

函數的圖形

$$y = mx + b$$

$$\textcircled{1} \quad y = x + 0$$

$$1 \quad 0$$

$$\textcircled{2} \quad y = 2x + 0$$

$$2 \quad 0$$

$$\textcircled{3} \quad y = \frac{1}{2}x + 0$$

$$\frac{1}{2} \quad 0$$

$$\textcircled{4} \quad y = x + 2$$

$$1 \quad 2$$

$$\textcircled{5} \quad y = 2x + 2$$

$$2 \quad 2$$

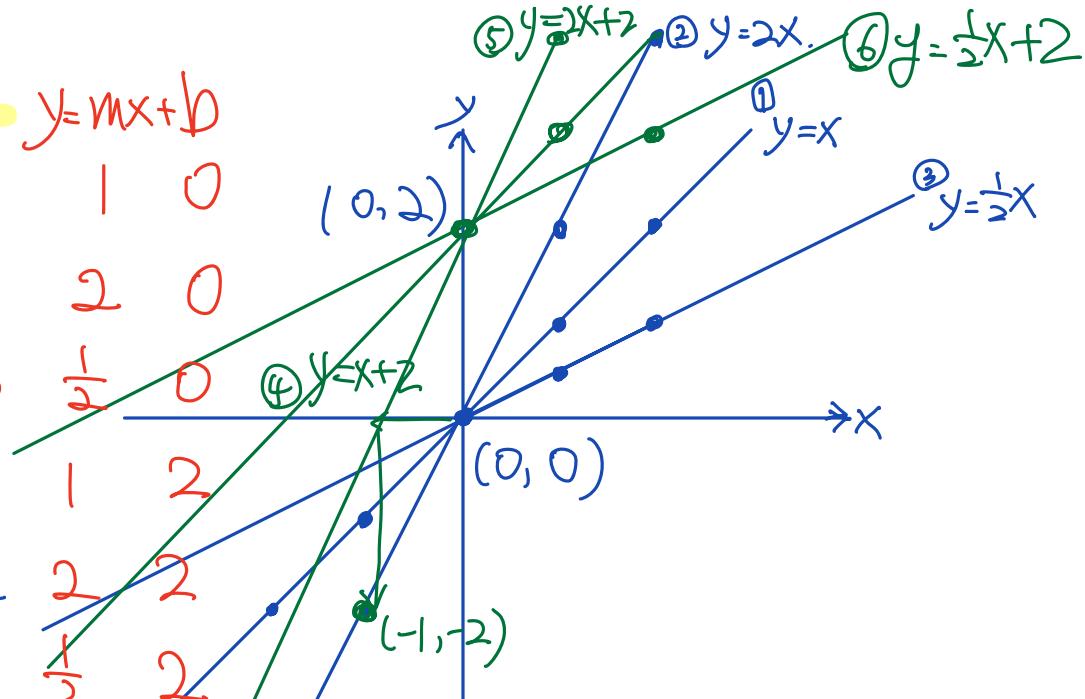
$$\textcircled{6} \quad y = \frac{1}{2}x + 2$$

$$\frac{1}{2} \quad 2$$

$$\textcircled{7} \quad y = |x|$$

絕對值
↑

$$y = 2x$$



①	x	-2	-1	0	1	2	3
	y	-2	-1	0	1	2	3

②	x	-2	-1	0	1	2	3
	y	-4	-2	0	2	4	6

③	x	0	1	2			
	y	0	½	1			

④	x	0	1	2			
	y	2	3	4			

⑤	x	0	1			
	y	2	4			

⑥	x	0	2			
	y	2	3			

{ ① 代入相同的 x

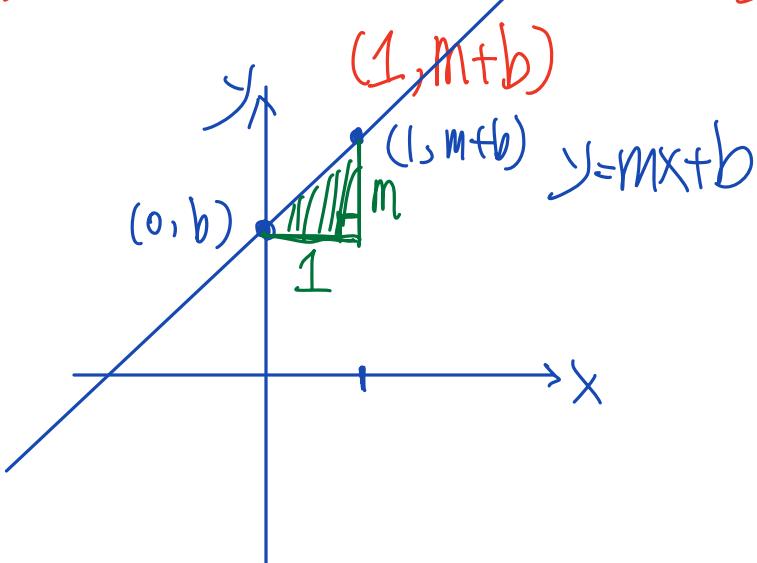
② 描點 (x, y) 在坐標平面上

③ 連起來

$$y = mx + b$$

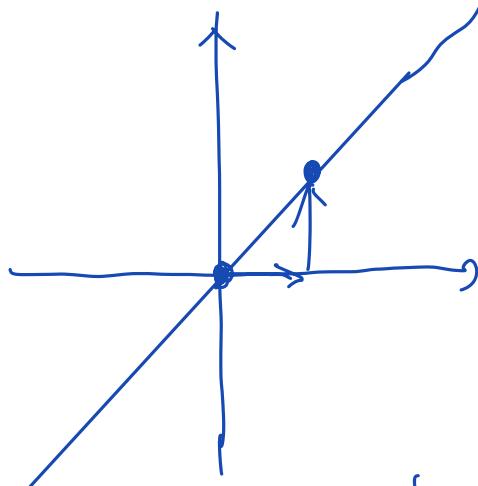
1) m 相同的直線平行. $\rightsquigarrow \left\{ \begin{array}{l} m: \text{斜率} \\ \text{下} \\ \text{(有多斜)} \end{array} \right.$
 2) 直線都通過 $(0, b)$. $\rightsquigarrow \left\{ \begin{array}{l} b: \text{y軸截距} \\ \uparrow \\ \text{(切在y軸上的y座標)} \end{array} \right.$

3) 直線一定會過 $(0, b)$

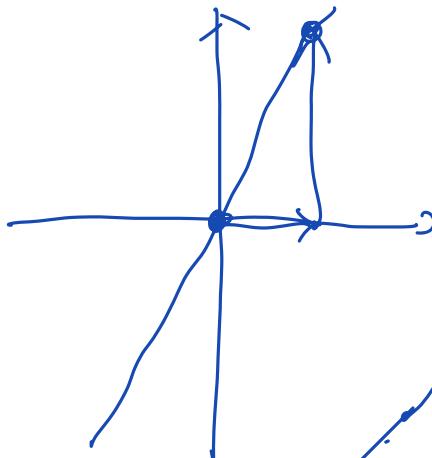


\Rightarrow x 往右走 1 單位時, y 會往上走 m 單位!!

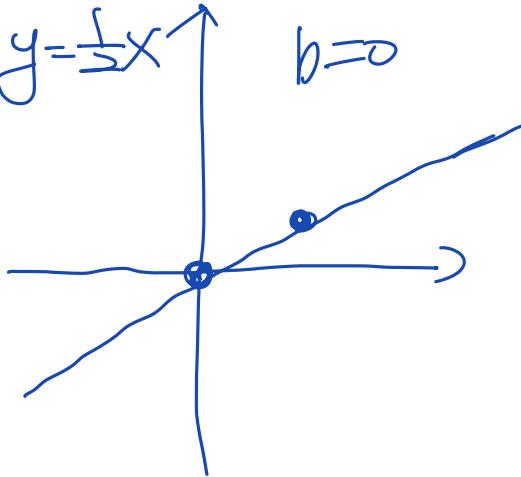
$$\textcircled{1} \quad y = x + 0 \quad : \text{過}(0,0), m=1, b=0$$



$$\textcircled{2} \quad y = 2x, m=2, b=0, (0,0)$$



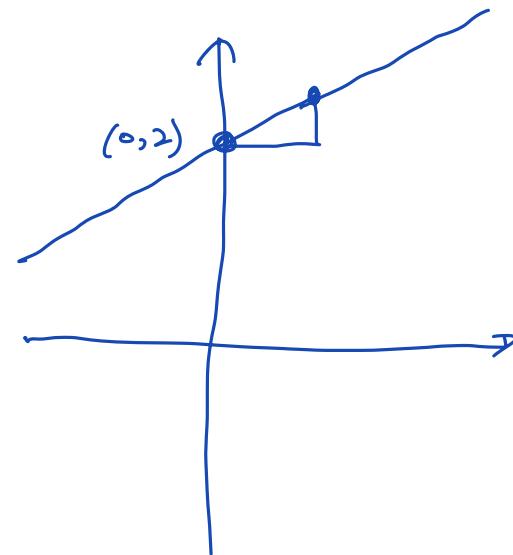
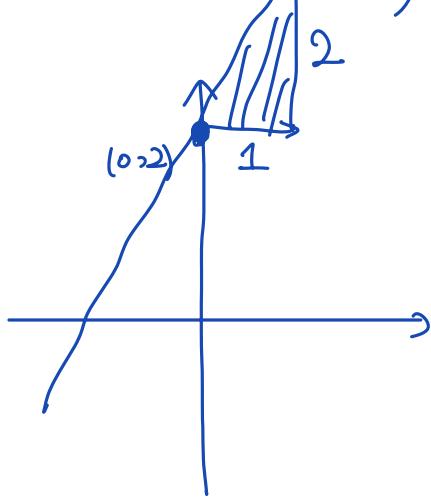
$$\textcircled{3} \quad y = \frac{1}{2}x, m=\frac{1}{2}, b=0$$



$$\textcircled{4} \quad y = x + 2, m=1, b=2 \Rightarrow (0,2)$$

$$\textcircled{6} \quad y = \frac{m}{2}x + b \quad m=\frac{1}{2} \text{ (xの倍数), } b=2$$

$$\textcircled{5} \quad y = 2x + 2, \frac{m}{2}=2 \Rightarrow (0,2)$$



• 比較係數

$$y = mx + b \text{ (通式)}$$

$$\textcircled{1} \quad \begin{aligned} y &= 3x + 9 \\ &\equiv \\ y &= mx + b \end{aligned}$$

$$m = 3, b = 9.$$

$$\textcircled{2} \quad \begin{aligned} y &= -2x + 4 \\ &\equiv \\ y &= mx + b \end{aligned}$$

$$m = -2, b = 4$$

$$\textcircled{3} \quad \begin{aligned} 2x + y &= 2 \xrightarrow{\text{移項}} y = -2x + 2 \\ y &= mx + b \quad y = mx + b \\ m &= -2, b = 2 \end{aligned}$$

$$\textcircled{4} \quad 3x + 4y = 5$$

$$4y = 5 - 3x$$

$$y = (5 - 3x) \div 4$$

$$y = \frac{5}{4} - \frac{3}{4}x$$

$$\begin{aligned} y &= -\frac{3}{4}x + \frac{5}{4} \\ y &= mx + b \end{aligned}$$

$$m = -\frac{3}{4}, b = \frac{5}{4}$$

↓

$$(0, \frac{5}{4}), (1, \frac{2}{4})$$

Step1. 先寫出通式

Step2. 一項一項對照 (需做一些處理)

Step3. 得出通式中的數值

$$\textcircled{5} \quad 4x + 3y = 5$$

$$3y = 5 - 4x \Rightarrow ey = f - dx$$

$$y = \frac{5 - 4x}{3} \Rightarrow y = \frac{f - dx}{e}$$

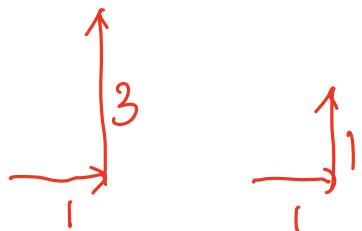
$$y = \frac{5}{3} - \frac{4}{3}x = \frac{f}{e} - \frac{d}{e}x$$

$$\Rightarrow y = -\frac{d}{e}x + \frac{f}{e}$$

$$y = -\frac{4}{3}x + \frac{5}{3} \Rightarrow m = -\frac{d}{e}, b = \frac{f}{e}$$

$$\Rightarrow m = -\frac{4}{3}, b = \frac{5}{3}$$

Q1: $y = 3x$ 和 $y = x$ 哪一條線比較陡?
 $m=3$ $m=1$ Ans: $y = 3x$



下次: ① $y = |x|$, $y = x^2$
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 絕對值.

② 不是直線的話怎麼知道多陡?

