Sample size analysis with non informative prior

BZ

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Sample size calculation using non informative prior

The choice of non-informative prior for binomial distribution resulting in posterior distribution see http://www.stats.org.uk/priors/noninformative/YangBerger1998.pdf

- if we choose Beta(1,1), that is, the uniform distribution, then the posterior mean ADA+ rate would be (x + 1)/(n + 2) where x and n are the number of ADA+ incidence and the total number of subjects at cohort 1, respectively;
- if we choose Jefferys' prior, then the posterior mean ADA+ rate would be (x + 0.5)/(n + 1).

In the following section, we'll base sample size re-estimation on these two non-informative priors. Note that the initial sample size 102 (with 46 in the first cohort) is calculated based on the assumption that ADA+rate is 1%.

The following is variable specifications for tables below:

- n ADA: number of ADA observed in cohort 1
- n_cohort1: number of subjects enrolled in cohort 1
- obs ADA rate: n ADA/n cohort1
- posterior_ADA_rate: obtained using Bayes prior and data from cohort 1
- N_required_per_arm: sample size re-estimated using posterior_ADA_rate. This number has already accounted for 10% drop out.
- N_increased_per_arm: number of subjects needed per arm (N_required_per_arm 51, and 51 is sample size per arm originally).

Please note that these sample sizes may change due to the type 1 error analysis, addressing comment 3 from FDA.

when initial ADA rate is 1%

In this part, the initial sample size 102 (with 46 in the first cohort) is calculated based on the assumption that ADA+ rate is 1%.

Uniform prior

| n_ADA | n_cohort1 | obs_ADA_rate | posterior_ADA_rate | N_required_per_arm | N_increase_per_arm |
|-------|-----------|--------------|--------------------|--------------------|--------------------|
| 0 | 46 | 0.0000 | 0.0208 | 58 | 7 |
| 1 | 46 | 0.0217 | 0.0417 | 77 | 26 |
| 2 | 46 | 0.0435 | 0.0625 | 98 | 47 |
| 3 | 46 | 0.0652 | 0.0833 | 118 | 67 |
| 4 | 46 | 0.0870 | 0.1042 | 138 | 87 |
| 5 | 46 | 0.1087 | 0.1250 | 158 | 107 |
| 6 | 46 | 0.1304 | 0.1458 | 176 | 125 |
| 7 | 46 | 0.1522 | 0.1667 | 194 | 143 |

Jeffery's prior

| n_ADA | $n_cohort1$ | obs_ADA_rate | posterior_ADA_rate | $N_{required_per_arm}$ | N_increase_per_arm |
|-------|--------------|------------------|--------------------|--------------------------|--------------------|
| 0 | 46 | 0.0000 | 0.0106 | 47 | 0 |
| 1 | 46 | 0.0217 | 0.0319 | 69 | 18 |
| 2 | 46 | 0.0435 | 0.0532 | 88 | 37 |
| 3 | 46 | 0.0652 | 0.0745 | 109 | 58 |
| 4 | 46 | 0.0870 | 0.0957 | 130 | 79 |
| 5 | 46 | 0.1087 | 0.1170 | 150 | 99 |
| 6 | 46 | 0.1304 | 0.1383 | 170 | 119 |
| 7 | 46 | 0.1522 | 0.1596 | 189 | 138 |

Reproducing Table 1 using our package

| n_ADA | n_cohort1 | obs_ADA_rate | posterior_ADA_rate | N_required_per_arm | N_increase_per_arm |
|-------|-----------|--------------|--------------------|--------------------|--------------------|
| 0 | 46 | 0.0000 | 0.0068 | 41 | 0 |
| 1 | 46 | 0.0217 | 0.0136 | 50 | 0 |
| 2 | 46 | 0.0435 | 0.0204 | 57 | 6 |
| 3 | 46 | 0.0652 | 0.0272 | 63 | 12 |
| 4 | 46 | 0.0870 | 0.0340 | 70 | 19 |
| 5 | 46 | 0.1087 | 0.0408 | 77 | 26 |
| 6 | 46 | 0.1304 | 0.0476 | 84 | 33 |
| 7 | 46 | 0.1522 | 0.0544 | 91 | 40 |

when initial ADA rate is 3%

In this part, the initial sample size 132 (with 60 in the first cohort) is calculated based on the assumption that ADA+ rate is 3%.

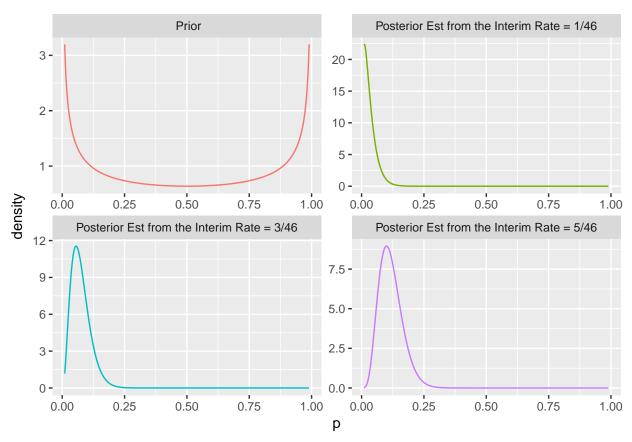
Uniform prior

| n_ADA | n_cohort1 | obs_ADA_rate | posterior_ADA_rate | N_required_per_arm | N_increase_per_arm |
|-------|-----------|--------------|--------------------|--------------------|--------------------|
| 0 | 60 | 0.0000 | 0.0161 | 52 | 0 |
| 1 | 60 | 0.0167 | 0.0323 | 69 | 3 |
| 2 | 60 | 0.0333 | 0.0484 | 84 | 18 |
| 3 | 60 | 0.0500 | 0.0645 | 101 | 35 |
| 4 | 60 | 0.0667 | 0.0806 | 116 | 50 |
| 5 | 60 | 0.0833 | 0.0968 | 131 | 65 |
| 6 | 60 | 0.1000 | 0.1129 | 147 | 81 |
| 7 | 60 | 0.1167 | 0.1290 | 161 | 95 |

Jeffery's prior

| n_ADA | $n_cohort1$ | obs_ADA_rate | posterior_ADA_rate | $N_{required_per_arm}$ | N_increase_per_arm |
|-------|--------------|------------------|--------------------|--------------------------|--------------------|
| 0 | 60 | 0.0000 | 0.0082 | 43 | 0 |
| 1 | 60 | 0.0167 | 0.0246 | 61 | 0 |
| 2 | 60 | 0.0333 | 0.0410 | 77 | 11 |
| 3 | 60 | 0.0500 | 0.0574 | 93 | 27 |
| 4 | 60 | 0.0667 | 0.0738 | 109 | 43 |
| 5 | 60 | 0.0833 | 0.0902 | 125 | 59 |
| 6 | 60 | 0.1000 | 0.1066 | 140 | 74 |
| 7 | 60 | 0.1167 | 0.1230 | 156 | 90 |

Posterior distribution based on Jeffreys prior and 1% initial ADA rate



The top left is the Jeffreys prior. The top right shows the posterior distribution Beta(1.5, 45.5); The lower left Beta(3.5, 43.5) and the lower right Beta(5.5, 41.5).