         plt.xlabel('Epoch')
         plt.subplot(3, 1, 3)
         plt.title('Validation accuracy')
         plt.xlabel('Epoch')
         plt.subplot(3, 1, 1)
         plt.plot(solver.loss_history, 'o', label='baseline')
         plt.plot(bn_solver.loss_history, 'o', label='batchnorm')
         plt.subplot(3, 1, 2)
         plt.plot(solver.train_acc_history, '-o', label='baseline')
         plt.plot(bn_solver.train_acc_history, '-o', label='batchnorm')
         plt.subplot(3, 1, 3)
         plt.plot(solver.val_acc_history, '-o', label='baseline')
         plt.plot(bn_solver.val_acc_history, '-o', label='batchnorm')
         for i in [1, 2, 3]:
           plt.subplot(3, 1, i)
           plt.legend(loc='upper center', ncol=4)
         plt.gcf().set_size_inches(15, 15)
         plt.show()
```

/Users/stathismegas/opt/anaconda3/envs/nndl/lib/python3.6/site-packages/matplotlib/cbook/deprewarnings.warn(message, mplDeprecation, stacklevel=1)



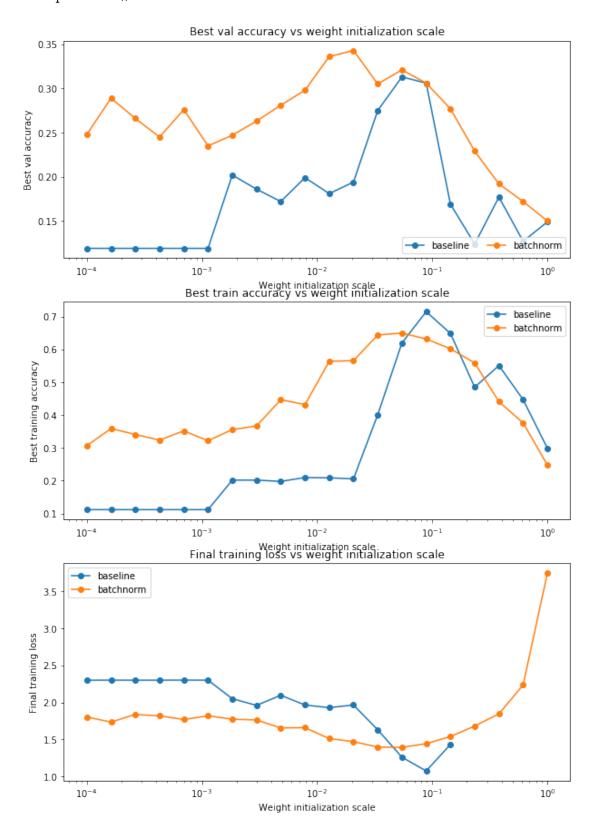
1.5 Batchnorm and initialization

The following cells run an experiment where for a deep network, the initialization is varied. We do training for when batchnorm layers are and are not included.

```
small_data = {
           'X_train': data['X_train'][:num_train],
           'y_train': data['y_train'][:num_train],
           'X_val': data['X_val'],
           'y_val': data['y_val'],
         }
         bn_solvers = {}
         solvers = {}
         weight_scales = np.logspace(-4, 0, num=20)
         for i, weight_scale in enumerate(weight_scales):
           print('Running weight scale {} / {}'.format(i + 1, len(weight_scales)))
           bn model = FullyConnectedNet(hidden_dims, weight_scale=weight_scale, use_batchnorm='
           model = FullyConnectedNet(hidden_dims, weight_scale=weight_scale, use_batchnorm=Fals
           bn_solver = Solver(bn_model, small_data,
                           num_epochs=10, batch_size=50,
                           update_rule='adam',
                           optim_config={
                             'learning_rate': 1e-3,
                           },
                           verbose=False, print_every=200)
           bn_solver.train()
           bn_solvers[weight_scale] = bn_solver
           solver = Solver(model, small_data,
                           num_epochs=10, batch_size=50,
                           update_rule='adam',
                           optim_config={
                             'learning_rate': 1e-3,
                           verbose=False, print_every=200)
           solver.train()
           solvers[weight_scale] = solver
Running weight scale 1 / 20
Running weight scale 2 / 20
Running weight scale 3 / 20
Running weight scale 4 / 20
Running weight scale 5 / 20
Running weight scale 6 / 20
Running weight scale 7 / 20
Running weight scale 8 / 20
Running weight scale 9 / 20
Running weight scale 10 / 20
Running weight scale 11 / 20
Running weight scale 12 / 20
Running weight scale 13 / 20
```

```
Running weight scale 14 / 20
Running weight scale 15 / 20
Running weight scale 16 / 20
Running weight scale 17 / 20
Running weight scale 18 / 20
Running weight scale 19 / 20
Running weight scale 20 / 20
In [58]: # Plot results of weight scale experiment
         best train accs, bn best train accs = [], []
         best_val_accs, bn_best_val_accs = [], []
         final_train_loss, bn_final_train_loss = [], []
         for ws in weight_scales:
           best_train_accs.append(max(solvers[ws].train_acc_history))
           bn_best_train_accs.append(max(bn_solvers[ws].train_acc_history))
           best_val_accs.append(max(solvers[ws].val_acc_history))
           bn_best_val_accs.append(max(bn_solvers[ws].val_acc_history))
           final_train_loss.append(np.mean(solvers[ws].loss_history[-100:]))
           bn_final_train_loss.append(np.mean(bn_solvers[ws].loss_history[-100:]))
         plt.subplot(3, 1, 1)
         plt.title('Best val accuracy vs weight initialization scale')
         plt.xlabel('Weight initialization scale')
         plt.ylabel('Best val accuracy')
         plt.semilogx(weight_scales, best_val_accs, '-o', label='baseline')
         plt.semilogx(weight_scales, bn_best_val_accs, '-o', label='batchnorm')
         plt.legend(ncol=2, loc='lower right')
         plt.subplot(3, 1, 2)
         plt.title('Best train accuracy vs weight initialization scale')
         plt.xlabel('Weight initialization scale')
         plt.ylabel('Best training accuracy')
         plt.semilogx(weight_scales, best_train_accs, '-o', label='baseline')
         plt.semilogx(weight_scales, bn_best_train_accs, '-o', label='batchnorm')
         plt.legend()
         plt.subplot(3, 1, 3)
         plt.title('Final training loss vs weight initialization scale')
         plt.xlabel('Weight initialization scale')
         plt.ylabel('Final training loss')
         plt.semilogx(weight_scales, final_train_loss, '-o', label='baseline')
         plt.semilogx(weight_scales, bn_final_train_loss, '-o', label='batchnorm')
         plt.legend()
```

plt.gcf().set_size_inches(10, 15)
plt.show()



1.6 Question:

In the cell below, summarize the findings of this experiment, and WHY these results make sense.

1.7 Answer:

- The third plot (Training loss vs WIS) is a great illustration of the trappings of the problem of weight initialization scale (also known as the vanishing gradients problem) and how it is fixed using batch normalization. If weights are too big then by backwards propagation through the ReLU we get tiny gradients, such that the training process effectively is brought to a halt. Indeed the blue line has reached inifinity after ~9e0. A similar halting of the training would happen at very small weight initializations, and indeed we already observed an up tick of the value of the final training loss. The batch normalize curve, exhibits a similar behavior but much more tempered, which illustrates its effectiveness in dealing with the problem of WIS.
- The second plot (Train_acc vs WIS) illustrates similar points as the third. It shows that for large and small WIS no training happens for the baseline such that we have a very low training accuracy. In contrast, with batch-norm we get almost constant training accuracy for all WIS.
- The first plot (Val_acc vs WIS) besides the same points as before also illustrates the regularization properties of batch normalization. Indeed the discrepancy between train_acc val acc is much smaller with batch-normalization across all WIS.

layers

February 10, 2021

```
In [ ]: import numpy as np
       import pdb
        11 11 11
        This code was originally written for CS 231n at Stanford University
        (cs231n.stanford.edu). It has been modified in various areas for use in the
       ECE 239AS class at UCLA. This includes the descriptions of what code to
        implement as well as some slight potential changes in variable names to be
        consistent with class nomenclature. We thank Justin Johnson & Serena Yeung for
       permission to use this code. To see the original version, please visit
        cs231n.stanford.edu.
        11 11 11
       def affine_forward(x, w, b):
         Computes the forward pass for an affine (fully-connected) layer.
         The input x has shape (N, d_1, \ldots, d_k) and contains a minibatch of N
         examples, where each example x[i] has shape (d_1, \ldots, d_k). We will
         reshape each input into a vector of dimension D = d_1 * ... * d_k, and
          then transform it to an output vector of dimension M.
          - x: A numpy array containing input data, of shape (N, d_1, ..., d_k)
         - w: A numpy array of weights, of shape (D, M)
          - b: A numpy array of biases, of shape (M,)
         Returns a tuple of:
          - out: output, of shape (N, M)
          - cache: (x, w, b)
          n n n
          # ------ #
          # YOUR CODE HERE:
             Calculate the output of the forward pass. Notice the dimensions
             of w are D x M, which is the transpose of what we did in earlier
```

assignments.

```
# ----- #
 dim_size = x[0].shape
 X = x.reshape(x.shape[0], np.prod(dim_size))
 out = X.dot(w) + b
 # ------ #
 # END YOUR CODE HERE
 # ------ #
 cache = (x, w, b)
 return out, cache
def affine_backward(dout, cache):
 Computes the backward pass for an affine layer.
 Inputs:
 - dout: Upstream derivative, of shape (N, M)
 - cache: Tuple of:
   - x: A numpy array containing input data, of shape (N, d_1, \ldots, d_k)
   - w: A numpy array of weights, of shape (D, M)
   - b: A numpy array of biases, of shape (M,)
 Returns a tuple of:
 - dx: Gradient with respect to x, of shape (N, d1, ..., d_k)
 - dw: Gradient with respect to w, of shape (D, M)
 - db: Gradient with respect to b, of shape (M,)
 x, w, b = cache
 dx, dw, db = None, None, None
 # YOUR CODE HERE:
    Calculate the gradients for the backward pass.
 # Notice:
    dout is NxM
 # dx should be N x d1 x ... x dk; it relates to dout through multiplication with w
    dw should be D x M; it relates to dout through multiplication with x, which is N
    db should be M; it is just the sum over dout examples
 dim_shape = np.prod(x[0].shape)
 N = x.shape[0]
 X = x.reshape(N, dim_shape)
 # input gradient
 dx = dout.dot(w.T)
 dx = dx.reshape(x.shape)
```

```
# weight gradient
 dw = X.T.dot(dout)
 # bias gradient
 db = dout.sum(axis=0)
 # ============ #
 # END YOUR CODE HERE
 # ----- #
 return dx, dw, db
def relu_forward(x):
 Computes the forward pass for a layer of rectified linear units (ReLUs).
 Input:
 - x: Inputs, of any shape
 Returns a tuple of:
 - out: Output, of the same shape as x
 - cache: x
 # ------ #
 # YOUR CODE HERE:
    Implement the ReLU forward pass.
 out = np.maximum(0, x)
 # ------ #
 # END YOUR CODE HERE
 # ------ #
 cache = x
 return out, cache
def relu_backward(dout, cache):
 Computes the backward pass for a layer of rectified linear units (ReLUs).
 Input:
 - dout: Upstream derivatives, of any shape
 - cache: Input x, of same shape as dout
 Returns:
 - dx: Gradient with respect to x
 x = cache
```

Forward pass for batch normalization.

During training the sample mean and (uncorrected) sample variance are computed from minibatch statistics and used to normalize the incoming data. During training we also keep an exponentially decaying running mean of the mean and variance of each feature, and these averages are used to normalize data at test-time.

At each timestep we update the running averages for mean and variance using an exponential decay based on the momentum parameter:

```
running_mean = momentum * running_mean + (1 - momentum) * sample_mean
running_var = momentum * running_var + (1 - momentum) * sample_var
```

Note that the batch normalization paper suggests a different test-time behavior: they compute sample mean and variance for each feature using a large number of training images rather than using a running average. For this implementation we have chosen to use running averages instead since they do not require an additional estimation step; the torch7 implementation of batch normalization also uses running averages.

```
Input:
```

- x: Data of shape (N, D)
- gamma: Scale parameter of shape (D,)
- beta: Shift paremeter of shape (D,)
- bn_param: Dictionary with the following keys:
 - mode: 'train' or 'test'; required
 - eps: Constant for numeric stability
 - momentum: Constant for running mean / variance.
 - running_mean: Array of shape (D,) giving running mean of features
 - running_var Array of shape (D,) giving running variance of features

```
Returns a tuple of:
- out: of shape (N, D)
```

```
- cache: A tuple of values needed in the backward pass
mode = bn_param['mode']
eps = bn_param.get('eps', 1e-5)
momentum = bn_param.get('momentum', 0.9)
N, D = x.shape
running_mean = bn_param.get('running_mean', np.zeros(D, dtype=x.dtype))
running_var = bn_param.get('running_var', np.zeros(D, dtype=x.dtype))
out, cache = None, None
if mode == 'train':
 pass
 # ----- #
 # YOUR CODE HERE:
    A few steps here:
      (1) Calculate the running mean and variance of the minibatch.
      (2) Normalize the activations with the running mean and variance.
      (3) Scale and shift the normalized activations. Store this
          as the variable 'out'
      (4) Store any variables you may need for the backward pass in
         the 'cache' variable.
 mu = x.mean(axis=0)
 var = x.var(axis=0) + eps
 std = np.sqrt(var)
 z = (x - mu)/std
 out = gamma * z + beta
 running_mean = momentum * running_mean + (1 - momentum) * mu
 running_var = momentum * running_var + (1 - momentum) * (std**2)
 cache={'x':x,'mean':mu,'std':std,'gamma':gamma,'z':z,'var':var}
 # ----- #
 # END YOUR CODE HERE
 elif mode == 'test':
 pass
 # ------ #
 # YOUR CODE HERE:
    Calculate the testing time normalized activation. Normalize using
    the running mean and variance, and then scale and shift appropriately.
   Store the output as 'out'.
```

```
# ----- #
   out = gamma * (x - running_mean) / np.sqrt(running_var + eps) + beta
   # END YOUR CODE HERE
   # ----- #
 else:
   raise ValueError('Invalid forward batchnorm mode "%s"' % mode)
 # Store the updated running means back into bn_param
 bn_param['running_mean'] = running_mean
 bn_param['running_var'] = running_var
 return out, cache
def batchnorm_backward(dout, cache):
 Backward pass for batch normalization.
 For this implementation, you should write out a computation graph for
 batch normalization on paper and propagate gradients backward through
 intermediate nodes.
 Inputs:
 - dout: Upstream derivatives, of shape (N, D)
 - cache: Variable of intermediates from batchnorm_forward.
 Returns a tuple of:
 - dx: Gradient with respect to inputs x, of shape (N, D)
 - dgamma: Gradient with respect to scale parameter gamma, of shape (D,)
 - dbeta: Gradient with respect to shift parameter beta, of shape (D,)
 11 11 11
 dx, dgamma, dbeta = None, None, None
 # ----- #
 # YOUR CODE HERE:
    Implement the batchnorm backward pass, calculating dx, dgamma, and dbeta.
 # ----- #
 dbeta = dout.sum(axis=0)
 dgamma = np.sum(dout * cache['z'], axis=0)
 N = 1.0 * dout.shape[0]
 dfdz = dout * cache['gamma']
                                                      # the dimensions are
 dvdx = 2/N * (cache['x'] - cache['mean'])
 dzdx = 1 / cache['std']
 dzdu = -1 / cache['std']
```

```
dzdv = -0.5*(cache['var']**-1.5)*(cache['x']-cache['mean'])
 dvdu = -2/N * np.sum(cache['x'] - cache['mean'], axis=0)
 dx = dfdz*dzdx + np.sum(dfdz*dzdu,axis=0)*dudx + \
       np.sum(dfdz*dzdv,axis=0)*(dvdx+dvdu*dudx)
 # ----- #
 # END YOUR CODE HERE
 # ------ #
 return dx, dgamma, dbeta
def dropout_forward(x, dropout_param):
 Performs the forward pass for (inverted) dropout.
 Inputs:
 - x: Input data, of any shape
 - dropout_param: A dictionary with the following keys:
   - p: Dropout parameter. We drop each neuron output with probability p.
   - mode: 'test' or 'train'. If the mode is train, then perform dropout;
     if the mode is test, then just return the input.
   - seed: Seed for the random number generator. Passing seed makes this
     function deterministic, which is needed for gradient checking but not in
     real networks.
 Outputs:
  - out: Array of the same shape as x.
 - cache: A tuple (dropout_param, mask). In training mode, mask is the dropout
   mask that was used to multiply the input; in test mode, mask is None.
 ##############print(dropout_param['p'])
 p, mode = dropout_param['p'], dropout_param['mode']
 if 'seed' in dropout_param:
   np.random.seed(dropout_param['seed'])
 mask = None
 out = None
 if mode == 'train':
   # YOUR CODE HERE:
      Implement the inverted dropout forward pass during training time.
      Store the masked and scaled activations in out, and store the
      dropout mask as the variable mask.
   # ----- #
   mask = (np.random.rand(*x.shape) < 1- p) / (1-p)
   out = x * mask
```

```
# ----- #
  # END YOUR CODE HERE
  # ----- #
 elif mode == 'test':
  # ----- #
  # YOUR CODE HERE:
    Implement the inverted dropout forward pass during test time.
  out = x
  # ----- #
  # END YOUR CODE HERE
  # ----- #
 cache = (dropout_param, mask)
 out = out.astype(x.dtype, copy=False)
 return out, cache
def dropout_backward(dout, cache):
 Perform the backward pass for (inverted) dropout.
 Inputs:
 - dout: Upstream derivatives, of any shape
 - cache: (dropout_param, mask) from dropout_forward.
 dropout_param, mask = cache
 mode = dropout_param['mode']
 dx = None
 if mode == 'train':
  pass
  # ----- #
  # YOUR CODE HERE:
    Implement the inverted dropout backward pass during training time.
  # ----- #
  dx = dout * mask
  # END YOUR CODE HERE
  # ------ #
 elif mode == 'test':
  # ----- #
  # YOUR CODE HERE:
    Implement the inverted dropout backward pass during test time.
  # ----- #
```

```
dx = dout
   # ----- #
   # END YOUR CODE HERE
   # ----- #
 return dx
def svm loss(x, y):
  11 11 11
 Computes the loss and gradient using for multiclass SVM classification.
 Inputs:
  - x: Input data, of shape (N, C) where x[i, j] is the score for the jth class
   for the ith input.
  - y: Vector of labels, of shape (N,) where y[i] is the label for x[i] and
   0 \leftarrow y[i] < C
 Returns a tuple of:
 - loss: Scalar giving the loss
  - dx: Gradient of the loss with respect to x
 N = x.shape[0]
 correct_class_scores = x[np.arange(N), y]
 margins = np.maximum(0, x - correct_class_scores[:, np.newaxis] + 1.0)
 margins[np.arange(N), y] = 0
 loss = np.sum(margins) / N
 num_pos = np.sum(margins > 0, axis=1)
 dx = np.zeros_like(x)
 dx[margins > 0] = 1
 dx[np.arange(N), y] -= num_pos
 dx /= N
 return loss, dx
def softmax_loss(x, y):
 Computes the loss and gradient for softmax classification.
 Inputs:
 - x: Input data, of shape (N, C) where x[i, j] is the score for the jth class
   for the ith input.
  - y: Vector of labels, of shape (N,) where y[i] is the label for x[i] and
   0 <= y[i] < C
 Returns a tuple of:
  - loss: Scalar giving the loss
  - dx: Gradient of the loss with respect to x
```

```
probs = np.exp(x - np.max(x, axis=1, keepdims=True))
  probs /= np.sum(probs, axis=1, keepdims=True)
  N = x.shape[0]
  loss = -np.sum(np.log(probs[np.arange(N), y])) / N
  dx = probs.copy()
  dx[np.arange(N), y] = 1
  dx /= N
  return loss, dx
def affine_norm_relu_forward(x, w, b, gamma, beta, bn_param, use_batchnorm, use_dropou
    bn_cache, do_cache = None, None
    # affine layer
    \#print(') before the affine forward we have the types ', type(x), 'for x; ', type(w)
    out, fc_cache = affine_forward(x,w,b)
    # batch norm
    if use batchnorm:
        out, bn_cache = batchnorm_forward(out, gamma, beta, bn_param)
    # relu
    out, relu_cache = relu_forward(out)
    # dropout
    if use_dropout:
        out, do_cache = dropout_forward(out, dropout_param)
    return out, (fc_cache, bn_cache, relu_cache, do_cache)
def affine_norm_relu_backward(dout, cache, use_batchnorm, use_dropout):
    fc_cache, bn_cache, relu_cache, do_cache = cache
    # backprop dropout
    if use_dropout:
        dout = dropout_backward(dout, do_cache)
    # backprop relu
    dout = relu_backward(dout, relu_cache)
    # backprop batch/layer norm
    dgamma, dbeta = None, None
    if use_batchnorm:
```

```
dout, dgamma, dbeta = batchnorm_backward(dout, bn_cache)
```

```
# affine layer
dx, dw, db = affine_backward(dout, fc_cache)
return dx, dw, db, dgamma, dbeta
```

Dropout

February 10, 2021

1 Dropout

In this notebook, you will implement dropout. Then we will ask you to train a network with batchnorm and dropout, and acheive over 55% accuracy on CIFAR-10.

CS231n has built a solid API for building these modular frameworks and training them, and we will use their very well implemented framework as opposed to "reinventing the wheel." This includes using their Solver, various utility functions, and their layer structure. This also includes nndl.fc_net, nndl.layers, and nndl.layer_utils. As in prior assignments, we thank Serena Yeung & Justin Johnson for permission to use code written for the CS 231n class (cs231n.stanford.edu).

```
In [1]: ## Import and setups
        import time
        import numpy as np
        import matplotlib.pyplot as plt
        from nndl.fc_net import *
        from nndl.layers import *
        from cs231n.data_utils import get_CIFAR10_data
        from cs231n.gradient_check import eval_numerical_gradient, eval_numerical_gradient_arra
        from cs231n.solver import Solver
        %matplotlib inline
        plt.rcParams['figure.figsize'] = (10.0, 8.0) # set default size of plots
        plt.rcParams['image.interpolation'] = 'nearest'
        plt.rcParams['image.cmap'] = 'gray'
        # for auto-reloading external modules
        \# see http://stackoverflow.com/questions/1907993/autoreload-of-modules-in-ipython
        %load_ext autoreload
        %autoreload 2
        def rel_error(x, y):
          """ returns relative error """
          return np.max(np.abs(x - y) / (np.maximum(1e-8, np.abs(x) + np.abs(y))))
In [2]: # Load the (preprocessed) CIFAR10 data.
```

```
data = get_CIFAR10_data()
    for k in data.keys():
        print('{}: {} '.format(k, data[k].shape))

X_train: (49000, 3, 32, 32)
y_train: (49000,)
X_val: (1000, 3, 32, 32)
y_val: (1000,)
X_test: (1000, 3, 32, 32)
y_test: (1000,)
```

1.1 Dropout forward pass

Implement the training and test time dropout forward pass, dropout_forward, in nndl/layers.py. After that, test your implementation by running the following cell.

```
In [3]: x = np.random.randn(500, 500) + 10
       for p in [0.3, 0.6, 0.75]:
         out, _ = dropout_forward(x, {'mode': 'train', 'p': p})
         out_test, _ = dropout_forward(x, {'mode': 'test', 'p': p})
         print('Running tests with p = ', p)
         print('Mean of input: ', x.mean())
         print('Mean of train-time output: ', out.mean())
         print('Mean of test-time output: ', out_test.mean())
         print('Fraction of train-time output set to zero: ', (out == 0).mean())
         print('Fraction of test-time output set to zero: ', (out_test == 0).mean())
Running tests with p = 0.3
Mean of input: 9.99876159164
Mean of train-time output: 9.98706418418
Mean of test-time output: 9.99876159164
Fraction of train-time output set to zero: 0.300888
Fraction of test-time output set to zero: 0.0
Running tests with p = 0.6
Mean of input: 9.99876159164
Mean of train-time output: 10.0051578499
Mean of test-time output: 9.99876159164
Fraction of train-time output set to zero: 0.599736
Fraction of test-time output set to zero: 0.0
Running tests with p = 0.75
Mean of input: 9.99876159164
Mean of train-time output: 10.0302996525
Mean of test-time output: 9.99876159164
Fraction of train-time output set to zero: 0.749128
Fraction of test-time output set to zero: 0.0
```

1.2 Dropout backward pass

Implement the backward pass, dropout_backward, in nndl/layers.py. After that, test your gradients by running the following cell:

1.3 Implement a fully connected neural network with dropout layers

Modify the FullyConnectedNet() class in nndl/fc_net.py to incorporate dropout. A dropout layer should be incorporated after every ReLU layer. Concretely, there shouldn't be a dropout at the output layer since there is no ReLU at the output layer. You will need to modify the class in the following areas:

- (1) In the forward pass, you will need to incorporate a dropout layer after every relu layer.
- (2) In the backward pass, you will need to incorporate a dropout backward pass layer.

Check your implementation by running the following code. Our W1 gradient relative error is on the order of 1e-6 (the largest of all the relative errors).

```
Running check with dropout = 0
Initial loss: 2.3051948274
W1 relative error: 2.5272575351926774e-07
W2 relative error: 1.5034484932141387e-05
W3 relative error: 2.753446846744471e-07
b1 relative error: 2.9369574464090924e-06
b2 relative error: 5.051339805546953e-08
b3 relative error: 1.1740467838205477e-10
Running check with dropout = 0.25
Initial loss: 2.29898614757
W1 relative error: 9.737728851260064e-07
W2 relative error: 5.0736579542673615e-08
W3 relative error: 3.042456529982271e-08
b1 relative error: 2.0056188687011756e-08
b2 relative error: 1.897778283870511e-09
b3 relative error: 1.302003889798156e-10
Running check with dropout = 0.5
Initial loss: 2.30243758771
W1 relative error: 4.5533879914978946e-08
W2 relative error: 2.9742181126932173e-08
W3 relative error: 4.3413246880173414e-07
b1 relative error: 1.8724629972989974e-08
b2 relative error: 1.6327629805532402e-09
b3 relative error: 7.487013797161614e-11
```

1.4 Dropout as a regularizer

In class, we claimed that dropout acts as a regularizer by effectively bagging. To check this, we will train two small networks, one with dropout and one without dropout.

In [6]: # Train two identical nets, one with dropout and one without

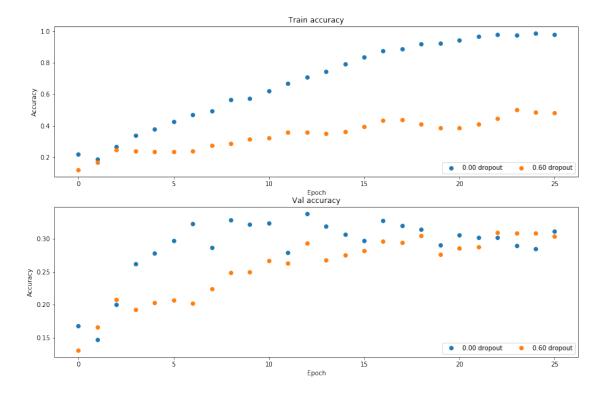
num_train = 500
small_data = {
 'X_train': data['X_train'][:num_train],
 'y_train': data['y_train'][:num_train],
 'X_val': data['X_val'],
 'y_val': data['y_val'],
}

solvers = {}

```
dropout_choices = [0, 0.6]
       for dropout in dropout_choices:
         model = FullyConnectedNet([100, 100, 100], dropout=dropout)
         solver = Solver(model, small_data,
                          num_epochs=25, batch_size=100,
                          update rule='adam',
                          optim_config={
                            'learning_rate': 5e-4,
                          },
                          verbose=True, print_every=100)
         solver.train()
         solvers[dropout] = solver
(Iteration 1 / 125) loss: 2.300804
(Epoch 0 / 25) train acc: 0.220000; val_acc: 0.168000
(Epoch 1 / 25) train acc: 0.188000; val_acc: 0.147000
(Epoch 2 / 25) train acc: 0.266000; val_acc: 0.200000
(Epoch 3 / 25) train acc: 0.338000; val_acc: 0.262000
(Epoch 4 / 25) train acc: 0.378000; val_acc: 0.278000
(Epoch 5 / 25) train acc: 0.428000; val_acc: 0.297000
(Epoch 6 / 25) train acc: 0.468000; val_acc: 0.323000
(Epoch 7 / 25) train acc: 0.494000; val acc: 0.287000
(Epoch 8 / 25) train acc: 0.566000; val_acc: 0.328000
(Epoch 9 / 25) train acc: 0.572000; val acc: 0.322000
(Epoch 10 / 25) train acc: 0.622000; val_acc: 0.324000
(Epoch 11 / 25) train acc: 0.670000; val_acc: 0.279000
(Epoch 12 / 25) train acc: 0.710000; val_acc: 0.338000
(Epoch 13 / 25) train acc: 0.746000; val_acc: 0.319000
(Epoch 14 / 25) train acc: 0.792000; val_acc: 0.307000
(Epoch 15 / 25) train acc: 0.834000; val_acc: 0.297000
(Epoch 16 / 25) train acc: 0.876000; val_acc: 0.327000
(Epoch 17 / 25) train acc: 0.886000; val_acc: 0.320000
(Epoch 18 / 25) train acc: 0.918000; val_acc: 0.314000
(Epoch 19 / 25) train acc: 0.922000; val_acc: 0.290000
(Epoch 20 / 25) train acc: 0.944000; val acc: 0.306000
(Iteration 101 / 125) loss: 0.156105
(Epoch 21 / 25) train acc: 0.968000; val acc: 0.302000
(Epoch 22 / 25) train acc: 0.978000; val_acc: 0.302000
(Epoch 23 / 25) train acc: 0.976000; val acc: 0.289000
(Epoch 24 / 25) train acc: 0.986000; val_acc: 0.285000
(Epoch 25 / 25) train acc: 0.978000; val acc: 0.311000
(Iteration 1 / 125) loss: 2.306395
(Epoch 0 / 25) train acc: 0.120000; val_acc: 0.131000
(Epoch 1 / 25) train acc: 0.170000; val_acc: 0.166000
(Epoch 2 / 25) train acc: 0.246000; val_acc: 0.208000
(Epoch 3 / 25) train acc: 0.240000; val_acc: 0.193000
(Epoch 4 / 25) train acc: 0.234000; val_acc: 0.203000
```

```
(Epoch 5 / 25) train acc: 0.234000; val_acc: 0.207000
(Epoch 6 / 25) train acc: 0.238000; val_acc: 0.202000
(Epoch 7 / 25) train acc: 0.276000; val_acc: 0.224000
(Epoch 8 / 25) train acc: 0.288000; val_acc: 0.249000
(Epoch 9 / 25) train acc: 0.314000; val acc: 0.250000
(Epoch 10 / 25) train acc: 0.324000; val_acc: 0.267000
(Epoch 11 / 25) train acc: 0.360000; val_acc: 0.263000
(Epoch 12 / 25) train acc: 0.360000; val_acc: 0.293000
(Epoch 13 / 25) train acc: 0.350000; val_acc: 0.268000
(Epoch 14 / 25) train acc: 0.362000; val_acc: 0.275000
(Epoch 15 / 25) train acc: 0.394000; val_acc: 0.282000
(Epoch 16 / 25) train acc: 0.436000; val_acc: 0.296000
(Epoch 17 / 25) train acc: 0.438000; val_acc: 0.294000
(Epoch 18 / 25) train acc: 0.410000; val_acc: 0.305000
(Epoch 19 / 25) train acc: 0.388000; val_acc: 0.276000
(Epoch 20 / 25) train acc: 0.386000; val_acc: 0.286000
(Iteration 101 / 125) loss: 1.882977
(Epoch 21 / 25) train acc: 0.410000; val_acc: 0.288000
(Epoch 22 / 25) train acc: 0.448000; val_acc: 0.309000
(Epoch 23 / 25) train acc: 0.500000; val_acc: 0.308000
(Epoch 24 / 25) train acc: 0.486000; val_acc: 0.308000
(Epoch 25 / 25) train acc: 0.482000; val acc: 0.304000
In [7]: # Plot train and validation accuracies of the two models
        train_accs = []
        val_accs = []
        for dropout in dropout_choices:
          solver = solvers[dropout]
          train_accs.append(solver.train_acc_history[-1])
          val_accs.append(solver.val_acc_history[-1])
       plt.subplot(3, 1, 1)
        for dropout in dropout_choices:
          plt.plot(solvers[dropout].train_acc_history, 'o', label='%.2f dropout' % dropout)
       plt.title('Train accuracy')
       plt.xlabel('Epoch')
        plt.ylabel('Accuracy')
       plt.legend(ncol=2, loc='lower right')
       plt.subplot(3, 1, 2)
        for dropout in dropout_choices:
          plt.plot(solvers[dropout].val_acc_history, 'o', label='%.2f dropout' % dropout)
       plt.title('Val accuracy')
       plt.xlabel('Epoch')
       plt.ylabel('Accuracy')
        plt.legend(ncol=2, loc='lower right')
```

plt.gcf().set_size_inches(15, 15)
plt.show()



1.5 Question

Based off the results of this experiment, is dropout performing regularization? Explain your answer.

1.6 Answer:

Regularization is defined as any modification of a learning algorithm that reduces the generalization error without reducing the training error. Indeed, during training non-zero dropout has worse error (top fig.), but during validation non-zero dropout eventually has better error (bottom fig.). Hence, these plots are consistent with the interpretation of dropout as regularization.

1.7 Final part of the assignment

Get over 55% validation accuracy on CIFAR-10 by using the layers you have implemented. You will be graded according to the following equation:

min(floor((X - 32%)) / 28%, 1) where if you get 60% or higher validation accuracy, you get full points.

```
In [120]: # ------ #
         # YOUR CODE HERE:
            Implement a FC-net that achieves at least 55% validation accuracy
             on CIFAR-10.
         # =========== #
         # Train two identical nets, one with dropout and one without
         num_train = 49000
         small_data = {
           'X_train': data['X_train'][:num_train],
           'y_train': data['y_train'][:num_train],
           'X_val': data['X_val'],
           'y_val': data['y_val'],
         solvers = {}
         dropout_choices = [ 0.25, 0.2, 0.15] # 0.3, 0.25, 0.15, 0.1] # 0.7, 0.5,
                                                                               [0.13,
         epochs = [35]
         learning_rates = [ 8e-4]
         # 0.008000 ; rain acc: 0.487000; val_acc: 0.429000
         # lr 0.001; 0.750000; val_acc: 0.553000
         # lr 0.0005; train acc: 0.711000; val_acc: 0.528000
         # lr 0.0001; train acc: 0.579000; val_acc: 0.507000
         # 2e-1,9e-2, 3e-2, 1e-2, 9e-3, 8e-3, 7e-3, 1e-3, 9e-4, 8e-4, 5e-4, 1e-4]
         # learning rate 0.000800; epoch 35; dropout 0.200000; train acc: 0.772000; val acc
         batches = [800]
         best_lr = None
         best_epo = None
         best do = None
         best_solver = None
         best size = None
         \#best_hy = None
         best_acc = 0
         for size in batches:
            for lr in learning_rates:
                for epoch in epochs:
                    for dropout in dropout_choices:
                       print('We will use learning rate %f; epoch %d; dropout %f' %(lr,epoc
                       model = FullyConnectedNet([700, 400, 400, 400, 100, 50], dropout=dro
```

```
solver = Solver(model, small_data,
                              num_epochs=epoch, batch_size=size,
                              update_rule='adam',
                              optim_config={
                                'learning rate': lr,
                              },
                              verbose=True, print every=100)
                        solver.train()
                        acc = solver.best val acc
                        if acc>best_acc:
                            best_acc = acc
                            best_lr = lr
                            best_epo = epoch
                            best_do = dropout
                            best_solver= solver
                            best_size = size
                            best_model = model
         # ------ #
         # END YOUR CODE HERE
         # ----- #
         print('best val acc', best_acc,'for learning rate: ', best_lr, ' and dropout rate:
We will use learning rate 0.000800; epoch 35; dropout 0.250000
(Iteration 1 / 2135) loss: 2.302585
(Epoch 0 / 35) train acc: 0.131000; val_acc: 0.110000
(Epoch 1 / 35) train acc: 0.278000; val acc: 0.277000
(Iteration 101 / 2135) loss: 1.776460
(Epoch 2 / 35) train acc: 0.325000; val_acc: 0.326000
(Epoch 3 / 35) train acc: 0.381000; val_acc: 0.379000
(Iteration 201 / 2135) loss: 1.750268
(Epoch 4 / 35) train acc: 0.407000; val_acc: 0.415000
(Iteration 301 / 2135) loss: 1.595897
(Epoch 5 / 35) train acc: 0.476000; val_acc: 0.447000
(Epoch 6 / 35) train acc: 0.501000; val_acc: 0.451000
(Iteration 401 / 2135) loss: 1.500134
(Epoch 7 / 35) train acc: 0.514000; val_acc: 0.495000
(Epoch 8 / 35) train acc: 0.550000; val acc: 0.520000
(Iteration 501 / 2135) loss: 1.362064
(Epoch 9 / 35) train acc: 0.553000; val acc: 0.511000
(Iteration 601 / 2135) loss: 1.408755
(Epoch 10 / 35) train acc: 0.519000; val_acc: 0.479000
(Epoch 11 / 35) train acc: 0.552000; val_acc: 0.516000
(Iteration 701 / 2135) loss: 1.347892
(Epoch 12 / 35) train acc: 0.583000; val_acc: 0.514000
(Epoch 13 / 35) train acc: 0.571000; val_acc: 0.538000
(Iteration 801 / 2135) loss: 1.295760
(Epoch 14 / 35) train acc: 0.580000; val_acc: 0.515000
```

```
(Iteration 901 / 2135) loss: 1.226998
(Epoch 15 / 35) train acc: 0.593000; val_acc: 0.516000
(Epoch 16 / 35) train acc: 0.597000; val_acc: 0.543000
(Iteration 1001 / 2135) loss: 1.231912
(Epoch 17 / 35) train acc: 0.634000; val acc: 0.529000
(Epoch 18 / 35) train acc: 0.635000; val_acc: 0.548000
(Iteration 1101 / 2135) loss: 1.128184
(Epoch 19 / 35) train acc: 0.633000; val_acc: 0.542000
(Iteration 1201 / 2135) loss: 1.133395
(Epoch 20 / 35) train acc: 0.654000; val_acc: 0.549000
(Epoch 21 / 35) train acc: 0.634000; val_acc: 0.541000
(Iteration 1301 / 2135) loss: 1.123553
(Epoch 22 / 35) train acc: 0.650000; val_acc: 0.539000
(Iteration 1401 / 2135) loss: 1.063651
(Epoch 23 / 35) train acc: 0.687000; val_acc: 0.545000
(Epoch 24 / 35) train acc: 0.650000; val_acc: 0.546000
(Iteration 1501 / 2135) loss: 1.074959
(Epoch 25 / 35) train acc: 0.694000; val_acc: 0.551000
(Epoch 26 / 35) train acc: 0.674000; val_acc: 0.554000
(Iteration 1601 / 2135) loss: 1.015043
(Epoch 27 / 35) train acc: 0.684000; val acc: 0.565000
(Iteration 1701 / 2135) loss: 1.006437
(Epoch 28 / 35) train acc: 0.703000; val_acc: 0.572000
(Epoch 29 / 35) train acc: 0.700000; val_acc: 0.554000
(Iteration 1801 / 2135) loss: 1.017733
(Epoch 30 / 35) train acc: 0.702000; val_acc: 0.548000
(Epoch 31 / 35) train acc: 0.719000; val_acc: 0.555000
(Iteration 1901 / 2135) loss: 1.003456
(Epoch 32 / 35) train acc: 0.727000; val_acc: 0.549000
(Iteration 2001 / 2135) loss: 0.986155
(Epoch 33 / 35) train acc: 0.711000; val_acc: 0.554000
(Epoch 34 / 35) train acc: 0.732000; val_acc: 0.561000
(Iteration 2101 / 2135) loss: 0.948083
(Epoch 35 / 35) train acc: 0.714000; val_acc: 0.567000
We will use learning rate 0.000800; epoch 35; dropout 0.200000
(Iteration 1 / 2135) loss: 2.302580
(Epoch 0 / 35) train acc: 0.102000; val acc: 0.119000
(Epoch 1 / 35) train acc: 0.248000; val_acc: 0.254000
(Iteration 101 / 2135) loss: 1.860165
(Epoch 2 / 35) train acc: 0.281000; val_acc: 0.315000
(Epoch 3 / 35) train acc: 0.379000; val_acc: 0.382000
(Iteration 201 / 2135) loss: 1.714171
(Epoch 4 / 35) train acc: 0.377000; val_acc: 0.369000
(Iteration 301 / 2135) loss: 1.627309
(Epoch 5 / 35) train acc: 0.430000; val_acc: 0.418000
(Epoch 6 / 35) train acc: 0.469000; val_acc: 0.461000
(Iteration 401 / 2135) loss: 1.476592
(Epoch 7 / 35) train acc: 0.506000; val_acc: 0.472000
```

```
(Epoch 8 / 35) train acc: 0.536000; val_acc: 0.478000
(Iteration 501 / 2135) loss: 1.388971
(Epoch 9 / 35) train acc: 0.560000; val_acc: 0.527000
(Iteration 601 / 2135) loss: 1.315141
(Epoch 10 / 35) train acc: 0.552000; val acc: 0.533000
(Epoch 11 / 35) train acc: 0.587000; val_acc: 0.516000
(Iteration 701 / 2135) loss: 1.250110
(Epoch 12 / 35) train acc: 0.584000; val_acc: 0.533000
(Epoch 13 / 35) train acc: 0.603000; val_acc: 0.550000
(Iteration 801 / 2135) loss: 1.286570
(Epoch 14 / 35) train acc: 0.602000; val_acc: 0.525000
(Iteration 901 / 2135) loss: 1.179458
(Epoch 15 / 35) train acc: 0.625000; val_acc: 0.531000
(Epoch 16 / 35) train acc: 0.627000; val_acc: 0.549000
(Iteration 1001 / 2135) loss: 1.204724
(Epoch 17 / 35) train acc: 0.638000; val_acc: 0.541000
(Epoch 18 / 35) train acc: 0.656000; val_acc: 0.540000
(Iteration 1101 / 2135) loss: 1.029992
(Epoch 19 / 35) train acc: 0.658000; val_acc: 0.547000
(Iteration 1201 / 2135) loss: 1.097619
(Epoch 20 / 35) train acc: 0.665000; val acc: 0.559000
(Epoch 21 / 35) train acc: 0.671000; val acc: 0.558000
(Iteration 1301 / 2135) loss: 1.018237
(Epoch 22 / 35) train acc: 0.697000; val_acc: 0.560000
(Iteration 1401 / 2135) loss: 1.030829
(Epoch 23 / 35) train acc: 0.701000; val_acc: 0.549000
(Epoch 24 / 35) train acc: 0.700000; val_acc: 0.545000
(Iteration 1501 / 2135) loss: 0.998335
(Epoch 25 / 35) train acc: 0.711000; val_acc: 0.561000
(Epoch 26 / 35) train acc: 0.721000; val_acc: 0.547000
(Iteration 1601 / 2135) loss: 1.004681
(Epoch 27 / 35) train acc: 0.730000; val_acc: 0.550000
(Iteration 1701 / 2135) loss: 0.957758
(Epoch 28 / 35) train acc: 0.738000; val_acc: 0.558000
(Epoch 29 / 35) train acc: 0.721000; val acc: 0.573000
(Iteration 1801 / 2135) loss: 0.923795
(Epoch 30 / 35) train acc: 0.744000; val acc: 0.554000
(Epoch 31 / 35) train acc: 0.765000; val_acc: 0.578000
(Iteration 1901 / 2135) loss: 0.926848
(Epoch 32 / 35) train acc: 0.742000; val_acc: 0.558000
(Iteration 2001 / 2135) loss: 0.912702
(Epoch 33 / 35) train acc: 0.745000; val_acc: 0.569000
(Epoch 34 / 35) train acc: 0.771000; val_acc: 0.569000
(Iteration 2101 / 2135) loss: 0.886432
(Epoch 35 / 35) train acc: 0.773000; val_acc: 0.558000
We will use learning rate 0.000800; epoch 35; dropout 0.150000
(Iteration 1 / 2135) loss: 2.302584
(Epoch 0 / 35) train acc: 0.108000; val_acc: 0.108000
```

```
(Epoch 1 / 35) train acc: 0.258000; val_acc: 0.260000
(Iteration 101 / 2135) loss: 1.851462
(Epoch 2 / 35) train acc: 0.309000; val_acc: 0.322000
(Epoch 3 / 35) train acc: 0.377000; val_acc: 0.393000
(Iteration 201 / 2135) loss: 1.687320
(Epoch 4 / 35) train acc: 0.428000; val_acc: 0.434000
(Iteration 301 / 2135) loss: 1.452792
(Epoch 5 / 35) train acc: 0.488000; val_acc: 0.458000
(Epoch 6 / 35) train acc: 0.493000; val_acc: 0.472000
(Iteration 401 / 2135) loss: 1.373739
(Epoch 7 / 35) train acc: 0.550000; val_acc: 0.509000
(Epoch 8 / 35) train acc: 0.547000; val_acc: 0.508000
(Iteration 501 / 2135) loss: 1.339907
(Epoch 9 / 35) train acc: 0.563000; val_acc: 0.525000
(Iteration 601 / 2135) loss: 1.253705
(Epoch 10 / 35) train acc: 0.576000; val_acc: 0.540000
(Epoch 11 / 35) train acc: 0.592000; val_acc: 0.538000
(Iteration 701 / 2135) loss: 1.282914
(Epoch 12 / 35) train acc: 0.618000; val_acc: 0.510000
(Epoch 13 / 35) train acc: 0.625000; val acc: 0.542000
(Iteration 801 / 2135) loss: 1.122056
(Epoch 14 / 35) train acc: 0.624000; val acc: 0.541000
(Iteration 901 / 2135) loss: 1.120466
(Epoch 15 / 35) train acc: 0.643000; val_acc: 0.547000
(Epoch 16 / 35) train acc: 0.656000; val_acc: 0.545000
(Iteration 1001 / 2135) loss: 0.988456
(Epoch 17 / 35) train acc: 0.665000; val_acc: 0.537000
(Epoch 18 / 35) train acc: 0.697000; val_acc: 0.558000
(Iteration 1101 / 2135) loss: 1.019334
(Epoch 19 / 35) train acc: 0.698000; val_acc: 0.547000
(Iteration 1201 / 2135) loss: 1.015661
(Epoch 20 / 35) train acc: 0.715000; val_acc: 0.567000
(Epoch 21 / 35) train acc: 0.737000; val_acc: 0.568000
(Iteration 1301 / 2135) loss: 0.888493
(Epoch 22 / 35) train acc: 0.739000; val acc: 0.557000
(Iteration 1401 / 2135) loss: 0.843797
(Epoch 23 / 35) train acc: 0.743000; val acc: 0.575000
(Epoch 24 / 35) train acc: 0.769000; val acc: 0.559000
(Iteration 1501 / 2135) loss: 0.839095
(Epoch 25 / 35) train acc: 0.755000; val_acc: 0.569000
(Epoch 26 / 35) train acc: 0.766000; val_acc: 0.568000
(Iteration 1601 / 2135) loss: 0.835214
(Epoch 27 / 35) train acc: 0.756000; val_acc: 0.576000
(Iteration 1701 / 2135) loss: 0.762013
(Epoch 28 / 35) train acc: 0.780000; val_acc: 0.566000
(Epoch 29 / 35) train acc: 0.780000; val_acc: 0.569000
(Iteration 1801 / 2135) loss: 0.792854
(Epoch 30 / 35) train acc: 0.784000; val_acc: 0.571000
```

```
(Epoch 31 / 35) train acc: 0.795000; val_acc: 0.567000
      (Iteration 1901 / 2135) loss: 0.755856
      (Epoch 32 / 35) train acc: 0.825000; val_acc: 0.572000
      (Iteration 2001 / 2135) loss: 0.810583
      (Epoch 33 / 35) train acc: 0.826000; val acc: 0.569000
      (Epoch 34 / 35) train acc: 0.861000; val_acc: 0.567000
      (Iteration 2101 / 2135) loss: 0.650040
      (Epoch 35 / 35) train acc: 0.820000; val_acc: 0.557000
      best val acc 0.578 for learning rate: 0.0008 and dropout rate: 0.2 and epochs 35 and size
Training continues below by using annealing, to eventually get val acc=0.605
      In [121]: # Train two identical nets, one with dropout and one without
                # num_train = 49000
                # small_data = {
                    'X_train': data['X_train'][:num_train],
                   'y_train': data['y_train'][:num_train],
                    'X_val': data['X_val'],
                   'y_val': data['y_val'],
                # }
                print('implement change in the learning rate in the spirit of an elaborate leraning
                solvers = {}
                dropout_choices = [best_do] #[0.17, 0.15, 0.13] 0.567 0.002 0.13 100
                epoch = 12
                xi = best_lr/12.0
                learning_rates = [ xi ]
                                            #[5e-3, 3.5e-3, 2.5e-3, 2e-3, 1e-3, 7e-4, 5e-4]
                batches = [200]
                size = 800
                best_lr = None
                best_epo = None
                best_do = None
                best_solver = None
                best_size = None
                \#best_hy = None
                best_acc = 0
                print('We will use learning rate %f; epoch %d; dropout %f' %(lr,epoch, dropout) )
                #model = FullyConnectedNet([200, 150, 100, 100, 100, 50, 50], dropout=dropout)
                solver = Solver(best_model, small_data,
                      num_epochs=epoch, batch_size=size,
                      update_rule='adam',
```

```
optim_config={
                 'learning_rate': xi,
               },
               verbose=True, print_every=100)
         solver.train()
         acc = solver.best_val_acc
         if acc>best acc:
             best_acc = acc
             best lr = xi
             best_epo = epoch
             best_do = dropout
             best_solver= solver
             best_size = size
             best_best_model = best_model
         # ------ #
         # END YOUR CODE HERE
         print('best val acc', best acc,'for learning rate: ', best lr, ' and dropout rate:
implement change in the learning rate in the spirit of an elaborate leraning schedule
We will use learning rate 0.000800; epoch 40; dropout 0.150000
(Iteration 1 / 2440) loss: 0.890947
(Epoch 0 / 40) train acc: 0.743000; val acc: 0.582000
(Epoch 1 / 40) train acc: 0.769000; val_acc: 0.592000
(Iteration 101 / 2440) loss: 0.840512
(Epoch 2 / 40) train acc: 0.785000; val_acc: 0.593000
(Epoch 3 / 40) train acc: 0.788000; val_acc: 0.583000
(Iteration 201 / 2440) loss: 0.772719
(Epoch 4 / 40) train acc: 0.795000; val_acc: 0.599000
(Iteration 301 / 2440) loss: 0.819006
(Epoch 5 / 40) train acc: 0.761000; val_acc: 0.595000
(Epoch 6 / 40) train acc: 0.813000; val_acc: 0.596000
(Iteration 401 / 2440) loss: 0.740634
(Epoch 7 / 40) train acc: 0.785000; val_acc: 0.597000
(Epoch 8 / 40) train acc: 0.797000; val_acc: 0.588000
(Iteration 501 / 2440) loss: 0.730205
(Epoch 9 / 40) train acc: 0.779000; val_acc: 0.600000
(Iteration 601 / 2440) loss: 0.774681
(Epoch 10 / 40) train acc: 0.812000; val_acc: 0.601000
(Epoch 11 / 40) train acc: 0.807000; val_acc: 0.598000
(Iteration 701 / 2440) loss: 0.724010
(Epoch 12 / 40) train acc: 0.831000; val_acc: 0.594000
(Epoch 13 / 40) train acc: 0.802000; val_acc: 0.591000
(Iteration 801 / 2440) loss: 0.767440
(Epoch 14 / 40) train acc: 0.787000; val_acc: 0.596000
(Iteration 901 / 2440) loss: 0.657926
```

```
(Epoch 15 / 40) train acc: 0.815000; val_acc: 0.597000
(Epoch 16 / 40) train acc: 0.800000; val_acc: 0.591000
(Iteration 1001 / 2440) loss: 0.740929
(Epoch 17 / 40) train acc: 0.823000; val_acc: 0.590000
(Epoch 18 / 40) train acc: 0.818000; val acc: 0.597000
(Iteration 1101 / 2440) loss: 0.721587
(Epoch 19 / 40) train acc: 0.844000; val acc: 0.594000
(Iteration 1201 / 2440) loss: 0.623354
(Epoch 20 / 40) train acc: 0.804000; val_acc: 0.591000
(Epoch 21 / 40) train acc: 0.845000; val_acc: 0.604000
(Iteration 1301 / 2440) loss: 0.669358
(Epoch 22 / 40) train acc: 0.820000; val_acc: 0.599000
(Iteration 1401 / 2440) loss: 0.660870
(Epoch 23 / 40) train acc: 0.833000; val_acc: 0.595000
(Epoch 24 / 40) train acc: 0.806000; val_acc: 0.597000
(Iteration 1501 / 2440) loss: 0.682781
(Epoch 25 / 40) train acc: 0.836000; val_acc: 0.599000
(Epoch 26 / 40) train acc: 0.816000; val_acc: 0.599000
(Iteration 1601 / 2440) loss: 0.707949
(Epoch 27 / 40) train acc: 0.841000; val acc: 0.593000
(Iteration 1701 / 2440) loss: 0.723006
(Epoch 28 / 40) train acc: 0.829000; val acc: 0.592000
(Epoch 29 / 40) train acc: 0.846000; val_acc: 0.600000
(Iteration 1801 / 2440) loss: 0.609438
(Epoch 30 / 40) train acc: 0.843000; val_acc: 0.594000
(Epoch 31 / 40) train acc: 0.832000; val_acc: 0.594000
(Iteration 1901 / 2440) loss: 0.625446
(Epoch 32 / 40) train acc: 0.842000; val_acc: 0.590000
(Iteration 2001 / 2440) loss: 0.633570
(Epoch 33 / 40) train acc: 0.847000; val_acc: 0.592000
(Epoch 34 / 40) train acc: 0.859000; val_acc: 0.594000
(Iteration 2101 / 2440) loss: 0.694739
(Epoch 35 / 40) train acc: 0.833000; val_acc: 0.593000
(Epoch 36 / 40) train acc: 0.837000; val_acc: 0.588000
(Iteration 2201 / 2440) loss: 0.680477
(Epoch 37 / 40) train acc: 0.841000; val acc: 0.592000
(Iteration 2301 / 2440) loss: 0.631987
(Epoch 38 / 40) train acc: 0.845000; val_acc: 0.597000
(Epoch 39 / 40) train acc: 0.836000; val_acc: 0.597000
(Iteration 2401 / 2440) loss: 0.649395
(Epoch 40 / 40) train acc: 0.869000; val_acc: 0.592000
best val acc 0.604 for learning rate: 6.666666666666667e-05 and dropout rate: 0.15 and epo-
In [122]: # Train two identical nets, one with dropout and one without
```

num_train = 49000

```
'X_train': data['X_train'][:num_train],
   'y_train': data['y_train'][:num_train],
    'X_val': data['X_val'],
#
    'y_val': data['y_val'],
# }
print('implement change in the learning rate in the spirit of an elaborate leraning
solvers = {}
dropout_choices = [best_do] #[0.17, 0.15, 0.13] 0.567 0.002 0.13 100
epoch = 12
xi = xi/12.0
learning_rates = [ xi ] #[5e-3, 3.5e-3, 2.5e-3, 2e-3, 1e-3, 7e-4, 5e-4]
batches = [200]
size = 800
best_lr = None
best_epo = None
best_do = None
best_solver = None
best size = None
\#best_hy = None
best_acc = 0
print('We will use learning rate %f; epoch %d; dropout %f' %(lr,epoch, dropout) )
#model = FullyConnectedNet([200, 150, 100, 100, 100, 50, 50], dropout=dropout)
solver = Solver(best_best_model, small_data,
      num_epochs=epoch, batch_size=size,
      update_rule='adam',
      optim_config={
        'learning_rate': xi,
      },
     verbose=True, print_every=100)
solver.train()
acc = solver.best_val_acc
if acc>best_acc:
   best_acc = acc
   best_lr = xi
   best_epo = epoch
   best_do = dropout
   best_solver= solver
   best_size = size
   best_best_model = best_best_model
```

```
# ----- #
         # END YOUR CODE HERE
         print('best val acc', best acc,'for learning rate: ', xi, ' and dropout rate: ', be
implement change in the learning rate in the spirit of an elaborate leraning schedule
We will use learning rate 0.000800; epoch 12; dropout 0.150000
(Iteration 1 / 732) loss: 0.665470
(Epoch 0 / 12) train acc: 0.831000; val acc: 0.605000
(Epoch 1 / 12) train acc: 0.840000; val_acc: 0.600000
(Iteration 101 / 732) loss: 0.751433
(Epoch 2 / 12) train acc: 0.847000; val_acc: 0.600000
(Epoch 3 / 12) train acc: 0.831000; val_acc: 0.599000
(Iteration 201 / 732) loss: 0.653424
(Epoch 4 / 12) train acc: 0.824000; val_acc: 0.599000
(Iteration 301 / 732) loss: 0.675666
(Epoch 5 / 12) train acc: 0.837000; val_acc: 0.600000
(Epoch 6 / 12) train acc: 0.862000; val_acc: 0.600000
(Iteration 401 / 732) loss: 0.740022
(Epoch 7 / 12) train acc: 0.829000; val_acc: 0.605000
(Epoch 8 / 12) train acc: 0.830000; val_acc: 0.600000
(Iteration 501 / 732) loss: 0.674710
(Epoch 9 / 12) train acc: 0.815000; val_acc: 0.599000
(Iteration 601 / 732) loss: 0.686065
(Epoch 10 / 12) train acc: 0.826000; val_acc: 0.598000
(Epoch 11 / 12) train acc: 0.832000; val acc: 0.597000
(Iteration 701 / 732) loss: 0.618604
(Epoch 12 / 12) train acc: 0.844000; val_acc: 0.600000
best val acc 0.605 for learning rate: 5.55555555555556e-06 and dropout rate: 0.15 and epo-
```

fc_net

February 10, 2021

```
In [ ]: import numpy as np
        import pdb
        from .layers import *
        from .layer_utils import *
        This code was originally written for CS 231n at Stanford University
        (cs231n.stanford.edu). It has been modified in various areas for use in the
        ECE 239AS class at UCLA. This includes the descriptions of what code to
        implement as well as some slight potential changes in variable names to be
        consistent with class nomenclature. We thank Justin Johnson & Serena Yeung for
        permission to use this code. To see the original version, please visit
        cs231n.stanford.edu.
        11 11 11
        class TwoLayerNet(object):
          11 11 11
          A two-layer fully-connected neural network with ReLU nonlinearity and
          softmax loss that uses a modular layer design. We assume an input dimension
          of D, a hidden dimension of H, and perform classification over C classes.
          The architecure should be affine - relu - affine - softmax.
          Note that this class does not implement gradient descent; instead, it
          will interact with a separate Solver object that is responsible for running
          optimization.
          The learnable parameters of the model are stored in the dictionary
          self.params that maps parameter names to numpy arrays.
          HHHH
          def __init__(self, input_dim=3*32*32, hidden_dims=100, num_classes=10,
                       dropout=0, weight_scale=1e-3, reg=0.0):
            Initialize a new network.
            Inputs:
```

```
- input_dim: An integer giving the size of the input
 - hidden_dims: An integer giving the size of the hidden layer
 - num_classes: An integer giving the number of classes to classify
 - dropout: Scalar between 0 and 1 giving dropout strength.
 - weight scale: Scalar giving the standard deviation for random
   initialization of the weights.
 - reg: Scalar giving L2 regularization strength.
 self.params = {}
 self.reg = reg
 # ----- #
 # YOUR CODE HERE:
    Initialize W1, W2, b1, and b2. Store these as self.params['W1'],
    self.params['W2'], self.params['b1'] and self.params['b2']. The
 # biases are initialized to zero and the weights are initialized
   so that each parameter has mean 0 and standard deviation weight_scale.
 # The dimensions of W1 should be (input_dim, hidden_dim) and the
 # dimensions of W2 should be (hidden_dims, num_classes)
 # ----- #
 # ----- #
 # END YOUR CODE HERE
 def loss(self, X, y=None):
 Compute loss and gradient for a minibatch of data.
 Inputs:
 - X: Array of input data of shape (N, d_1, \ldots, d_k)
 - y: Array of labels, of shape (N,). y[i] gives the label for X[i].
 Returns:
 If y is None, then run a test-time forward pass of the model and return:
 - scores: Array of shape (N, C) giving classification scores, where
   scores[i, c] is the classification score for X[i] and class c.
 If y is not None, then run a training-time forward and backward pass and
 return a tuple of:
 - loss: Scalar value giving the loss
 - grads: Dictionary with the same keys as self.params, mapping parameter
   names to gradients of the loss with respect to those parameters.
 scores = None
 # ----- #
```

```
# YOUR CODE HERE:
      Implement the forward pass of the two-layer neural network. Store
      the class scores as the variable 'scores'. Be sure to use the layers
      you prior implemented.
   # ------ #
   # ----- #
   # END YOUR CODE HERE
   # If y is None then we are in test mode so just return scores
   if y is None:
    return scores
   loss, grads = 0, {}
   # ----- #
   # YOUR CODE HERE:
      Implement the backward pass of the two-layer neural net. Store
      the loss as the variable 'loss' and store the gradients in the
      'grads' dictionary. For the grads dictionary, grads['W1'] holds
     the gradient for W1, grads['b1'] holds the gradient for b1, etc.
      i.e., grads[k] holds the gradient for self.params[k].
     Add L2 regularization, where there is an added cost 0.5*self.reg*W^2
   #
      for each W. Be sure to include the 0.5 multiplying factor to
   #
      match our implementation.
     And be sure to use the layers you prior implemented.
   # ----- #
   # END YOUR CODE HERE
   # ----- #
  return loss, grads
class FullyConnectedNet(object):
 11 11 11
 A fully-connected neural network with an arbitrary number of hidden layers,
 ReLU nonlinearities, and a softmax loss function. This will also implement
 dropout and batch normalization as options. For a network with L layers,
 the architecture will be
 \{affine - [batch norm] - relu - [dropout]\} x (L - 1) - affine - softmax
 where batch normalization and dropout are optional, and the {...} block is
 repeated L-1 times.
```

```
Similar to the TwoLayerNet above, learnable parameters are stored in the
self.params dictionary and will be learned using the Solver class.
def __init__(self, hidden_dims, input_dim=3*32*32, num_classes=10,
            dropout=0, use batchnorm=False, reg=0.0,
            weight_scale=1e-2, dtype=np.float32, seed=None):
  Initialize a new FullyConnectedNet.
  Inputs:
  - hidden_dims: A list of integers giving the size of each hidden layer.
  - input_dim: An integer giving the size of the input.
  - num_classes: An integer giving the number of classes to classify.
  - dropout: Scalar between 0 and 1 giving dropout strength. If dropout=0 then
    the network should not use dropout at all.
  - use batchnorm: Whether or not the network should use batch normalization.
  - reg: Scalar giving L2 regularization strength.
  - weight scale: Scalar giving the standard deviation for random
    initialization of the weights.
  - dtype: A numpy datatype object; all computations will be performed using
   this datatype. float32 is faster but less accurate, so you should use
   float64 for numeric gradient checking.
  - seed: If not None, then pass this random seed to the dropout layers. This
   will make the dropout layers deteriminstic so we can gradient check the
   model.
  11 11 11
  self.use_batchnorm = use_batchnorm
  self.use_dropout = dropout > 0
  self.reg = reg
  self.num_layers = 1 + len(hidden_dims)
  self.dtype = dtype
  self.params = {}
  # ----- #
  # YOUR CODE HERE:
     Initialize all parameters of the network in the self.params dictionary.
     The weights and biases of layer 1 are W1 and b1; and in general the
     weights and biases of layer i are Wi and bi. The
  #
     biases are initialized to zero and the weights are initialized
     so that each parameter has mean O and standard deviation weight scale.
  #
     BATCHNORM: Initialize the gammas of each layer to 1 and the beta
  #
```

is true and DO NOT do batch normalize the output scores.

#

parameters to zero. The gamma and beta parameters for layer 1 should be self.params['gamma1'] and self.params['beta1']. For layer 2, they

should be gamma2 and beta2, etc. Only use batchnorm if self.use_batchnorm

```
# ----- #
   layers_dims = np.hstack([input_dim, hidden_dims, num_classes])
   for i in range(self.num_layers):
       self.params['W'+str(i+1)] = weight_scale*np.random.randn(layers_dims[i],layers_
       self.params['b'+str(i+1)] = np.zeros(layers_dims[i+1])
   if self.use_batchnorm:
       for i in range(self.num_layers-1):
          self.params['gamma'+str(i+1)] = np.ones(layers_dims[i+1])
          self.params['beta' +str(i+1)] = np.zeros(layers_dims[i+1])
# ----- #
   # END YOUR CODE HERE
   # ----- #
   # When using dropout we need to pass a dropout param dictionary to each
   # dropout layer so that the layer knows the dropout probability and the mode
   # (train / test). You can pass the same dropout param to each dropout layer.
   self.dropout_param = {}
   if self.use_dropout:
     self.dropout_param = {'mode': 'train', 'p': dropout}
     if seed is not None:
       self.dropout_param['seed'] = seed
   # With batch normalization we need to keep track of running means and
   # variances, so we need to pass a special bn_param object to each batch
   # normalization layer. You should pass self.bn_params[0] to the forward pass
   # of the first batch normalization layer, self.bn_params[1] to the forward
   # pass of the second batch normalization layer, etc.
   self.bn_params = []
   if self.use_batchnorm:
     self.bn_params = [{'mode': 'train'} for i in np.arange(self.num_layers - 1)]
   # Cast all parameters to the correct datatype
   for k, v in self.params.items():
     self.params[k] = v.astype(dtype)
 def loss(self, X, y=None):
   11 11 11
   Compute loss and gradient for the fully-connected net.
   Input / output: Same as TwoLayerNet above.
   X = X.astype(self.dtype)
   mode = 'test' if y is None else 'train'
```

```
if self.dropout_param is not None:
 self.dropout_param['mode'] = mode
if self.use_batchnorm:
 for bn_param in self.bn_params:
   bn_param[mode] = mode
scores = None
# ------ #
# YOUR CODE HERE:
   Implement the forward pass of the FC net and store the output
   scores as the variable "scores".
#
#
   BATCHNORM: If self.use_batchnorm is true, insert a bathnorm layer
   between the affine_forward and relu_forward layers. You may
#
   also write an affine_batchnorm_relu() function in layer_utils.py.
#
#
#
   DROPOUT: If dropout is non-zero, insert a dropout layer after
   every ReLU layer.
# ------ #
x = X
caches = []
gamma, beta, bn_params = None, None, None
for i in range(self.num_layers-1):
   ww = self.params['W'+str(i+1)]
   bb = self.params['b'+str(i+1)]
     print('type of w ',str(i+1),' is ', type(ww))
     print('type of w is ', type(self.params['W'+str(i+1)]))
   if self.use_batchnorm:
       gamma = self.params['gamma'+str(i+1)]
       beta = self.params['beta'+str(i+1)]
       bn_params = self.bn_params[i]
       #print( type(gamma), type(beta) , type(bn_params) )
     else:
         gamma = None
         beta = None
     if ww is None:
         print(ww)
   x, cache = affine_norm_relu_forward(x,ww,bb, gamma, beta, bn_params, self.use_
   caches.append(cache)
```

Set train/test mode for batchnorm params and dropout param since they

behave differently during training and testing.

```
w = self.params['W'+str(self.num_layers)]
b = self.params['b'+str(self.num_layers)]
scores, cache = affine_forward(x,w,b)
caches.append(cache)
# ----- #
# END YOUR CODE HERE
# If test mode return early
if mode == 'test':
 return scores
loss, grads = 0.0, {}
# ----- #
# YOUR CODE HERE:
   Implement the backwards pass of the FC net and store the gradients
   in the grads dict, so that grads[k] is the gradient of self.params[k]
   Be sure your L2 regularization includes a 0.5 factor.
   BATCHNORM: Incorporate the backward pass of the batchnorm.
  DROPOUT: Incorporate the backward pass of dropout.
# for loss
loss, softmax_grad = softmax_loss(scores, y)
for i in range(self.num_layers):
   w = self.params['W'+str(i+1)]
   loss += 0.5 * self.reg * np.sum(w * w)
# for gradients
dout = softmax_grad
dout, dw, db = affine_backward(dout, caches[self.num_layers - 1])
grads['W' + str(self.num_layers)] = dw + self.reg * self.params['W' + str(self.num
grads['b' + str(self.num_layers)] = db
for i in range(self.num_layers - 2, -1, -1):
   dx, dw, db, dgamma, dbeta = affine norm relu backward(dout, caches[i], self.us
   if self.use_batchnorm:
      grads['gamma'+str(i+1)] = dgamma
      grads['beta' +str(i+1)] = dbeta
   grads['W' + str(i + 1)] = dw + self.reg * self.params['W' + str(i + 1)]
   grads['b' + str(i + 1)] = db
   dout = dx
```

#		#
#	END YOUR CODE HERE	
#		#

return loss, grads