# Defining tissue specific gene sets using Bayesian unsupervised clustering

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## Stephen Coleman 940309160050

supervised by

Bas Zwaan

Laboratory of Genetics, Wageningen University
and
Chris Wallace

Department of Medicine, Cambridge University

#### **Abstract**

A priori defined gene sets are key to gene set enrichment analysis [20] a powerful tool in genetic analysis. Gene sets are constructed through linking genes by some common feature. This can be a function, the location of the gene product, the participation of the product in some metabolic or signalling pathway, the protein structure, the presence of transcription-factor-binding sites or other regulatory elements, the participation in multiprotein complexes, or any one of several other definitions [21][20][7][1]. However, all of these criteria are tissue agnostic. We propose to produce tissue specific gene sets by applying multiple dataset integration [8] (a Bayesian unsupervised clustering method) to the gene expression data from the CEDAR cohort [23], a dataset of 9 tissue / cell types.

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## 1 Introduction

This project, which consists of applying a Bayesian unsupervised clustering method across multiple datasets to define tissue specific gene sets, is interesting on a number of fronts. It provides a chance to learn relevant, topical biology in understanding gene sets, the role context plays in gene expression and to learn the basics of immunology. From an informatics / statistics perspective, Bayesian inference, unsupervised clustering and the use of multiple datasets are all interesting. These are relevant skills to both industry and research that I wish to develop.

Beyond developing new skills, this project also offers the opportunity to be involved in relevant research. Gene sets are commonly used in genetic analyses, thus if we can produce sets that are informed by the context of interest, it could be relevant to many researchers. Hopefully by producing more informative gene sets we can help narrow the gap between biology and disease.

## 2 Theory

## 2.1 Clustering

Given data  $X = (x_1, ..., x_n)$ , we define a *clustering* or partition of the data by:

$$Y = \{Y_1, \dots, Y_K\} \tag{1}$$

$$Y_k = \{x_{1_k}, \dots, x_{n_k}\}$$
 (2)

$$Y_i \cap Y_j = \emptyset \ \forall \ i, j \in \{1, K\}, i \neq j$$
 (3)

$$n_k \geq 1 \ \forall \ k \in \{1, K\} \tag{4}$$

$$\sum_{k=1}^{K} n_k = n \tag{5}$$

In short we have K nonempty disjoint sets of data, each of which is referred to as a *cluster*, the set of which form a *clustering*. We define a *label*  $c = (c_1, ..., c_n)$  as denoting the membership of each point. A label  $c_i = k$  states that point  $x_i$  is assigned to cluster  $Y_k$ .

#### 2.2 Mixture models

Given some data  $X = (x_1, ..., x_n)$ , we assume a number of unobserved processes generate the data, and membership to a process for individual i is represented using the latent variable  $c_i$ . It is assumed that each of the K processes can be modelled by a parametric distribution,  $f(\cdot)$  with associated parameters  $\theta$  and that the full model density is then the weighted sum of these probability density functions where the

weights are the component proportions,  $\pi_k$ :

$$p(x_i) = \sum_{k=1}^{K} \pi_k f(x_i | \theta_k)$$
 (6)

## 2.3 Bayesian inference

We carry out Bayesian inference of this model using Markov chain Monte Carlo methods. We sample first the component parameters,  $\theta_k$ , and associated weights,  $\pi_k$ , from the associated distributions and then sample component membership. Basically:

- 1. For each of K clusters sample  $\theta_k$  and  $\pi_k$  from the associated distributions based on current memberships,  $c_i$ ; and
- 2. For each of n individuals sample  $c_i$  based on the new  $\theta_k$  and  $\pi_k$ .

For the mixture model we update the parameters after we allocate each observation to a cluster. For a given cluster with associated data X and parameter  $\theta$ , we sample  $\theta$  using Bayes' theorem from the distribution:

$$p(\theta|X) = \frac{p(X|\theta)p(\theta)}{\int_{\Theta} p(X|\theta')p(\theta')d\theta'}$$
(7)

Here  $\Theta$  is the entire sample space for  $\theta$ .

- We refer to  $p(\theta|X)$  as the *posterior* distribution of  $\theta$  as it is the distribution associated with  $\theta$  *after* observing X.
- $p(\theta)$  is the *prior* distribution of  $\theta$  and captures our beliefs about  $\theta$  before we observe X.
- $p(X|\theta)$  is the *likelihood* of X given  $\theta$ , the probability of data X being generated given our model is true. It is the criterion we focus on in our model if we would use a frequentist approach to the inference; maximising this quantity in our model generates the curve that best describes the observed data.
- $\int_{\Theta} p(X|\theta')p(\theta')d\theta'$  is the *normalising constant*. This quantity is also referred to as the *evidence* [11] or *marginal likelihood* and is normally represented by Z. It is referred to as the marginal likelihood as we marginalise the parameter  $\theta$  by integrating over its entire sample space.

In terms of sampling, the prior is very useful as a clever choice of prior can ensure that the posterior is always solvable, that we do not encounter singularities in our distribution.

## 2.4 Multiple dataset integration

Consider the case when we have observed paired datasets  $X_1 = (x_{1,1}, \dots, x_{n,1}), X_2 = (x_{1,2}, \dots, x_{n,2})$ , where observations in the *i*th row of each dataset represent information about the same individual. We would like to cluster individuals using information common to both datasets. One could concatenate the datasets, adding additional covariates for each individual. However, if the two datasets have different clustering structures this would reduce the signal of both clusterings and probably have one dominate. If the two datasets have the same structure but different signal-to-noise ratios this would reduce the signal in the final clustering. In both these cases independent models on each dataset would be preferable. Kirk et al. [8] suggest a method to carry out clustering on both datasets where common information is used but two individual clusterings are outputted. This method is driven by the allocation prior:

$$p(c_{i1}, c_{i2}|\phi) \propto \pi_{i1}\pi_{i2}(1 + \phi \mathbb{I}(c_{i1} = c_{i2}))$$
 (8)

Here  $\phi \in \mathbb{R}_+$  controls the strength of association between datasets. (8) states that the probability of allocating individual i to component  $c_{i,1}$  in dataset 1 and to component  $c_{i,2}$  in dataset 2 is proportional to the proportion of these components within each dataset and up-weighted by  $\phi$  if the individual has the same labelling in each dataset. Thus as  $\phi$  grows the correlation between the clusterings grow and we are more likely to see the same clustering emerge from each dataset. Conversely if  $\phi = 0$  we have independent mixture models.

The generalised case for L datasets,  $X_1 = (x_{1,1}, \dots, x_{n,1}), \dots, X_L = (x_{1,l}, \dots, x_{n,l})$  for any  $L \in \mathbb{N}$  is simply a matter of combinatorics. In this case, (8) extends to:

$$p(c_{i1},\ldots,c_{iL}|\boldsymbol{\phi}) \propto \left[\prod_{l_1=1}^{L} \pi_{c_{il_1}l_1}\right] \left[\prod_{l_2=1}^{L-1} \prod_{l_3=l_2+1}^{L} \left(1 + \phi_{l_2l_3} \mathbb{1}(c_{il_2} = c_{il_3})\right)\right]$$
(9)

Here  $\phi$  is the  $\binom{L}{2}$ -vector of all  $\phi_{ij}$  where  $\phi_{12}$  is the variable  $\phi$  in (8).

Thus MDI is an extension of mixture models to multiple datasets where correlated clustering structure is used to "upweigh" similar clusters across datasets. MDI has been applied to precision medicine, specifically glioblastoma sub-typing [19], in the past showing its potential as a tool.

#### 2.5 Rand index

A popular metric for comparing the similarity of two clusterings of the data is the *Rand index* [18]. If one assumes that all points are of equal importance in determining clusterings, then in combination with the discrete nature of clusters and the fact that a cluster is defined as much by what it does not contain as that which it does, Rand [18] proposes a metric to measure similarity between clusterings. Between

Table 1: Contingency table used by Rand [18] to calculate a measure of similarity between clusterings Y and Y'.

clusterings Y and Y' for any two points  $x_i$  and  $x_j$  there can exist one of a number of scenarios regarding their labeling. Let  $\gamma_{ij}$  be a measure between the two points  $x_i$  and  $x_j$ . For the two points, they can have:

- 1. the same label in both clusterings ( $c_i = c_j \wedge c_i' = c_i'$ ) ( $\gamma_{ij} = 1$ );
- 2. different labels in both ( $c_i \neq c_j \land c_i' \neq c_j'$ ) ( $\gamma_{ij} = 1$ ); or
- 3. the same label in one but not in the other  $(c_i \neq c_j \land c_i' = c_j' \lor c_i = c_j \land c_i' \neq c_j')$   $(\gamma_{ij} = 0)$ .

Thus Rand [18] propose counting the number of times any two points have one of 1 or 2 from list 2.5 and finding the proportion of these compared to the number of all possible point combinations. More formally, this is:

$$A\binom{n}{2}^{-1} = \frac{1}{\binom{n}{2}} \sum_{i=1}^{n-1} \sum_{j=i+1}^{n} \gamma_{ij}$$
 (10)

This can be envisioned as a  $K \times K'$  contingency table of the count of overlapping points, as shown in table 1. Table 1 uses the following notation:

- $n_{ij}$  is the number of points that have membership in  $Y_i$  in clustering Y and  $Y'_j$  in clustering Y';
- $n_{.j}$  is the number of points in cluster  $Y'_{j}$  in clustering Y';
- $n_i$  is the number of points in cluster  $Y_i$  in clustering Y; and
- n = n is the number of points in clusterings Y and Y'.

One can restate equation 10 in terms of the notation from table 1 citeBrennanLight:

$$A = \binom{n}{2} + \sum_{i=1}^{K} \sum_{j=1}^{K'} n_{ij}^2 - \frac{1}{2} \left( \sum_{i=1}^{K} n_{i\cdot}^2 + \sum_{j=1}^{K'} n_{\cdot j}^2 \right)$$
 (11)

$$= \binom{n}{2} + 2\sum_{i=1}^{K} \sum_{j=1}^{K'} \binom{n_{ij}}{2} - \left[\sum_{i=1}^{K} \binom{n_{i.}}{2} + \sum_{j=1}^{K'} \binom{n_{.j}}{2}\right]$$
(12)

Hubert and Arabie [5] extend the Rand index to account for chance. They include a null hypothesis and assume that there is a probability of some points having a  $\gamma$  value of 1 by chance. Consider the scenario where a point  $x_i$  has the same label as another point  $x_j$  under clustering Y. For another clustering Y', there a non-zero is a probability  $c_i' = c_j'$  purely by chance and does not represent a similarity between Y and Y'. If one generates two clusterings Y and Y' by sampling from the integers in the closed interval [1, K] (i.e. by sampling from discrete unfirom distribution  $\mathcal{U}\{1, K\}$ ), then the contingency table generated is constructed from the generalised hyper-geometric distribution [5]. It can be shown that the expected number of points with common membership in both clusters is non-zero. Specifically:

$$\mathbb{E}\left(\sum_{i=1}^{K}\sum_{j=1}^{K} \binom{n_{ij}}{2}\right) = \frac{\sum_{i=1}^{K} \binom{n_{i\cdot}}{2} \sum_{j=1}^{K} \binom{n_{\cdot j}}{2}}{\binom{n}{2}}$$
(13)

This is the product of the number of distinct pairs that can be formed from rows and the number of distinct pairs that can be constructed from columns, divided by the total number of pairs.

For a particular cell of the contingency table, the expected number of entries of the type described in point 1, is the product of number of pairs in its row and in its column divided by the total number of possible pairs:

$$\mathbb{E}\left(\binom{n_{ij}}{2}\right) = \frac{\binom{n_{i\cdot}}{2}\binom{n_{\cdot j}}{2}}{\binom{n}{2}} \tag{14}$$

One can see that as each component of equation 11 is some transformation of  $\sum_{i,j} \binom{n_{ij}}{2}$ , one can directly state the expected value of the Rand index by combining equations 11 and 14:

$$\mathbb{E}\left(A\binom{n}{2}^{-1}\right) = 1 + 2\sum_{i=1}^{K} \binom{n_{i\cdot}}{2} \sum_{j=1}^{K'} \binom{n_{\cdot j}}{2} \binom{n}{2}^{-2} - \left[\sum_{i=1}^{K} \binom{n_{i\cdot}}{2} + \sum_{j=1}^{K'} \binom{n_{\cdot j}}{2}\right] \binom{n}{2}^{-1} (15)$$

Defining an index corrected for chance as:

$$Corrected index = \frac{Index - Expected index}{Maximum index - Expected index}$$
 (16)

Asusming a maximum value of 1 for the Rand index then gives a corrected Rand index:

$$\frac{\sum_{i=1}^{K} \sum_{j=1}^{K'} \binom{n_{ij}}{2} - \sum_{i=1}^{K} \binom{n_{i\cdot}}{2} \sum_{j=1}^{K'} \binom{n_{\cdot j}}{2} \binom{n}{2}^{-1}}{\frac{1}{2} \left[\sum_{i=1}^{K} \binom{n_{i\cdot}}{2} + \sum_{j=1}^{K'} \binom{n_{\cdot j}}{2}\right] - \sum_{i=1}^{K} \binom{n_{i\cdot}}{2} \sum_{j=1}^{K'} \binom{n_{\cdot j}}{2} \binom{n}{2}^{-1}}$$
(17)

We define this quantity described in equation 17 as the *adjusted Rand index* and we use it as our measure of choice for similarity between clusterings.

We describe an explicit example motivating the adjusted Rand index in section 2.5.1.

Y'	$Y_1'$	$Y_2'$	$Y_3'$	Sums
$Y_1$	$\frac{n}{2}$	$\frac{n}{16}$	$\frac{n}{16}$	$\frac{10n}{16}$
$Y_2$	$\frac{\overline{n}}{16}$	$\frac{n}{16}$	$\frac{n}{16}$	$\frac{3\tilde{n}}{16}$
$Y_3$	$\frac{n}{16}$	$\frac{\overline{n}}{16}$	$\frac{n}{16}$	$\frac{3\tilde{n}}{16}$
Sums	10n 16	<u>3n</u> 16	<u>3n</u>	$\frac{16n}{16} = n$

Table 2: Contingency table for the non-random clustering described in section ??.

#### 2.5.1 Motivating example: adjusted Rand index

Consider the case of n labels Y and Y' generated from  $\mathcal{U}\{1,3\}$  where n is some arbitrarily large number. Then as n tends to infinity we can expect that our contingency table has entries of  $\frac{n}{Q}$  in each cell. If one calculates the Rand index on these random partitions where any similarity is purely by chance one finds, it comes to (approximately) 0.56. This suggests there is some similarity between Y and Y', but this is misleading as we know any similarity is stochastic. In the same scenario the adjusted Rand index between the partitions is 0. This seems preferable. Based on this, one could argue that the Rand index has inflated values. Consider the case that we have n points in total, but we let the first  $\frac{7n}{16}$  have a common label (say  $(c_1,\ldots,c_{n_1})=1$  for  $n_1=\frac{7n}{16}$ ) and then draw the remaining  $\frac{9n}{16}$  points from  $\mathcal{U}\{1,3\}$ . Then, as n tends to infinity, our contingency table tends to that described in table 2. One feels that the high Rand index for such a clustering, 0.64, is misleading in its magnitude. In such a scenario we feel one has to consider this 0.64 in the context of the 0.56 for a purely random similarity - this is difficult to do without explicitly checking what the Rand index is for a random partitioning for a given K and K'. Thus the use of the full unit interval in comparing similarity by a corrected index such as the adjusted Rand index requires less vigilance on the part of the analyst. In the second scenario, the adjusted Rand index is 0.28.

#### 2.6 Standardisation

For a *p*-vector of observations,  $X_i = (x_{i1}, ..., x_{1p})$ , we define *standardisation* of  $X_i$  as the mapping from  $X_i$  to  $X_i' = (x_{i1}', ..., x_{ip}')$  defined by the *sample mean*,  $\bar{x}_i$ , and *sample standard deviation*,  $s_i$ :

$$\bar{x}_i = \frac{1}{p} \sum_{j=1}^p x_{ij} \tag{18}$$

$$s_i^2 = \frac{1}{p-1} \sum_{i=1}^p (x_{ij} - \bar{x}_i)^2$$
 (19)

$$x'_{ij} = \frac{x_{ij} - \bar{x}_i}{s_i} \quad \forall \quad j \in (1, \dots, p)$$
 (20)

We refer to  $X_i'$  as the standardised form of X. If we are given a dataset  $X = (X_1, ..., X_n)$  where each  $X_i$  is a p-vector of observations of the form referred to above, then in referring to the standardised form of X, we mean the dataset  $X' = (X_1', ..., X_n')$  where each  $X_i'$  is the standardised form of  $X_i$ .

Standardisation moves the values observed for each  $X_i$  to a common scale where each vector has an observed mean and standard deviation of 0 and 1 respectively.

We describe an example in section 2.9.1 which shows an explicit application and motivation for standardisation in the context of this project.

## 2.7 Consensus clustering

In the scenario that MDI struggles to explore the entire posterior distribution from any given initialisation for any realistic number of iterations of MCMC, we propose use of a "consensus" clustering [14]. In this scenario we draw samples of clusterings from MCMC chains with different initialisations and use these clusterings to describe the posterior distribution. In practice this involves running  $n_{seeds}$  different chains of MDI for a smaller number of iterations (some  $n_{iter} \in [500, 1000]$ ), burning out the first  $n_{iter} - 1$  iterations and saving the clustering from the final iteration. We then combine the clusterings from all  $n_{seeds}$  within a posterior similarity matrix (PSM), a  $N \times N$  matrix where the (i, j) entry is the proportion of times genes i and j are in the same cluster. This means that the PSM is not affected by label-flipping and that it is a symmetric matrix with 1's along the diagonal and all entries in the unit interval. From this PSM a summary clustering may be calculated. The combination of different initialisations explores all the possible likelihood maixma and thus provides a more informed clustering. As the algorithm is not exploring the full space in any given iteration, we expect that the uncertainty quantification is optimistic, however we argue that an estimate made using insufficient data is better than one made using none at all and that this method is the best currently available to us for quantifying the uncertainty and exploring the posterior distribution.

## 2.8 Tissue specificity

Cell-type specific gene pathways are pivotal in differentiating tissue function, implicated in hereditary organ failure, and mediate acquired chronic disease [6]. More and more evidence is being accrued to highlight the cell-type specific level of gene expression [3][17][12].

We also see that there are many auto-immune disease, normally associated with a specific tissue type, that have strong genetic associations. Tissue specific isoforms and expression have also been observed [25]. This shows that genes have context-specific interactions that should be considered in analysis.

#### 2.9 Gene sets

With the onset of microarrays and RNAseq, producing gene expression data in large quantities for a wide number of genes is increasingly enabled. Unfortunately the large amount of data gifted onto the genomics community by these methods is difficult to interpret and analyse. Gene Set Enrichment Analysis (GSEA) attempts to overcome some of these issues by analysing pre-defined gene sets and changes in the expression of the full set rather than considering each constituent member on an individual basis [15]. Consider, that in analysing gene sets as a group, the degree of perturbation in the expression of the full gene set due to the disease state / alternative phenotype that is required to be considered significant is much less than that required in analysing each of its constituent members individually [2][26]. This use of gene sets can increase the power of the analysis.

Furthermore, we know from Genome Wide Association Studies (GWAS) that many diseases are polygenic in nature [15]. Furthermore, Subramanian et al. [20] highlight the importance of gene sets, claiming that within a single metabolic pathway an increase of 20% in all the associated gene products may be more important than a 20-fold increase in a single gene.

Thus clustering genes into groups known as "gene sets" is natural and useful from both a biological and statistical perspective - it can increase the interpretability and the power of an analysis [16][24].

However, the problem of defining gene sets is non-trivial with many variations in-use. There exist many databases of gene sets [1][7][21]. The Molecular Signature Database [20] (MSigDB) is one of the most popular resources for GSEA and encompasses many different gene sets defined under various criteria or generated from separate resources. However, none of these definitions of a "set" incorporate tissue specific information. We believe that this is an oversight as there is evidence that some genes are involved in tissue specific pathways (see section 2.8). Thus we propose defining tissue specific gene sets. Previous attempts to achieve this have used the Genotype Tissue Expression (GTEx) [4] database [10], but here the profiles are for human donors post-mortem. We suspect that the data derived from these cells may not contain the same information as that collected from living, active cells. Furthermore, the GTEx data is across many different tissues (144 are used in [10]), but we focus on cell types relevant to autoimmune disease in general (i.e. blood cells) and IBD in particular (intestinal samples). This restricted focus should offer relevant gene sets.

Gene sets should contain sets of genes that have correlated expression. If this is the case, it is often assumed that the genes are common members of some metabolic pathway and that their products interact. As this correlated expression is represented by a common variation across people rather than in the magnitude of expression, we will standardise the expression data. We describe a small example to explain our reasoning.

Genes	Person 1	Person 2	Person 3	Person 4
A	5.1	5.2	4.9	5.0
В	5.1	4.9	5.2	5.4
C	1.4	1.5	1.2	1.3
D	1.4	1.2	1.5	1.7
E	1.4	1.5	1.4	1.5

Table 3: Example gene expression data.

#### 2.9.1 Motivating example: Standardising gene expression data

If one considers table 3 which contains an example of expression data for some genes A, B, C, D and E across people 1 to 4. One can see that genes A and C have similar

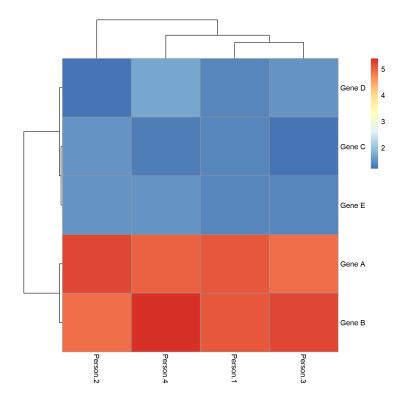


Figure 1: Heatmap of expression data in table 3 showing the clusters based upon magnitude of expression.

patters in variation across the people, as do genes B and D. Gene E is not consistent with any other gene here. However, as this relative variation is of interest rather than the magnitude of expression, one can see that standardising the data is required. If one were to cluster the data as represented in table 3, one would place genes A and B in one cluster and genes C, D and E in another as their absolute expression levels are similar (as can be seen in figure 1). However, if the expression level of each gene

Genes	Person 1	Person 2	Person 3	Person 4
A	0.39	1.16	-1.16	-0.39
В	-0.24	-1.20	0.24	1.20
C	0.39	1.16	-1.16	-0.39
D	-0.24	-1.20	0.24	1.20
E	-0.87	0.87	-0.87	0.87

Table 4: Example standardised gene expression data.

is standardised as per section 2.6, the data is then as represented in table 4. As the data are now on the same scale the characteristic that will determine a clustering is the variation of expression across people. As we want genes with similar patterns of variation (i.e. that are co-expressed) this enables us to cluster under our objective of defining gene sets. In this case genes A and C are one cluster, genes B and D another with gene E in a cluster alone, as can be seen in figure 2. As this is the type of data we wish to cluster across, we therefore most standardise our expression data before clustering can be implemented.

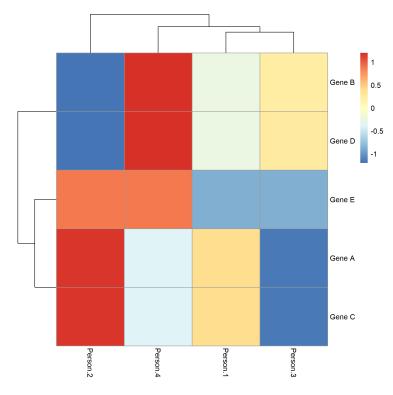


Figure 2: Heatmap of expression data in table 4 showing the clusters based upon variation of expression across people.

## 3 Data

The data is from the Correlated Expression and Disease Association Research (CEDAR) cohort [23]. We have 9 .csv files, one for each tissue / cell type present of normalised gene expression data for 323 individuals. These are healthy individuals of European descent; the cohort consists of 182 women and 141 men with an average age of 56 years (but ranging from 19 to 86). None of the individuals are suffering from any autoimmune or inflammatory disease and were not taking corticosteroids or non-steroid anti-inflammatory drugs (with the exception of aspirin).

With regards to tissue types, samples from six circulating immune cells types:

- CD4+ T lymphocytes;
- CD8+ T lymphocytes;
- CD14+ monocytes;
- CD15+ granulocytes;
- CD19+ B lymphocytes; and
- platelets.

Data from intestinal biopsies are also present, with sample taken from three distinct locations:

- the illeum;
- the rectum; and
- the colon.

Not every individual is present in every dataset. However, as we are clustering genes this should not present a problem.

Whole genome expression data were generated using HT-12 Expression Beadchips following the instructions of the manufacturer (Illumina). 29,464 autosomal probes (corresponding to 19,731 genes) were included across the datasets, but further thinning under various criteria reduced this further in each dataset. The fluorescence intensities were  $\log_2$  transformed and Robust Spline Normalized with Lumi38.

It should be noted that some datasets are less information rich than others (for instance the platelets dataset has only around 8 thousand probes present).

## 4 Methods

We intend to follow this pipeline to produce the clusters:

1. Transpose the data to have rows associated with gene probes and columns associated with individuals;

- 2. Remove NAs either imputing values using the minimum expressed value (as missingness is not random) or if above a threshold of missingness removing the column;
- 3. Standardise the data;
- 4. To apply MDI we require that each dataset have the same row names in the same order, so we re-arrange our datasets to have common order of probes and include rows of 0's for probes entirely missing from a given dataset; and
- 5. Apply MDI [13].

To validate our clusters we intend to check if some well-annotated gene sets (such as the interleukin pathways) cluster appropriately.

### 5 Results

To check if the algorithm ran and as an initial exploration of the data, we implemented the steps described in 4 applying MDI to all 9 datasets. This was done twice - on the first occasion probes missing from a dataset or containing NAs were dropped (resulting in a total dataset of 4,964 probes in each dataset) and on the second occasion using an imputed value of 0 for missing probes (on this occasion we dropped probes that had NAs in some columns in all datasets reducing the dataset from 18,523 to 18,517 probes).

The algorithm was capable of running for 10,000 iterations with a thinning factor of 25 over both these set of data.

We used the modal clustering as the predicted clustering as the labels became fixed and did not vary for the majority of iterations. We did not use the clustering implied by the PSM as the clusters were very defined and thus the uncertainty captured by the PSM was not necessary for the predicted clustering. Furthermore, the computational cost of calculating the PSM, particularly for the larger dataset, was quite high (the PSM is a  $n \times n$  matrix).

MDI begins with 50 clusters (as an approximation of a Dirichlet process - note that we can change the number of clusters present). In the 9 datasets the number of occupied clusters stabilised around 10 (ranging from 8 - 13).

We inspected the resulting clusters using the *pheatmap* package [9] in R [22].

We can see from figure 3 that some genes cluster across all datasets (the beige band about 0.25 along the vertical axis). Between the combination of a visual inspect and the hierarchical clustering visible in the tree at the top of figure 3 combined with the information in figure 4, one can see that the platelets behave significantly differently to the other datasets - very few rows align with other datasets. We can see that we have 4 distinct groups of datasets here:

#### 1. CD14, CD4 and CD8;

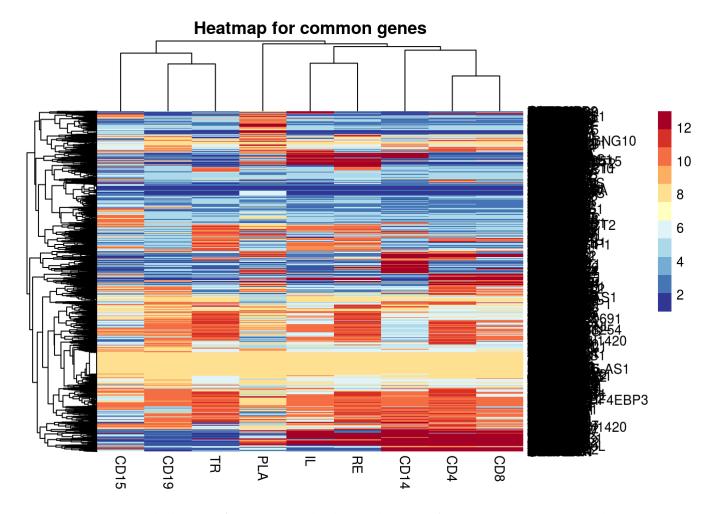


Figure 3: Predicted clusters for MDI applied to 9 datasets for common probes with datasets as columns and probes as rows.

- 2. IL and RE;
- 3. CD15, CD19 and TR; and
- 4. PLA.

However, there is too much information in figure 3 for serious analysis and we must use subsets of the data to better understand the information contained here. Based on the clusters of datasets mentioned in , we visualise the clustering in these groups.

From figures 5 and 6, one can see that inspecting the clusters in subsets of the datasets makes it easier to see similarity in clustering.

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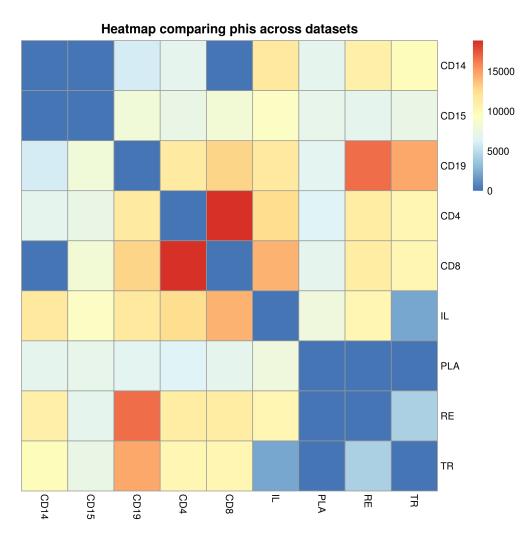


Figure 4: Mean  $\phi$  value between datasets across iterations.  $\phi$  can be considered a measure of similarity between datasets - the greater  $\phi_{i,j}$  is, the more correlated the clustering in datasets i and j is.

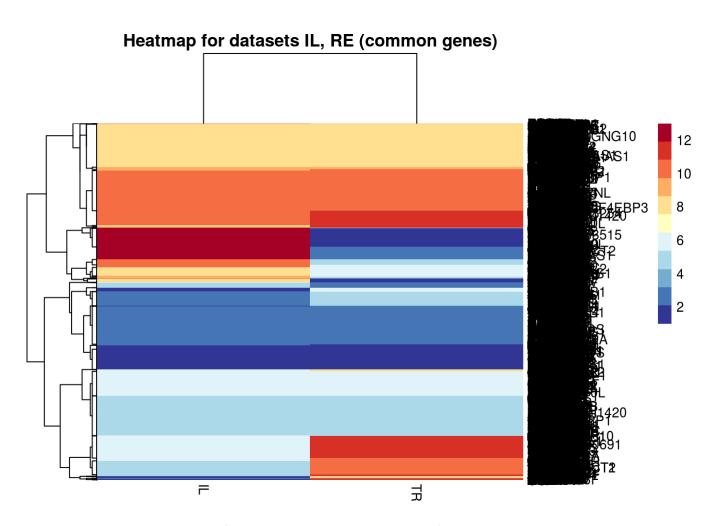


Figure 5: Predicted clusters for MDI applied to 9 datasets for common probes with datasets as columns and probes as rows.

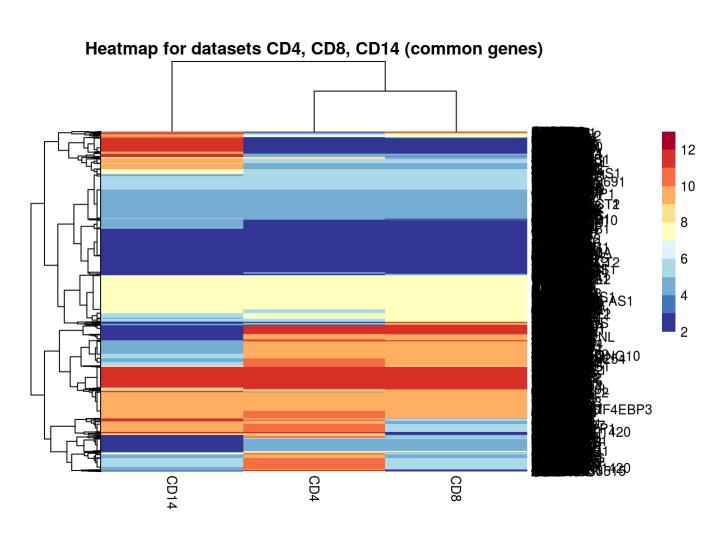


Figure 6: Predicted clusters for MDI applied to 9 datasets for common probes with datasets as columns and probes as rows.

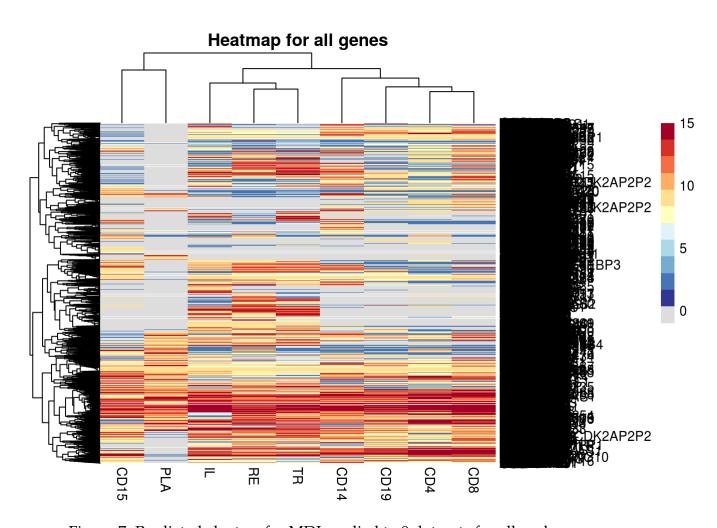


Figure 7: Predicted clusters for MDI applied to 9 datasets for all probes.