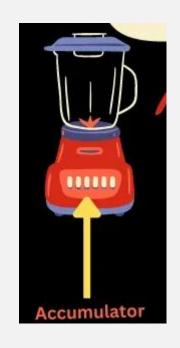
UMass Boston Computer Science CS450 High Level Languages Accumulators

Thursday, March 6, 2025



Logistics

- HW 5 out
 - <u>Due</u>: Tues 3/11 11am EST
 - Yes: cons, first, rest, empty, list, empty?
 - No: map, fold, filter, etc
 - 1 if allowed, if following multi-arg recipe



HW Minimum Submission Requirements

• "main" runs without errors

Tests run without errors

- 100% (Test / Example) "Coverage"
 - In "Choose Language" Menu
 - NOTE: only works with single files

```
Dynamic Properties
No debugging or profiling Debugging and profiling
Debugging

    Syntactic test suite coverage

☐ Populate "compiled" directories (for faster loading)

☑ Preserve stacktrace (disable some optimizations)

Enforce constant definitions (enables some inlining)
Submodules to Run ▼
  ;; YCoord is either

    before target

                        This code was not run
     - in target
     - after target
   :: - out of scene
  (define (PENDING-Note? n) (PENDING? (Note-state n)
  (define (HIT-Note? n) (HIT? (Note-state n)))
  (define (MISSED-Note? n) (MISSED? (Note-state n)))
  (define (OUTOFSCENE-Note? n) (OUTOFSCENE? (Note-state n)))
  (define out-Note? OUTOFSCENE-Note?)
  :: NEW
  ;; A WorldState is a List<Note>
```

(define (num-Notes w) (length w

Common List Function #1: map

```
map: (X -> Y) Listof<X> -> Listof<Y>
Produces a list resulting from applying
   a given fn to each element of a given 1st
(define (map fn lst)
  (cond
    [(empty? lst) empty]
     [else (cons (fn (first lst))
                   (map (rest lst))))))
```

```
function "application"
(in high-level languges)
= function "call"
(in imperative languages)
```

```
(map proc lst ...+) \rightarrow list?
                                                                     procedure
  proc : procedure?
  lst : list?
```

Applies *proc* to the elements of the *lsts* from the first elements to the last. The proc argument must accept the same number of arguments as the number of supplied lsts, and all lsts must have the same number of elements. The result is a list containing each result of *proc* in order.

Examples:

```
> (map (lambda (number1 number2)
         (+ number1 number2))
       '(1 2 3 4)
       '(10 100 1000 10000))
'(11 102 1003 10004)
```

RACKET's map can take multiple lists!























map in other high-level languages

Array.prototype.map()

The map() method of Array instances creates a new array populated with the results of calling a provided function on every element in the calling array.

```
JavaScript Demo: Array.map()

1   const array1 = [1, 4, 9, 16];

2   // Pass a function to map
4   const map1 = array1.map((x) => x * 2);

5   console.log(map1);
7   // Expected output: Array [2, 8, 18, 32]

Lambda
("arrow function expression")
```

Python3

```
# Add two lists using map and lambda

numbers1 = [1, 2, 3]
numbers2 = [4, 5, 6]

lambda

result = map(lambda x, y: x + y, numbers1, numbers2)
print(list(result))
```

Common List Function #2: fold1 / foldr

```
;; foldr: (X Y -> Y) Y Listof<X> -> Y
  Computes a single value from given list, determined by given fn and initial val.
;; fn is applied to each list element, last-element-first
(define (foldr fn initial lst)
                                                         (1 + (2 + (3 + 0)))
  (cond
   [(empty? lst) initial]
   [else (fn (first lst) (foldr fn initial (rest lst)))]))
;; foldl: (X Y -> Y) Y Listof<X> -> Y
  Computes a single value from given list, determined by given fn and initial val.
  fn is applied to each list element, first-element-first
                                                            ((1 + 0) + 2) + 3)
(define (foldl fn result-so-far lst)
                                                            (((1 - 0) - 2) - 3)
  (cond
   [(empty? lst) result-so-far]
   [else (foldl fn (fn (first lst) result-so-far) (rest lst)))]))
```

Last Time

fold (reduce) in other high-level languages

```
JavaScript Demo: Array.reduce()
1 const array1 = [1, 2, 3, 4];
                                                       lambda
                                                                                  "initial"
                            "list"
  const initialValue = 0;
  const sumWithInitial = array1.reduce((resultSoFar, x) \stackrel{\forall}{=} resultSoFar + x, initial);
  console.log(sumWithInitial);
   // Expected output: 10
                                         JavaScript Demo: Array.reduceRight()
                                          1 const array1 = [
                                              [0, 1],
                                              [2, 3],
                                              [4, 5],
                                                                                                        "initial" optional?
                                          7 const result = array1.reduceRight((resultSoFar, x) => resultSoFar.concat(x));
                                          9 console.log(result);
                                            // Expected output: Array [4, 5, 2, 3, 0, 1]
                                         11
```

Fold "dual": build-list

```
(build-list \ n \ proc) \rightarrow list? procedure n: exact-nonnegative-integer? proc: (exact-nonnegative-integer? . -> . any)
```

Creates a list of n elements by applying proc to the integers from 0 to (sub1 n) in order. If lst is the resulting list, then (list-ref lst i) is the value produced by (proc i).

Examples:

```
> (build-list 10 values)
'(0 1 2 3 4 5 6 7 8 9)
> (build-list 5 (lambda (x) (* x x)))
'(0 1 4 9 16)
```

```
(build-list 4 add1)

;; = (map add1 (list 0 1 2 3))

;; = (list 1 2 3 4)
```

Fold "alternative": apply (with "variable-arity" fns)

- apply applies its fn argument to the contents of its list arg
- function arg must accept:# of arguments = <u>length</u> of list arg

Common list function #3: filter

```
;; filter: (X -> Boolean) Listof<X> -> Listof<X>
     ;; Returns a list containing elements of given list
     ;; for which the given predicate returns true
     (define (filter pred? lst)
       (cond
        [(empty? lst) empty]
        [else (if (pred? (first lst))
                    (cons (first lst) (filter pred? (rest lst)))
pred and lst must be
                    (filtent pred? (rest lst))))))
processed together.
so 1 if allowed here
                       .filter (

)
```

filter in other high-level languages

```
JavaScript Demo: Array.filter()

1   const words = ['spray', 'limit', 'elite', 'exuberant', 'destruction', 'present'];
2   const result = words.filter((word) => word.length > 6);
4   console.log(result);
6   // Expected output: Array ["exuberant", "destruction", "present"]
7
```

Common list function #3: filter

```
;; filter: (X -> Boolean) Listof<X> -> Listof<X>
                                          lambda rules:
  Returns a list containing elements of
                                           - Can skip the design recipe steps,
;; for which the given predicate returns
                                             <u>BUT</u>
(define (filter pred? lst)
                                            name, description, and signature
  (cond
                                             must be "obvious"
   [(empty? lst) empty]
                                           - code is arithmetic only
   [else (if (pred? (first lst))
             (cons (first lst) (filter pre
                                             otherwise, create standalone
             (filter pred? (rest lst)))])
                                             function define
```

```
;; smaller-than: Listof<Int> Int -> Listof<Int>
;; Returns a list containing elements of given list less than the given int

(define (smaller-than lst thresh)
    (filter (lambda (x) (< x thresh)) lst)

lambda creates an anonymous "inline" function (expression)</pre>
```

Another Useful List Function: andmap

```
"all"
```

"every"

```
> (andmap positive? '(1 2 3))
#t
```

```
> (andmap positive? '(1 -2 a))
#f
```

```
      (andmap p? 1st)
      similar to:
      (apply and (map p? 1st))
      But (won't run): and map is "short circuiting"

      But (won't run): and is not a function
```

(foldl (λ (x y) (and x y)) #t lst)

See also: ormap

"any", "some"

Function design recipe:

- 1. Name
- 2. Signature
- 3. Description
- 4. Examples
- 5. Template

• • •

```
;; lst-max : Listof<Int> -> Int
;; Returns the largest number in the given list
```

```
1. Name
2. Signature
3. Description
4. Examples
5. Template
....

;; lst-max : Listof<Int> -> Int
Returns the largest number in the given list
```

Function design recipe:

```
(check-equal?
  (lst-max (list)) ???))
```

(lst-max (list 1 2 3)) 3))

(check-equal?

Function design recipe: 1. Name 2. Signature 3. Description 4. Examples 5. Template ...

Function design recipe:

- 1. Name
- 2. Signature
- 3. Description
- 4. Examples
- 5. Template

• • •

Function design recipe:

- 1. Name
- 2. Signature
- 3. Description
- 4. Examples
- 5. Template

• • •

Design Recipe For <u>Accumulator</u> Functions

When a function needs "extra information":

- 1. Specify accumulator:
 - Name
 - Signature
 - Invariant
 - A property of the accumulator that is always true

```
lst-max : Listof<Int> Int -> Int
  Returns the largest number in the given list
   accumulator max-so-far : Int
  invariant: is the largest val in 1st "so far"
(define (lst-max lst max-so-far)
  (cond
                              Need extra information?
    [(empty? lst) ???]
    [(cons? lst) .... (first lst) ....
       .... (1st-max (rest 1st)) ....]))
```

```
lst-max : Listof<Int> Int -> Int
  Returns the largest number in the given list
  accumulator max-so-far : Int
;; invariant: is the largest val in lst "so far"
(define (lst-max lst max-so-far)
  (cond
                              Need extra information?
    [(empty? lst) ???]
    [(cons? lst) .... (first lst) ....
       .... (1st-max (rest 1st)) ....]))
```

```
lst-max : Listof<Int> Int -> Int
  Returns the largest number in the given list
;; accumulator max-so-far : Int
;; invariant: is the largest val in 1st "so far"
(define (lst-max lst max-so-far)
  (cond
    [(empty? lst) max-so-far]
    [(cons? lst) .... (first lst) ....
       .... (1st-max (rest 1st)) ....]))
```

But this is not the same function as before!

Design Recipe For <u>Accumulator</u> Functions

When a function needs "extra information":

- 1. Specify accumulator:
 - Name
 - Signature
 - Invariant
 - A property of the accumulator that is always true
- 2. Define internal "helper" fn with extra accumulator arg (Helper fn does <u>not</u> need extra description, statement, or examples, if they are the same ...)
- 3. Call "helper" fn , with initial accumulator value, from original fn

```
Function needs "extra information" ...
 lst-max : List<Int> -> Int
  Returns the largest value in the given list
(define (lst-max initial-lst)
  ;; lst-max/accum : List<Int> Int -> Int
                                        1. Specify accumulator: name, signature, invariant
    accumulator max-so-far : Int
    invariant: is the largest val in initial-lst "so far"
  (define (lst-max/accum lst max-so-far)
    (cond
                                    2. Define internal "helper" fn with accumulator arg
      [(empty? lst) max-so-far]
      [else (lst-max/accum (rest lst)
                          (max (first lst) max-so-far))])
```

```
lst-max : List<Int> -> Int
  Returns the largest value in the given list
(define (lst-max initial-lst)
  ;; lst-max/accum : List<Int> Int -> Int
     accumulator max-so-far : Int
    invariant: is the largest val in initial-lst
                                                   "so far"
  (define (lst-max/accum lst max-so-far)
    (cond
      [(empty? lst) max-so-far]
      [else (lst-max/accum (rest lst)
                            (max (first lst) max-so-far))])
```

3.Call "helper" fn, with initial accumulator (and other args)

```
(lst-max/accum ( initial-lst) (first initial-lst) ))
```

```
;; lst-max : List<Int> -> Int
  Returns the largest value in the given list
(define (lst-max initial-lst)
  ;; lst-max/accum : List<Int> Int -> Int
    accumulator max-so-far : Int
    invariant: is the largest val in initial-lst
                                                   "so far"
  (define (lst-max/accum lst max-so-far)
    (cond
      [(empty? lst) max-so-far]
      [else (lst-max/accum (rest lst)
                            (max (first lst) max-so-far))])
```

3.Call "helper" fn, with initial accumulator (and other args)

```
;; lst-max : NonEmptyList<Int> -> Int
  Returns the largest value in the given list
(define (lst-max initial-lst)
  ;; lst-max/accum : List<Int> Int -> Int
    accumulator max-so-far : Int
  ;; invariant: is the largest val in initial-lst
                                                   "so far"
  (define (lst-max/accum lst max-so-far)
    (cond
      [(empty? lst) max-so-far]
      [else (lst-max/accum (rest lst)
                            (max (first lst) max-so-far))])
                                      (first initial-lst)
  (lst-max/accum (rest initial-lst)
```

```
;; lst-max : NonEmptyList<Int> -> Int
  Returns the largest value in the given list
(define (lst-max initial-lst)
                                            Helper needs signature, etc if different
  ;; lst-max/accum : List<Int> Int -> Int
     accumulator max-so-far : Int
    invariant: is the largest val in initial-lst "so far"
  (define (lst-max/accum lst max-so-far)
    (cond
      [(empty? lst) max-so-far]
       [else (lst-max/accum (rest lst)
                            (max (first lst) max-so-far))])
                                       (first initial-lst)
  (lst-max/accum (rest initial-lst)
```

```
;; lst-max : NonEmptyList<Int> -> Int
  Returns the largest value in the given list
(define (lst-max initial-lst)
  ;; lst-max/accum : List<Int> Int -> Int
                                                       Invariant should be specific
    accumulator max-so-far : Int
    invariant: is the largest val in initial-lst "minus" lst
  (define (lst-max/accum lst max-so-far)
    (cond
      [(empty? lst) max-so-far]
      [else (lst-max/accum (rest lst)
                            (max (first lst) max-so-far))])
                                       (first initial-lst)
  (lst-max/accum (rest initial-lst)
```

```
;; lst-max : NonEmptyList<Int> -> Int
  Returns the largest value in the given list
(define (lst-max lst0)
  ;; lst-max/a : List<Int> Int -> Int
    accumulator max-so-far : Int
    invariant: is the largest val in lst0 "minus" rst-lst
  (define (lst-max/a rst-lst max-so-far)
    (cond
      [(empty? rst-lst) max-so-far]
      [else (lst-max/accum (rest lst)
                            (max (first lst) max-so-far))])
  (lst-max/a (rest lst0) (first lst0)))
```

Can Implement with ...

X

map?

filter?

fold ? ✓

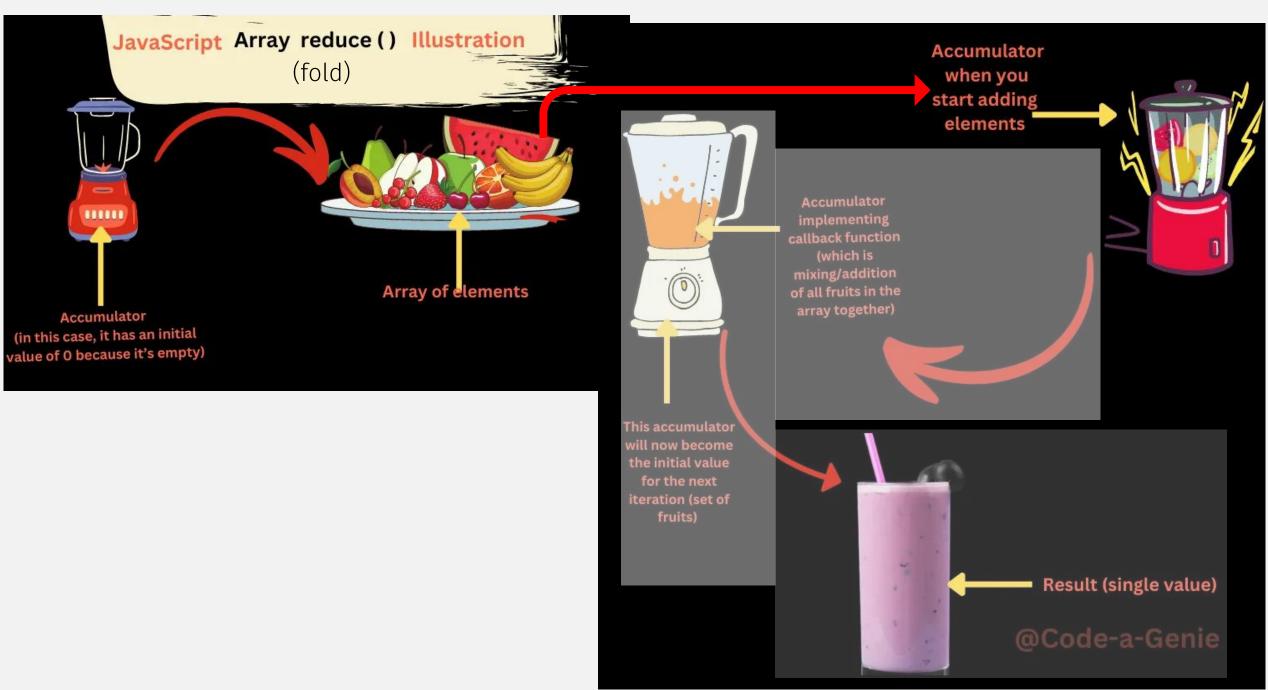
Common List Function: fold1

```
;; foldl: (X Y -> Y) Y Listof<X> -> Y
  Computes a single value from given list,
  determined by given fn and initial val.
;; fn is applied to each list element, first-element-first
(define (foldl fn result-so-far lst)
                                     Accumulator!
  (cond
                                                     Update the accumulator
   [(empty? lst) result-so-far]
   [else (foldl fn (first lst) result-so-far) (rest lst)))))
        .reduce (acc + curr) →
```

```
;; sum-lst: ListofInt -> Int
(define (sum-lst lst) (foldl + ∅ lst))
```

$$(((1 + 0) + 2) + 3)$$

$$(((1 - 0) - 2) - 3)$$



In-class Coding 3/6: Accumulators

```
rev : List<X> -> List<X>
  Returns the given list with elements in reverse order
(define (rev lst0)
     accumulator ??? : ???
                                      1. Specify accumulator: name, signature, invariant
     invariant: ???
  (define (rev/a lst acc ???)
                                  2. Define internal "helper" fn with accumulator arg
     555
  (rev/a lst0 ???))
                                          3.Call "helper" fn, with initial accumulator
```