





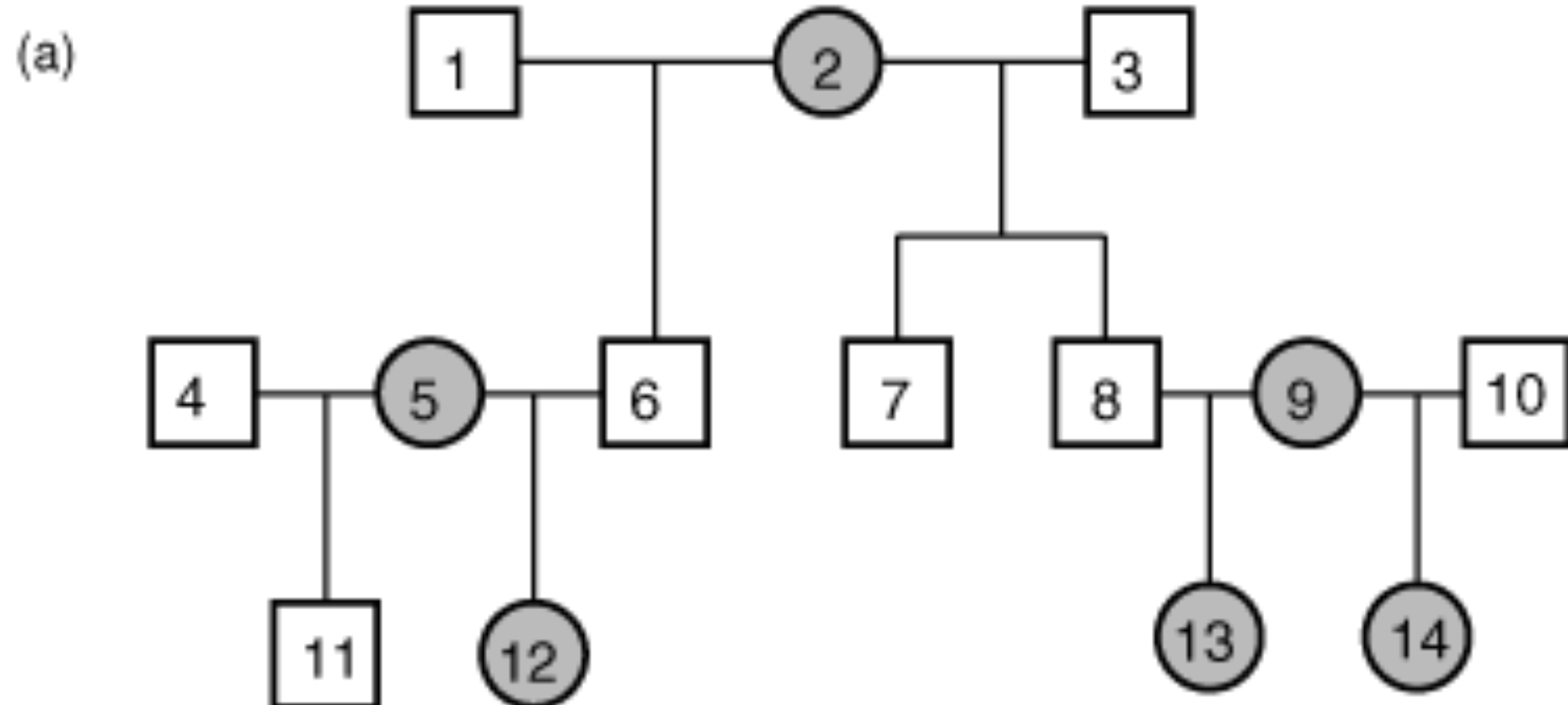
$$y_i \sim \text{Normal}(\mu_i, \sigma_R)$$

$$\mu_i = \alpha_0 + \alpha_i$$

$$\alpha \sim \text{MVNormal}(0, \sigma_G \times A)$$

$$\sigma_G, \sigma_R \sim \text{Exponential}(1)$$

EXAMPLE: ANIMAL MODEL

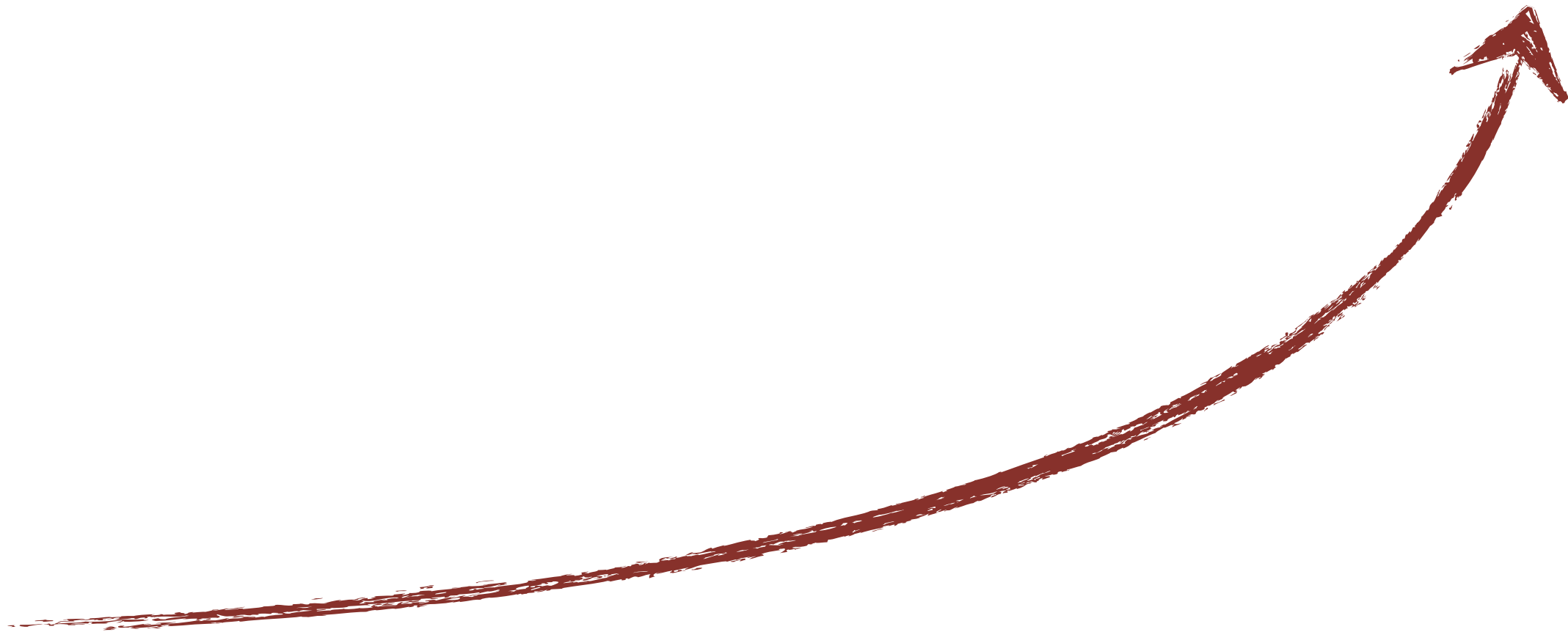


(b)

$$\mathbf{A} = \begin{pmatrix} 1 & 0 & 0 & 0 & 0 & 0.5 & 0 & 0 & 0 & 0 & 0 & 0.25 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 & 0.5 & 0.5 & 0.5 & 0 & 0 & 0 & 0.25 & 0.25 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 & 0.5 & 0.5 & 0 & 0 & 0 & 0 & 0.25 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0.5 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0.5 & 0.5 & 0 \\ 0.5 & 0.5 & 0 & 0 & 0 & 1 & 0.25 & 0.25 & 0 & 0 & 0 & 0.5 & 0.125 & 0 \\ 0 & 0.5 & 0.5 & 0 & 0 & 0.25 & 1 & 0.5 & 0 & 0 & 0 & 0.125 & 0.25 & 0 \\ 0 & 0.5 & 0.5 & 0 & 0 & 0.25 & 0.5 & 1 & 0 & 0 & 0 & 0.125 & 0.5 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0.5 & 0.5 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0.5 \\ 0 & 0 & 0 & 0.5 & 0.5 & 0 & 0 & 0 & 0 & 0 & 1 & 0.25 & 0 & 0 \\ 0.25 & 0.25 & 0 & 0 & 0.5 & 0.5 & 0.125 & 0.125 & 0 & 0 & 0.25 & 1 & 0.0625 & 0 \\ 0 & 0.25 & 0.25 & 0 & 0 & 0.125 & 0.25 & 0.5 & 0.5 & 0 & 0 & 0.0625 & 1 & 0.25 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0.5 & 0.5 & 0 & 0 & 0.25 & 1 \end{pmatrix}$$

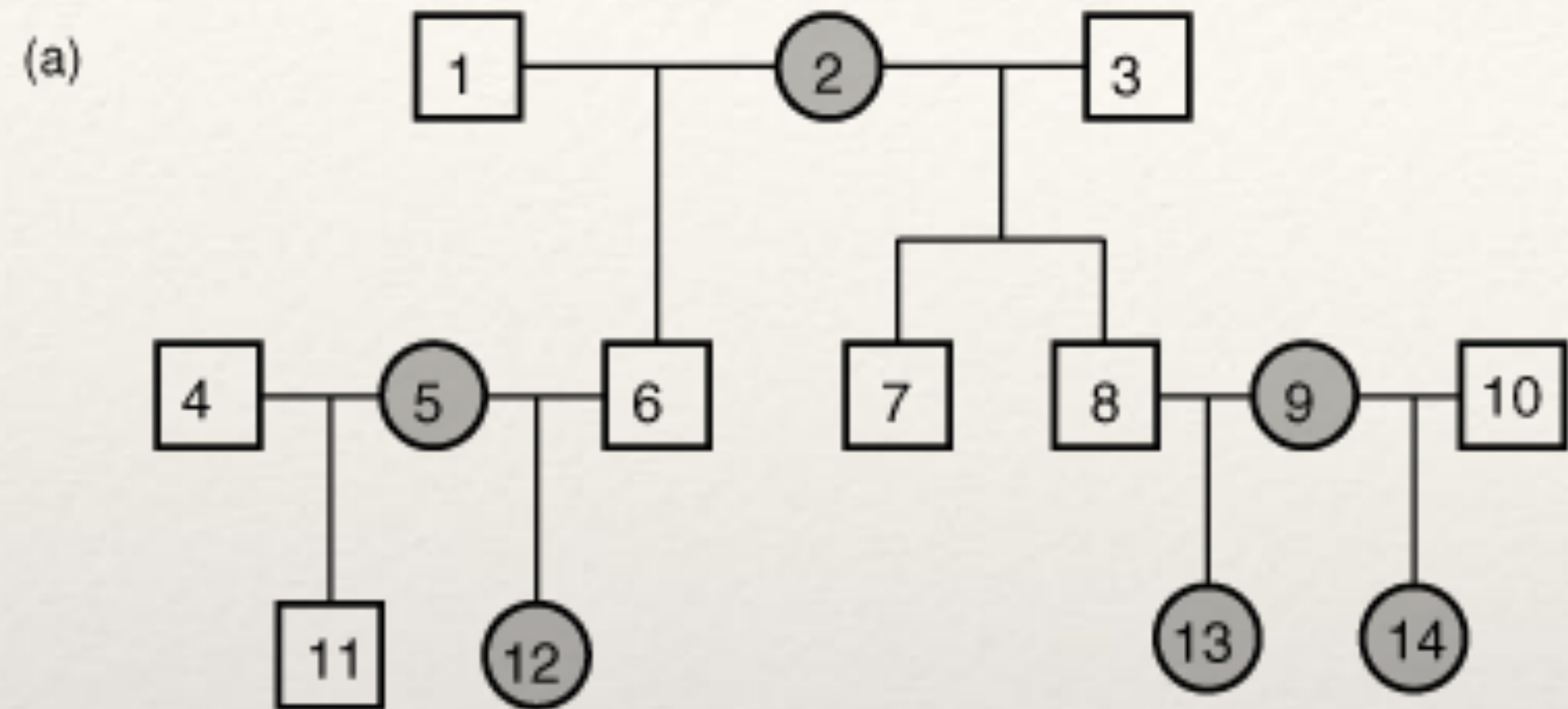
Wilson, A.J. et al. An ecologist's guide to the animal model. J. Anim. Ecol. 79, 13-26 (2010)

Same thing for the phylogeny or  
the spacial auto-correlation





# EXAMPLE: ANIMAL MODEL



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