

UMass Boston Computer Science
CS450 High Level Languages

Programming with Compound Data

Thursday, February 19, 2026

```
class Horse
    implements Animal {
        Int age;
        Float weight;
    }
```



Logistics

- HW 3 out
 - due: Tues 2/24 11am EST
 - Similar to HW 2, but with compound data defs
(start from scratch!)
- New Office Hour Time
 - Thurs 2-3:30pm

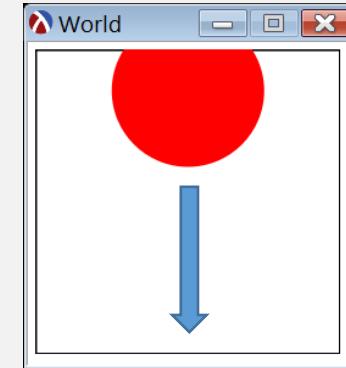
(oo languages love compound data)

```
class Horse
implements Animal {
    Int age;
    Float weight;
}
```



Falling “Ball” Example

```
;; A WorldState is a Non-negative Integer  
;; Represents: the y Coordinate of the center of a  
;; ball in a `big-bang` animation.
```



What if ... the ball can also move side-to-side??

WorldState would need two pieces of data:
the **x** and **y** coordinates

;; A WorldState is an Integer ...
;; ... and another Integer???

We need a way to create **compound data**
i.e., a data definition that
combines values of other data defs

Kinds of Data Definitions

- Basic data
 - E.g., numbers, strings, etc
- Intervals
 - Data that is from a range of values, e.g., [0, 100)
- Enumerations
 - Data that is one of a list of possible values, e.g., “green”, “red”, “yellow”
- Itemizations
 - Data value that can be from a list of possible other data definitions
 - E.g., either a string or number (Generalizes enumerations)
- • Compound Data
 - Data that is a combination of values from other data definitions

Falling “Ball” Example

a struct defines a
new kind of
compound data

```
;; A WorldState is a (mk-WorldState [x : Int] [y : Int])
;; Represents: coordinate in big-bang animation where:
;; - x is ball (red solid circle) horizontal center
;; - y is ball vertical center
→(struct World [x y])
(define/contract (mk-WorldState x y)
  (-> integer? integer? WorldState?))
(World x y)
;; ...
```

Parts of a struct definition

(Implicitly) defines:

- A **constructor** function → **World**

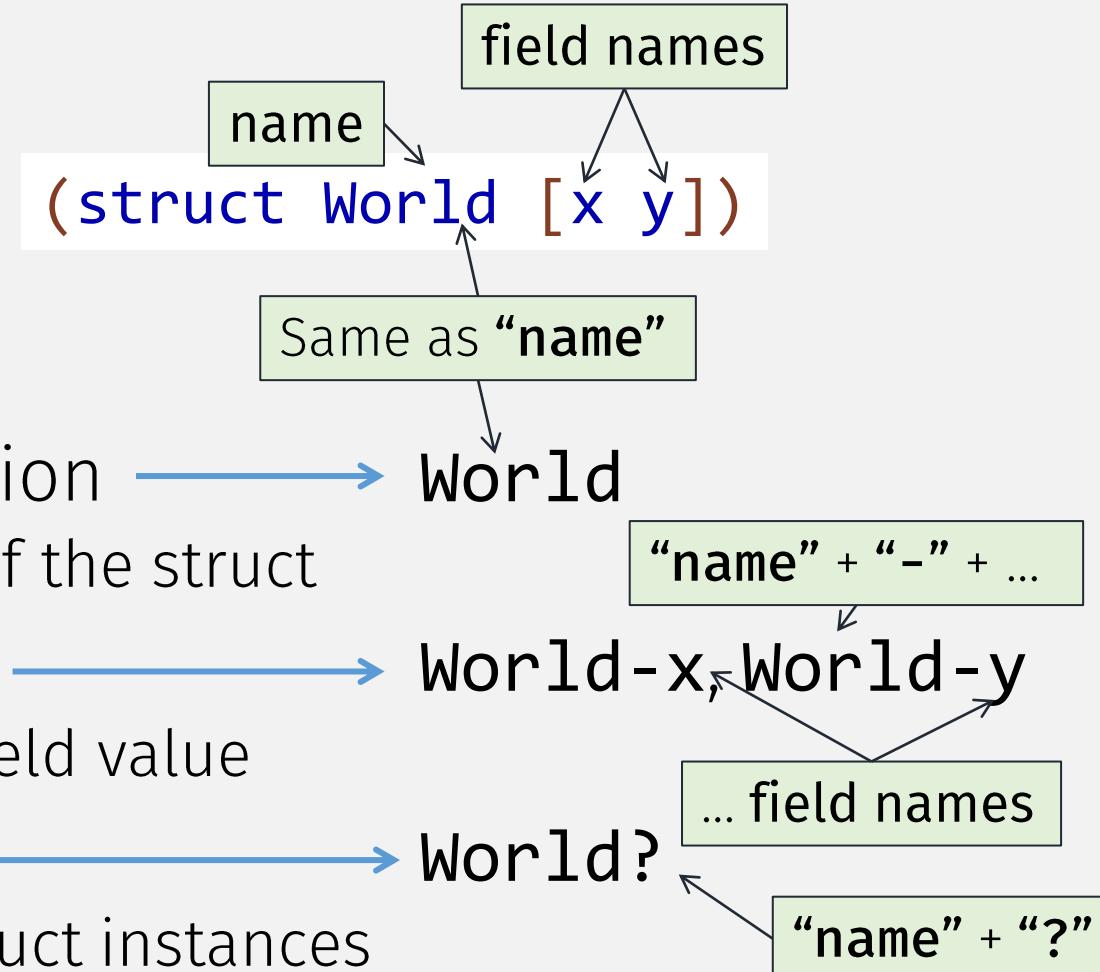
- Creates instances of the struct

- **Accessor** functions → **World-x, World-y**

- Get an instance's field value

- A **predicate** → **World?**

- Returns true for struct instances



Falling “Ball” Example

a struct defines a new kind of compound data

```
;; A WorldState is a (mk-WorldState [x : Int] [y : Int])
;; Represents: coordinate in big-bang animation where:
;; - x is ball (red solid circle) horizontal center
;; - y is ball vertical center
(struct World [x y])
(define/contract (mk-WorldState x y)
  (-> integer? integer? WorldState?))
(World x y)
;; ...
```

Checked constructor
(programmer must define)

Unchecked (internal) constructor
(implicitly defined by **struct**)

```
(define INIT-WORLDSTATE (mk-WorldState 0 0))
```

Produces instances of the struct that are values of the new data definition

Data Design Recipe

Data Definition

- Has **4** parts:
 1. **Name**
 2. Description of **all possible values** of the data
 3. **Interpretation** explaining the real world concepts the data represents
 4. **Predicate** returning **false** for (most?) values **not** in the Data Definition
 - If needed, define extra predicates for each **enumeration** or **itemization**

Data Design Recipe - Compound Data Update

Data Definition (for compound data)

- Has ~~4~~ Has 5 parts:

1. Name
2. Description of **all possible values** of the data
3. Interpretation explaining the real world concepts the data represents
4. Predicate returning **false** for (most?) values not in the Data Definition
 - If needed, define extra predicates for each enumeration or itemization
- 5. (checked) **Constructor** for compound data def values

Data Design Recipe - Compound Data Predicate

Data Definition (for compound data)

- Has 5 parts:
 1. Name
 2. Description of **all possible values** of the data
 3. Interpretation explaining the real world concepts the data represents
 4. **Predicate** returning **false** for (most?) values not in the Data Definition
 - For compound data ...
 5. (checked) **Constructor** for compound data def values

Predicates for Compound Data

```
;; A WorldState is a (mk-WorldState [x : Int] [y : Int])  
;; Represents: coordinate in big-bang animation where:  
;; - x is ball (red solid circle) horizontal center  
;; - y is ball vertical center  
(struct World [x y])
```

predicate?

struct already defines World? ...
but does not enforce field types?

```
(define (WorldState? arg)  
  (and (World? arg)  
        (integer? (World-x arg))  
        (integer? (World-y arg))))
```

???

This “deep” predicate checks too much...

... because it’s the job of “field data type” processing functions to check those kinds of data

Instead, use checked constructor: ensures that only valid instances are created!

```
(define/contract (mk-WorldState x y)  
  (-> integer? integer? WorldState?)  
  (World x y))
```

Also not practical? maybe exponential overhead ...

Compound data predicates should be “shallow” checks, i.e., World?



Data Design Recipe - Predicate Update

Data Definition (for compound data)

- Has 5 parts:
 1. Name
 2. Description of all possible values of the data
 3. Interpretation explaining the real world concepts the data represents
 4. Predicate (shallow, conservative approximation of the Data Def)
 - Evaluates to true for all values in the Data Def ... and maybe some not
 - False positives maybe ok Might let in some invalid values
 - Evaluates to false for (most?) values not in the Data Def ... but maybe not all
 - False negatives not ok Must only reject invalid values
 5. (checked) Constructor for compound data def values

Function Design Recipe

1. **Name**
2. **Signature** – types of the function input(s) and output
3. **Description** – explain (in English prose) the function behavior
4. **Examples** – show (using check-equal?) the function behavior
5. **Template** – sketch out the function structure (using input's **Data Definition**)
6. **Code** – implement the rest of the function (arithmetic)
7. **Tests** – check (using check-equal? and other test forms) the function behavior

Functions For Compound Data

- A function that processes compound data must ...
 - extract the individual pieces, using accessors
 - combine them, with arithmetic

Functions For Compound Data - Template

- A function that processes compound data must

- extract the individual pieces, using accessors ← Done with template
- combine them, with arithmetic

```
;; A WorldState is a (mk-WorldState [x : Int] [y : Int])
(struct World [x y])
(define/contract (mk-WorldState x y)
  (-> integer? integer? WorldState?))
(World x y))
```

```
;; TEMPLATE for WorldState-fn: WorldState -> ???
(define (WorldState-fn w)
  .... (World-x w) ....
  .... (World-y w) .... )
```

A function's template is completely determined by the input's **Data Definition**

Functions For Compound Data - Template

- A function that processes compound data must

- extract the individual pieces, using accessors ← Done with template
- combine them, with arithmetic

```
;; A WorldState is a (mk-WorldState [x : Int] [y : Int])
(struct World [x y])
(define/contract (mk-WorldState x y)
  (-> integer? integer? WorldState?))
  (World x y))
```

A function's template is completely determined by the input's **Data Definition**

```
;; TEMPLATE for WorldState-fn: WorldState -> ????
(define/contract (WorldState-fn w)
  (-> WorldState? ??? )
  .... (World-x w) ....
  .... (World-y w) .... )
```

Function Design Recipe

Still must program with these steps,
in this order!

1. **Name**
2. **Signature** – types of the function input(s) and output
(not submitted in comments,
if there are valid **contracts**)
3. **Description** – explain (in English prose) the function behavior
4. **Examples** – show (using `check-equal?`) the function behavior
(not submitted)
5. **Template** – sketch out the function structure (using input's **Data Definition**)
6. **Code** – implement the rest of the function (arithmetic)
7. **Tests** – check (using `check-equal?` and other test forms) the function behavior

```
;; A WorldState is a (mk-WorldState [x : Int] [y : Int])
(struct World [x y])
(define/contract (mk-WorldState x y)
  (-> integer? integer? WorldState?))
(World x y))
```

```
(check-equal?
  (next-WorldState
    (mk-WorldState 0 0))
  (mk-WorldState X-VEL Y-VEL))
```

(assuming constant velocity)

```
;; next-WorldState : WorldState -> WorldState
;; Computes the ball position after 1 tick
```

```
;; TEMPLATE for WorldState:
(define/contract (WorldState-fn w)
  (-> WorldState? ??? )
  .... (World-x w) ....
  .... (World-y w) .... )
```

```
(check-equal?
  (next-WorldState
    (mk-WorldState 0 0))
  (mk-WorldState X-VEL Y-VEL))
```

```
;; next-WorldState
;; Computes the ball position after 1 tick
```

```
(define/contract (next-WorldState w)
  (-> WorldState? WorldState? )
  .... (World-x w) ....
  .... (World-y w) .... )
```

```
(check-equal?
  (next-WorldState
    (mk-WorldState 0 0))
  (mk-WorldState X-VEL Y-VEL))
```

```
;; next-WorldState
;; Computes the ball position after 1 tick
```

```
(define/contract (next-WorldState w)
  (-> WorldState? WorldState?)
  (mk-WorldState
    (+ (World-x w) X-VEL)
    (+ (World-y w) Y-VEL))))
```

Example + Template helps
to write the function!

Extract Compound Pieces - let

alternatives

See also **let***

```
(define/contract (next-WorldState w)
  ; ...
  (let ([x (World-x w)]
        [y (World-y w)])
    (mk-WorldState (+ x X-VEL) (+ y Y-VEL))))
```

Defines new local variables

in scope only in the body

(let ([id val-expr] ...) body ...+)

Extract all compound data pieces first, before doing “arithmetic”

Local variables **shadow** previously defined vars

Extract Compound Pieces – (internal) **define**

alternatives

```
(define/contract (next-WorldState w)
```

```
; ...
```

```
(define x (World-x w))  
(define y (World-y w))
```

```
(mk-WorldState (+ x X-VEL) (+ y Y-VE)
```

Extract all compound
data pieces first, before
doing “arithmetic”

(is there an easier way to do this?)

Extract Compound Pieces – Pattern Match!

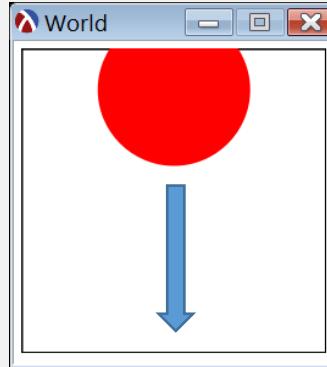
alternatives

```
(define/contract (next-WorldState w)
; ...
(match#define (World x y) w)
```

Extract all compound
data pieces, at the
same time!

```
(mk-WorldState (+ x X-VEL) (+ y Y-VEL))))
```

Falling “Ball” Example



← What if the ball can also move side-to-side ... →

... on a key-press?

WorldState would need two pieces of data:
the **x** and **y** coordinates

Last
Time

Some Pre-defined Enumerations

```
; A KeyEvent is one of:  
; - 1String  
; - "left"  
; - "right"  
; - "up"
```

"KeyEvent"
function

... cannot do
"WorldState"
function "things"!

```
; WorldState KeyEvent -> ...  
(define (handle-key-events w ke)  
  (cond  
    [(= (string-length ke) 1) ...]  
    [(string=? "left" ke) .. (handle-left w) ???]  
    [(string=? "right" ke) .. (handle-right w) ???]  
    [(string=? "up" ke) ...]  
    [(string=? "down" ke) ...]  
    ...))
```

Or even better: **key=?**

(result must be **WorldState**)

WorldState

Give to: **big-bang on-key clause**

Must call separate: "**WorldState fn**"

... to do "WorldState" function "things"

Do not put all code in one function! e.g.,
Do not process "WorldState" data in a
"KeyEvent" function!

But remember:

1 function does
1 task which processes
1 kind of data

Compound Data can be nested

But remember:

1 function does
1 task which processes
1 kind of data

Need a different function (that uses `GameState` template) to process `GameState` data

Uses `KeyEvent` template

```
(define/contract (key-handler g k)
  (-> GameState? key-event? GameState?)
  (cond
    [(key=? k GET-RED) (handle-red-key g)]
    [(key=? k GET-BLUE) (handle-blue-key g)]
    [else w]))
```

Compound Data can be nested

But remember:

1 function does
1 task which processes
1 kind of data

Makes testing easier!

```
(check-equal? (key-handler ANY-GAMESTATE "r")
               (handle-red-key ANY-GAMESTATE))
(check-equal? (key-handler ANY-GAMESTATE "b")
               (handle-blue-key ANY-GAMESTATE))
```

(but still need some “full stack” tests)

```
(define/contract (key-handler g k)
  (-> GameState? key-event? GameState?)
  (cond
    [(key=? k GET-RED) (handle-red-key g)]
    [(key=? k GET-BLUE) (handle-blue-key g)]
    [else w]))
```

Function Design Recipe

- Testing Update

- “Full Stack”

- For “top level” functions
- Tests: all functionality from input to final result
- Should be more comprehensive

```
(check-equal? (key-handler SOME-GAMESTATE1 "r")  
               NEXT-GAMESTATE2)  
  
(check-equal? (key-handler SOME-GAMESTATE3 "b")  
               NEXT-GAMESTATE4)
```

- “Incremental”

- For “helper” (and top level) functions
- Tests: more local functionality – dictated by data design
- delegate to other helpers, should test “control flow” paths

```
(check-equal? (key-handler ANY-GAMESTATE "r")  
               (handle-red-key ANY-GAMESTATE))  
  
(check-equal? (key-handler ANY-GAMESTATE "b")  
               (handle-blue-key ANY-GAMESTATE))
```

A “GameState” data def + function ...

```
;; A GameState is a (hypothetically ...)
;; (mk-GGameState [p1 : Player] [p2 : Player]
;;                 [active : PlayerID])
;; where:
;; - p1 : represents “Player 1” data ...
;; - p2 : represents “Player 2” data ...
;; - active : it’s this player’s turn
```

```
(define/contract (GameState-fn g)
  (-> GameState? .... ))
```

TEMPLATE

```
....  (GameState-p1 g)  ....
....  (GameState-p2 g)  ....
....  (GameState-active g)  .... )
```

(extracts pieces of compound data)

A “GameState” function ...

```
;; A GameState is a (hypothetically ...)
;; (mk-GGameState [p1 : Player] [p2 : Player]
;;                 [active : PlayerID])
;; where:
;; - p1 : represents “Player 1” data ...
;; - p2 : represents “Player 2” data ...
;; - active : it’s this player’s turn
```

```
(define/contract (handle-red-key g)
  (-> GameState? ....)

  ....      (GameState-p1 g)      ....
  ....      (GameState-p2 g)      ....
  ....      (GameState-active g) .... )
```

A “GameState” function ...

```
;; A GameState is a (hypothetically ...)
;; (mk-GGameState [p1 : Player] [p2 : Player]
;;                 [active : PlayerID])
;; where:
;; - p1 : represents “Player 1” data ...
;; - p2 : represents “Player 2” data ...
;; - active : it’s this player’s turn
```

```
(define/contract (handle-red-key g)
  (-> GameState? GameState?)  
  (mk-GGameState
    ....      (GameState-p1 g)      ....
    ....      (GameState-p2 g)      ....
    ....      (GameState-active g) .... ))
```

Look at type(s) to help fill in template

A “GameState” function ...

```
;; A GameState is a (hypothetically ...)  
;; (mk-GGameState [p1 : Player] [p2 : Player]  
;; [active : PlayerID])  
;; where:  
;; - p1 : represents “Player 1” data ...  
;; - p2 : represents “Player 2” data ...  
;; - active : it’s this player’s turn
```

But remember:

**1 function does
1 task which processes
1 kind of data**

```
(define/contract (handle-red-key g)  
  (-> GameState? GameState?)  
  (mk-GGameState  
   ....      (GameState-p1 g)      ....  
   ....      (GameState-p2 g)      ....  
   ....      (GameState-active g) .... ))
```

A “GameState” function ...

```
;; A GameState is a (hypothetically ...)
;; (mk-GGameState [p1 : Player] [p2 : Player]
;;                [active : PlayerID])
;; where:
;; - p1 : represents “Player 1” data ...
;; - p2 : represents “Player 2” data ...
;; - active : it’s this player’s turn
```

But remember:

**1 function does
1 task which processes
1 kind of data**

```
(define/contract (handle-red-key g)
  (-> GameState? GameState?)
  (mk-GGameState
    (Player-fn (GameState-p1 g))
    (Player-fn (GameState-p2 g))
    (PlayerID-fn (GameState-active g))))
```

Don’t do “Player” function “things” in a “GameState” function!

A “GameState” function ...

```
;; A GameState is a (hypothetically ...)  
;; (mk-GGameState [p1 : Player] [p2 : Player]  
;; [active : PlayerID])  
;; where:  
;; - p1 : represents “Player 1” data ...  
;; - p2 : represents “Player 2” data ...  
;; - active : it’s this player’s turn
```

NOTE: don’t “prematurely optimize!”

Programmers waste enormous amounts of time thinking about, or worrying about, the speed of noncritical parts of their programs... We should forget about small efficiencies, say about 97% of the time: premature optimization is the root of all evil.

— Donald Knuth

(define/contract (handle-red-key g)

(can always refactor to be “cleaner” later)

(-> GameState? GameState?)

Pass as many compound data pieces as needed ...

(mk-GGameState

(trust the recipe ... follow the data design ... resist temptation to “prematurely optimize”)

(Player-fn (GameState-p1 g) (GameState-p2 g) (GameState-active g))

(Player-fn (GameState-p2 g) (GameState-p1 g) (GameState-active g))

(PlayerID-fn (GameState-active g) (GameState-p1 g) (GameState-p2 g)))

Data Definition Invariants

```
;; A GameState is a (hypothetically ...)  
;; (mk-GGameState [p1 : Player] [p2 : Player]  
;;                 [active : PlayerID])  
;; where:  
;; - p1 : represents “Player 1” data ...  
;; - p2 : represents “Player 2” data ...  
;; - active : it’s this player’s turn  
(struct GameState [p1 p2 active])
```

```
;; Invariant1: p1 “red” + p2 “red” <= MAX-TOKENS  
;; Invariant2: p1 “blue” + p2 “blue” <= MAX-TOKENS
```

“invariant” = “must always be true!”

Previously

```
(define/contract (mk-GGameState p1 p2 id)  
  (-> Player? Player? PlayerID? GameState?)  
  (GameState p1 p2 id))
```

Can these be “any” Player values?

```
;; A Player is a Assume hypothetically ...  
;; (mk-Player [red : TokenCount]  
;;             [blue : TokenCount])
```

Every function that creates a GameState is responsible for maintaining its invariants!

Can this be automatically checked?

Data Definition Invariants

```
;; A GameState is a (hypothetically ...)  
;; (mk-GGameState [p1 : Player] [p2 : Player]  
;; [active : PlayerID])  
;; where:  
;; - p1 : represents “Player 1” data ...  
;; - p2 : represents “Player 2” data ...  
;; - active : it’s this player’s turn  
(struct GameState [p1 p2 active])
```

Every function that creates a GameState is responsible for maintaining its invariants!

```
;; Invariant1: p1 “red” + p2 “red” <= MAX-TOKENS  
;; Invariant2: p1 “blue” + p2 “blue” <= MAX-TOKENS
```

Can this be automatically checked?

One possibility:
define a separate “output” predicate

With Invariant Check

```
(define/contract (mk-GGameState p1 p2 id)  
  (-> Player? Player? PlayerID? GameState/invariant?)  
  (GameState p1 p2 id))
```

```
(define (GameState/invariant? x)  
  (and (GameState? x)  
        (<= (+ (red-count (GameState-p1 x))  
               (red-count (GameState-p2 x)))  
             MAX-TOKENS)  
        (<= (+ (blue-count (GameState-p1 x))  
               (blue-count (GameState-p2 x)))  
             MAX-TOKENS))))
```

Data Definition Invariants

```
;; A GameState is a (hypothetically ...)  
;; (mk-GGameState [p1 : Player] [p2 : Player]  
;; [active : PlayerID])  
;; where:  
;; - p1 : represents "Player 1" data ...  
;; - p2 : represents "Player 2" data ...  
;; - active : it's this player's turn  
(struct GameState [p1 p2 active])
```

But remember:

- compound data contracts should be “shallow”
- i.e., don’t traverse an entire (nested) data structure
- Programmer must decide what is “too deep”

;; Invariant1: p1 “red” + p2 “red” <= MAX-TOKENS

;; Invariant2: p1 “blue” + p2 “blue” <= MAX-TOKENS

This one probably ok because ...
still “constant” time check

Every function that creates a
GameState is responsible for
maintaining its invariants!

“Dependent”
Contract

Can this be automatically checked?

One possibility:
define a separate “output” predicate

```
(define (GameState/invariant? x)  
  (and (GameState? x)  
        (GameState-red-invariant? x)  
        (GameState-blue-invariant? x)))
```

```
(define/contract (mk-GGameState p1 p2 id)  
  (-> Player? Player? PlayerID? GameState/invariant?)  
  (GameState p1 p2 id))
```

(with better-named helper functions!
Avoid large unreadable boolean
expressions!)

Data Design Recipe - Predicate Update

Data Definition (for compound data)

- Has 5 parts:
 1. Name
 2. Description of **all possible values** of the data
 3. Interpretation explaining the real world concepts the data represents
 4. **Predicate** (shallow, conservative approximation of the Data Def)
 - Evaluates to **true** for all values in the Data Def, and maybe some not
 - False positives maybe ok Might let in some invalid values
 - Evaluates to **false** for (most?) values not in the Data Def, but maybe not all
 - False negatives not ok Must only reject invalid values
 5. (checked) **Constructor** for compound data def values
- 

Follow data definitions whenever possible, but ...

Sometimes you need “if” ... ?

```
(define/contract (key-handler g k)
  (-> GameState? key-event? GameState?))
  (cond
    ...
    [(key=? k SPEND-KEY) (handle-spend g)]
    ...
    [else w])
```

a “GameState” function!

A “GameState” data def + function ...

```
;; A GameState is a (hypothetically ...)
;; (mk-GGameState [p1 : Player] [p2 : Player]
;;                 [active : PlayerID])
;; where:
;; - p1 : represents “Player 1” data ...
;; - p2 : represents “Player 2” data ...
;; - active : it’s this player’s turn
```

```
(define/contract (GameState-fn g)
  (-> GameState? .... ))
```

TEMPLATE

```
....  (GameState-p1 g)  ....
....  (GameState-p2 g)  ....
....  (GameState-active g)  .... )
```

(extracts pieces of compound data)

A “GameState” function ...

```
;; A GameState is a (hypothetically ...)
;; (mk-GGameState [p1 : Player] [p2 : Player]
;;                 [active : PlayerID])
;; where:
;; - p1 : represents “Player 1” data ...
;; - p2 : represents “Player 2” data ...
;; - active : it’s this player’s turn
```

```
(define/contract (handle-spend g)
  (-> GameState? ....)

  ....      (GameState-p1 g)      ....
  ....      (GameState-p2 g)      ....
  ....      (GameState-active g) .... )
```

A “GameState” function ...

```
;; A GameState is a (hypothetically ...)
;; (mk-GGameState [p1 : Player] [p2 : Player]
;;               [active : PlayerID])
;; where:
;; - p1 : represents “Player 1” data ...
;; - p2 : represents “Player 2” data ...
;; - active : it’s this player’s turn
```

```
(define/contract (handle-spend g)
  (-> GameState? GameState?)  
  (mk-GGameState
    ....      (GameState-p1 g)      ....
    ....      (GameState-p2 g)      ....
    ....      (GameState-active g) .... ))
```

Look at type(s) to help fill in template

A “GameState” function ...

```
;; A GameState is a (hypothetically ...)
;; (mk-GGameState [p1 : Player] [p2 : Player]
;;                [active : PlayerID])
;; where:
;; - p1 : represents “Player 1” data ...
;; - p2 : represents “Player 2” data ...
;; - active : it’s this player’s turn
```

But remember:

**1 function does
1 task which processes
1 kind of data**

```
(define/contract (handle-spend g)
  (-> GameState? GameState?))
(mk-GGameState
  ....      (GameState-p1 g)      ....
  ....      (GameState-p2 g)      ....
  ....      (GameState-active g) .... )
```

A “GameState” function ...

```
;; A GameState is a (hypothetically ...)  
;; (mk-GGameState [p1 : Player] [p2 : Player]  
;; [active : PlayerID])  
;; where:  
;; - p1 : represents “Player 1” data ...  
;; - p2 : represents “Player 2” data ...  
;; - active : it’s this player’s turn
```

But remember:

**1 function does
1 task which processes
1 kind of data**

```
(define/contract (handle-spend g)  
  (-> GameState? GameState?)  
  (mk-GGameState  
   (Player-fn (GameState-p1 g))  
   (Player-fn (GameState-p2 g))  
   (PlayerID-fn (GameState-active g))))
```

Don’t do “Player” function “things” in a “GameState” function!

A “GameState” function needs “Player” fn

```
(define/contract (handle-spend g)
  (-> GameState? GameState?))
(mk-GameState
  (player-spend (GameState-p1 g)) (assuming this is “active” player)
  (Player-fn (GameState-p2 g))
  (PlayerID-fn (GameState-active g))))
```

A “Player” function ...

```
;; A Player is a Assume hypothetically ...
;; (mk-Player [red : TokenCount]
;;             [blue : TokenCount])
```

```
(define/contract (player-fn p)
  (-> Player? ....)

    .... (Player-red p) ....)
    .... (Player-blue p) ....))
```

(template)

A “Player” function ...

Are there any invariants to maintain?

Player should only “spend” if they have sufficient tokens, e.g., 1 red and 1 blue

“Dependent” contract won’t suffice here
... because we don’t want to error

We really need “if”!

```
(define/contract (player-spend p)
  (-> Player? Player?)
  (mk-Player
    (spend-token (Player-red p))
    (spend-token (Player-blue p))))
```

(from hw1)

A “Player” function ...

(not great)
Don't write this!

No giant boolean expressions!

```
(define/contract (player-spend p)
  (-> Player? Player?)
  (if (and (not (zero? (Player-red p)))
            (not (zero? (Player-blue p))))
      (mk-Player
        (spend-token (Player-red p))
        (spend-token (Player-blue p))))
```

Are there any invariants to maintain?

Player should only “spend” if they have sufficient tokens, e.g., 1 red and 1 blue

“Dependent” contract won’t suffice here
... because we don’t want to error

We really need “if”!

A ““Player” function ...

(not great)
Don't write this!

Name doesn't accurately describe
what the function does!

```
(define/contract (player-spend p)
  (-> Player? Player?)
  (if (can-spend? .... )
      (mk-Player
       (spend-token (Player-red p))
       (spend-token (Player-blue p))))
      ))
```

Are there any invariants to maintain?

Player should only “spend” if they have sufficient tokens, e.g., 1 red and 1 blue

“Dependent” contract won’t suffice here
... because we don’t want to error

We really need “if”!

A ““Player” function ...

Write this!

Name accurately describes what the function does!

```
(define/contract (player-maybe-spend p)
  (-> Player? Player?)
  (if (can-spend? p)
    (player-spend p)
    p))
```

Are there any invariants to maintain?

Player should only “spend” if they have sufficient tokens, e.g., 1 red and 1 blue

“Dependent” contract won’t suffice here ... because we don’t want to error

We really need “if”!

Function Design Recipe - “if” edition

- Avoid if possible ...
 - Most of the time, function can follow some data definition template!
- Sometimes needed ...
 - E.g., to enforce compound invariants, without error
- Use helper predicate(s) to clearly describe invariant
 - E.g., “can-spend?”
 - No huge, unreadable boolean expressions!
- Function name and purpose stmt must indicate “if” usage!
 - E.g., “maybe-”
- 1 per function only
 - no nested “if”s!

Random

Ball Animation

Design a **big-bang** animation that:

- Start: a single ball, moving with **random x and y velocity**

Randomness

[bracketed args] = optional

(**random** *k* [*rand-gen*]) → exact-nonnegative-integer?

k : (integer-in 1 4294967087)

rand-gen : pseudo-random-generator?

= (current-pseudo-random-generator)

When called with an integer argument *k*, returns a random exact integer in the range 0 to *k*-1.

Optional arg Default value

(**random** *min* *max* [*rand-gen*]) → exact-integer?

min : exact-integer?

max : (integer-in (+ 1 *min*) (+ 4294967087 *min*))

rand-gen : pseudo-random-generator?

= (current-pseudo-random-generator)

When called with two integer arguments *min* and *max*, returns a random exact integer in the range *min* to *max*-1.

“random” is not random???

Not secure!
e.g., for generating
passwords

A pseudorandom number generator (PRNG), also known as a deterministic random bit generator (DRBG),^[1] is an algorithm for generating a sequence of numbers whose properties approximate the properties of sequences of random numbers. The PRNG-generated sequence is not truly random, because it is completely determined by an initial value, called the PRNG's seed

VS

A cryptographically secure pseudorandom number generator (CSPRNG) or cryptographic pseudorandom number generator (CPRNG) is a pseudorandom number generator (PRNG) with properties that make it suitable for use in cryptography.

Random Functions: Same Recipe (almost)!

```
;; A Velocity is a non-negative integer  
;; Interp: represents pixels/tick change in a ball coordinate  
(define MAX-VELOCITY 10)
```

```
;; random-velocity : -> Velocity  
;; returns a random velocity between 0 and MAX-VELOCITY  
(define (random-velocity)  
  (random MAX-VELOCITY))
```

Functions can have zero args

Random functions have no examples

```
(check-true (< (random-velocity) MAX-VELOCITY))  
(check-true (>= (random-velocity) 0))  
(check-true (integer? (random-velocity)))  
(check-pred (λ (v) (and (integer? v)  
                           (< v MAX-VELOCITY)  
                           (>= v 0)))  
            (random-velocity))
```

Can still **test!**
Just less precise

```
;; random-x      : -> ???  
;; random-y      : -> ???  
;; random-ball   : -> ???
```