UMass Boston Computer Science

CS450 High Level Languages (section 2)

Defining New Variables in CS450js lang

Monday, November 20, 2023



Logistics

- HW 7 out
 - <u>due</u>: Sun 11/19 11:59 pm EST
 - Really due: Wed 11/22 11:59 pm EST
 - 2 submissions



• (no hw over Thanksgiving)



Key Points

- Think about data organization
 - As World gets more components, need subgroupings of data
 - Be careful with: extraneous data, e.g., does player need x data?

```
A WorldState is a
  A WorldState is a:
                                                 (world b p1 p2 sc1 sc2)
  (world x y vx vy p1 p2 sc1 sc2)
                                      VS
                                                 b : Ball
      : XCoordinate
                                                     : YCoordinate
  y : YCoordinate
                                                     : YCoordinate
  vx : Velocity
                         ;; A WorldState is a ;; sc1 : NatNum in [0,10]
      : Velocity
                                              ;; sc2 : NatNum in [0,10]
;; p1 : YCoordinate
                         ;; (world b p1 p2)
  p2 : YCoordinate
                            b : Ball
  sc1 : NaturalNum in [0]
                            p1 : Player
;; sc2 : NaturalNum in [0];; p2 : Player
```

Key Points

- Think about data organization
- Data organization affects code organization (and readability)

p2 : Player

Key Points

Think about data organization

```
Think about fn names! "ball-in-scene/x?" no longer makes sense!!!
```

<u>Data</u> organization affects <u>code</u> organization (and <u>readability</u>)

p2 : Player

```
242 ;; next-world : WorldState -> WorldState
       next-world
                                                                                     243 ;; Computes the next world state from the given one
120
                                                                                         (define/contract (next-world w)
121
                                                                                            (-> world? world?)
122
                                                                                            (match-define (world x y xvel yvel left-paddle-y right-paddle-y left-score right-score winner) w)
123
            (if (> mouse-y (- SCENE-HEIGHT PADDLE-HEIGHT))
                                                                                     247
                                                                                            (define (reset? x y)
                (- SCENE-HEIGHT PADDLE-HEIGHT)
124
                                                                                     248
                                                                                            (or (or (< x (+ LEFT-EDGE BALL-RADIUS))
125
                                                                                     249
126
                                                                                     250
127
      (define ball-x-next (+ (world-x w) (world-xvel w)))
                                                                                     251
      (define ball-y-next (+ (world-y w) (world-yvel w)))
128
                                                                                     252
                                                                                            (define new-left-score left-score)
129
                                                                                            (define new-right-score right-score)
130
      ;; Check for collision with the paddles
                                                                                            (define new-winner winner)
      (define paddle1-collision?
                                                                                     255
        (and (<= (world-x w) (+ PADDLE-PLAYER1-INIT-X PADDLE-WIDTH))
                                                                                     256
             (<= (world-y w) (+ (world-player1-y w) PADDLE-HEIGHT))
                                                                                     257
                                                                                            (define (left-paddle-collision? x y)
134
             (>= (world-y w) (world-player1-y w))))
                                                                                     258
135
      (define paddle2-collision?
136
                                                                                     260
137
        (and (>= (world-x w) (- PADDLE-PLAYER2-INIT-X BALL-SIZE))
                                                                                     261
            (<= (world-y w) (+ (world-player2-y w) PADDLE-HEIGHT))
138
                                                                                     262
                                                                                            (define (right-paddle-collision? x y)
139
            (>= (world-y w) (world-player2-y w))))
                                                                                     263
140
      ;; If a collision with a paddle occurs, reverse the ball's horizontal velocity
141
142
      (define ball-x-vel-bounce
        (if (or paddle1-collision? paddle2-collision?)
143
                                                                                   267
                                                                                            (define new-xvel
144
            (- (world-xvel w))
                                                                                     268
145
            (world-xvel w)))
                                                                                     269
146
                                                                                     270
      (define ball-y-vel-next
148
        (if (or (<= (sub1 ball-y-next) 0) (>= (add1 ball-y-next) SCENE-HEIGHT))
149
150
            (world-yvel w)))
                                                                                     274
151
                                                                                     275
                                                                                            (define new-yvel
152
      ;; Check for scoring
                                                                                     276
      (define player1-scores? (>= (world-x w) SCENE-WIDTH))
                                                                                     277
      (define player2-scores? (<= (world-x w) 0))</pre>
154
                                                                                     278
155
                                                                                     279
156
      (define player1-score
                                                                                     280
157
        (if player1-scores? (+ 1 (world-player1-score w)) (world-player1-score w)))
                                                                                     281
158
                                                                                     282
159
                                                                                     283
160
        (if player2-scores? (+ 1 (world-player2-score w)) (world-player2-score w)))
161
162
        (if (or player1-scores? player2-scores?)
                                                     Which is more
164
            (/ SCENE-WIDTH 2)
165
            (+ (world-x w) ball-x-vel-bounce)))
166
                                                      readable
167
        (if (or player1-scores? player2-scores?)
168
            (random (- SCENE-HEIGHT BALL-SIZE))
169
                                                     (by humans)?
170
            (+ (world-y w) ball-y-vel-next)))
171
172
      (define new-xvel
        (if (or player1-scores? player2-scores?)
173
174
            (if player1-scores? BALL-SPEED (- BALL-SPEED))
                                                                                     298
175
            ball-x-vel-bounce))
                                                                                     299
176
                                                                                     300
177
       (define new-yvel
                                                                                     301
178
        (if (or player1-scores? player2-scores?)
                                                                                     302
179
            (random BALL-SPEED)
                                                                                     303
            ball-y-vel-next))
180
                                                                                     304
181
182
       (make-world
                                                                                     306
183
                            60 lines
       new-x
184
       new-v
185
       new-xvel
186
       new-vvel
187
       (world-player1-y
       player2-v-next
       player1-score
        player2-score))
```

[(reset? x y) (random-velocity)] [(ball-in-scene/y? (make-y-coordinate y)) yvel] [else (- yvel)])) (define new-x (if (reset? x y) (begin (cond [(x (+ LEFT-EDGE BALL-RADIUS)) new-right-score (+ 1 right-score)) new-right-score 10) (set! new-winner "Right") (display "Player Right wins!\n")) et! new-winner "")) HT-EDGE 2)] RIGHT-EDGE BALL-RADIUS))

(cond

(cond

(> x (- RIGHT-EDGE BALL-RADIUS)))

(and (<= x (+ LEFT-PADDLE-X BALL-RADIUS))

(and (>= x (- RIGHT-PADDLE-X BALL-RADIUS))

[(reset? x y) (random-velocity)]

[(left-paddle-collision? x y) (abs xvel)]

[(right-paddle-collision? x y) (- (abs xvel))]

(>= y (- left-paddle-y (/ PADDLE-HEIGHT 2)))

(<= y (+ left-paddle-y (/ PADDLE-HEIGHT 2)))))

(>= y (- right-paddle-y (/ PADDLE-HEIGHT 2)))

(<= y (+ right-paddle-y (/ PADDLE-HEIGHT 2)))))

[else (if (ball-in-scene/x? (make-x-coordinate x)) xvel (- xvel))]))

new-left-score (+ 1 left-score))

(display "Player Left wins!\n")

new-left-score 10)

(set! new-winner "Left")

(set! new-winner ""))

(/ RIGHT-EDGE 2)]

(/ RIGHT-EDGE 2)]))

ſelse

(if (reset? x y)

(+ x new-xvel)))

(/ BOTTOM-EDGE 2)

(+ y new-yvel)))

(and (= x 0) (= y 0)))

Don't submit this kind of code in this class (or in software engineering)

```
3<sup>246</sup>247
                                                       70 lines
                                                                                                                   -249
                                                                                                                    250
  ; Check if the game is over and display the winning message
  (if (or (= new-left-score 10) (= new-right-score 10))
     (make-world new-x new-v new-xvel new-vvel left-paddle-v right-paddle-v new-left-score new-right-score new-winner)
; If the game is not over, continue updating the world
     (make-world new-x new-y new-xvel new-yvel left-paddle-y right-paddle-y new-left-score new-right-score winner)))
```

```
(match-define (world x y xvel yvel left-paddle-y right-paddle-y left-score right-score winner) w)
         (define (reset? x)
           (or (< x (+ LEFT-EDGE BALL-RADIUS))
              (> x (- RIGHT-EDGE BALL-RADIUS))
              (= x 0))
         (define new-left-score left-score)
         (define new-right-score right-score)
         (define (left-paddle-collision? x y)
          (and (<= x (+ LEFT-PADDLE-X BALL-RADIUS))
               (>= y (- left-paddle-y (/ PADDLE-HEIGHT 2)))
               (<= y (+ left-paddle-y (/ PADDLE-HEIGHT 2)))))
         (define (right-paddle-collision? x y)
          (and (>= x (- RIGHT-PADDLE-X BALL-RADIUS))
               (>= y (- right-paddle-y (/ PADDLE-HEIGHT 2)))
               (<= y (+ right-paddle-y (/ PADDLE-HEIGHT 2)))))
        (define new-xvel
          (cond
            [(reset? x) (random-velocity)]
             [(left-paddle-collision? x y) (abs xvel)]
             [(right-paddle-collision? x y) (- (abs xvel))]
             [else (if (ball-in-scene/x? (make-x-coordinate x)) xvel (- xvel))]))
         (define new-yvel
          (cond
             [(reset? x) (random-velocity)]
             [(ball-in-scene/y? (make-y-coordinate y)) yvel]
             [else (- yvel)]))
         (define new-x
          (if (reset? x)
                  [(< x (+ LEFT-EDGE BALL-RADIUS))
                   (set! new-right-score (+ 1 right-score))
                   (if (= new-right-score 10)
                         (set! winner "Right")
                         (display "Player Right wins!\n"))
                       (set! winner ""))
                   (/ RIGHT-EDGE 2)]
                   [(> x (- RIGHT-EDGE BALL-RADIUS))
                   (set! new-left-score (+ 1 left-score))
                   (if (= new-left-score 10)
                       (begin
                         (set! winner "Left")
                         (display "Player Left wins!\n"))
                       (set! winner ""))
                    (/ RIGHT-EDGE 2)]
                   (/ RIGHT-EDGE 2)]))
              (+ x new-xvel)))
243
         (define new-v
          (if (reset? x)
              (+ y new-yvel)))
         ;; Shows us who won in console mode
          [(= new-left-score 10)
                                                                 80 lines
           (begin
             (set! winner "Left")
              (display "Player Left wins!\n"))]
          [(= new-right-score 10)
             (set! winner "Right")
              (display "Player Right wins!\n"))]
         (make-world new-x new-y new-xvel new-yvel left-paddle-y right-paddle-y new-left-score new-right-score winner))
```

182 ;; Computes the next world state from the given one

183 (define/contract (next-world w)

194

203 204

205

211

212

213

214

215

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217

218

-219

225

226

228 229

231

232

233

234

235

237

239

241

248

251

252

254

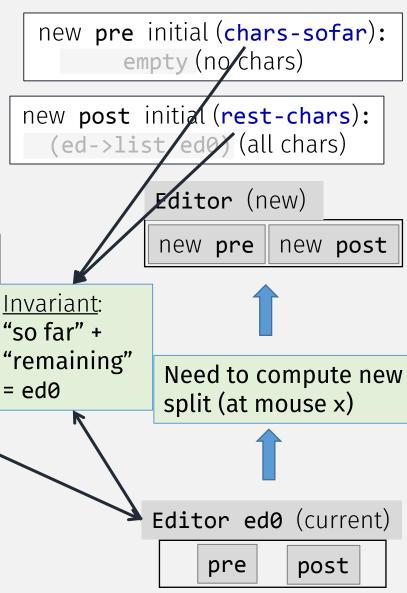
Key Points

- Think about data organization
- Data organization affects code organization (and readability)
- Break up large data defs into (logical) smaller, readable ones
- Break up large functions into (logical) smaller, readable ones



Key Points

```
;; mouse-handler : Editor Coord Coord MouseEvt -> Editor
(define (mouse-handler ed x y mevt)
  (cond
  [(mouse=/ mevt "button-down") (split ed x)]
  [else ed]))
```



new pre initial (chars-sofar):
empty (no chars)

Key Points

```
(define (split ed0 x) ;; split : Editor Coord -> Editor
  ;; split/a : List<1str> List<1str> Coord -> Editor
  ;; ACCUMULATOR: chars-so-far
  ;; invariant: represents (rev) of chars seen so far, where
     (append (rev chars-so-far) rest chars) = (ed->lst ed0)
           and: (image-width (render-chars chars-sofar)) < x</pre>
  (define (split/a chars-sofar rest-chars x)
    (cond [(empty? rest-chars) (editor chars-sofar rest-chars)]
                        (match-define (cons c rst) rest-chars)
           (if (chars-at-cursor? x (cons c chars-sofar))
               (editor (cons c chars-sofar) rst)
                sylit/a (cons c chars-sofar) rst x))])
  (split/a empt\sqrt{(ed->1st ed0)} x))
```

new pre initial (chars-sofar):
empty (no chars)

Key Points

new post initial (rest-chars):
 (ed->list ed0) (all chars)

```
(define (split ed0 x) ;; split : Editor Coord - → Editor
  ;; split/a : List<1str> List<1str> Coord -> Editor
  ;; ACCUMULATOR: chars-so-far
  ;; invariant: represents (rev) of chars seem so far, where
     (append (rev chars-so-far) rest-zhars) = (ed->lst ed0)
          and: (image-width (render-chars chars-sofar)) < x</pre>
  (define (split/a chars-sofar rest-chars x)
   (cond [(empty? rest-chars) (editor/chars-sofar rest-chars)]
                       (match-define (cons c rst) rest-chars)
           (if (chars-at-cursor? x (cons c chars-sofar))
               (editor (cons c chars-sofar) rst)
               (split/a (cons c chars-sofar) rst x))])
  (split/a empty (ed->lst ed0) x))
```

new pre initial (chars-sofar):
empty (no chars)

Key Points

new post initial (rest-chars):
 (ed->list ed0) (all chars)

```
(define (split ed0 x) ;; split : Editor Goord -> Editor
  ;; split/a : List<1str> List<1str> Coord -> Editor
  ;; ACCUMULATOR: chars-so-far
                                                                Invariant:
  ;; invariant: represents (rev) of chars seed so far, where
                                                                "so far" +
     (append (rev chars-so-far) rest-chars = (ed->1st ed0)
                                                                "remaining"
           and: (image-width (render-chars chars-sofar)) < x
                                                               ► ed0
  (define (split/a chars-sofar rest-chars x)
   (cond [(empty? rest-chars) (editor chars-sofar rest-chars)]
                       (match-define (cons c rst) rest-chars)
           (if (chars-at-cursor? x (cons c chars-sofar))
               (editor (cons c chars-sofar) rst)
               (split/a (cons c chars-sofar) rst x))])
  (split/a empty (ed->lst ed0) x))
```

Key Points

```
(define (split ed0 x) ;; split : Editor Coord -> Editor
  ;; split/a : List<1str> List<1str> Coord -> Editor
  ;; ACCUMULATOR: chars-so-far
  ;; invariant: represents (rev) of chars seen so far, where
      (append (rev chars-so-far) rest-chars) = (ed->lst ed0)
           and: (image-width (render-chars chars-sofar)) < x</pre>
                                                                 TEMPLATE
  (define (split/a chars-sofar rest-chars x)
   (cond [(empty? rest-chars) (editor chars-sofar rest-chars)]
                     (match-@???ine (cons c rst) rest-chars)
           (if (chars-at-cursor? x (cons c chars-sofar))
               (editor (cons????chars-sofar) rst)
               (split/a (cons c char????ofar) rst x))])
  (split/a empty (ed->lst ed0) x))
```

Key Points

```
(define (split ed0 x) ;; split : Editor Coord -> Editor
 ;; split/a : List<1str> List<1str> Coord -> Editor
 ;; ACCUMULATOR: chars-so-far
 ;; invariant: represents (rev) of chars seen so far, where
     (append (rev chars-so-far) rest-chars) = (ed->lst ed0)
          and: (image-width (render-chars chars-sofar)) < x</pre>
                                                           TEMPLATE
 (define (split/a chars-sofar rest-chars x)
   (cond [(empty? rest-chars) (editor chars-sofar rest-chars)]
         (if (chars-at-cursor? x (cons c chars-sofar))
              (editor (cons????chars-sofar) rst)
              (split/a (cons c char????ofar) rst x))])
  (split/a empty (ed->lst ed0) x))
```

Key Points

Designing functions with accumulators

```
(define (split ed0 x) ;; split : Editor Coord -> Editor
  ;; split/a : List<1str> List<1str> Coord -> Editor
  ;; ACCUMULATOR: chars-so-far
  ;; invariant: represents (rev) of chars seen so far, where
     (append (rev chars-so-far) rest-chars) = (ed->lst ed0)
           and: (image-width (render-chars chars-sofar)) < x</pre>
  (define (split/a chars-sofar rest-chars x)
    (cond [(empty? rest-chars) (editor chars-sofar rest-chars)]
                       (match-define (cons c rst) rest-chars)
           (if (chars-at-cursor? x (cons c chars-sofar))
               (editor (cons????chars-sofar) rst)
               (split/a (cons c char????far) rst x))])
  (split/a empty (ed->lst ed0) x))
```

Empty case

Invariant:

"so far" +

"remaining"

= ed0

✓

Key Points

```
(define (split ed0 x) ;; split : Editor Coord -> Editor
  ;; split/a : List<1str> List<1str> Coord -> Editor
                                                                         Non-empty
  ;; ACCUMULATOR: chars-so-far
                                                                           case?
  ;; invariant: represents (rev) of chars seen so far, where
      (append (rev chars-so-far) rest-chars) = (ed->lst ed0)
                                                                          Need one
           and: (image-width (render-chars chars-sofar)) < x
                                                                           more
                                                                          invariant!
  (define (split/a chars-so∕far rest-chars x)
    (cond [(empty? rest-chars) (editor chars-sofar rest-chars)]
                                                                         Invariant:
                    /(match-define (cons c rst) rest-chars)
                                                                         "so far" +
           (if (chars-at-cursor? x (cons c chars-sofar))
                                                                         "remaining"
                (editor (cons????chars-sofar) rst)
                                                              Done!
                                                                         = ed0 ▽
               (split/a (cons c char????ofar) rst x))])
                                                            Keep going ...
  (split/a empty (ed->lst ed0) x))
                                                                                16
```

Key Points

Designing functions with accumulators

```
(define (split ed0 x) ;; split : Editor Coord -> Editor
  ;; split/a : List<1str> List<1str> Coord -> Editor
  ;; ACCUMULATOR: chars-so-far
  ;; invariant: represents (rev) of chars seen so far, where
      (append (rev chars-so-far) rest-chars) = (ed->lst ed0)
           and: (image-width (render-chars chars-sofar)) < x</pre>
  (define (split/a chars-sofar rest-chars x)
    (cond [(empty? rest-chars) (editor chars-sofar rest-chars)]
                        (match-define (cons c rst) rest-chars)
           (if (chars-at-cursor? x (cons c chars-sofar))
            (compute-before/after x chars-sofar c rst)
                                                            Done????
               (split/a (cons c chars-sofar) rst x))|)
  (split/a empty (ed->lst ed0) x))
```

Need to compute whether cursor is before or after!

Key Points

- Designing functions with accumulators
- Code should be sufficiently "readable" such that ...
 - You can present your code like I just did!
 - (Still on the table for this semester ...)

Introducing: The "CS450JS" Programming Lang!

Programmer writes:



Next Feature: Variables?

```
A 450jsExpr is one of:
- Number
- String
- (list '+ 450jsExpr 450jsExpr)
- (list '- 450jsExpr 450jsExpr)
                   "eval450js"
    A 450jsResult is one of:
     - Number
     - String
     - NaN
          "meaning" of the program
```

```
parse450js
```

```
run450js
(JS semantics)
```

```
;; A 450jsAST is one of:
;; - (num Number)
;; - (str String)
;; - (add 450jsAST 450jsAST)
;; - (sub 450jsAST 450jsAST)

(struct num [val])
(struct str [val])
(struct add [lft rgt])
(struct sub [lft rgt])
```

Adding Variables

```
;; A Variable is a Symbol
   A 450jsExpr is one of:
                                                        ;; A 450jsAST is one of:
                                           parse450is
   - Number
                     Q<sub>1</sub>: What is the "meaning" of a variable?
   - String
   - Variable
   - (list '+ 450j A<sub>1</sub>: Whatever "value" it is bound to
   - (list '- 450j<del>e</del>
                                                                     |50jsAST 450jsAST)
                     Q<sub>2</sub>: Where do these "values" come from?
        A 450jsResu
                                                         struct num [val])
                     A<sub>2</sub>: Other parts of the program
        - Number
                                                         struct str [val])
        - String
                                                         (struct var [name])
                                            run450js
        - NaN
                                                        (struct add [lft rgt])
     The run function needs to "remember" these values (with an accumulator!)
```

run450js, with an accumulator

```
;; run: 450jsAST -> 450jsResult
;; Computes result of running a CS450js program AST
(define (run p)
  ;; accumulator acc : | Environment
  ;; invariant: Contains variable+result pairs that are currently in-scope
  (define (run/acc p acc)
    (match p
     [(num n) n]
     [(add x y) (450+ (run/acc x) (run/acc y))]))
 (run/acc p ??? ))
```

Environments

- A data structure that "associates" two things together
 - E.g., maps, hashes, etc
 - For simplicity, let's use list-of-pairs

```
;; An Environment is one of:
;; - empty
;; - (cons (list Var 450jsResult) Environment)
;; interpretation: a runtime environment for
;; (ie gives meaning to) cs450js-lang variables
;; if there are duplicates,
;; vars at front of list shadow those in back
```

Environments

- A data structure that "associates" two things together
 - E.g., maps, hashes, etc
 - For simplicity, let's use list-of-pairs
- Needed operations:

```
env-add : Env Var Result -> Env
```

• env-lookup : Env Var -> Result

- Repo: cs450f23/lecture21-inclass
- File: env-<your last name>.rkt

In-class Coding 11/21: write env ops

Needed operations:

```
• env-add : Env Var 450jsResult -> Env
```

env-lookup : Env Var -> 450jsResult

```
;; An Environment (Env) is one of:
;; - empty
;; - (cons (list Var 450jsResult) Environment)
;; interpretation: a runtime environment for
;; (ie gives meaning to) cs450js-lang variables
;; if there are duplicates,
;; vars at front of list shadow those in back
```

Think about examples where this happens!

run450js, with an Environment

- When are variables "added" to environment
- Initial environment? ;; run: 450jsAST -> 450jsResult

```
;; Computes result of running CS450js AST
```

```
(define (run p)
  ;; accumulator env : Environment
  ;; invariant: Contains variable+result pairs that are in-scope
  (define (run/acc p env)
    (match p
     [(num n) n]
     [(var x) (lookup env x)]
     [(add x y) (450+ (run/acc x env) (run/acc y env))]))
 (run/acc p ??? ))
```

NOTE: not needed for hw7

Programs that Create Variables

```
;; A 450jsExpr is one of:
;; - Number
;; - String (sometimes called "let")
;; - Variable
;; - (list 'bind Var 450jsExpr 450jsExpr)
;; - (list '+ 450jsExpr 450jsExpr)
;; - (list '- 450jsExpr 450jsExpr)
```

```
;; A 450jsAST is one of:
;; - (num Number)
;; - (str String)
;; - (var Symbol)
;; - (bind Symbol 450jsAST 450jsAST)
;; - (add 450jsAST 450jsAST)
;; - (sub 450jsAST 450jsAST)
(struct num [val])
(struct str [val])
(struct var [name])
(struct bind [var expr body])
(struct add [lft rgt])
(struct sub [lft rgt])
```

run450js, with an Environment

```
;; run: 450jsAST -> 450jsResult
(define (run p)
  ;; accumulator env : Environment
    invariant: Contains variable
                                     3. run body with that new environment
  (define (run/e p env)
                                              2. add variable x to environment
    (match p
     [(num n) n]
                                                         1. Compute 450jsResult
     [(var x) (lookup env x)]
                                                         that variable x represents
     [(bind x e body) (run/e body (add env x (run/e e env)))]
                  (450+ (run/e x env) (run/e y env
 (run/e p
```

- When are variables "added" to environment
- Initial environment?

```
(define (run p)
  ;; accumulator env : Environment
  ;; invariant: Contains variable+result pairs that are in-scope
  (define (run/e p env)
    (match p
     [(num n) n]
     [(var x) (lookup env x)]
     [(bind x e body) (run/e body (add env x (run/e e env)))]
     [(add x y) (450 + (run/e x env) (run/e y env))]))
(run/e p ???
```

;; A 450jsExpr is one of: ;; - Number ;; - String ;; - Variable ;; - (list 'bind Var 450jsExpr 450jsExpr) ;; - (list '+ 450jsExpr 450jsExpr) ;; - (list '- 450jsExpr 450jsExpr) Can these go into initial env?

TODO:

- When are variables "added" to environment
- Initial environment?

Should these be different language constructs?

Next Feature: Functions?

```
;; A 450jsExpr is one of:
;; - Number
;; - String
;; - Variable
;; - (list 'bind Var 450jsExpr 450jsExpr)
;; - (list '+ 450jsExpr 450jsExpr)
;; - (list '- 450jsExpr 450jsExpr)
;; - (list 'fn List<Variable> 450jsExpr)
```

TODO:

- When are variables "added" to environment
- Initial environment?
- Function representation

Next Feature: Functions?

```
;; A 450jsExpr is one of:
;; - Number
;; - String
;; - Variable
;; - (list 'bind Var 450jsExpr 450jsExpr)
;; - (list '+ 450jsExpr 450jsExpr)
;; - (list '- 450jsExpr 450jsExpr)
;; - (list 'fn List<Variable> 450jsExpr)
```

- When are variables "added" to environment
- Initial environment?
- Function representation
- Function result?

```
;; A 450jsResult is one of:
;; - Number
;; - String
;; - NaN
;; - ???
```

```
;; A 450jsExpr is one of:
;; - Number
;; - String
;; - Variable
;; - (list 'bind Var 450jsExpr 450jsExpr)
;; - (list '+ 450jsExpr 450jsExpr)
;; - (list '- 450jsExpr 450jsExpr)
;; - (list 'fn List<Variable> 450jsExpr)
;; - (list 'fncall 450jsExpr 450jsExpr)
```

- When are variables "added" to environment
- Initial environment?
- Function representation
- Function result?
- Function calls?

```
;; A 450jsResult is one of:
;; - Number
;; - String
;; - NaN
;; - ???
```

```
;; A 450jsExpr is one of:
;; - Number
;; - String
;; - Variable
;; - (list 'bind Var 450jsExpr 450jsExpr)
;; - (list '+ 450jsExpr 450jsExpr)
;; - (list '- 450jsExpr 450jsExpr)
;; - (list 'fn List<Variable> 450jsExpr)
;; - (list 'fncall 450jsExpr 450jsExpr)
```

- When are variables "added" to environment
- Initial environment?
- Function representation
- Function result?
- Function calls?

```
;; A 450jsResult is one of:
;; - Number
;; - String
;; - NaN
;; - ???
```

```
;; A 450jsExpr is one of:
;; - Number
;; - String
;; - Variable
;; - (list 'bind Var 450jsExpr 450jsExpr)
;; - (list '+ 450jsExpr 450jsExpr)
;; - (list '- 450jsExpr 450jsExpr)
;; - (list 'fn List<Variable> 450jsExpr)
;; - (list 'fncall 450jsExpr 450jsExpr)
```

TODO:

- When are variables "added" to environment
- Initial environment?
- Function representation
- Function result?
- Function calls?

```
;; A 450jsResult is one of:
;; - Number
;; - String
;; - NaN
... >>>
```

Most language function calls don't explicitly require saying "function call"

No More Quizzes!

but push your in-class work to:
 Repo: cs450f23/lecture21-inclass