

STATISTICAL MODEL WITHOUT THE CONFUNDER

Math

$$y \sim \text{Normal}(\mu, \sigma)$$

$$\mu = a + bx$$

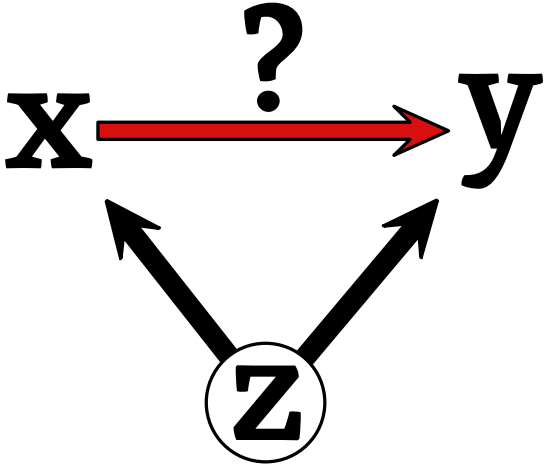
$$a \sim \text{Normal}(0, 0.3)$$

$$b \sim \text{Normal}(0, 0.3)$$

$$\sigma \sim \text{Exponential}(1)$$

Rethinking Code

```
m1 = ulam(alist(  
  y ~ normal(mu, sigma),  
  mu = a + bx*x,  
  a ~ normal(0, 0.3),  
  bx ~ normal(0, 0.3),  
  sigma ~ exponential(1)  
), data = list(y = y, x = x))
```





X



y

X



y



STATISTICAL MODEL WITHOUT THE CONFOUNDER Z

Math

$X \longrightarrow y$

$$y \sim \text{Normal}(\mu, \sigma)$$

$$\mu = a + bx$$

$$a \sim \text{Normal}(0, 0.3)$$

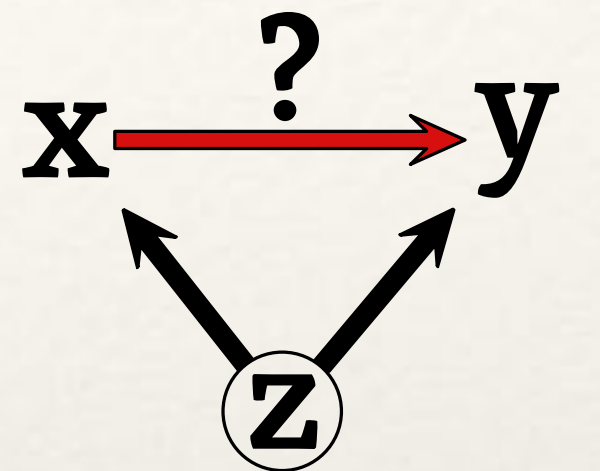
$$b \sim \text{Normal}(0, 0.3)$$

$$\sigma \sim \text{Exponential}(1)$$

Rethinking Code

$X \longrightarrow y$

```
m1 = ulam(alist(  
  y ~ normal(mu, sigma),  
  mu = a + bx*x,  
  a ~ normal(0, 0.3),  
  bx ~ normal(0, 0.3),  
  sigma ~ exponential(1)  
, data = list(y = y, x = x))
```



MODEL ESTIMATES WITHOUT THE CONFOUNDER

> precis(m1)

| | mean | sd | 5.5% | 94.5% | n_eff | Rhat4 |
|-------|------|------|------|-------|-------|-------|
| a | 0.54 | 0.14 | 0.32 | 0.77 | 1274 | 1 |
| bx | 1.47 | 0.08 | 1.34 | 1.60 | 1432 | 1 |
| sigma | 1.33 | 0.10 | 1.19 | 1.49 | 1418 | 1 |

X → y

Estimate of the effect of x on y