

UMass Boston Computer Science  
**CS450 High Level Languages**

# Programming with Compound Data

Thursday, February 19, 2026

```
class Horse
  implements Animal {
    Int age;
    Float weight;
  }
```



# Logistics

- HW 3 out
  - due: Tues 2/24 11am EST
  - Similar to HW 2, but with compound data defs (start from scratch!)
- New Office Hour Time
  - Thurs 2-3:30pm

(OO languages love compound data)

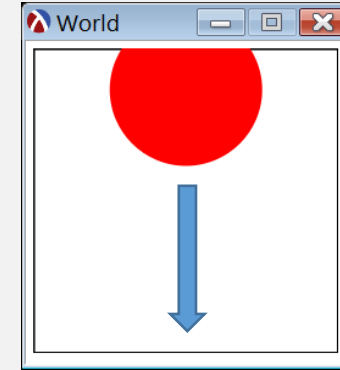
```
class Horse
  implements Animal {
    Int age;
    Float weight;
  }
```



Last  
Time

# Falling “Ball” Example

```
;; A WorldState is a Non-negative Integer  
;; Represents: the y Coordinate of the center of a  
;; ball in a `big-bang` animation.
```



← What if ... the ball can also move side-to-side?? →

WorldState would need two pieces of data:  
the **x** and **y** coordinates

```
;; A WorldState is an Integer ...  
;; ... and another Integer???
```

We need a way to create **compound data**  
i.e., a **data definition** that  
combines values of other data defs

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# Kinds of Data Definitions

- Basic data
  - E.g., numbers, strings, etc
- Intervals
  - Data that is from a range of values, e.g.,  $[0, 100)$
- Enumerations
  - Data that is one of a list of possible values, e.g., “green”, “red”, “yellow”
- Itemizations
  - Data value that can be from a list of possible other data definitions
  - E.g., either a string or number (Generalizes enumerations)
- ➔ • Compound Data
  - Data that is a combination of values from other data definitions

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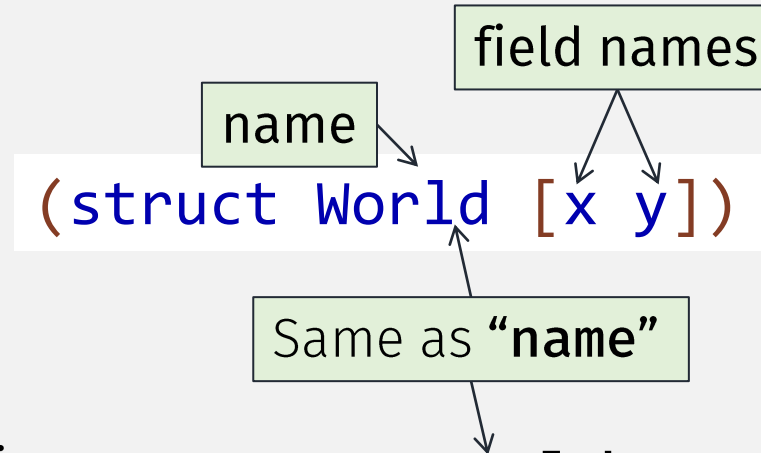
# Falling “Ball” Example

a struct defines a  
new kind of  
compound data

```
;; A WorldState is a (mk-WorldState [x : Int] [y : Int])  
;; Represents: coordinate in big-bang animation where:  
;; - x is ball (red solid circle) horizontal center  
;; - y is ball vertical center  
(struct World [x y])  
(define/contract (mk-WorldState x y)  
  (-> integer? integer? WorldState?)  
  (World x y)  
;; ...
```

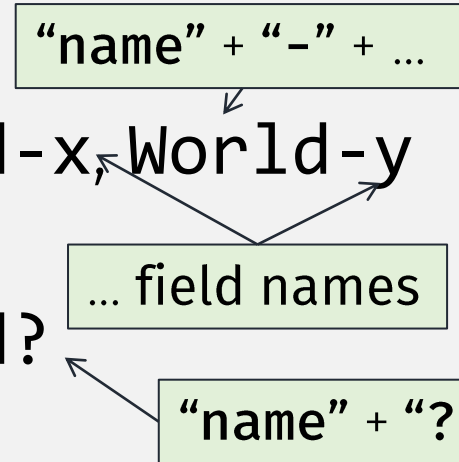
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# Parts of a **struct** definition



(Implicitly) defines:

- A **constructor** function  $\longrightarrow$  `World`
  - Creates instances of the struct
- **Accessor** functions  $\longrightarrow$  `World-x`, `World-y`
  - Get an instance's field value
- A **predicate**  $\longrightarrow$  `World?`
  - Returns true for struct instances



Last  
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# Falling “Ball” Example

```
;; A WorldState is a (mk-WorldState [x : Int] [y : Int])  
;; Represents: coordinate in big-bang animation where:  
;; - x is ball (red solid circle) horizontal center  
;; - y is ball vertical center  
(struct World [x y])  
(define/contract (mk-WorldState x y)  
  (-> integer? integer? WorldState?)  
  (World x y))  
;; ...
```

a struct defines a  
new kind of  
compound data

Checked constructor  
(programmer must define)

Unchecked (internal) constructor  
(implicitly defined by **struct**)

```
(define INIT-WORLDDSTATE (mk-WorldState 0 0))
```

Produces **instances** of the  
**struct** that are **values** of the  
new data definition

# Data Design Recipe

## Data Definition

- Has 4 parts:
  1. **Name**
  2. Description of **all possible values** of the data
  3. **Interpretation** explaining the real world concepts the data represents
  4. **Predicate** returning **false** for (most?) values not in the Data Definition
    - If needed, define extra predicates for each **enumeration** or **itemization**



# Data Design Recipe - Compound Data Update

## **Data Definition** (for compound data)

• ~~Has 4~~ Has 5 parts:

1. **Name**
2. Description of **all possible values** of the data
3. **Interpretation** explaining the real world concepts the data represents
4. **Predicate** returning **false** for (most?) values not in the Data Definition
  - If needed, define extra predicates for each **enumeration** or **itemization**
- ➔ 5. (checked) **Constructor** for compound data def values

# Data Design Recipe - Compound Data Predicate

## **Data Definition** (for compound data)

- Has 5 parts:
  1. **Name**
  2. Description of **all possible values** of the data
  3. **Interpretation** explaining the real world concepts the data represents
  - ➔ 4. **Predicate** returning **false** for (most?) values not in the Data Definition
    - For compound data ...
  5. (checked) **Constructor** for compound data def values

# Predicates for Compound Data

```
;; A WorldState is a (mk-WorldState [x : Int] [y : Int])  
;; Represents: coordinate in big-bang animation where:  
;; - x is ball (red solid circle) horizontal center  
;; - y is ball vertical center  
(struct World [x y])
```

predicate?

`struct` already defines `World?` ...  
but does not enforce field types?

```
(define (WorldState? arg)  
  (and (World? arg)  
    → (integer? (World-x arg))  
    → (integer? (World-y arg))))
```

???

This “deep” predicate checks too much...

... because it’s the job of  
“field data type” processing functions  
to check those kinds of data

Also not practical? maybe exponential  
overhead ...

Compound data predicates  
should be  
“**shallow**” checks,  
i.e., `World`?

Instead, use **checked constructor**: ensures that  
only valid instances are  
created!

```
(define/contract (mk-WorldState x y)  
  (-> integer? integer? WorldState?)  
  (World x y))
```

# Data Design Recipe - Predicate Update

## **Data Definition** (for compound data)

- Has 5 parts:
  1. **Name**
  2. Description of **all possible values** of the data
  3. **Interpretation** explaining the real world concepts the data represents
  4. **Predicate** (shallow, conservative approximation of the Data Def)
    - Evaluates to **true** for all values in the Data Def ... and maybe some not
      - False positives maybe **ok** Might let in some invalid values
    - Evaluates to **false** for (most?) values not in the Data Def ... but maybe not all
      - False negatives not **ok** Must only reject invalid values
  5. (checked) **Constructor** for compound data def values

# Function Design Recipe

1. **Name**
2. **Signature** – types of the function input(s) and output
3. **Description** – explain (in English prose) the function behavior
4. **Examples** – show (using `check-equal?`) the function behavior
5. **Template** – sketch out the function structure (using input's Data Definition)
6. **Code** – implement the rest of the function (arithmetic)
7. **Tests** – check (using `check-equal?` and other test forms) the function behavior

# Functions For Compound Data

- A function that processes compound data must ...
  - extract the individual pieces, using accessors
  - combine them, with arithmetic

# Functions For Compound Data - Template

- A function that processes compound data must

- extract the individual pieces, using accessors ← Done with template
- combine them, with arithmetic

```
;; A WorldState is a (mk-WorldState [x : Int] [y : Int])
(struct World [x y])

(define/contract (mk-WorldState x y)
  (-> integer? integer? WorldState?)
  (World x y))
```

```
;; TEMPLATE for WorldState-fn: WorldState -> ???
(define (WorldState-fn w)

  .... (World-x w) ....
  .... (World-y w) .... )
```

A function's  
template is  
completely  
determined by  
the input's  
**Data Definition**

# Functions For Compound Data - Template

- A function that processes compound data must

- extract the individual pieces, using accessors ← Done with template
- combine them, with arithmetic

```
;; A WorldState is a (mk-WorldState [x : Int] [y : Int])
(struct World [x y])

(define/contract (mk-WorldState x y)
  (-> integer? integer? WorldState?)
  (World x y))
```

```
;; TEMPLATE for WorldState-fn: WorldState -> ???
(define/contract (WorldState-fn w)
  (-> WorldState? ??? )
  .... (World-x w) ....
  .... (World-y w) .... )
```

A function's  
template is  
completely  
determined by  
the input's  
**Data Definition**



# Function Design Recipe

Still must program with these steps,  
in this order!

1. **Name**
2. **Signature** – types of the **function input(s)** and **output** (not submitted in comments, if there are valid **contracts**)
3. **Description** – explain (in English prose) the function behavior
4. **Examples** – show (using `check-equal?`) the function behavior
5. **Template** – sketch out the function structure (using input's Data Definition) (not submitted)
6. **Code** – implement the rest of the function (arithmetic)
7. **Tests** – check (using `check-equal?` and other test forms) the function behavior

```
;; A WorldState is a (mk-WorldState [x : Int] [y : Int])  
(struct World [x y])  
(define/contract (mk-WorldState x y)  
  (-> integer? integer? WorldState?)  
  (World x y))
```

```
(check-equal?  
  (next-WorldState  
    (mk-WorldState 0 0))  
  (mk-WorldState X-VEL Y-VEL))
```

(assuming constant velocity)

```
;; next-WorldState : WorldState -> WorldState  
;; Computes the ball position after 1 tick
```

```
;; TEMPLATE for WorldState:  
(define/contract (WorldState-fn w)  
  (-> WorldState? ??? )  
  .... (World-x w) ....  
  .... (World-y w) .... )
```

```
(check-equal?  
  (next-WorldState  
    (mk-WorldState 0 0))  
  (mk-WorldState X-VEL Y-VEL))
```

```
;; next-WorldState  
;; Computes the ball position after 1 tick
```

```
(define/contract (next-WorldState w)  
  (-> WorldState? WorldState?)  
  .... (World-x w) ....  
  .... (World-y w) .... )
```

```
;; next-WorldState  
;; Computes the ball position after 1 tick
```

```
(define/contract (next-WorldState w)  
  (-> WorldState? WorldState?)  
  (mk-WorldState  
    (+ (World-x w) X-VEL)  
    (+ (World-y w) Y-VEL)))
```

```
(check-equal?  
  (next-WorldState  
    (mk-WorldState 0 0))  
  (mk-WorldState X-VEL Y-VEL))
```

Example + Template helps  
to write the function!

# Extract Compound Pieces – **let**

alternatives

See also **let\***

```
(define/contract (next-WorldState w)
```

```
; ...
```

```
(let ([x (World-x w)]  
      [y (World-y w)]))
```

```
(mk-WorldState (+ x X-VEL) (+ y Y-VEL))))
```

Defines new  
local variables

Extract all compound  
data pieces first, before  
doing “arithmetic”

```
(let ([id val-expr] ...) body ...+)
```

Local variables **shadow**  
previously defined vars

in scope only in the body

# Extract Compound Pieces – (internal) **define**

alternatives

```
(define/contract (next-WorldState w)
  ; ...
  (define x (World-x w))
  (define y (World-y w))
  (mk-WorldState (+ x X-VEL) (+ y Y-VE
```

Extract all compound data pieces first, before doing “arithmetic”

(is there an easier way to do this?)

# Extract Compound Pieces – Pattern Match!

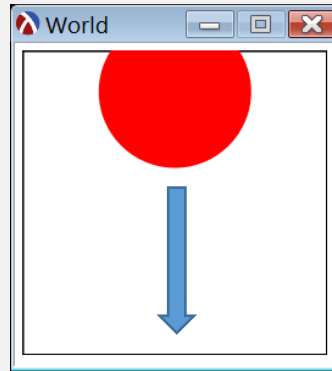
alternatives

```
(define/contract (next-WorldState w)
  ; ...
  (match-define (World x y) w)

  (mk-WorldState (+ x X-VEL) (+ y Y-VEL))))
```

Extract all compound  
data pieces, at the  
same time!

# Falling “Ball” Example



← What if the **ball** can also move side-to-side ... →

... on a key-press?

`WorldState` would need two pieces of data:  
the *x* and *y* coordinates



Last  
Time

# Some Pre-defined Enumerations

```
; A KeyEvent is one of:  
; - 1String  
; - "left"  
; - "right"  
; - "up"  
; ...
```

"KeyEvent"  
function"

... cannot do  
"WorldState"  
function "things"!

(result must be **WorldState**)

But remember:

1 function does  
1 task which processes  
1 kind of data

**WorldState**

Give to: **big-bang on-key** clause

Must call separate: "WorldState fn"

... to do "WorldState" function "things"

Template

```
; WorldState KeyEvent -> ..  
(define (handle-key-events w ke)  
  (cond  
    [(= (string-length ke) 1) ...]  
    [(string=? "left" ke) .. (handle-left w) ???]  
    [(string=? "right" ke) . (handle-right w) ???]  
    [(string=? "up" ke) ...]  
    [(string=? "down" ke) ...]  
    ...))
```

Or even better: **key=?**

Do not put all code in one function! e.g.,  
Do not process "WorldState" data in a  
"KeyEvent" function!

# Compound Data can be nested

But remember:

**1 function** does  
**1 task** which processes  
**1 kind of data**

Need a different function (that uses GameState template) to process GameState data

Uses KeyEvent template

```
(define/contract (key-handler g k)
  (-> GameState? key-event? GameState?)
  (cond
    [(key=? k GET-RED) (handle-red-key g)]
    [(key=? k GET-BLUE) (handle-blue-key g)]
    [else w]))
```

# Compound Data can be nested

But remember:

**1 function** does  
**1 task** which processes  
**1 kind of data**

Makes testing easier!

```
(check-equal? (key-handler ANY-GAMESTATE "r")  
              (handle-red-key ANY-GAMESTATE))  
(check-equal? (key-handler ANY-GAMESTATE "b")  
              (handle-blue-key ANY-GAMESTATE))
```

(but still need some "full stack" tests)

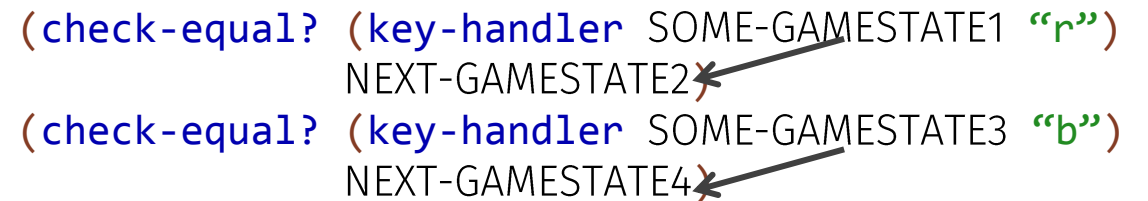
```
(define/contract (key-handler g k)  
  (-> GameState? key-event? GameState?)  
  (cond  
    [(key=? k GET-RED) (handle-red-key g)]  
    [(key=? k GET-BLUE) (handle-blue-key g)]  
    [else w]))
```

# Function Design Recipe – Testing Update

- “Full Stack”

- For “top level” functions
- Tests: all functionality from input to final result
- Should be more comprehensive

```
(check-equal? (key-handler SOME-GAMESTATE1 "r")  
              NEXT-GAMESTATE2)  
(check-equal? (key-handler SOME-GAMESTATE3 "b")  
              NEXT-GAMESTATE4)
```



- “Incremental”

- For “helper” (and top level) functions
- Tests: more local functionality – dictated by data design
- delegate to other helpers, should test “control flow” paths

```
(check-equal? (key-handler ANY-GAMESTATE "r")  
              (handle-red-key ANY-GAMESTATE))  
(check-equal? (key-handler ANY-GAMESTATE "b")  
              (handle-blue-key ANY-GAMESTATE))
```

# A “GameState” data def + function ...

```
;; A GameState is a (hypothetically ...)
;;   (mk-GameState [p1 : Player] [p2 : Player]
;;                 [active : PlayerID])
;; where:
;; - p1 : represents “Player 1” data ...
;; - p2 : represents “Player 2” data ...
;; - active : it’s this player’s turn
```

```
(define/contract (GameState-fn g)
  (-> GameState? .... )
```

TEMPLATE

```
    .... (GameState-p1 g) ....
    .... (GameState-p2 g) ....
    .... (GameState-active g) .... )
```

(extracts pieces of compound data)

# A “GameState” function ...

```
;; A GameState is a (hypothetically ...)
;;   (mk-GameState [p1 : Player] [p2 : Player]
;;                 [active : PlayerID])
;; where:
;; - p1 : represents “Player 1” data ...
;; - p2 : represents “Player 2” data ...
;; - active : it’s this player’s turn
```

```
(define/contract (handle-red-key g)
  (-> GameState? .... )

  .... (GameState-p1 g) ....
  .... (GameState-p2 g) ....
  .... (GameState-active g) .... )
```

# A “GameState” function ...

```
;; A GameState is a (hypothetically ...)
;;   (mk-GameState [p1 : Player] [p2 : Player]
;;                 [active : PlayerID])
;; where:
;; - p1 : represents “Player 1” data ...
;; - p2 : represents “Player 2” data ...
;; - active : it’s this player’s turn
```

```
(define/contract (handle-red-key g)
  (-> GameState? GameState?)
  (mk-GameState
    .... (GameState-p1 g) ....
    .... (GameState-p2 g) ....
    .... (GameState-active g) .... ))
```

Look at type(s) to help fill in template

# A “GameState” function ...

```
;; A GameState is a (hypothetically ...)
;;   (mk-GameState [p1 : Player] [p2 : Player]
;;                 [active : PlayerID])
;; where:
;; - p1 : represents “Player 1” data ...
;; - p2 : represents “Player 2” data ...
;; - active : it’s this player’s turn
```

But remember:

1 function does  
1 task which processes  
1 kind of data

```
(define/contract (handle-red-key g)
  (-> GameState? GameState?)
  (mk-GameState
    .... (GameState-p1 g) ....
    .... (GameState-p2 g) ....
    .... (GameState-active g) .... )
```



# A “GameState” function ...

```
;; A GameState is a (hypothetically ...)
;;   (mk-GameState [p1 : Player] [p2 : Player]
;;                 [active : PlayerID])
;; where:
;; - p1 : represents “Player 1” data ...
;; - p2 : represents “Player 2” data ...
;; - active : it’s this player’s turn
```

But remember:

1 function does  
1 task which processes  
1 kind of data

```
(define/contract (handle-red-key g)
  (-> GameState? GameState?)
  (mk-GameState
    (Player-fn (GameState-p1 g))
    (Player-fn (GameState-p2 g))
    (PlayerID-fn (GameState-active g))))
```

Don’t do “Player” function “things” in a “GameState” function!

# A “GameState” function ...

```
;; A GameState is a (hypothetically ...)
;; (mk-GameState [p1 : Player] [p2 : Player]
;;               [active : PlayerID])
;; where:
;; - p1 : represents “Player 1” data ...
;; - p2 : represents “Player 2” data ...
;; - active : it’s this player’s turn
```

NOTE: don’t “prematurely optimize!”

Programmers waste enormous amounts of time thinking about, or worrying about, the speed of noncritical parts of their programs... We should forget about small efficiencies, say about 97% of the time: premature optimization is the root of all evil.

— Donald Knuth

```
(define/contract (handle-red-key g)
  (-> GameState? GameState?)
  (mk-GameState
    (Player-fn (GameState-p1 g) (GameState-p2 g) (GameState-active g))
    (Player-fn (GameState-p2 g) (GameState-p1 g) (GameState-active g))
    (PlayerID-fn (GameState-active g) (GameState-p1 g) (GameState-p2 g))))
```

(can always refactor to be “cleaner” later)

Pass as many compound data pieces as needed ...

(trust the recipe ... follow the data design ... resist temptation to “prematurely optimize”)

# Data Definition Invariants

`;; A GameState is a` (hypothetically ...)  
`;; (mk-GameState [p1 : Player] [p2 : Player]`  
`;; [active : PlayerID])`  
  
`;; where:`  
`;; - p1 : represents "Player 1" data ...`  
`;; - p2 : represents "Player 2" data ...`  
`;; - active : it's this player's turn`  
`(struct GameState [p1 p2 active])`

`;; Invariant1: p1 "red" + p2 "red" <= MAX-TOKENS`

`;; Invariant2: p1 "blue" + p2 "blue" <= MAX-TOKENS`

"invariant" = "must always be true!"

*Previously*

```
(define/contract (mk-GameState p1 p2 id)
  (-> Player? Player? PlayerID? GameState?)
  (GameState p1 p2 id))
```

Can these be "any" Player values?

`;; A Player is a` Assume hypothetically ...  
`;; (mk-Player [red : TokenCount]`  
`;; [blue : TokenCount])`

Every function that creates a GameState is responsible for maintaining its invariants!

Can this be automatically checked?

# Data Definition Invariants

```
;; A GameState is a (hypothetically ...)
;; (mk-GameState [p1 : Player] [p2 : Player]
;;               [active : PlayerID])

;; where:
;; - p1 : represents "Player 1" data ...
;; - p2 : represents "Player 2" data ...
;; - active : it's this player's turn
(struct GameState [p1 p2 active])
```

Every function that creates a GameState is responsible for maintaining its invariants!

```
;; Invariant1: p1 "red" + p2 "red" <= MAX-TOKENS
```

```
;; Invariant2: p1 "blue" + p2 "blue" <= MAX-TOKENS
```

Can this be automatically checked?

One possibility:  
define a separate "output" predicate

With Invariant Check

```
(define/contract (mk-GameState p1 p2 id)
  (-> Player? Player? PlayerID? GameState/invariant?)
  (GameState p1 p2 id))
```

```
(define (GameState/invariant? x)
  (and (GameState? x)
       (<= (+ (red-count (GameState-p1 x))
              (red-count (GameState-p2 x)))
            MAX-TOKENS)
       (<= (+ (blue-count (GameState-p1 x))
              (blue-count (GameState-p2 x)))
            MAX-TOKENS))))
```

# Data Definition Invariants

```
;; A GameState is a (hypothetically ...)
;; (mk-GameState [p1 : Player] [p2 : Player
                             [active : PlayerID]])

;; where:
;; - p1 : represents "Player 1" data ...
;; - p2 : represents "Player 2" data ...
;; - active : it's this player's turn
(struct GameState [p1 p2 active])
```

But remember:

- compound data contracts should be "shallow"
- i.e., don't traverse an entire (nested) data structure
- Programmer must decide what is "too deep"

This one probably ok because ...  
still "constant" time check

Every function that creates a  
GameState is responsible for  
maintaining its invariants!

"Dependent"  
Contract

```
;; Invariant1: p1 "red" + p2 "red" <= MAX-TOKENS
```

```
;; Invariant2: p1 "blue" + p2 "blue" <= MAX-TOKENS
```

Can this be automatically checked?

One possibility:  
define a separate "output" predicate

```
(define (GameState/invariant? x)
  (and (GameState? x)
        (GameState-red-invariant? x)
        (GameState-blue-invariant? x)))
```

(with better-named helper functions!  
Avoid large unreadable boolean  
expressions!)

```
(define/contract (mk-GameState p1 p2 id)
  (-> Player? Player? PlayerID? GameState/invariant?)
  (GameState p1 p2 id))
```

# Data Design Recipe - Predicate Update

## Data Definition (for compound data)

- Has 5 parts:

1. **Name**

2. Description of **all possible values** of the data

3. **Interpretation** explaining the real world concepts the data represents

4. **Predicate** (shallow, conservative approximation of the Data Def)

- Evaluates to **true** for all values in the Data Def, and maybe some not

- False positives maybe **ok** Might let in some invalid values

- Evaluates to **false** for (most?) values not in the Data Def, but maybe not all

- False negatives not **ok** Must only reject invalid values

 • Consider “dependent” “output” contracts ... to check **invariants**

5. (checked) **Constructor** for compound data def values

Follow data definitions whenever possible, but ...

# Sometimes you need “**if**” ... ?

```
(define/contract (key-handler g k)
  (-> GameState? key-event? GameState?)
  (cond
    . . . .
    [(key=? k SPEND-KEY) (handle-spend g)]
    . . . .
    [else w]))
```

a “GameState” function!

# A “GameState” data def + function ...

```
;; A GameState is a (hypothetically ...)
;;   (mk-GameState [p1 : Player] [p2 : Player]
;;                 [active : PlayerID])
;; where:
;; - p1 : represents “Player 1” data ...
;; - p2 : represents “Player 2” data ...
;; - active : it’s this player’s turn
```

```
(define/contract (GameState-fn g)
  (-> GameState? .... )
```

TEMPLATE

```
    .... (GameState-p1 g) ....
    .... (GameState-p2 g) ....
    .... (GameState-active g) .... )
```

(extracts pieces of compound data)



# A “GameState” function ...

```
;; A GameState is a (hypothetically ...)
;;   (mk-GameState [p1 : Player] [p2 : Player]
;;                 [active : PlayerID])
;; where:
;; - p1 : represents “Player 1” data ...
;; - p2 : represents “Player 2” data ...
;; - active : it’s this player’s turn
```

```
(define/contract (handle-spend g)
  (-> GameState? .... )

  .... (GameState-p1 g) ....
  .... (GameState-p2 g) ....
  .... (GameState-active g) .... )
```

# A “GameState” function ...

```
;; A GameState is a (hypothetically ...)
;;   (mk-GameState [p1 : Player] [p2 : Player]
;;                 [active : PlayerID])
;; where:
;; - p1 : represents “Player 1” data ...
;; - p2 : represents “Player 2” data ...
;; - active : it’s this player’s turn
```

```
(define/contract (handle-spend g)
  (-> GameState? GameState?)
  (mk-GameState
    .... (GameState-p1 g) ....
    .... (GameState-p2 g) ....
    .... (GameState-active g) .... ))
```

Look at type(s) to help fill in template

# A “GameState” function ...

```
;; A GameState is a (hypothetically ...)
;;   (mk-GameState [p1 : Player] [p2 : Player]
;;                 [active : PlayerID])
;; where:
;; - p1 : represents “Player 1” data ...
;; - p2 : represents “Player 2” data ...
;; - active : it’s this player’s turn
```

But remember:

1 function does  
1 task which processes  
1 kind of data

```
(define/contract (handle-spend g)
  (-> GameState? GameState?)
  (mk-GameState
    .... (GameState-p1 g) ....
    .... (GameState-p2 g) ....
    .... (GameState-active g) .... )
```

# A “GameState” function ...

```
;; A GameState is a (hypothetically ...)
;;   (mk-GameState [p1 : Player] [p2 : Player]
;;                 [active : PlayerID])
;; where:
;; - p1 : represents “Player 1” data ...
;; - p2 : represents “Player 2” data ...
;; - active : it’s this player’s turn
```

But remember:

1 function does  
1 task which processes  
1 kind of data

```
(define/contract (handle-spend g)
  (-> GameState? GameState?)
  (mk-GameState
    (Player-fn (GameState-p1 g))
    (Player-fn (GameState-p2 g))
    (PlayerID-fn (GameState-active g))))
```

Don’t do “Player” function “things” in a “GameState” function!

# A “GameState” function needs “Player” fn

```
(define/contract (handle-spend g)
  (-> GameState? GameState?)
  (mk-GameState
    (player-spend (GameState-p1 g)) (assuming this is “active” player)
    (Player-fn (GameState-p2 g))
    (PlayerID-fn (GameState-active g))))
```

# A “Player” function ...

```
;; A Player is a Assume hypothetically ...  
;; (mk-Player [red : TokenCount]  
;;           [blue : TokenCount])
```

```
(define/contract (player-fn p)  
  (-> Player? ....)  
  
    .... (Player-red p) ....)  
    .... (Player-blue p) ....)) (template)
```

# A “Player” function ...

Are there any invariants to maintain?

Player should only “spend” if they have sufficient tokens, e.g., 1 red and 1 blue

“Dependent” contract won’t suffice here ... because we don’t want to error

We really need “if”!

```
(define/contract (player-spend p)
  (-> Player? Player?)
  (mk-Player
   (spend-token (Player-red p))
   (spend-token (Player-blue p))))
```

(from hw1)

# A “Player” function ...

Are there any invariants to maintain?

Player should only “spend” if they have sufficient tokens, e.g., 1 red and 1 blue

(not great)  
Don't write this!

No giant boolean expressions!

“Dependent” contract won't suffice here  
... because we don't want to error

We really need “if”!

```
(define/contract (player-spend p)
  (-> Player? Player?)
  (if (and (not (zero? (Player-red p)))
           (not (zero? (Player-blue p))))
      (mk-Player
        (spend-token (Player-red p))
        (spend-token (Player-blue p)))
```



# A “Player” function ...

Are there any invariants to maintain?

Player should only “spend” if they have sufficient tokens, e.g., 1 red and 1 blue

(not great)  
Don't write this!

Name doesn't accurately describe what the function does!

“Dependent” contract won't suffice here ... because we don't want to error

We really need “if”!

```
(define/contract (player-spend p)
  (-> Player? Player?)
  (if (can-spend? .... )
      (mk-Player
        (spend-token (Player-red p))
        (spend-token (Player-blue p)))
      )
  )
```

# A “Player” function ...

Write this!

Name accurately describes  
what the function does!

```
(define/contract (player-maybe-spend p)
  (-> Player? Player?)
  (if (can-spend? p)
      (player-spend p)
      p))
```

Are there any invariants to maintain?

Player should only “spend” if they have  
sufficient tokens, e.g., 1 red and 1 blue

“Dependent” contract won’t suffice here  
... because we don’t want to error

We really need “if”!

# Function Design Recipe – “**if**” edition

- Avoid if possible ...
  - Most of the time, function can follow some data definition template!
- Sometimes needed ...
  - E.g., to enforce compound invariants, without error
- Use helper predicate(s) to clearly describe invariant
  - E.g., “can-spend?”
  - No huge, unreadable boolean expressions!
- Function name and purpose stmt must indicate “**if**” usage!
  - E.g., “maybe-”
- 1 per function only
  - no nested “**if**”s!

*Random*

# Ball Animation

Design a **big-bang** animation that:

- Start: a single ball, moving with random  $x$  and  $y$  velocity

# Randomness

[bracketed args] = optional

```
(random k [rand-gen]) → exact-nonnegative-integer?
```

```
k : (integer-in 1 4294967087)
```

```
rand-gen : pseudo-random-generator?
```

```
= (current-pseudo-random-generator)
```

When called with an integer argument *k*, returns a random exact integer in the range 0 to *k*-1.

Optional arg Default value

```
(random min max [rand-gen]) → exact-integer?
```

```
min : exact-integer?
```

```
max : (integer-in (+ 1 min) (+ 4294967087 min))
```

```
rand-gen : pseudo-random-generator?
```

```
= (current-pseudo-random-generator)
```

When called with two integer arguments *min* and *max*, returns a random exact integer in the range *min* to *max*-1.

“random” is not random???

Not secure!  
e.g., for generating  
passwords

A pseudorandom number generator (PRNG), also known as a **deterministic random bit generator (DRBG)**,<sup>[1]</sup> is an **algorithm** for generating a sequence of numbers whose properties approximate the properties of sequences of **random numbers**. The PRNG-generated sequence is **not truly random**, because it is completely determined by an initial value, called the PRNG's **seed**

VS

A **cryptographically secure** pseudorandom number generator (CSPRNG) or **cryptographic pseudorandom number generator (CPRNG)** is a **pseudorandom number generator** (PRNG) with properties that make it suitable for use in **cryptology**.

# Random Functions: Same Recipe (almost)!

```
;; A Velocity is a non-negative integer
;; Interp: reresents pixels/tick change in a ball coordinate
(define MAX-VELOCITY 10)
```

```
;; random-velocity : -> Velocity
;; returns a random velocity between 0 and MAX-VELOCITY
(define (random-velocity)
  (random MAX-VELOCITY))
```

Functions can  
have zero args

Random functions have  
no examples

```
(check-true (< (random-velocity) MAX-VELOCITY))
(check-true (>= (random-velocity) 0))
(check-true (integer? (random-velocity)))
(check-pred (λ (v) (and (integer? v)
                        (< v MAX-VELOCITY)
                        (>= v 0))))
(random-velocity))
```

Can still **test!**  
Just less precise

```
;; random-x      : -> ???
;; random-y      : -> ???
;; random-ball   : -> ???
```