Defining tissue specific gene sets using consensus clustering

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Abstract

A priori defined gene sets are key to gene set enrichment analysis [22] a powerful tool in genetic analysis. Gene sets are constructed through linking genes by some common feature. This can be a function, the location of the gene product, the participation of the product in some metabolic or signalling pathway, the protein structure, the presence of transcription-factor-binding sites or other regulatory elements, the participation in multiprotein complexes, or any one of several other definitions [23][22][10][1]. However, all of these criteria are tissue agnostic. We propose to produce tissue specific gene sets by applying multiple dataset integration [11] (a Bayesian unsupervised clustering method) to the gene expression data from the Correlated Expression and Disease Association Research cohort [24], a dataset of 9 tissue / cell types.

We show that problems with convergence and dependence upon initialisation common in high dimensionality settings can be overcome by means of consensus clustering [16]. We then use Multiple Dataset Integration by means of consensus clustering to produce gene sets.

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1 Introduction

- Describe aim
- introduce concepts of gene sets (and why to cluster genes) and why might tissue specific ones be a thing
- Describe data in brief
- Consensus clustering
- Multiple dataset integration

We use consensus clustering to produce tissue-specific gene sets. In this section we briefly introduce the core components of this project such as gene sets, the data and the concepts of consensus and integrative clustering.

1.1 Gene sets

With the onset of microarrays and RNAseq, producing gene expression data in large quantities for a wide number of genes is increasingly enabled. Unfortunately the large amount of data gifted onto the genomics community by these methods is difficult to interpret and analyse. Gene Set Enrichment Analysis (GSEA) attempts to overcome some of these issues by using prior knowledge to define groups of genes linked through their biological function citeHEJBLUM. The set is defined using knowledge external to the current analysis; a common method is using the manually annotated pathways available on the Kyoto Encyclopedia of Genes and Genomes (KEGG) database citeFRIDLEYGene.

Analysing pre-defined gene sets and changes in the expression of the full set rather than considering each constituent member on an individual basis has more statistical power [17]. Consider, that in analysing gene sets as a group, the degree of perturbation in the expression of the full gene set due to the disease state / alternative phenotype that is required to be considered significant is much less than that required in analysing each of its constituent members individually [4][27].

1.1.1 Tissue specificity

The problem of defining gene sets is non-trivial with many variations in-use. There exist many databases of gene sets [1][10][23]. The Molecular Signature Database [22] (MSigDB) is one of the most popular resources for GSEA and encompasses many different gene sets defined under various criteria or generated from separate resources.

However, none of these definitions of a "set" incorporate tissue specific information. This seems an oversight. Cell-type specific gene pathways are pivotal in differentiating tissue function, implicated in hereditary organ failure, and mediate acquired chronic disease [9]. More and more evidence is being accrued to highlight the cell-type specific level of gene expression [6][19][14]. Thus we propose defining tissue specific gene sets.

2 Theory

2.1 Clustering

Given data $X = (x_1, ..., x_n)$, we define a *clustering* or partition of the data by:

$$Y = \{Y_1, \dots, Y_K\} \tag{1}$$

$$Y_k = \{x_{1_k}, \dots, x_{n_k}\}$$
 (2)

$$Y_i \cap Y_j = \emptyset \ \forall \ i, j \in \{1, K\}, i \neq j$$
 (3)

$$n_k \geq 1 \ \forall \ k \in \{1, K\} \tag{4}$$

$$\sum_{k=1}^{K} n_k = n \tag{5}$$

In short we have K nonempty disjoint sets of data, each of which is referred to as a *cluster*, the set of which form a *clustering*. We define a *label* $c = (c_1, ..., c_n)$ as denoting the membership of each point. A label $c_i = k$ states that point x_i is assigned to cluster Y_k .

2.2 Mixture models

Given some data $X = (x_1, ..., x_n)$, we assume a number of unobserved processes generate the data, and membership to a process for individual i is represented using the latent variable c_i . It is assumed that each of the K processes can be modelled by a parametric distribution, $f(\cdot)$ with associated parameters θ and that the full model density is then the weighted sum of these probability density functions where the weights are the component proportions, π_k :

$$p(x_i) = \sum_{k=1}^{K} \pi_k f(x_i | \theta_k)$$
 (6)

2.3 Bayesian inference

We carry out Bayesian inference of this model using Markov chain Monte Carlo methods. We sample first the component parameters, θ_k , and associated weights, π_k , from the associated distributions and then sample component membership. Basically:

- 1. For each of K clusters sample θ_k and π_k from the associated distributions based on current memberships, c_i ; and
- 2. For each of n individuals sample c_i based on the new θ_k and π_k .

For the mixture model we update the parameters after we allocate each observation to a cluster. For a given cluster with associated data X and parameter θ , we sample θ using Bayes' theorem from the distribution:

$$p(\theta|X) = \frac{p(X|\theta)p(\theta)}{\int_{\Theta} p(X|\theta')p(\theta')d\theta'}$$
(7)

Here Θ is the entire sample space for θ .

- We refer to $p(\theta|X)$ as the *posterior* distribution of θ as it is the distribution associated with θ *after* observing X.
- $p(\theta)$ is the *prior* distribution of θ and captures our beliefs about θ before we observe X.
- $p(X|\theta)$ is the *likelihood* of X given θ , the probability of data X being generated given our model is true. It is the criterion we focus on in our model if we would use a frequentist approach to the inference; maximising this quantity in our model generates the curve that best describes the observed data.
- $\int_{\Theta} p(X|\theta')p(\theta')d\theta'$ is the *normalising constant*. This quantity is also referred to as the *evidence* [13] or *marginal likelihood* and is normally represented by Z. It is referred to as the marginal likelihood as we marginalise the parameter θ by integrating over its entire sample space.

In terms of sampling, the prior is very useful as a clever choice of prior can ensure that the posterior is always solvable, that we do not encounter singularities in our distribution.

2.4 Multiple dataset integration

Consider the case when we have observed paired datasets $X_1 = (x_{1,1}, \dots, x_{n,1}), X_2 = (x_{1,2}, \dots, x_{n,2})$, where observations in the *i*th row of each dataset represent in-

formation about the same individual. We would like to cluster individuals using information common to both datasets. One could concatenate the datasets, adding additional covariates for each individual. However, if the two datasets have different clustering structures this would reduce the signal of both clusterings and probably have one dominate. If the two datasets have the same structure but different signal-to-noise ratios this would reduce the signal in the final clustering. In both these cases independent models on each dataset would be preferable. Kirk et al. [11] suggest a method to carry out clustering on both datasets where common information is used but two individual clusterings are outputted. This method is driven by the allocation prior:

$$p(c_{i1}, c_{i2}|\phi) \propto \pi_{i1}\pi_{i2}(1 + \phi \mathbb{I}(c_{i1} = c_{i2}))$$
 (8)

Here $\phi \in \mathbb{R}_+$ controls the strength of association between datasets. (8) states that the probability of allocating individual i to component $c_{i,1}$ in dataset 1 and to component $c_{i,2}$ in dataset 2 is proportional to the proportion of these components within each dataset and up-weighted by ϕ if the individual has the same labelling in each dataset. Thus as ϕ grows the correlation between the clusterings grow and we are more likely to see the same clustering emerge from each dataset. Conversely if $\phi = 0$ we have independent mixture models.

The generalised case for L datasets, $X_1 = (x_{1,1}, \dots, x_{n,1}), \dots, X_L = (x_{1,l}, \dots, x_{n,l})$ for any $L \in \mathbb{N}$ is simply a matter of combinatorics. In this case, (8) extends to:

$$p(c_{i1},\ldots,c_{iL}|\boldsymbol{\phi}) \propto \left[\prod_{l_1=1}^{L} \pi_{c_{il_1}l_1}\right] \left[\prod_{l_2=1}^{L-1} \prod_{l_3=l_2+1}^{L} \left(1+\phi_{l_2l_3}\mathbb{1}(c_{il_2}=c_{il_3})\right)\right]$$
(9)

Here ϕ is the $\binom{L}{2}$ -vector of all ϕ_{ij} where ϕ_{12} is the variable ϕ in (8).

Thus MDI is an extension of mixture models to multiple datasets where correlated clustering structure is used to "upweigh" similar clusters across datasets. MDI has been applied to precision medicine, specifically glioblastoma sub-typing [21], in the past showing its potential as a tool.

2.5 Rand index

A popular metric for comparing the similarity of two clusterings of the data is the *Rand index* [20]. If one assumes that all points are of equal importance in determining clusterings, then in combination with the discrete nature of clusters and the fact that a cluster is defined as much by what it does not contain as that which it does, Rand [20] proposes a metric to measure similarity between clusterings. Between clusterings Y and Y' for any two points x_i and x_j there can exist one of a number of scenarios regarding their labeling. Let γ_{ij} be a measure between the two points x_i and x_j . For the two points, they can have:

Table 1: Contingency table used by Rand [20] to calculate a measure of similarity between clusterings Y and Y'.

- 1. the same label in both clusterings ($c_i = c_j \wedge c_i' = c_j'$) ($\gamma_{ij} = 1$);
- 2. different labels in both ($c_i \neq c_j \land c_i' \neq c_j'$) ($\gamma_{ij} = 1$); or
- 3. the same label in one but not in the other $(c_i \neq c_j \land c_i' = c_j' \lor c_i = c_j \land c_i' \neq c_j')$ $(\gamma_{ij} = 0)$.

Thus Rand [20] propose counting the number of times any two points have one of 1 or 2 from list 2.5 and finding the proportion of these compared to the number of all possible point combinations. More formally, this is:

$$A\binom{n}{2}^{-1} = \frac{1}{\binom{n}{2}} \sum_{i=1}^{n-1} \sum_{j=i+1}^{n} \gamma_{ij}$$
 (10)

This can be envisioned as a $K \times K'$ contingency table of the count of overlapping points, as shown in table 1. Table 1 uses the following notation:

- n_{ij} is the number of points that have membership in Y_i in clustering Y and Y'_j in clustering Y';
- $n_{i,j}$ is the number of points in cluster $Y'_{i,j}$ in clustering $Y'_{i,j}$;
- n_i is the number of points in cluster Y_i in clustering Y; and
- $n_{\cdot \cdot \cdot} = n$ is the number of points in clusterings Y and Y'.

One can restate equation 10 in terms of the notation from table 1 [2]:

$$A = \binom{n}{2} + \sum_{i=1}^{K} \sum_{j=1}^{K'} n_{ij}^2 - \frac{1}{2} \left(\sum_{i=1}^{K} n_{i\cdot}^2 + \sum_{j=1}^{K'} n_{\cdot j}^2 \right)$$
 (11)

$$= \binom{n}{2} + 2\sum_{i=1}^{K} \sum_{j=1}^{K'} \binom{n_{ij}}{2} - \left[\sum_{i=1}^{K} \binom{n_{i}}{2} + \sum_{j=1}^{K'} \binom{n_{.j}}{2} \right]$$
(12)

Hubert and Arabie [8] extend the Rand index to account for chance. They include a null hypothesis and assume that there is a probability of some points having a γ value of 1 by chance. Consider the scenario where a point x_i has the same label as another point x_j under clustering Y. For another clustering Y', there a non-zero is a probability $c_i' = c_j'$ purely by chance and does not represent a similarity between Y and Y'. If one generates two clusterings Y and Y' by sampling from the integers in the closed interval [1, K] (i.e. by sampling from discrete unfirom distribution $\mathcal{U}\{1, K\}$), then the contingency table generated is constructed from the generalised hyper-geometric distribution [8]. It can be shown that the expected number of points with common membership in both clusters is non-zero. Specifically:

$$\mathbb{E}\left(\sum_{i=1}^{K}\sum_{j=1}^{K} \binom{n_{ij}}{2}\right) = \frac{\sum_{i=1}^{K} \binom{n_{i\cdot}}{2} \sum_{j=1}^{K} \binom{n_{\cdot j}}{2}}{\binom{n}{2}}$$
(13)

This is the product of the number of distinct pairs that can be formed from rows and the number of distinct pairs that can be constructed from columns, divided by the total number of pairs.

For a particular cell of the contingency table, the expected number of entries of the type described in point 1, is the product of number of pairs in its row and in its column divided by the total number of possible pairs:

$$\mathbb{E}\left(\binom{n_{ij}}{2}\right) = \frac{\binom{n_{i\cdot}}{2}\binom{n_{\cdot j}}{2}}{\binom{n}{2}} \tag{14}$$

One can see that as each component of equation 11 is some transformation of $\sum_{i,j} \binom{n_{ij}}{2}$, one can directly state the expected value of the Rand index by combining equations 11 and 14:

$$\mathbb{E}\left(A\binom{n}{2}^{-1}\right) = 1 + 2\sum_{i=1}^{K} \binom{n_{i}}{2} \sum_{j=1}^{K'} \binom{n_{ij}}{2} \binom{n}{2}^{-2} - \left[\sum_{i=1}^{K} \binom{n_{i}}{2} + \sum_{j=1}^{K'} \binom{n_{ij}}{2}\right] \binom{n}{2}^{-1}$$
(15)

Defining an index corrected for chance as:

$$Corrected index = \frac{Index - Expected index}{Maximum index - Expected index}$$
 (16)

Assuming a maximum value of 1 for the Rand index then gives a corrected Rand index:

$$\frac{\sum_{i=1}^{K} \sum_{j=1}^{K'} {n_{ij} \choose 2} - \sum_{i=1}^{K} {n_{i\cdot} \choose 2} \sum_{j=1}^{K'} {n_{i\cdot j} \choose 2} {n \choose 2}^{-1}}{\frac{1}{2} \left[\sum_{i=1}^{K} {n_{i\cdot} \choose 2} + \sum_{j=1}^{K'} {n_{i\cdot j} \choose 2} \right] - \sum_{i=1}^{K} {n_{i\cdot} \choose 2} \sum_{j=1}^{K'} {n_{i\cdot j} \choose 2} {n \choose 2}^{-1}}$$
(17)

$Y^{Y'}$	Y_1'	Y_2'	Y_3'	Sums
Y_1	$\frac{n}{2}$	$\frac{n}{16}$	$\frac{n}{16}$	$\frac{10n}{16}$
Y_2	$\frac{\overline{n}}{16}$	$\frac{n}{16}$	$\frac{n}{16}$	$\frac{3\tilde{n}}{16}$
Y_3	$\frac{n}{16}$	$\frac{n}{16}$	$\frac{n}{16}$	$\frac{3n}{16}$
Sums	1 <u>0n</u> 16	<u>3n</u> 16	<u>3n</u>	$\frac{16n}{16} = n$

Table 2: Contingency table for the non-random clustering described in section ??.

We define this quantity described in equation 17 as the *adjusted Rand index* and we use it as our measure of choice for similarity between clusterings.

We describe an explicit example motivating the adjusted Rand index in section 2.5.1.

2.5.1 Motivating example: adjusted Rand index

Consider the case of *n* labels Y and Y' generated from \mathcal{U} {1,3} where *n* is some arbitrarily large number. Then as n tends to infinity we can expect that our contingency table has entries of $\frac{n}{9}$ in each cell. If one calculates the Rand index on these random partitions where any similarity is purely by chance one finds, it comes to (approximately) 0.56. This suggests there is some similarity between Y and Y', but this is misleading as we know any similarity is stochastic. In the same scenario the adjusted Rand index between the partitions is 0. This seems preferable. Based on this, one could argue that the Rand index has inflated values. Consider the case that we have n points in total, but we let the first $\frac{7n}{16}$ have a common label (say $(c_1,\ldots,c_{n_1})=1$ for $n_1=\frac{7n}{16}$) and then draw the remaining $\frac{9n}{16}$ points from $\mathcal{U}\{1,3\}$. Then, as n tends to infinity, our contingency table tends to that described in table 2. One feels that the high Rand index for such a clustering, 0.64, is misleading in its magnitude. In such a scenario we feel one has to consider this 0.64 in the context of the 0.56 for a purely random similarity - this is difficult to do without explicitly checking what the Rand index is for a random partitioning for a given K and K'. Thus the use of the full unit interval in comparing similarity by a corrected index such as the adjusted Rand index requires less vigilance on the part of the analyst. In the second scenario, the adjusted Rand index is 0.28.

2.6 Standardisation

For a *p*-vector of observations, $X_i = (x_{i1}, ..., x_{1p})$, we define *standardisation* of X_i as the mapping from X_i to $X_i' = (x_{i1}', ..., x_{iv}')$ defined by the *sample mean*, \bar{x}_i ,

and sample standard deviation, s_i :

$$\bar{x}_i = \frac{1}{p} \sum_{j=1}^p x_{ij}$$
 (18)

$$s_i^2 = \frac{1}{p-1} \sum_{j=1}^p (x_{ij} - \bar{x}_i)^2$$
 (19)

$$x'_{ij} = \frac{x_{ij} - \bar{x}_i}{s_i} \quad \forall \quad j \in (1, \dots, p)$$
 (20)

We refer to X'_i as the standardised form of X. If we are given a dataset $X = (X_1, ..., X_n)$ where each X_i is a p-vector of observations of the form referred to above, then in referring to the standardised form of X, we mean the dataset $X' = (X'_1, ..., X'_n)$ where each X'_i is the standardised form of X_i .

Standardisation moves the values observed for each X_i to a common scale where each vector has an observed mean and standard deviation of 0 and 1 respectively.

We describe an example in section 2.8.2 which shows an explicit application and motivation for standardisation in the context of this project.

2.7 Consensus clustering

In the scenario that MDI struggles to explore the entire posterior distribution from any given initialisation for any realistic number of iterations of MCMC, we propose use of a "consensus" clustering [16]. In this scenario we draw samples of clusterings from MCMC chains with different initialisations and use these clusterings to describe the posterior distribution. In practice this involves running n_{seeds} different chains of MDI for a smaller number of iterations (some $n_{iter} \in [500, 1000]$), burning out the first $n_{iter} - 1$ iterations and saving the clustering from the final iteration. We then combine the clusterings from all n_{seeds} within a posterior similarity matrix (PSM), a $N \times N$ matrix where the (i, j) entry is the proportion of times genes i and j are in the same cluster. This means that the PSM is not affected by label-flipping and that it is a symmetric matrix with 1's along the diagonal and all entries in the unit interval. From this PSM a summary clustering may be calculated. The combination of different initialisations explores all the possible likelihood maixma and thus provides a more informed clustering. As the algorithm is not exploring the full space in any given iteration, we expect that the uncertainty quantification is optimistic, however we argue that an estimate made using insufficient data is better than one made using none at all and that this method is the best currently available to us for quantifying the uncertainty and exploring the posterior distribution.

2.8 Gene sets

Analysing pre-defined gene sets and changes in the expression of the full set rather than considering each constituent member on an individual basis has more statistical power [17]. Consider, that in analysing gene sets as a group, the degree of perturbation in the expression of the full gene set due to the disease state / alternative phenotype that is required to be considered significant is much less than that required in analysing each of its constituent members individually [4][27].

We know from Genome Wide Association Studies (GWAS) that many diseases are polygenic in nature [17]. This suggests that it is natural to be considering sets of genes in analysis of many diseases. Subramanian et al. [22] highlight the importance of gene sets, claiming that within a single metabolic pathway an increase of 20% in all the associated gene products may be more important than a 20-fold increase in a single gene.

Thus clustering genes into groups known as "gene sets" is natural and useful from both a biological and statistical perspective - it can increase the interpretability and the power of an analysis [18][25].

2.8.1 Tissue specificity

Previous attempts to achieve this have used the Genotype Tissue Expression (GTEx) [7] database [12], but here the profiles are for human donors post-mortem. We suspect that the data derived from these cells may not contain the same information as that collected from living, active cells. Furthermore, the GTEx data is across many different tissues (144 are used in [12]), but we focus on cell types relevant to autoimmune disease in general (i.e. blood cells) and Inflammatory Bowel Disease in particular (intestinal samples).

Gene sets should contain sets of genes that have correlated expression. If this is the case, it is often assumed that the genes are common members of some metabolic pathway and that their products interact. As this correlated expression is represented by a common variation across people rather than in the magnitude of expression, we will standardise the expression data. We describe a small example to explain our reasoning.

2.8.2 Motivating example: Standardising gene expression data

If one considers table 3 which contains an example of expression data for some genes A, B, C, D and E across people 1 to 4. One can see that genes A and C have similar patters in variation across the people, as do genes B and D. Gene E is not consistent with any other gene here. However, as this relative variation is

Genes	Person 1	Person 2	Person 3	Person 4
A	5.1	5.2	4.9	5.0
В	5.1	4.9	5.2	5.4
C	1.4	1.5	1.2	1.3
D	1.4	1.2	1.5	1.7
E	1.4	1.5	1.4	1.5

Table 3: Example gene expression data.

Genes	Person 1	Person 2	Person 3	Person 4
A	0.39	1.16	-1.16	-0.39
В	-0.24	-1.20	0.24	1.20
C	0.39	1.16	-1.16	-0.39
D	-0.24	-1.20	0.24	1.20
E	-0.87	0.87	-0.87	0.87

Table 4: Example standardised gene expression data.

of interest rather than the magnitude of expression, one can see that standardising the data is required. If one were to cluster the data as represented in table 3, one would place genes A and B in one cluster and genes C, D and E in another as their absolute expression levels are similar (as can be seen in figure 1). However, if the expression level of each gene is standardised as per section 2.6, the data is then as represented in table 4. As the data are now on the same scale the characteristic that will determine a clustering is the variation of expression across people. As we want genes with similar patterns of variation (i.e. that are co-expressed) this enables us to cluster under our objective of defining gene sets. In this case genes A and C are one cluster, genes B and D another with gene E in a cluster alone, as can be seen in figure 2. As this is the type of data we wish to cluster across, we therefore most standardise our expression data before clustering can be implemented.

2.9 Data

We use the gene expression data from Correlated Expression and Disease Association Research (CEDAR) cohort [24]. This data is avialable in a processed form online. This consists of 9 .csv files, one for each tissue / cell type present of normalised gene expression data for 323 individuals. These are healthy individuals of European descent; the cohort consists of 182 women and 141 men with an average age of 56 years (but ranging from 19 to 86). None of the individuals are suffering from any autoimmune or inflammatory disease and were not tak-

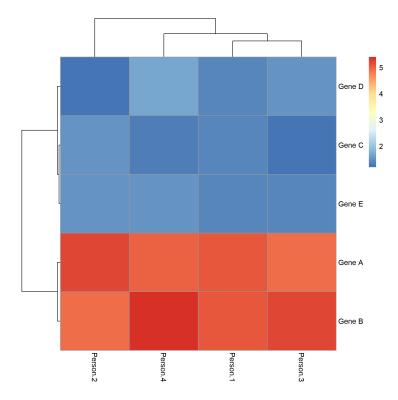


Figure 1: Heatmap of expression data in table 3 showing the clusters based upon magnitude of expression.

ing corticosteroids or non-steroid anti-inflammatory drugs (with the exception of aspirin).

With regards to tissue types, samples from six circulating immune cells types (followed in brackets by the abbreviation for the associated dataset):

- CD4+ T lymphocytes (CD4);
- CD8+ T lymphocytes (CD8);
- CD14+ monocytes (CD14);
- CD15+ granulocytes (CD15);
- CD19+ B lymphocytes (CD19); and
- platelets (PLA).

Data from intestinal biopsies are also present, with samples taken from three distinct locations:

- the illeum (IL);
- the rectum (RE); and

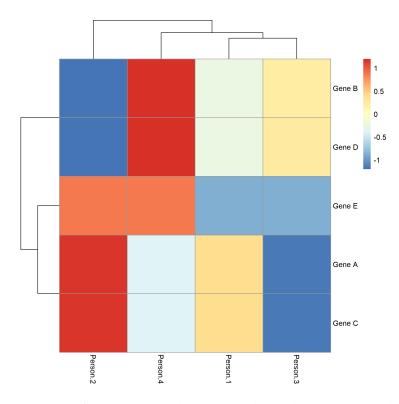


Figure 2: Heatmap of expression data in table 4 showing the clusters based upon variation of expression across people.

• the colon (TR).

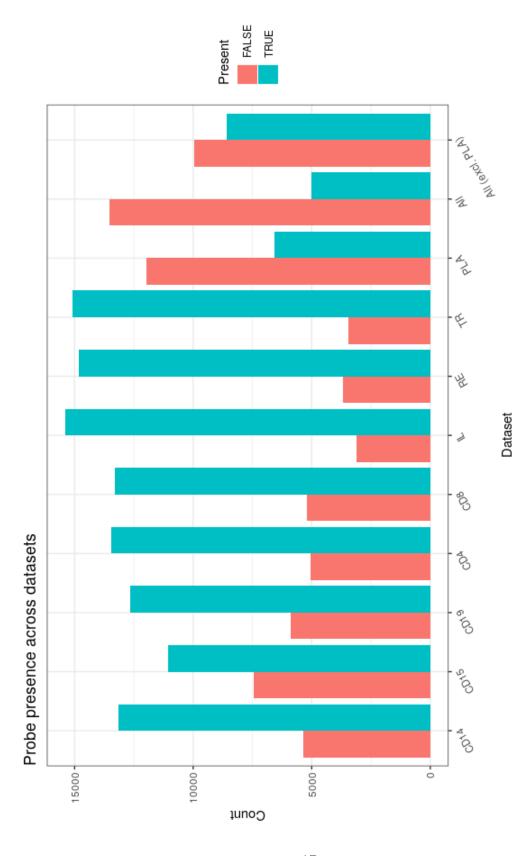
Not every individual is present in every dataset. However, as we are clustering genes this should not present a problem.

Whole genome expression data were generated using HT-12 Expression Beadchips following the instructions of the manufacturer (Illumina). There are 18,524 probes present between the 9 datasets.

The fluorescence intensities were \log_2 transformed and Robust Spline Normalized with Lumi38.

It should be noted that there are differing degrees of missingness between the datasets (for instance the platelets dataset has 6,564 probes present in comparison to an average of 12,838 probes present per dataset, see figure 3).

Due to this and the exponential increase in computational cost for each additional dataset, we use only the 8 most informative datasets, dropping PLA from our analysis. From a biological perspective we also expect PLA to be the least rich as platelets have no nucleus citeWRIGHT and therefore any gene expression is an artefact from before they differentiated into platelets.



under "All (excl. PLA)" we have the number of probes present in every dataset bar PLA. Note how there is Figure 3: Probe presence across datasets. Under "All" we have the number of probes present in every dataset, greater missingness in the PLA dataset in comparison to the others.

3 Methods

We first show via simulated data that MDI can cluster appropriately and that the consensus clustering does produce similar results to a converged single run.

We then simulate data where individual chains of MDI will struggle to converge and possibly will not converge in finite time. We show that consensus clustering explores a wider space than any individual chain and appears to describe something similar to the space described by the union of the chains.

Finally we apply consensus clustering to 1,000 probes for 8 datasets from the CEDAR dataset. An initial set of probes are chosen based on the members of 3 KEGG pathways:

- 1. Inositol phosphate metabolism (a broad biological pathway);
- 2. NOD-like receptor signaling pathway (a specific biological pathway with known involvement in IBD [3][5]); and
- 3. Inflammatory bowel disease (IBD) (a pathological pathway).

The union of these sets corresponds to 169 unique genes (or 287 probes as the mapping from the space of probes to that of genes is non-injective) that are present in the CEDAR dataset. The remaining probes are randomly selected from the total possible space (18,524 probes) less those corresponding to these genes (leaving 18,287 possible candidate probes). We then expect that the genes from the sets mentioned above (list 3) should cluster together. We use this as a test of our final clustering.

3.1 CEDAR data pipeline

For the CEDAR data, we follow this pipeline to prepare the data for clustering:

- 1. Transpose the data to have rows associated with gene probes and columns associated with individuals;
- Remove NAs either imputing values using the minimum expressed value (as missingness is not random) or if above a threshold of missingness removing the column;
- 3. Standardise the data;
- 4. To apply MDI we require that each dataset have the same row names in the same order, so we re-arrange our datasets to have common order of probes;
- 5. For probes entirely missing from a given dataset we generate expression from a standard normal distribution for each probe. Then these probes are

expressed as noise in the dataset and any clustering imposed upon them should be due to information about these probes present in other datasets; and

6. Apply MDI [15].

4 Results

4.1 Case 1: Proof of consensus

Generated data based on data from original MDI paper with some additional noisy clusters that MDI succeeds with.

4.2 Case 2: Overcoming multiple modes

Generated data that MDI struggles with.

4.3 Case 3: CEDAR data

Actual data.

5 Conclusion

We conclude, and finish dispute.

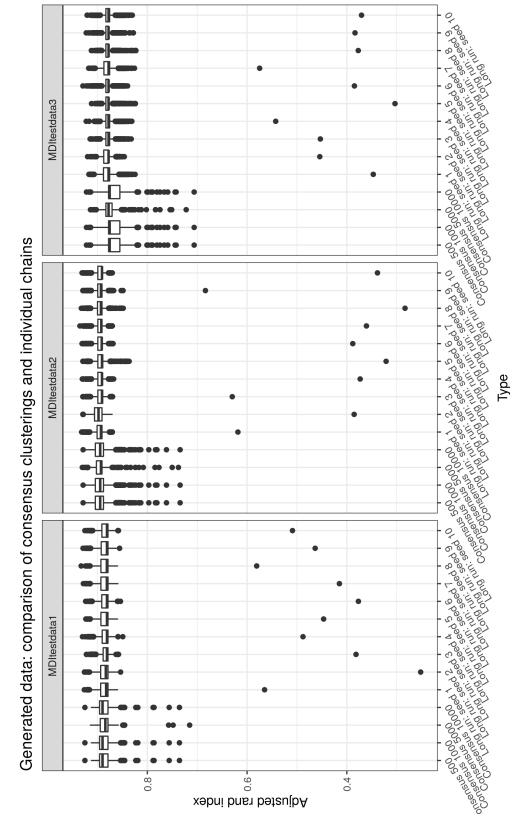


Figure 4: Box plots for distribution of adjusted rand index between the clustering at each iteration to the true clustering for different lengths of consensus clustering and different initialisation of long chains.

Generated data: comparison of consensus clusterings and collapsed chains MDItestdata2 MDItestdata1

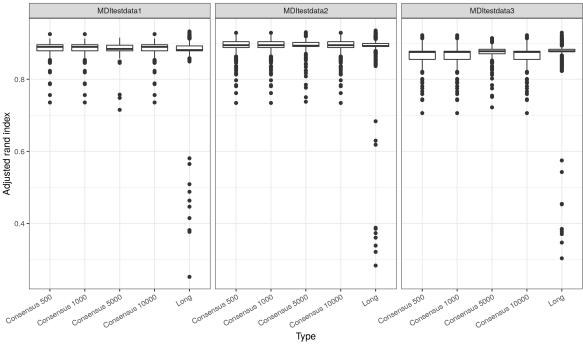


Figure 5: Box plots for distribution of adjusted rand index between the clustering at each iteration to the true clustering for different lengths of consensus clustering and the collapsed long chains.

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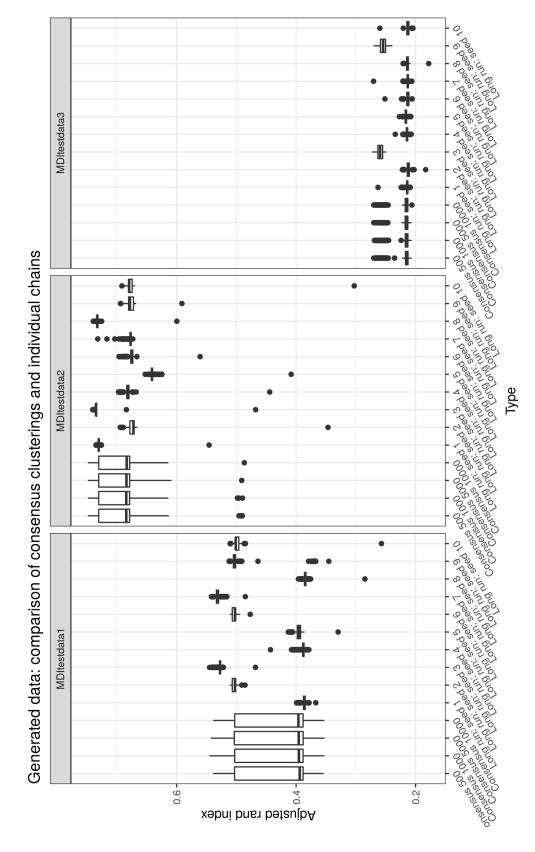
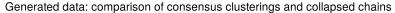


Figure 6: Box plots for distribution of adjusted rand index between the clustering at each iteration to the true clustering for different lengths of consensus clustering and different initialisation of long chains.



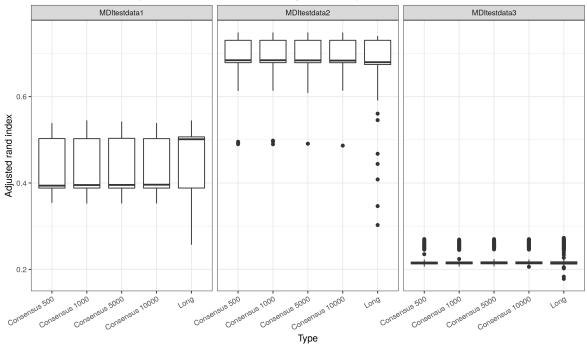
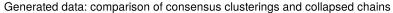


Figure 7: Box plots for distribution of adjusted rand index between the clustering at each iteration to the true clustering for different lengths of consensus clustering and the collapsed long chains.

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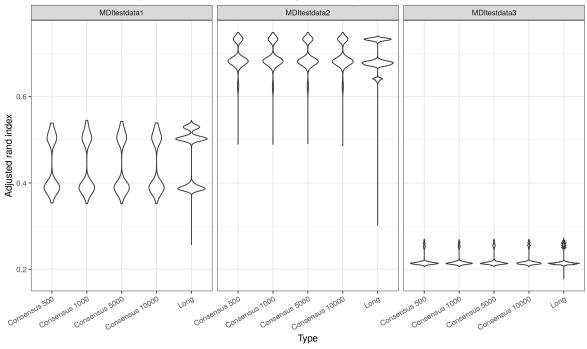


Figure 8: Violoin plots for distribution of adjusted rand index between the clustering at each iteration to the true clustering for different lengths of consensus clustering and the collapsed long chains. We can see that the consensus clustering approximates the modes described across chains quite well.

Stephen B Montgomery, Leopold Parts, Simon Potter, Gabriela Surdulescu, Loukia Tsaprouni, Sophia Tsoka, Veronique Bataille, Richard Durbin, Frank O Nestle, Stephen O'Rahilly, Nicole Soranzo, Cecilia M Lindgren, Krina T Zondervan, Kourosh R Ahmadi, Eric E Schadt, Kari Stefansson, George Davey Smith, Mark I McCarthy, Panos Deloukas, Emmanouil T Dermitzakis, and Tim D Spector. Mapping cis- and trans-regulatory effects across multiple tissues in twins. *Nature Genetics*, 44(10):1084–1089, October 2012. ISSN 1061-4036, 1546-1718. doi: 10.1038/ng.2394.

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Martina Müller-Nurasyid, Matthias Nauck, Michel Nivard, Brenda Penninx, Jonathan Pritchard, Olli Raitakari, Olaf Rotzschke, Eline P. Slagboom, Coen D.A. Stehouwer, Michael Stumvoll, Patrick Sullivan, Peter A.C. 't Hoen, Joachim Thiery, Anke Tönjes, Jenny van Dongen, Maarten van Iterson, Jan Veldink, Uwe Völker, Cisca Wijmenga, Morris Swertz, Anand Andiappan, Grant W. Montgomery, Samuli Ripatti, Markus Perola, Zoltan Kutalik, Emmanouil Dermitzakis, Sven Bergmann, Timothy Frayling, Joyce van Meurs, Holger Prokisch, Habibul Ahsan, Brandon Pierce, Terho Lehtimäki, Dorret Boomsma, Bruce M. Psaty, Sina A. Gharib, Philip Awadalla, Lili Milani, Willem H. Ouwehand, Kate Downes, Oliver Stegle, Alexis Battle, Jian Yang, Peter M. Visscher, Markus Scholz, Gregory Gibson, Tõnu Esko, and Lude Franke. Unraveling the polygenic architecture of complex traits using blood eQTL meta-analysis. Preprint, Genomics, October 2018.

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A Data generation explained

B Additional convergence plots

- B.1 Case 1: Convergence diagnostics
- B.1.1 Geweke plots
- B.1.2 Estimated burn in

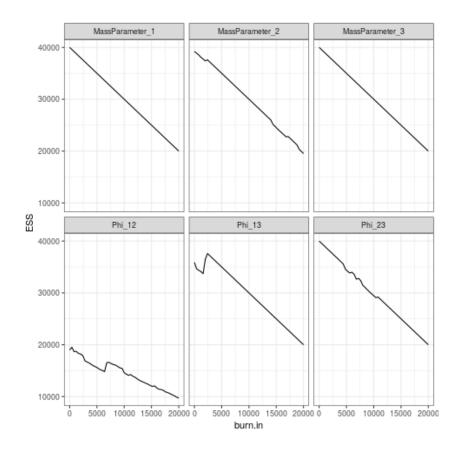


Figure 9: Box plots for distribution of adjusted rand index between the clustering at each iteration to the true clustering for different lengths of consensus clustering and the collapsed long chains.

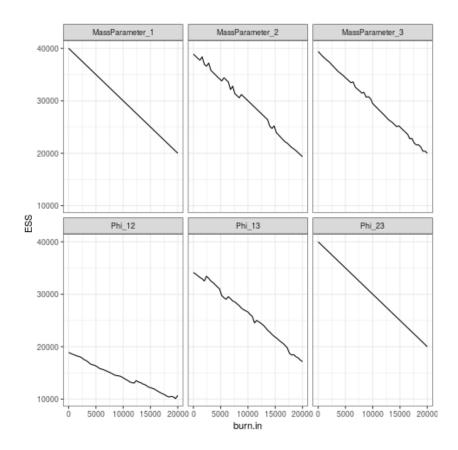


Figure 10: Box plots for distribution of adjusted rand index between the clustering at each iteration to the true clustering for different lengths of consensus clustering and the collapsed long chains.

- B.2 Case 2: Convergence diagnostics
- B.2.1 Geweke plots
- B.2.2 Estimated burn in

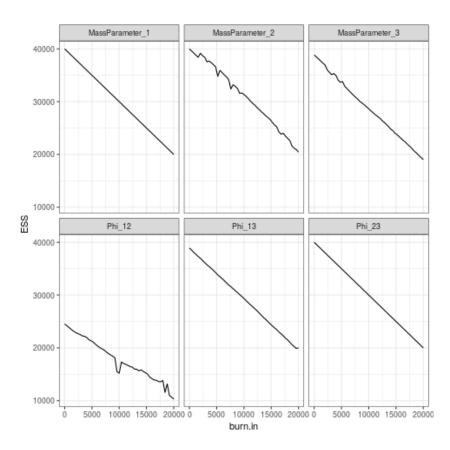


Figure 11: Box plots for distribution of adjusted rand index between the clustering at each iteration to the true clustering for different lengths of consensus clustering and the collapsed long chains.

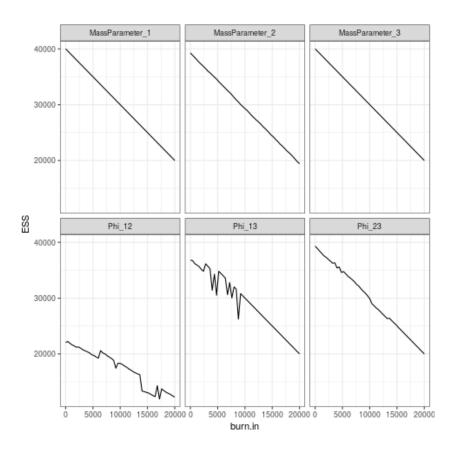


Figure 12: Box plots for distribution of adjusted rand index between the clustering at each iteration to the true clustering for different lengths of consensus clustering and the collapsed long chains.

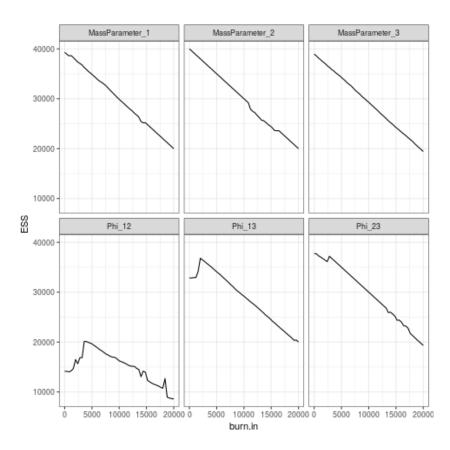


Figure 13: Box plots for distribution of adjusted rand index between the clustering at each iteration to the true clustering for different lengths of consensus clustering and the collapsed long chains.

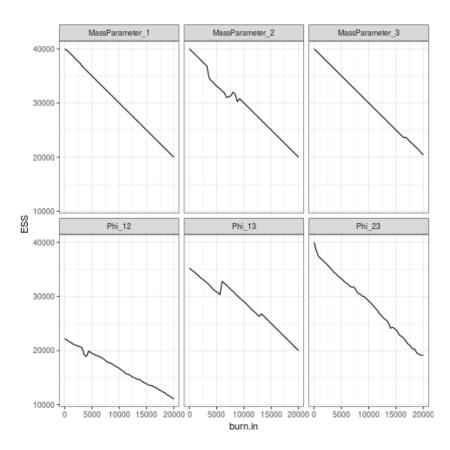


Figure 14: Box plots for distribution of adjusted rand index between the clustering at each iteration to the true clustering for different lengths of consensus clustering and the collapsed long chains.

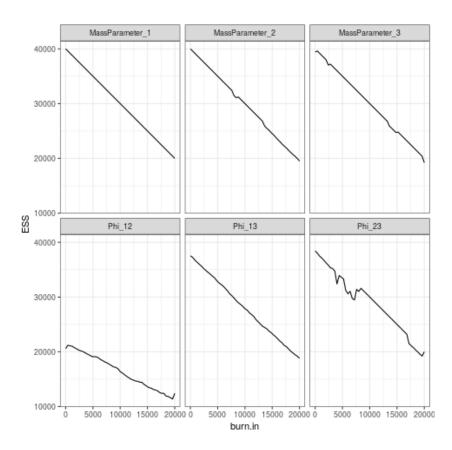


Figure 15: Box plots for distribution of adjusted rand index between the clustering at each iteration to the true clustering for different lengths of consensus clustering and the collapsed long chains.

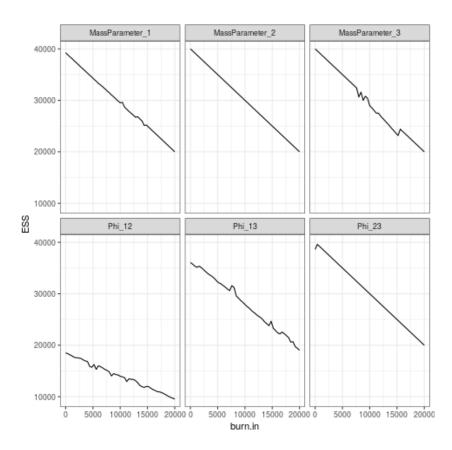


Figure 16: Box plots for distribution of adjusted rand index between the clustering at each iteration to the true clustering for different lengths of consensus clustering and the collapsed long chains.

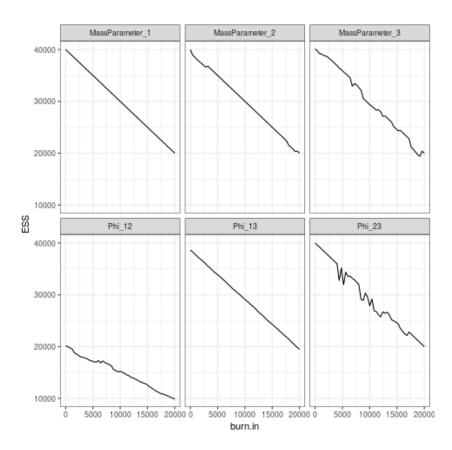


Figure 17: Box plots for distribution of adjusted rand index between the clustering at each iteration to the true clustering for different lengths of consensus clustering and the collapsed long chains.

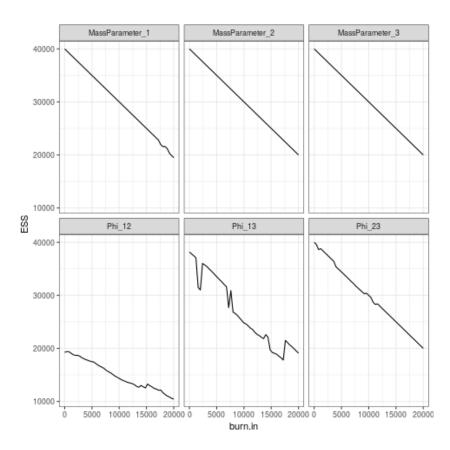


Figure 18: Box plots for distribution of adjusted rand index between the clustering at each iteration to the true clustering for different lengths of consensus clustering and the collapsed long chains.

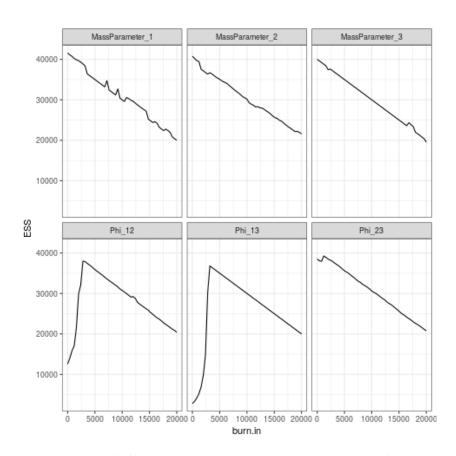


Figure 19: Plot of effective sample size (ESS) to burn-in for chain 1.

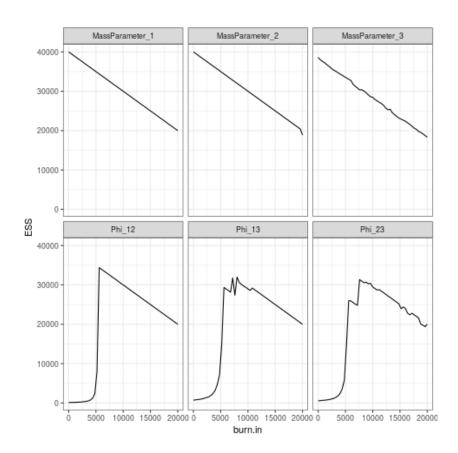


Figure 20: Plot of effective sample size (ESS) to burn-in for chain 2.

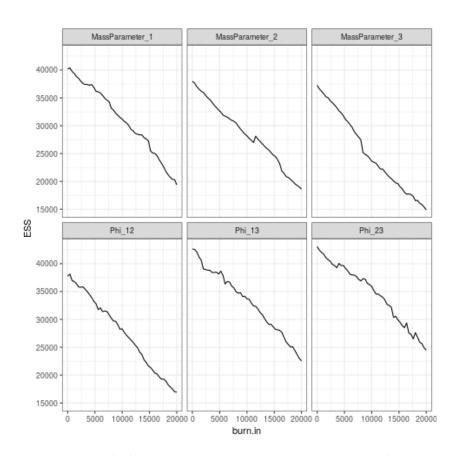


Figure 21: Plot of effective sample size (ESS) to burn-in for chain 3.

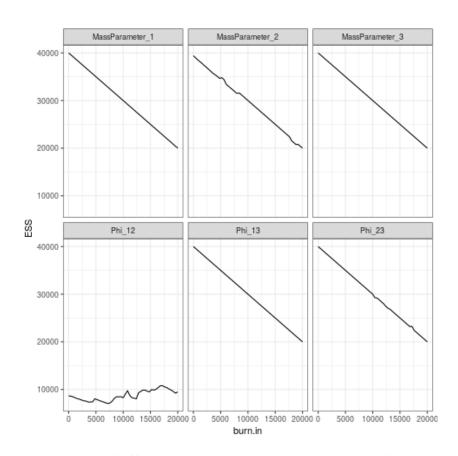


Figure 22: Plot of effective sample size (ESS) to burn-in for chain 4.

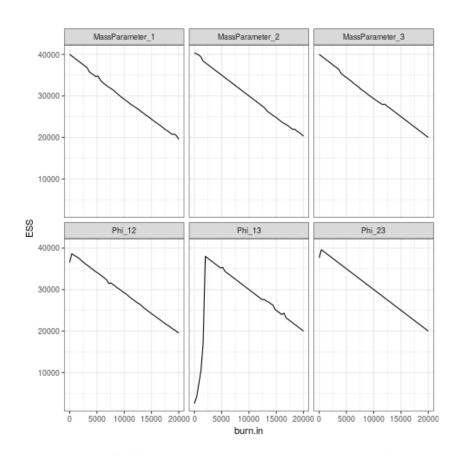


Figure 23: Plot of effective sample size (ESS) to burn-in for chain 5.

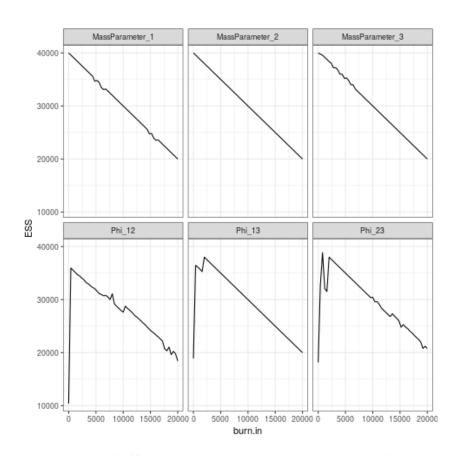


Figure 24: Plot of effective sample size (ESS) to burn-in for chain 6.

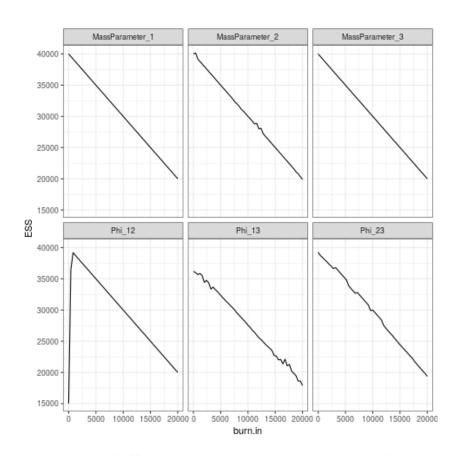


Figure 25: Plot of effective sample size (ESS) to burn-in for chain 7.

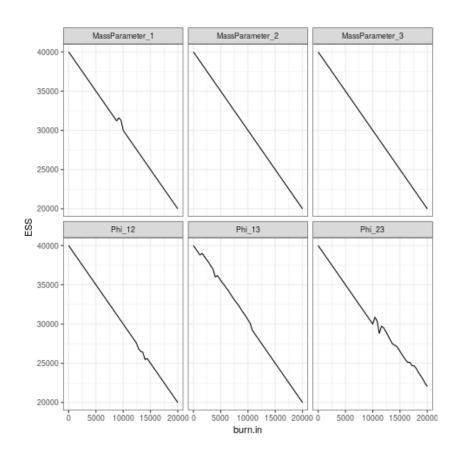


Figure 26: Plot of effective sample size (ESS) to burn-in for chain 8.

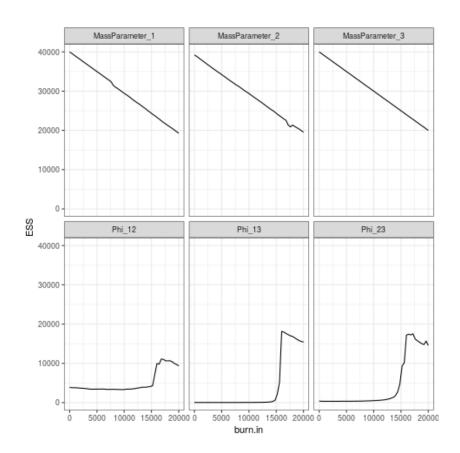


Figure 27: Plot of effective sample size (ESS) to burn-in for chain 9.

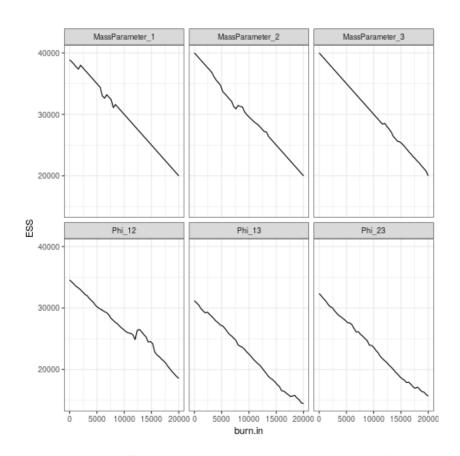


Figure 28: Plot of effective sample size (ESS) to burn-in for chain 10.