

函數的圖形

$$y = mx + b$$

直線
[通式]

① $y = 1x + 0$

② $y = 2x + 0$

③ $y = \frac{1}{2}x + 0$

④ $y = 1x + 2$

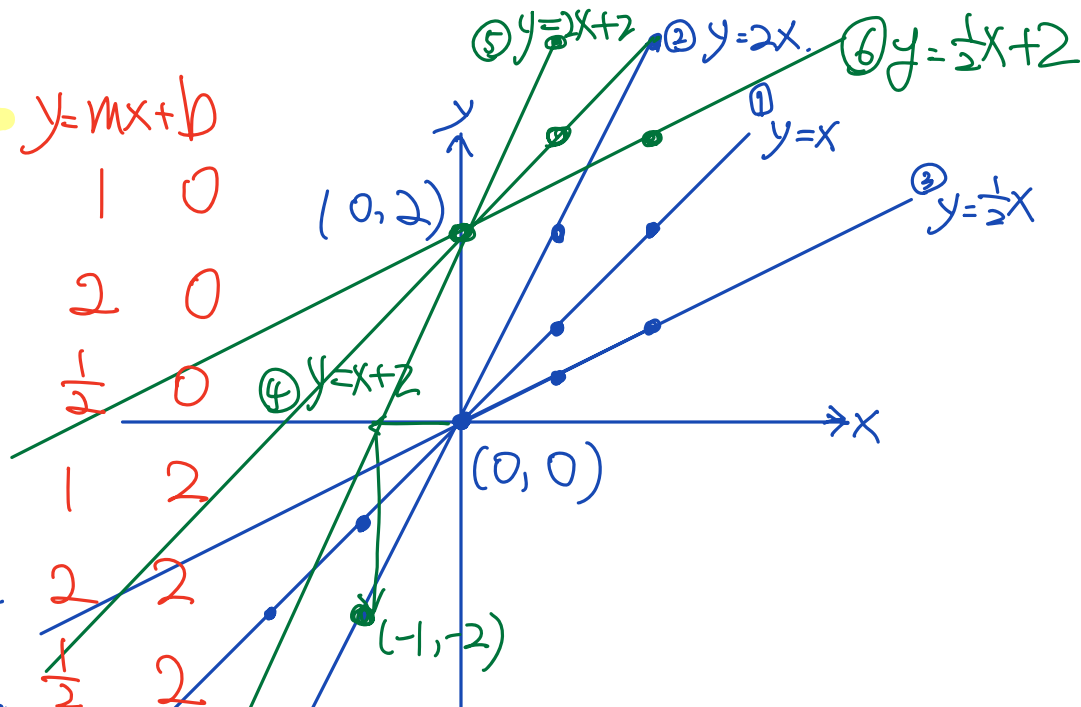
⑤ $y = 2x + 2$

⑥ $y = \frac{1}{2}x + 2$

⑦ $y = |x|$

$y = 2x$

絕對值



①	x	-2	-1	0	1	2	3
	y	-2	-1	0	1	2	3

②	x	-2	-1	0	1	2	3
	y	-4	-2	0	2	4	6

③	x	0	1	2
	y	0	$\frac{1}{2}$	1

④	x	0	1	2
	y	2	3	4

⑤	x	0	1
	y	2	4

⑥	x	0	2
	y	2	3

① 代入相同的x

② 描點 (x,y) 在坐標平面上

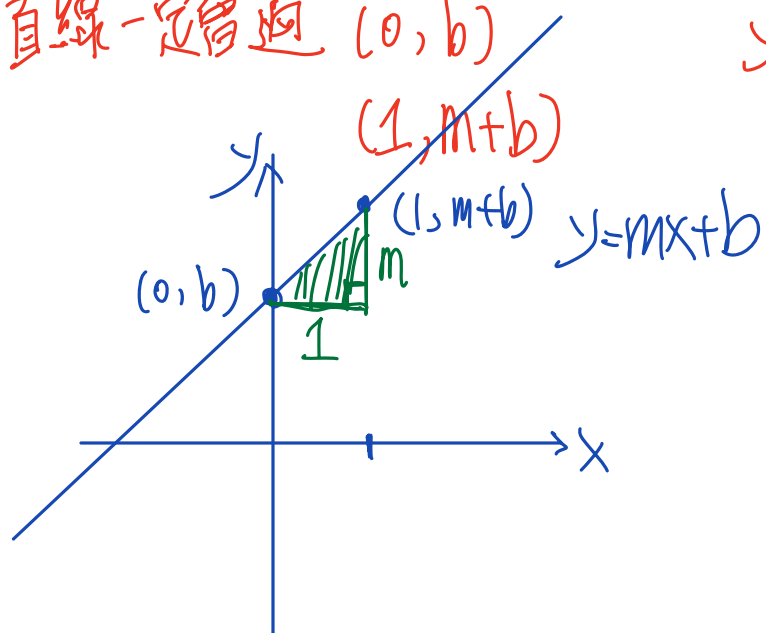
③ 連起來

$$y = mx + b$$

- 1) m 相同的直線平行. \rightsquigarrow m : 斜率
 2) 直線都通過 $(0, b)$ \rightsquigarrow b : y 軸截距

\uparrow
 (切)
 (切在 y 軸上的 y 座標)

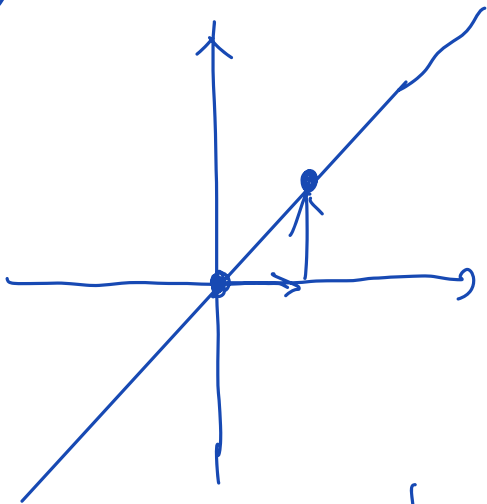
3) 直線一定通過 $(0, b)$



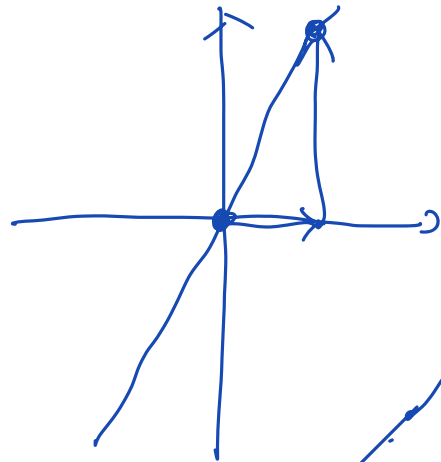
$$\begin{aligned} y &= mx + b \\ &= m + b \end{aligned}$$

\Rightarrow 又往右走 1 單位時, y 會往上走 m 單位!!

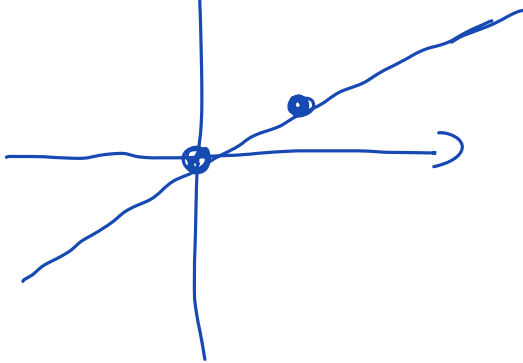
① $y = x + 0$: $\underline{y=0}$ (0,0), $m=1$
 $b=0$



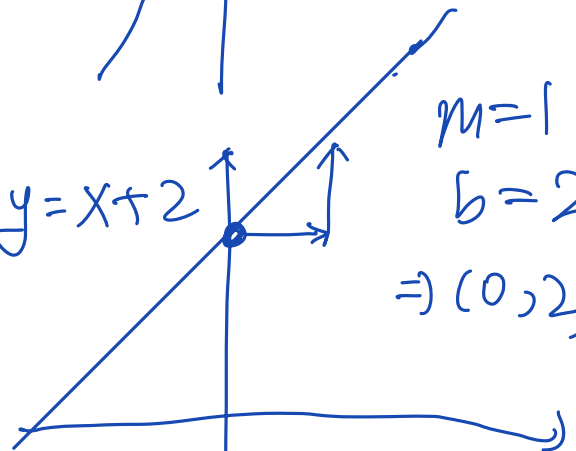
② $y = 2x$, $m=2$
 $b=0$, (0,0)



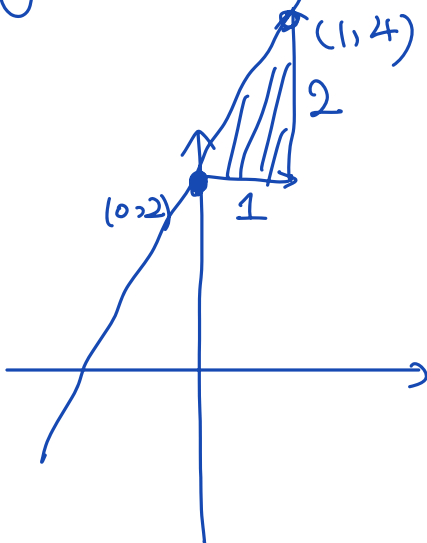
③ $y = \frac{1}{2}x$
 $m = \frac{1}{2}$
 $b=0$



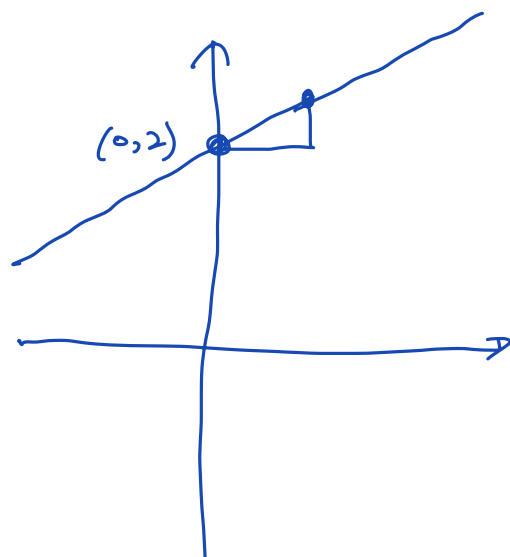
④ $y = x + 2$
 $m=1$
 $b=2$
 $\Rightarrow (0,2)$



⑤ $y = 2x + 2$, $m=2$, $b=2 \Rightarrow (0,2)$



⑥ $y = \frac{m}{1}x + \frac{b}{1}$
 $y = \frac{1}{2}x + 2$
 $m = \frac{1}{2}$ (x slope)
 $b = 2$ (y intercept)



· 比較係數

$$y = mx + b \text{ (通式)}$$

① $y = 3x + 9$
 $y = mx + b$
 $m = 3, b = 9$

② $y = 2x + 4$
 $y = mx + b$
 $m = 2, b = 4$

③ $2x + y = 2 \Rightarrow y = -2x + 2$
 $y = mx + b$
 $m = -2, b = 2$

④ $3x + 4y = 5$
 $4y = 5 - 3x$
 $y = (5 - 3x) \div 4$
 $y = \frac{5}{4} - \frac{3}{4}x$

$y = -\frac{3}{4}x + \frac{5}{4}$
 $y = mx + b$
 $m = -\frac{3}{4}, b = \frac{5}{4}$

\downarrow
 $(0, \frac{5}{4}), (1, \frac{2}{4})$

Step 1. 先寫出通式

Step 2. 一項一項對照 (需做一些處理)

Step 3. 得出通式中的數值

⑤ $4x + 3y = 5$

$3y = 5 - 4x$
 $y = \frac{5 - 4x}{3}$

$y = \frac{5}{3} - \frac{4}{3}x$

$y = -\frac{4}{3}x + \frac{5}{3}$

$\Rightarrow m = -\frac{4}{3}, b = \frac{5}{3}$

⑥ $dx + ey = f$

$\Rightarrow ey = f - dx$

$\Rightarrow y = \frac{f - dx}{e}$

$= \frac{f}{e} - \frac{d}{e}x$

$\Rightarrow y = -\frac{d}{e}x + \frac{f}{e}$

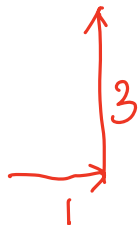
$\Rightarrow m = -\frac{d}{e}, b = \frac{f}{e}$

Q₁: $y = \underline{3}x$ 和 $y = \underline{1}x$ 哪一條線比較陡?

$m=3$

$m=1$

Ans: $y = 3x$



下次: ① $y = |x|$, $y = x^2$
 ↑
 絕對值.

② 不是直線的話怎麼知道多陡?

