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# 2. Basic Image Features

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Artificial Intelligence  
& Computer Vision  
L a b o r a t o r y



# Color



- Used heavily in human vision
- Color is a pixel property, making some recognition problems easy
- Visible spectrum for humans is 400 nm (blue) to 700 nm (red)
- Machines can “see” much more;  
ex. X-rays, infrared, radio waves



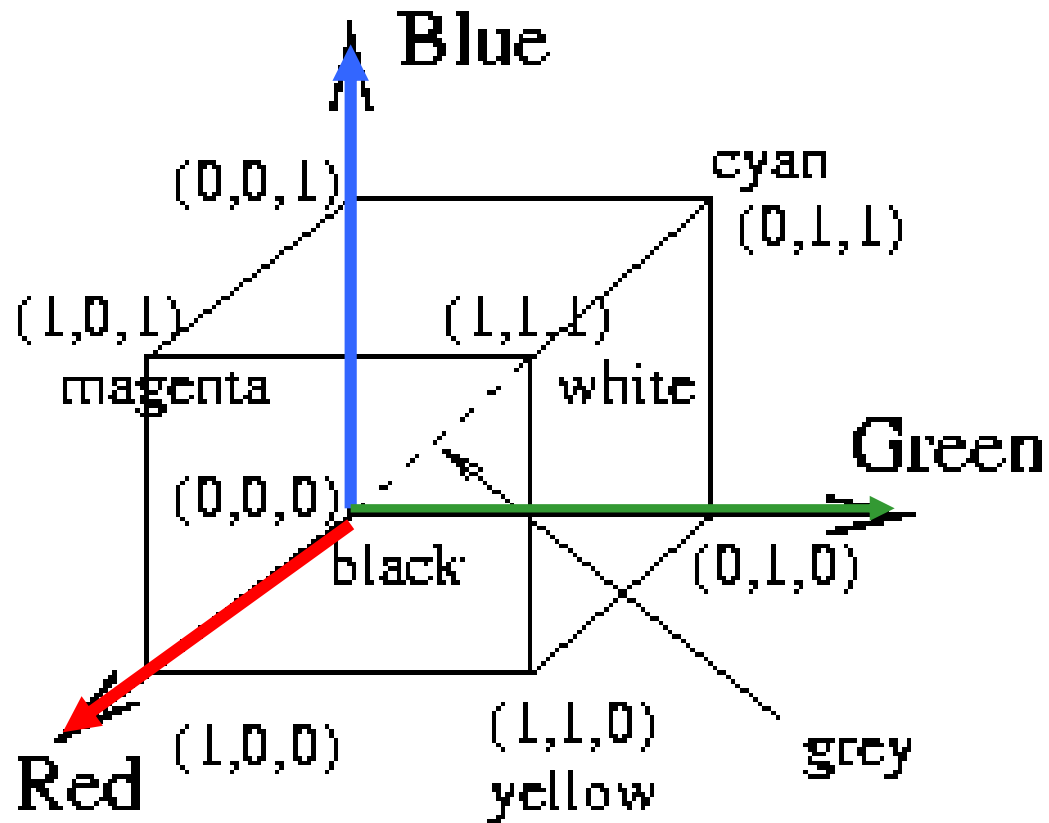


# Coding methods for humans

- ☐ RGB is an additive system (add colors to black) used for displays.
- ☐ CMY is a subtractive system for printing.
- ☐ HSI is a good perceptual space for art, psychology, and recognition.
- ☐ YIQ used for TV is good for compression.



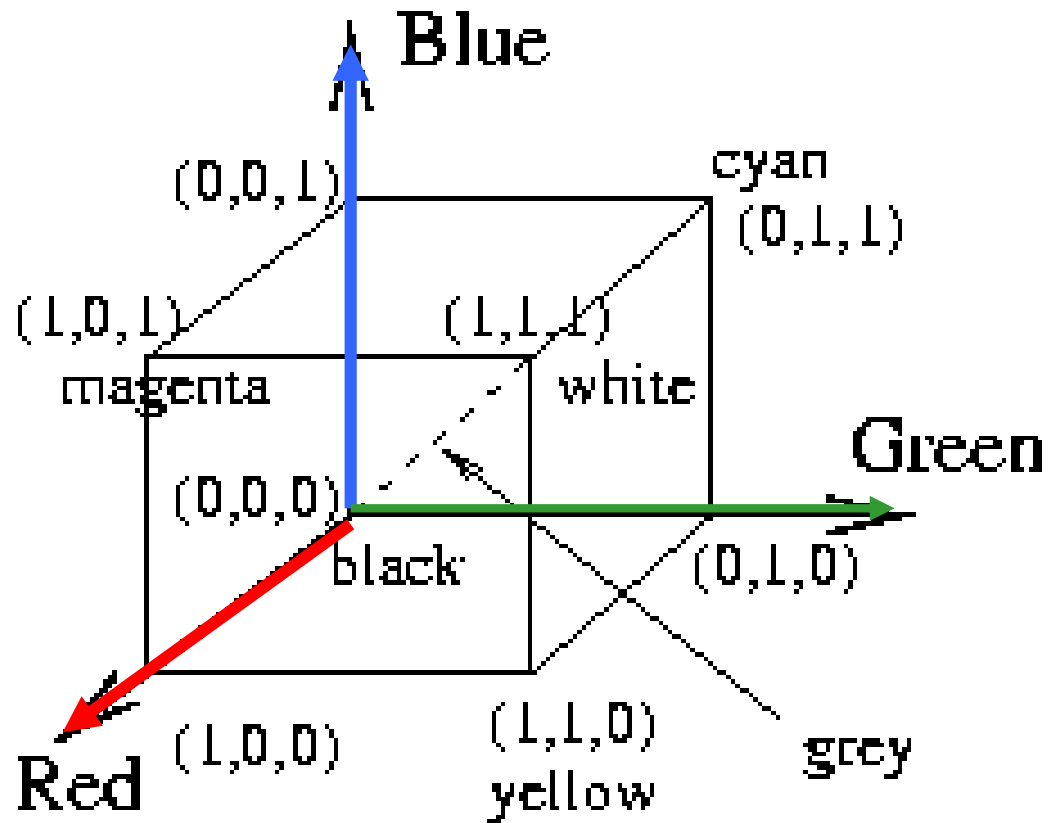
# RGB color cube



- R, G, B values normalized to (0, 1) interval
- human perceives gray for triples on the diagonal
- "Pure colors" on corners



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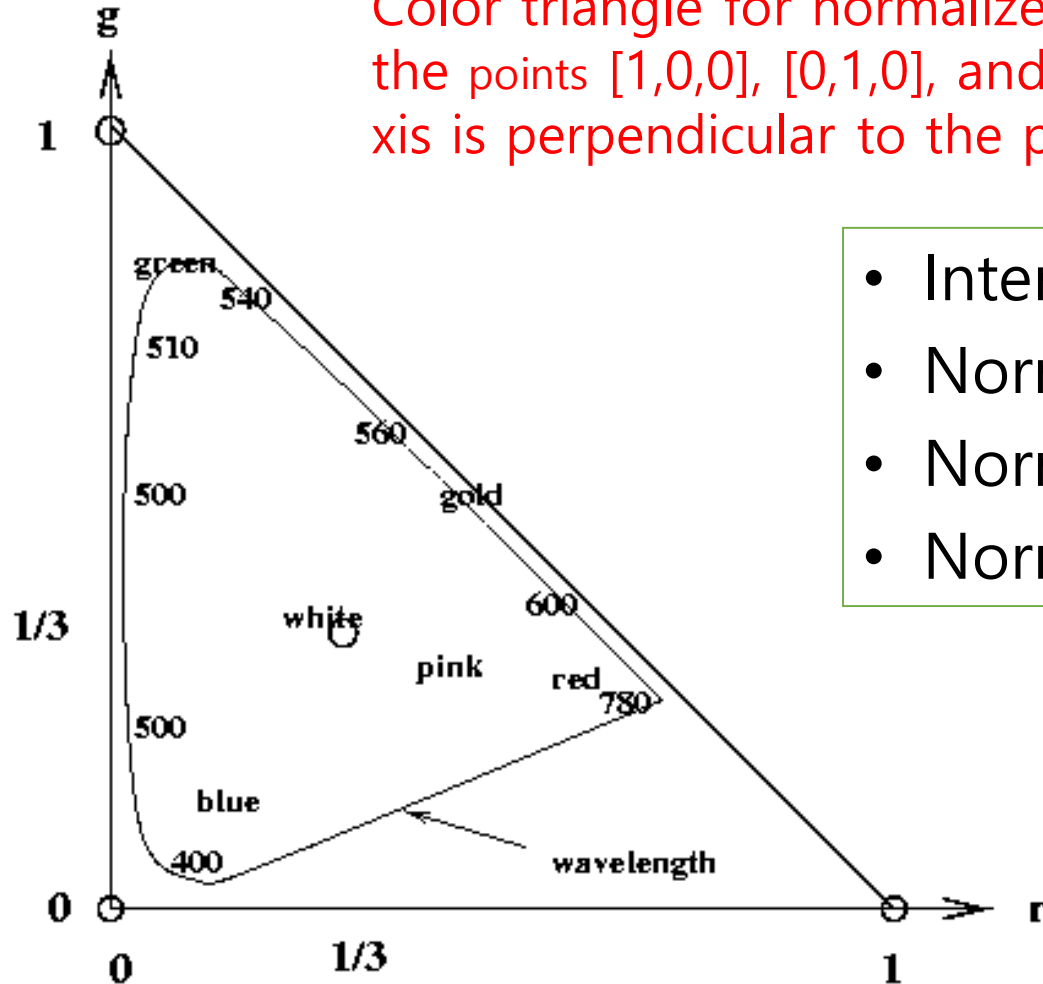


# Color palette and normalized RGB



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Color triangle for normalized RGB coordinates is a slice through the points  $[1,0,0]$ ,  $[0,1,0]$ , and  $[0,0,1]$  of the RGB cube. The blue axis is perpendicular to the page.



- Intensity  $I = (R+G+B) / 3$
- Normalized red  $r = R/(R+G+B)$
- Normalized green  $g = G/(R+G+B)$
- Normalized blue  $b = B/(R+G+B)$

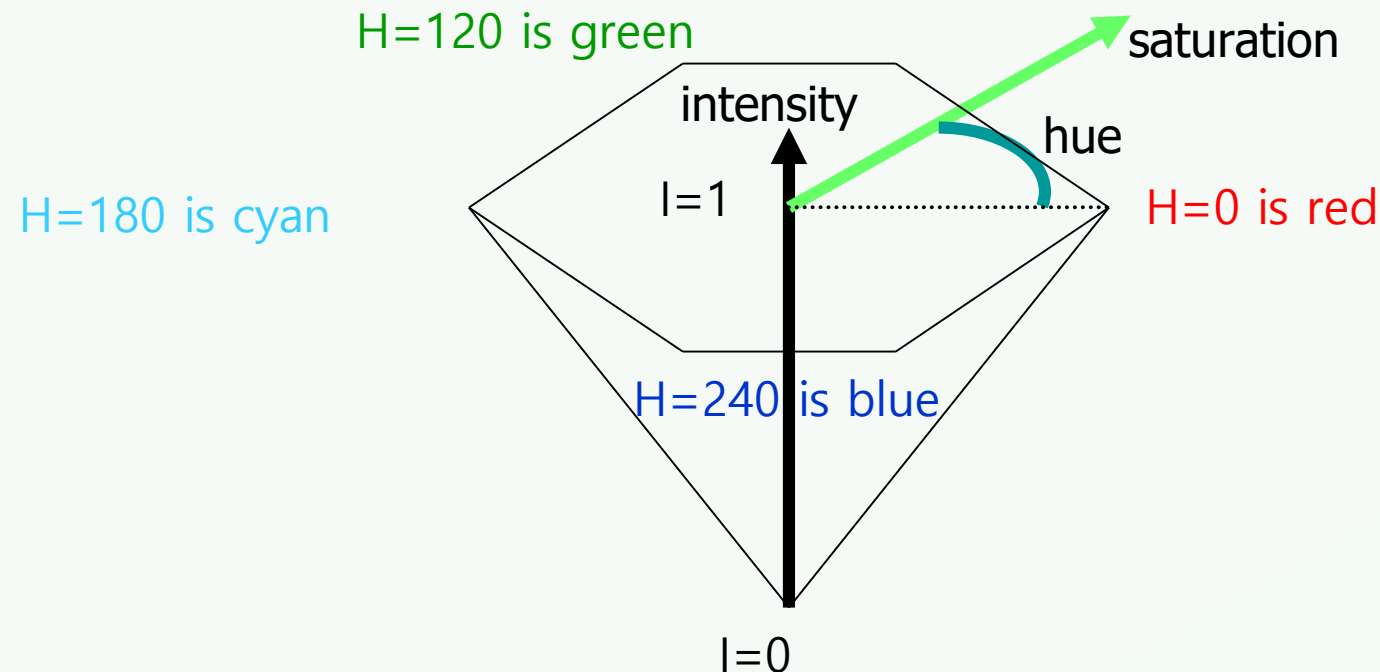
In this normalized representation,  $b = 1 - r - g$ , so we only need to look at  $r$  and  $g$  to characterize the color.



# Color hexagon for HSI (HSV)



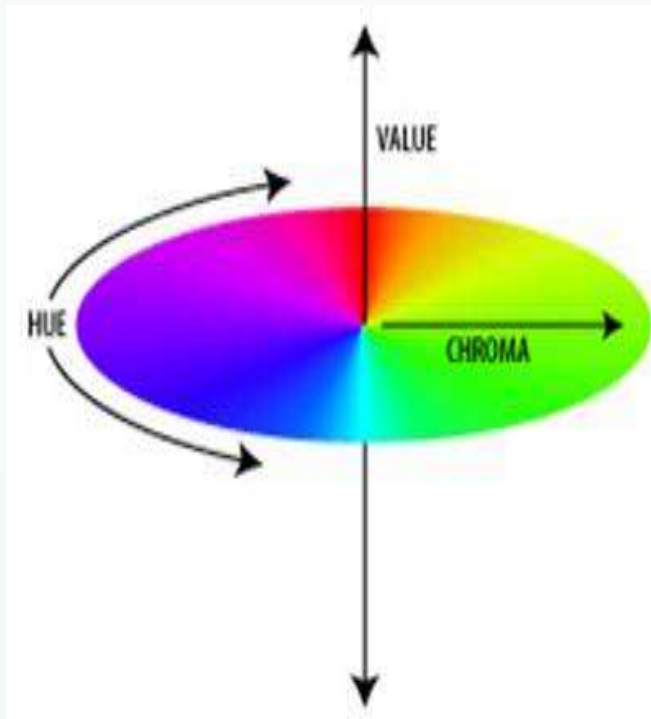
- Hue is encoded as an angle (0 to  $2\pi$ ).
- Saturation is the distance to the vertical axis (0 to 1).
- Intensity is the height along the vertical axis (0 to 1).



# RGB to HSI Transform



- RGB  $\rightarrow$  HSI



$$r = \frac{R}{R+G+B}, g = \frac{G}{R+G+B}, b = \frac{B}{R+G+B}$$

$$s = 1 - 3 \cdot \min(r, g, b); \quad s \in [0, 1]$$

$$i = (R + G + B) / (3 \cdot 255); \quad i \in [0, 1]$$

$$h = \cos^{-1} \left\{ \frac{0.5 \cdot [(r-g) + (r-b)]}{[(r-g)^2 + (r-b)(g-b)]^{1/2}} \right\}$$

$$h \in [0, \pi] \text{ for } b \leq g$$

$$h = 2\pi - \cos^{-1} \left\{ \frac{0.5 \cdot [(r-g) + (r-b)]}{[(r-g)^2 + (r-b)(g-b)]^{1/2}} \right\}$$

$$h \in [\pi, 2\pi] \text{ for } b > g$$







## □ HSI $\rightarrow$ RGB

### ■ RG area ( $0 \leq H \leq 120$ )

$$b = \frac{1}{3} (1 - S)$$

$$r = \frac{1}{3} \left[ 1 + \frac{S \cos(H)}{\cos(60 - H)} \right]$$

$$g = 1 - (r + b)$$

### ■ GB area ( $120 \leq H \leq 240$ )

$$H = H - 120$$

$$g = \frac{1}{3} \left[ 1 + \frac{S \cos(H)}{\cos(60 - H)} \right]$$

$$r = \frac{1}{3} (1 - S)$$

$$b = 1 - (r + g)$$

## ■ Notes

- Saturation is not defined when intensity  $I = 0$ .
- Hue is not defined when  $S = 0$ .



# Editing saturation of colors



- (Left) Image of food originating from a digital camera;
- (center) saturation value of each pixel decreased 20%;
- (right) saturation value of each pixel increased 40%.



# YIQ and YUV for TV signals



- Have better compression properties
- Luminance Y encoded using more bits than chrominance values I and Q; humans more sensitive to Y than I,Q
- Luminance used by black/white TVs
- All 3 values used by color TVs
- YUV encoding used in some digital video and JPEG and MPEG compression



# Conversion from RGB to YIQ



An approximate linear transformation from RGB to YIQ:

$$\begin{array}{lll} \text{luminance } Y & = & 0.30R + 0.59G + 0.11B \\ R - \text{cyan } I & = & 0.60R - 0.28G - 0.32B \\ \text{magenta} - \text{green } Q & = & 0.21R - 0.52G + 0.31B \end{array}$$

We often use this for color to gray-tone conversion.



# Histogram



- Color histogram can represent an image
- Histogram is fast and easy to compute.
- Size can easily be normalized so that different image histograms can be compared.
- Can match color histograms for database query or classification.

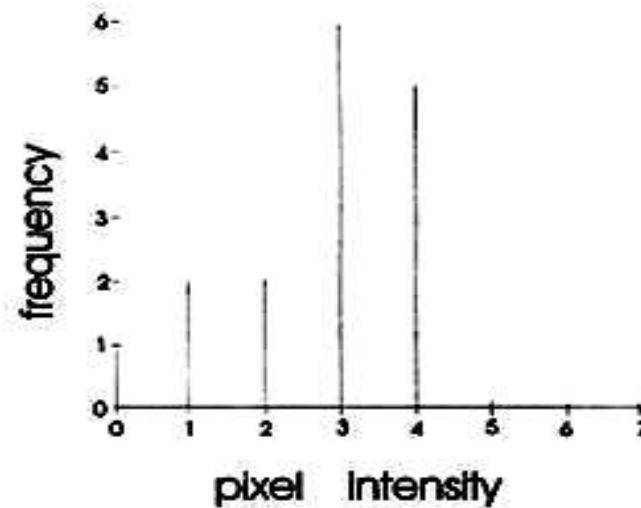


# Histogram



4	4	3	3
4	4	3	3
4	1	2	3
0	1	2	3

image

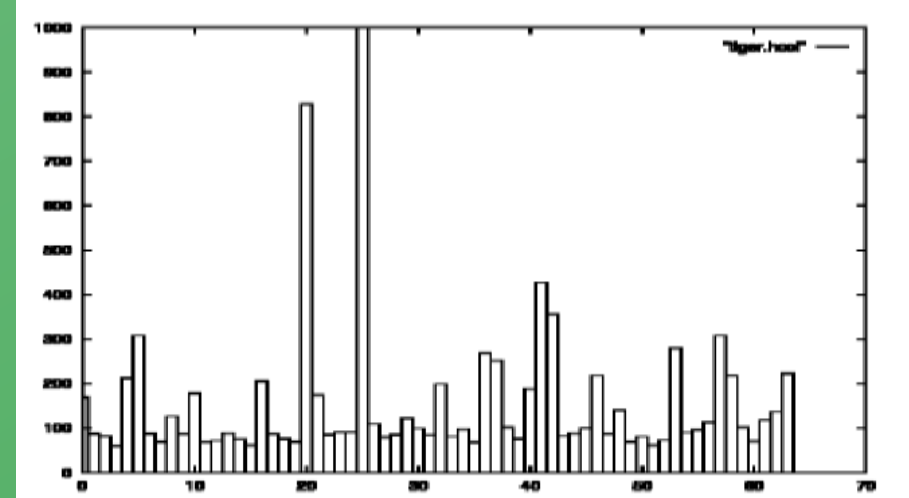
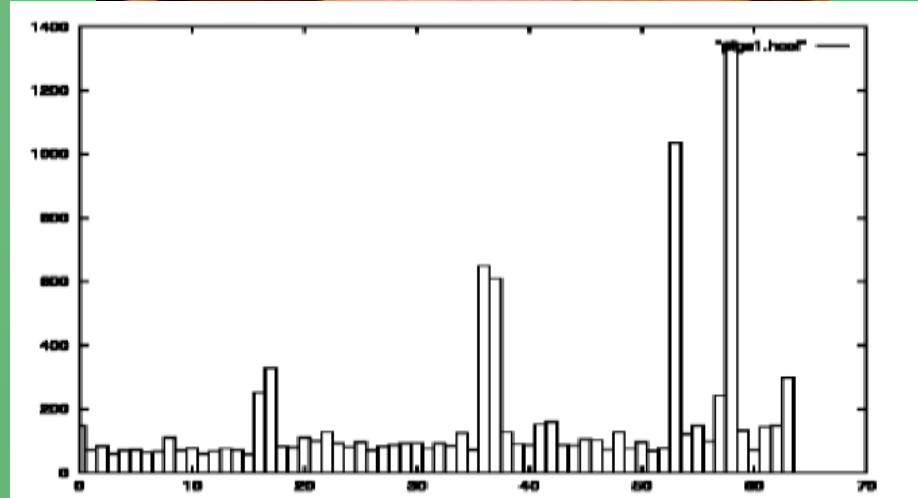
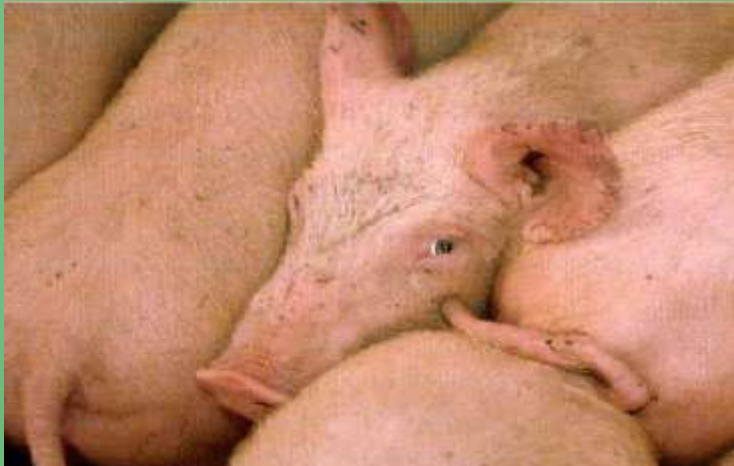


**Sample image with histogram**

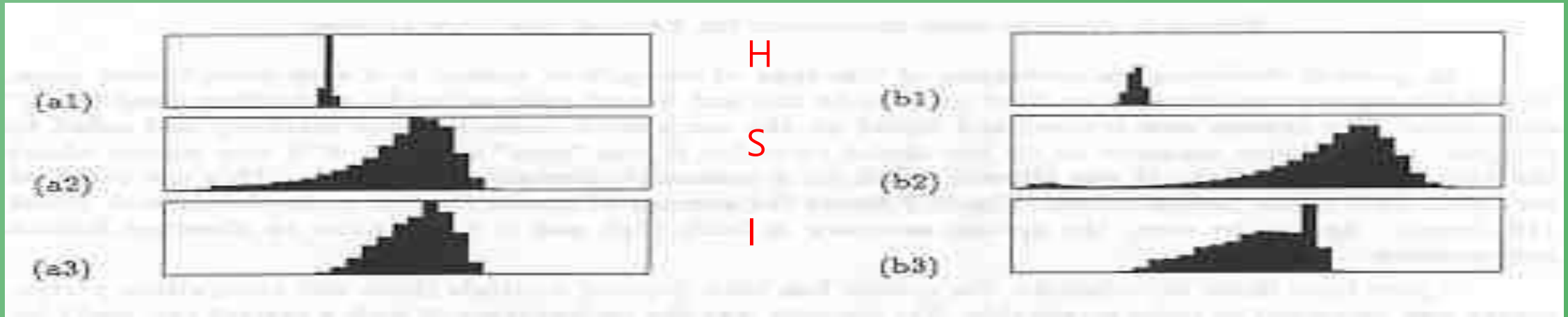




# Histograms of two color images



# Apples versus Oranges



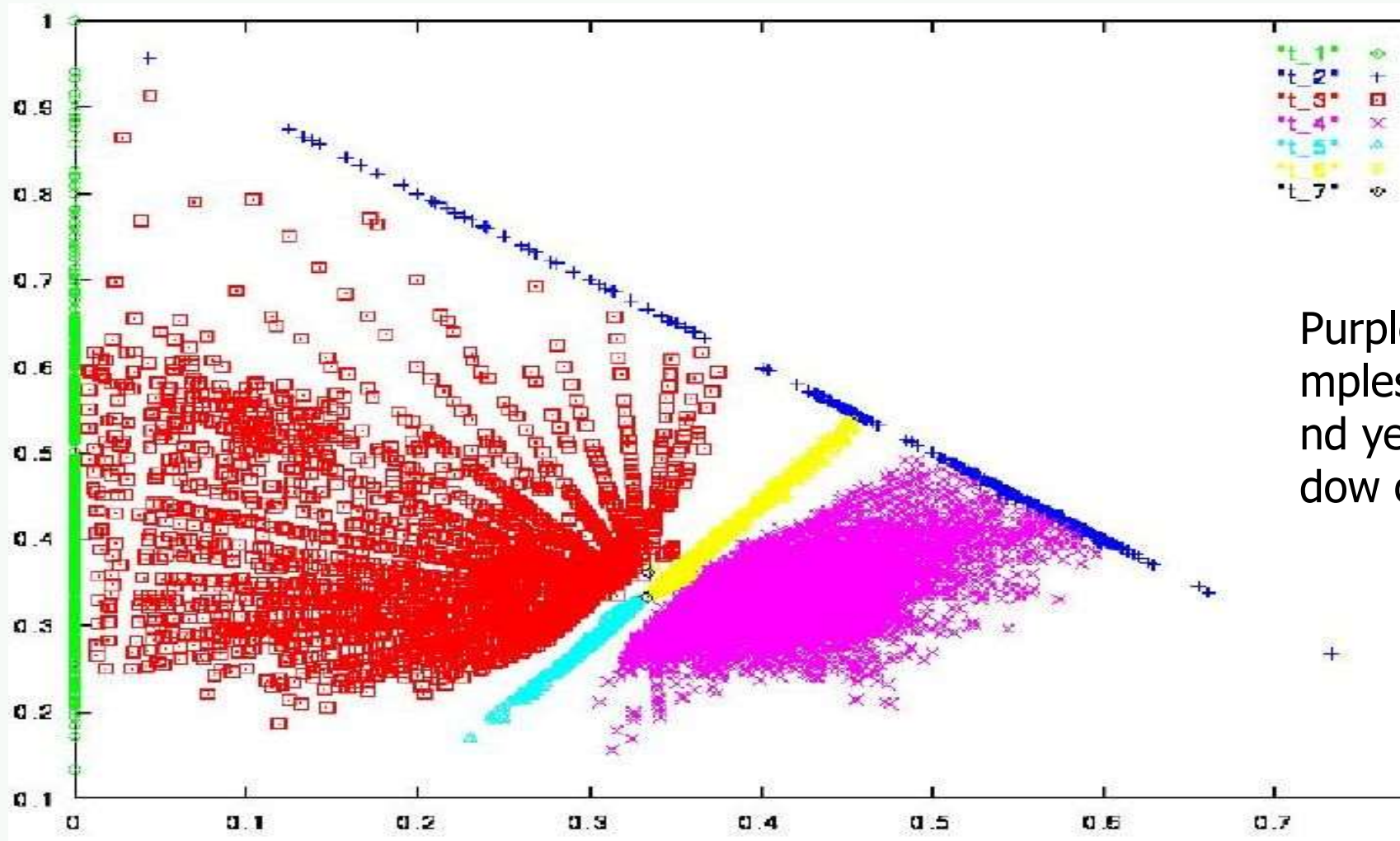
Separate HSI histograms for apples (left) and oranges (right) used by IBM's VeggieVision for recognizing produce at the grocery store checkout station.





# Skin color in RGB space

(shown as normalized red vs normalized green)



Purple region shows skin color samples from several people. Blue and yellow regions show skin in shadow or behind a beard.

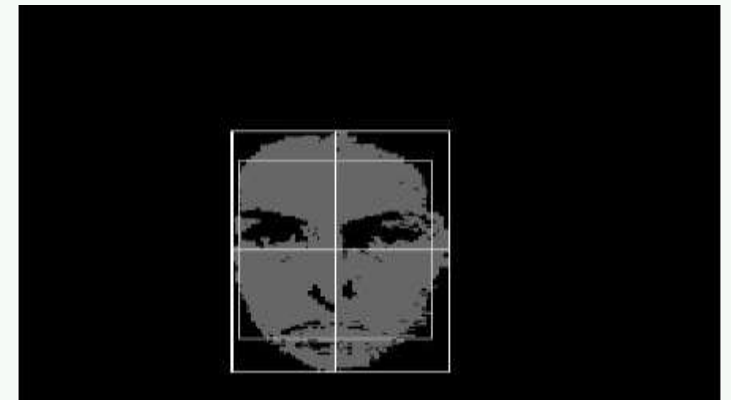


# Finding a face in video frame



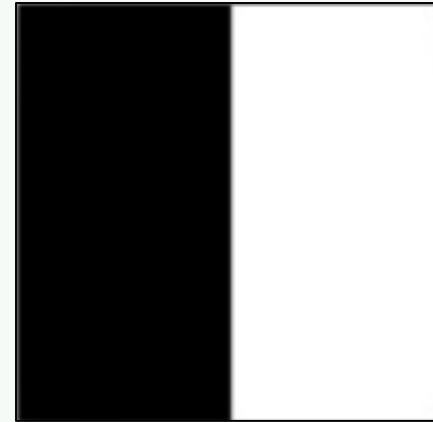
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- (left) input video frame
- (center) pixels classified according to RGB space
- (right) largest connected component with aspect similar to a face (all work contributed by Vera Bakic)





- Abrupt changes in the intensity of pixels
- Discontinuity in image brightness or contrast
- Usually edges occur on the boundary of two regions



# Edges



Tulips Image

Part of the image

Edge of the part of the image

255	255	255	255	255	255	255	255	255	255	250	198	126
255	255	255	255	255	255	255	255	220	152	92	26	0
255	255	255	254	255	255	251	152	49	16	9	9	8
255	254	255	255	255	215	117	38	19	28	33	31	37
254	254	255	255	217	74	19	25	34	33	30	35	46
254	255	255	206	94	25	33	33	34	32	31	37	48
255	237	145	57	24	30	33	28	31	31	39	47	49
255	162	33	28	38	37	36	35	35	37	48	60	59
179	66	33	40	40	43	44	49	51	56	62	67	67
39	23	34	42	45	45	50	55	65	71	72	73	73
28	38	38	41	46	51	61	62	66	71	73	73	76

Matrix generated by the part of the image



# Edge Detection

- Process of identifying edges in an image to be used as a fundamental asset in image analysis
- Locating areas with strong intensity contrasts
- A kind of filtering that leads to useful features





# Edge Detection Usage



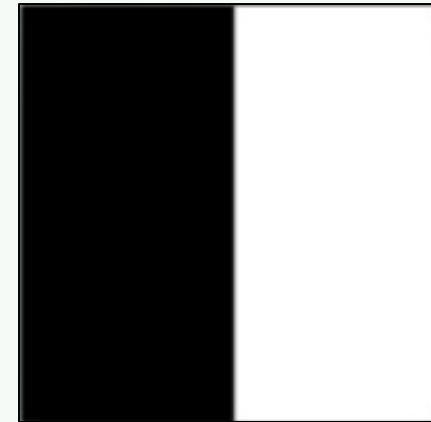
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- Reduce unnecessary information in the image while preserving the structure of the image
- Extract important features of an image
  - Textures and shapes
  - Corners, Lines and Curves
- Recognize objects, boundaries, segmentation
- Part of computer vision and recognition





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# Differential Operators

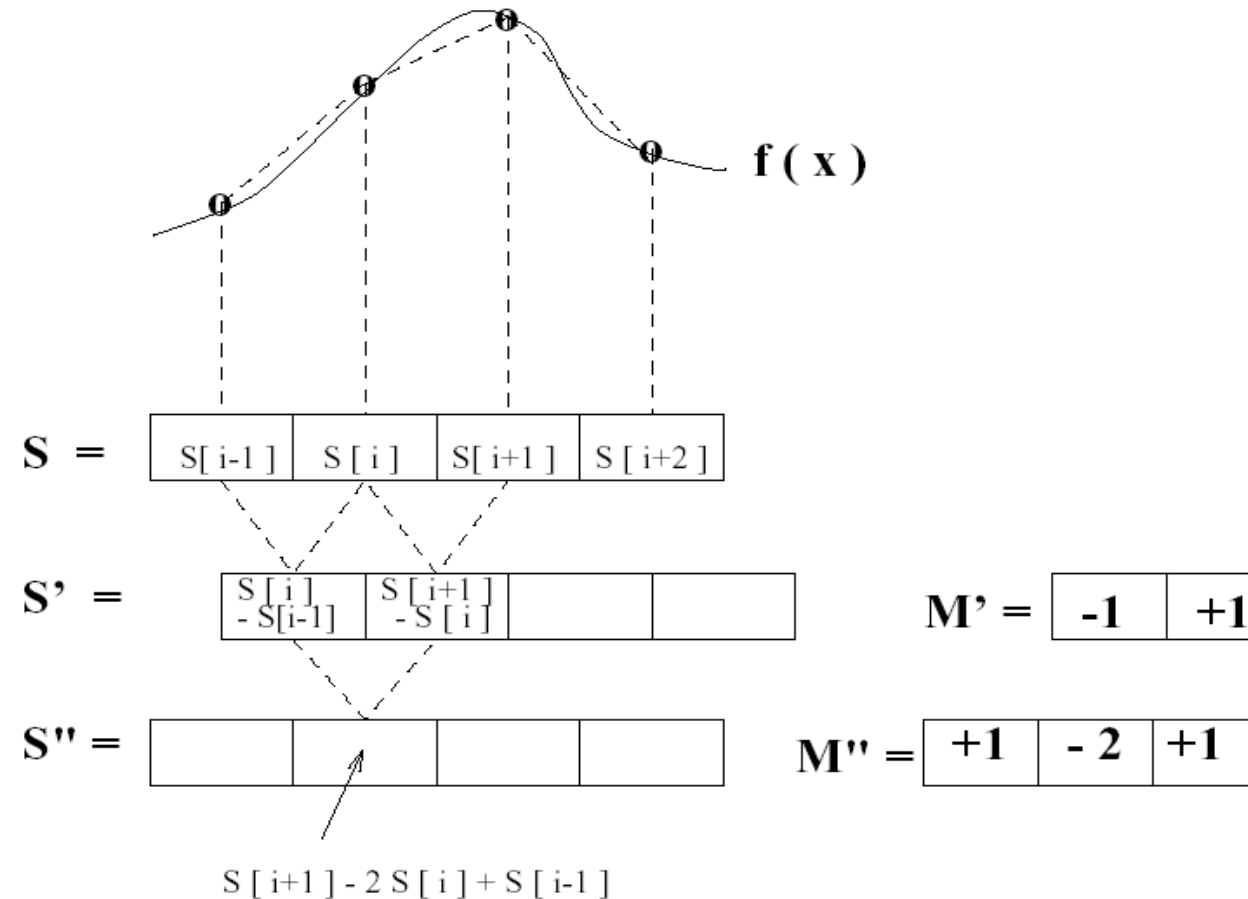


- Attempt to approximate the gradient at a pixel via masks
- Threshold the gradient to select the edge pixels





# Differencing 1D Signals



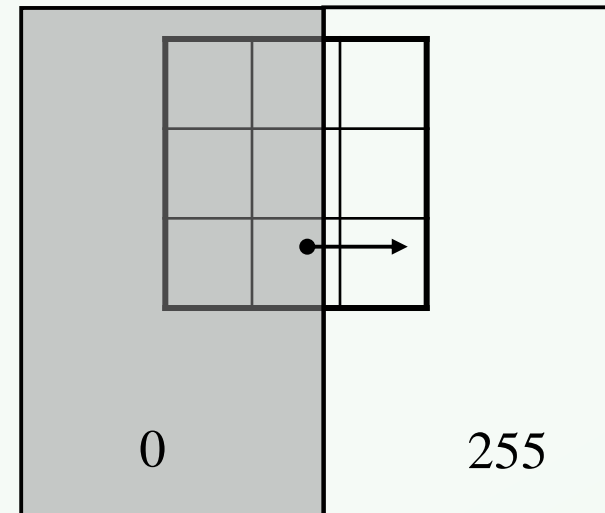


- Two dimensional equivalent of the first order derivative

$$G[f(x, y)] = \begin{bmatrix} G_x \\ G_y \end{bmatrix} = \begin{bmatrix} \frac{\partial f}{\partial x} \\ \frac{\partial f}{\partial y} \end{bmatrix}$$

points in the direction of max rate  
of increase of the function  $f(x, y)$

$$\left\{ \begin{array}{ll} \text{magnitude} & G[f(x, y)] = \sqrt{G_x^2 + G_y^2} \\ \text{direction} & \alpha(x, y) = \tan^{-1}\left(\frac{G_y}{G_x}\right) \end{array} \right.$$





- For digital images, the derivatives are approximated by differences.

$$G_x \cong f[i, j+1] - f[i, j]$$

$$G_y \cong f[i, j] - f[i+1, j]$$

Differencing masks using first derivatives

$$G_x = \begin{bmatrix} -1 & 1 \end{bmatrix} \quad G_y = \begin{bmatrix} 1 \\ -1 \end{bmatrix}$$

Differencing masks using second derivatives

$$G_x = \begin{bmatrix} 1 & -2 & 1 \end{bmatrix} \quad G_y = \begin{bmatrix} 1 \\ -2 \\ 1 \end{bmatrix}$$



# Common Masks for Computing Gradient

- Sobel :

$$\begin{bmatrix} -1 & 0 & 1 \\ -2 & 0 & 2 \\ -1 & 0 & 1 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 2 & 1 \\ 0 & 0 & 0 \\ -1 & -2 & -1 \end{bmatrix}$$

- Prewitt:

$$\begin{bmatrix} -1 & 0 & 1 \\ -1 & 0 & 1 \\ -1 & 0 & 1 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 1 & 1 \\ 0 & 0 & 0 \\ -1 & -1 & -1 \end{bmatrix}$$

- Roberts:

$$\begin{bmatrix} 0 & 1 \\ -1 & 0 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 0 \\ 0 & -1 \end{bmatrix}$$

**Sx**

**Sy**



# Common Masks for Computing Gradient

On a pixel of the image  $I$

- let  $G_x$  be the response to  $S_x$
- let  $G_y$  be the response to  $S_y$

Then the gradient is  
 $\nabla I = [G_x \ G_y]^T$

And  $g = (G_x^2 + G_y^2)^{1/2}$  is the gradient magnitude.

$\theta = \text{atan2}(G_y, G_x)$  is the gradient direction.



# Roberts Operator



- Gradient computed across diagonals
- Faster because of 2×2 neighborhood

$$G[f(i, j)] = |f(i, j) - f(i+1, j+1)| + |f(i+1, j) - f(i, j+1)| = |G_x| + |G_y|$$

Convolution masks

$$G_x = \begin{array}{|c|c|} \hline 1 & 0 \\ \hline 0 & -1 \\ \hline \end{array}$$

$$G_y = \begin{array}{|c|c|} \hline 0 & -1 \\ \hline 1 & 0 \\ \hline \end{array}$$



# Prewitt Operator



## Convolution masks

$$S_x = \begin{bmatrix} -1 & 0 & 1 \\ -1 & 0 & 1 \\ -1 & 0 & 1 \end{bmatrix}$$

$$S_y = \begin{bmatrix} 1 & 1 & 1 \\ 0 & 0 & 0 \\ -1 & -1 & -1 \end{bmatrix}$$

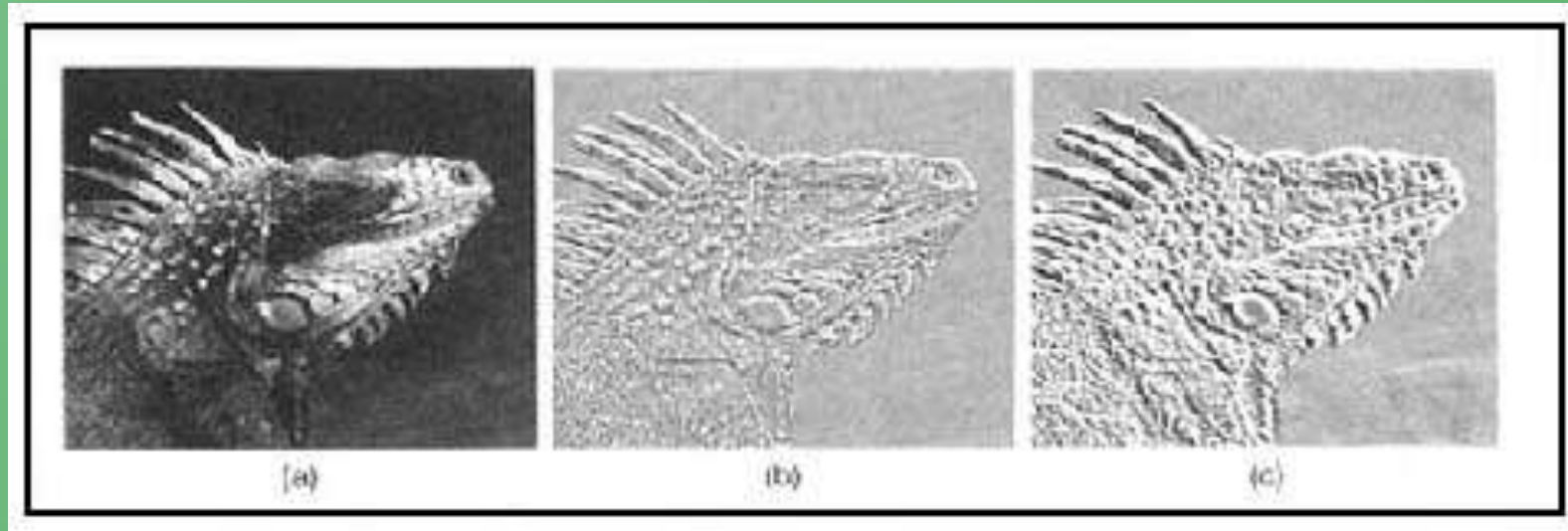
Magnitude of the gradient,  $M = \sqrt{G_x^2 + G_y^2}$

If  $M \geq threshold$ , the current pixel is marked as an edge pixel.

Direction  $\theta \approx \tan^{-1}\left(\frac{\partial f}{\partial y} / \frac{\partial f}{\partial x}\right)$



# Example



a) Input image

b) Robert

c) Prewitt





# Sobel Operator



## Convolution masks

$$S_x = \begin{array}{|c|c|c|} \hline -1 & 0 & 1 \\ \hline -2 & 0 & 2 \\ \hline -1 & 0 & 1 \\ \hline \end{array}$$

$$S_y = \begin{array}{|c|c|c|} \hline 1 & 2 & 1 \\ \hline 0 & 0 & 0 \\ \hline -1 & -2 & -1 \\ \hline \end{array}$$

Magnitude of the gradient,  $M$

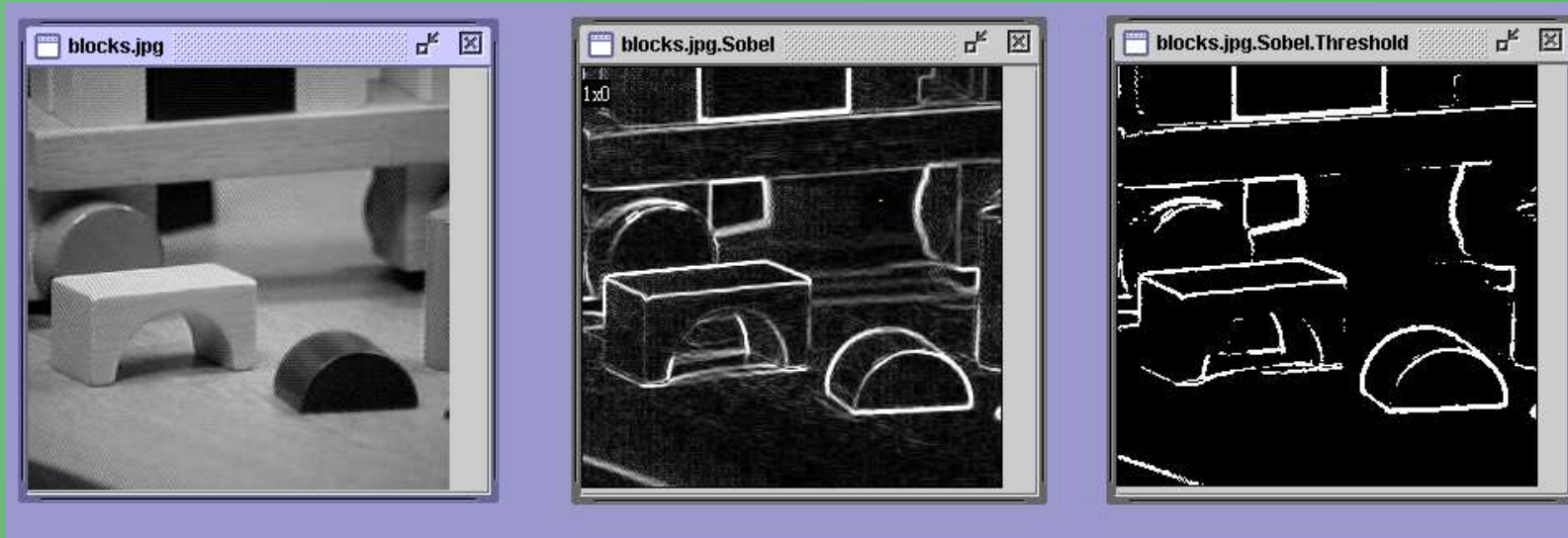
$$M = \sqrt{G_x^2 + G_y^2}$$

If  $M \geq threshold$ , the current pixel is marked as an edge pixel.

- places an emphasis on pixels closer to the center of the mask.
- most commonly used.



# Example



original image

gradient  
magnitude

thresholded  
gradient  
magnitude



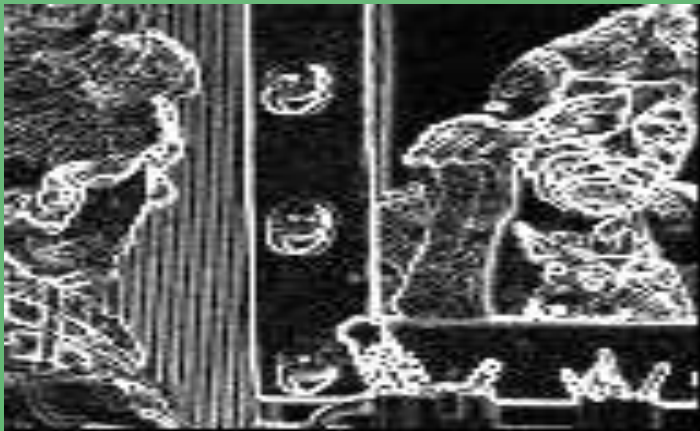
# Example



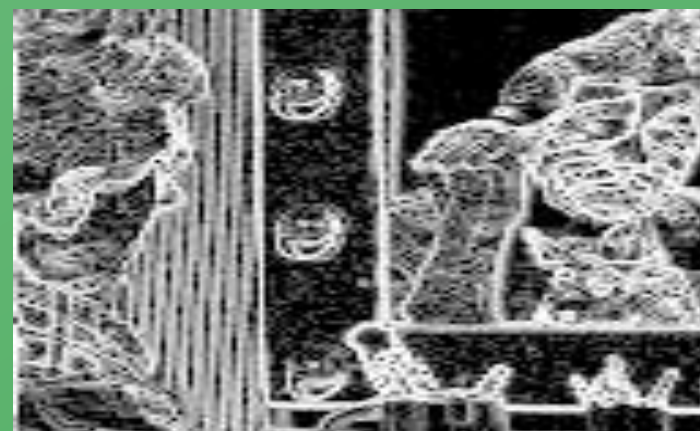
Input Image



Roberts Operator



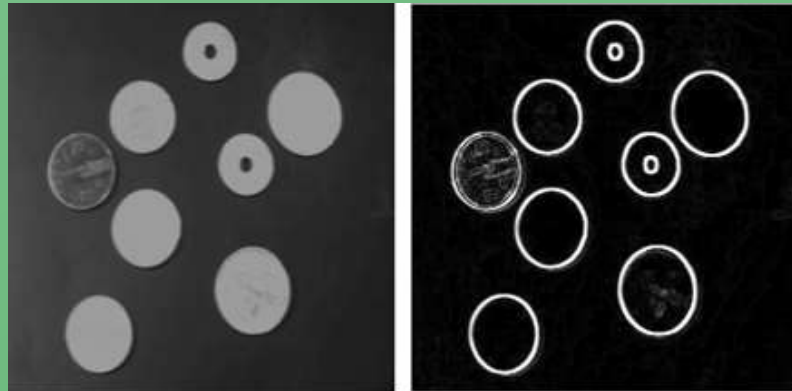
Sobel Operator



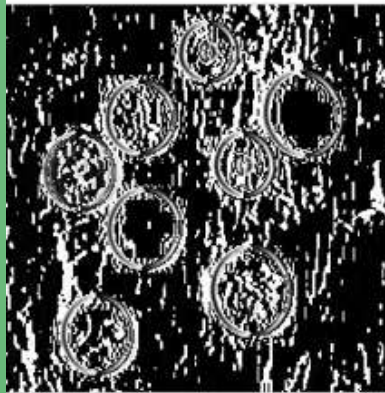
Prewitt Operator



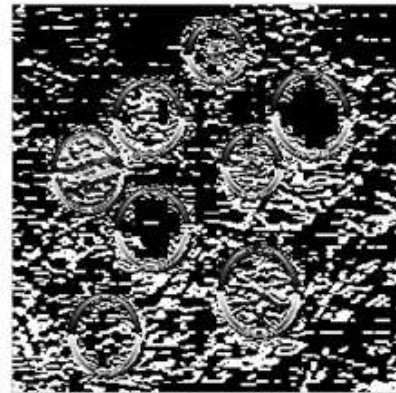
# Example



← Edge 검출 결과



↑ X축 Edge  
mask 적용한  
검출 결과

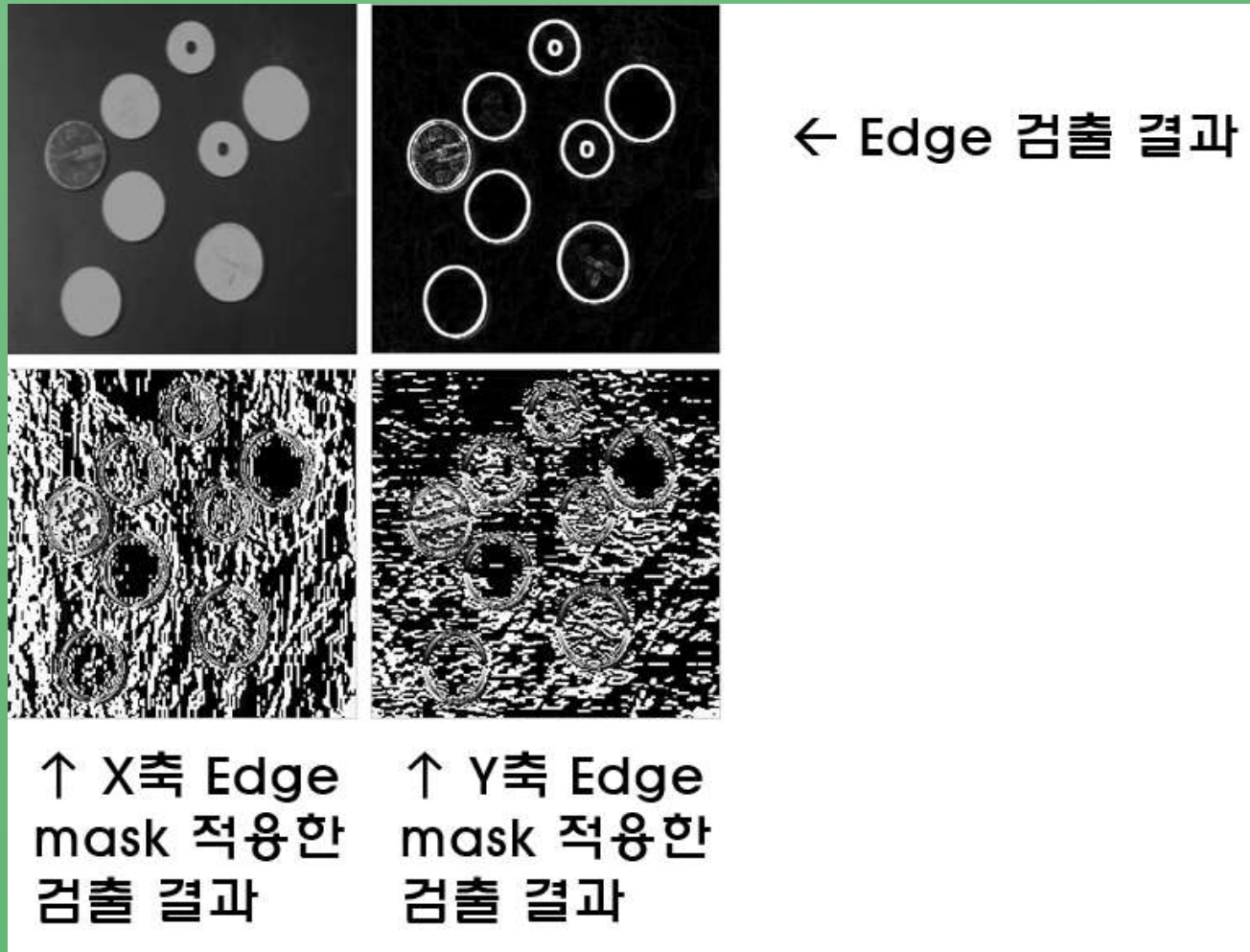


↑ Y축 Edge  
mask 적용한  
검출 결과

Prewitt operator + Edge thresholding



# Example



Sobel operator + Edge thresholding





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**Sx**

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