Worksheet 10 (Solutions)

1. (**Ratio Test**) Let $X_1, ..., X_n \stackrel{iid}{\sim} Poisson(\lambda)$. What is the test statistic G for the corresponding likelihood ratio test for the null hypothesis $H_0: \lambda = 1$.

Solution: TODO

2. (Ratio Test) Let $X_1, \ldots, X_n \stackrel{iid}{\sim} Poisson(\lambda)$. What is the test statistic G for the corresponding likelihood ratio test for the null hypothesis $H_0: \lambda = 1$.

Solution: TODO

3. (Regression I) Consider a completely different task, where we start with a set of fixed real values x_1, \ldots, x_n . We observe a random sample of independent observations Y_1, \ldots, Y_n , where $Y_i \sim N(b \cdot x_i, \sigma^2)$. So, the observations are independent but not identically distributed (they have different means). What is the log-likelihood of the sample?

Solution: TODO

4. (**Regression II**) Continuing from the previous question, what are $si\hat{gma}_{MLE}^2$ and \hat{a}_{MLE} for the regression problem?

Solution: TODO

5. (Regression III) Consider an hypothesis test with H_0 : a=0. Using the results we established the first few weeks (that is, without using the log-likelyhood test), find a pivot statistic to test this hypothesis.

Solution: TODO

6. (MLE) Let $X_1, \ldots, X_n \stackrel{iid}{\sim} Uniform(0, a)$. Find the MLE estimator for a. Note: You cannot do this using the derivative. Just think about it!

Solution: TODO

¹ In these questions, y_i will be play the role that we have previously been calling x_i . This is the unquestioned standard notation for regression, so I wanted to use it even though it requires a bit of translation work.