

Olivier Sigaud RL Labs: Instructions 2019-2020

1 Final report instructions and evaluation

• Send an email to Olivier.Sigaud@upmc.fr.

- The email subject must contain: "RL Lab, NAME1 NAME2" where NAME1 and NAME2 are the names of the involved students.
- The email must contain your report included as a pdf file and a copy of your source files, altogether included into an archive whose name must be RL_NAME1_ NAME2 (.zip or .tar.gz).
- For each function required in a question, the corresponding piece of code should be copy-pasted into your report to facilitate evaluation.
- The evaluation will take into account the quantity of work done, the accuracy of the results and the quality of the content (including written english).

2 MDPs and mazes

A reinforcement learning agent interacts with an environment represented as a Markov Decision Process (MDP). It is defined by a tuple (S, A, P, r, γ) where S is the state space, A the action space, $P(state_t, action_t, state_{t+1})$ the transition function, $r(state_t, action_t)$ the reward function and $\gamma \in [0, 1]$ the discount factor.

2.1 Documentation of the provided code

Some code is provided to create mazes, transform them into MDPs and visualize them together with policies or value functions. It is contained into three files: maze.py, mdp.py and maze_plotter.py. The following sections give an overview of this code.

2.1.1 Content of the maze.py file

A maze is represented as an object of the Maze class. It is defined as a grid of $width \times height$ cells, and some of these cells contain a wall.

The build_maze(width, height, walls, hit=False) function is used to create a Maze, where walls is a list of the number of the cells which contain a wall. The hit parameter has an impact on the MDP reward function: if hit is true, the agent is penalized each time it tries to move to a wall cell. Otherwise, the agent is just rewarded when it reaches terminal states. In the provided function, the list of terminal states is a singleton corresponding to the last cell that the agent can visit.

Apart from representing the two reward functions described above, the Maze class only contains a constructor whose only role is to create the MDP corresponding to the maze and the maze plotter used to display simulations. A key point is that only cells where there is no wall are considered as states of the underlying MDP. To facilitate the correspondence between mazes and mdps, each free cell (i.e. with no wall) knows the number of its corresponding MDP state.

The maze constructors also builds the action space, the initial state distribution, the transition function and the reward function of the MDP. Once all these data structures have been created, the resulting MDP is built.

2.1.2 Content of the mdp.py file

The mdp.py file contains the SimpleActionSpace class and the Mdp class.

The SimpleActionSpace class contains the list of actions and a method to sample from this list. In our maze environment, the possible actions for the agent are going north, south, east or west (resp. [0, 1, 2, 3]).

The Mdp class is designed to be compatible with the OpenAI gym interface¹. The main methods are reset(self, uniform=False), which resets the MDP into an initial state drawn from the initial state distribution, and step(self, u, deviation=0) which is used to let the agent perform a step in the environment, sending and action and receiving the next state, the reward, and a signal telling whether a terminal state was reached.

2.1.3 Content of the maze_plotter.py file

The code to display the effect of the algorithms in these environment is in maze_plotter.py, in the MazePlotter class. In order to visualize the environment, you use the new_render() function to initialize the rendering, then render(V, policy, agent_pos) to refresh the maze with either the newly calculated state values and the policy, or the state-action values, and eventually the current position of the agent. There is also a render_pi(policy) function which only displays the policy (useful for policy iteration). The function save_fig(title) is used to save the last render into a file.

You can see examples of calls to these different visualizations in the functions defined in dynamic_programming.py and reinforcement_learning.py.

2.2 Playing with differents MDPs (optional)

Though it is not crucial for these labs, you may have a look at how MDPs and mazes are defined and try to design different ones.

Question 1:(**OPTIONAL and easy**) In dynamic_programming.py, in the run() function, modify the call to the build_maze function so as to get a maze corresponding to Figure 1.

¹https://gym.openai.com/

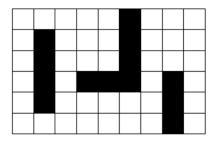


Figure 1: A sample maze

Question 2: (**OPTIONAL and more difficult**) Copy the mdp.py file into my_mdp.py and modify the MDP so that actions have a stochastic outcome: each time the agent chooses a direction, there is a proba_success chance that it performs the expected movement, and the remaining chances are evenly distributed between available directions, i.e. directions where there is no wall.

Later, when running your dynamic programming and reinforcement learning functions, you can evaluate them on the various MDPs you have designed and see if there is a difference in convergence time and properties.

3 Dynamic Programming

The goal of an RL agent is to find the optimal behaviour, defined by a function called "policy" π that assigns an action (or distribution over actions) to each state so as to maximize the agent's total expected reward. In order to estimate how good a state is, either a state value function V(x) or a state-action value function Q(x, u) is used.

Dynamic programming algorithms are used for planning, they require a full knowledge of the MDP from the agent (in contrast to "true" RL where the agent does not know the transition and reward functions). They find the optimal policy by computing a value function V or an action-value function Q over the state space or state-action space of the given MDP. VALUE ITERATION and POLICY ITERATION are two standard dynamic programming algorithms. You should study both of them using both V and Q, as these algorithms contain the basic building blocks for most RL algorithms.

3.1 Value iteration

3.1.1 Value iteration with the *V* function

Value Iteration aims at finding the optimal values V^* based on the Bellman Optimality Equation:

$$V^*(x) = \max_{u} \left[r(x, u) + \gamma \sum_{y \in S} P(x, u, y) V^*(y) \right].$$

In dynamic_programming.py, the value_iteration_v(mdp) function provides the code of value iteration using the V function. It is given as an example from which

you will derive other instances of dynamic programming algorithms. Look at it more closely, this will help for later questions:

- you can ignore the mdp.new_render() and mdp.render(...) functions which are here to provide the visualization of the iterations.
- find in the code the loop over states, the main loop that performs these updates until the values don't change significantly anymore, the main update equation. Found them? OK, you can continue...

3.1.2 Value iteration with the *Q* function

The state-action value function $Q^{\pi}(s,a)$ defines the value of being in state x, taking action u then following policy π . The Bellman Optimality Equation for Q^* is:

$$Q^{*}(x,u) = r(x,u) + \gamma \sum_{y} P(x,u,y) \max_{u'} Q^{*}(y,u').$$

Question 3: By taking inspiration from the value_iteration_v(mdp) function given in dynamic_programming.py, fill the blank (given with #Q[x,u]=...) in the code of value_iteration_q(mdp) and run it. Your final report must contain the missing piece of code.

3.2 Policy Iteration

Policy Iteration is more complicated than value iteration. Given a MDP and a policy π , policy iteration iterates the following steps:

- Evaluate policy π : compute V or Q based on the policy π ;
- Improve policy π : compute a better policy based on V or Q.

This process is repeated until convergence, i.e. when the policy cannot be improved anymore.

When using V, $V^{\pi}(x)$ is the expected return when starting from state x and following policy π . It is processed based on the Bellman Expectation Equation for deterministic policies:

$$V^{\pi}(x) = r(x, \pi(x)) + \gamma \sum_{y} P(x, \pi(x), y) V^{\pi}(y),$$

where:

- π is a deterministic policy, meaning that in a state x, the agent always selects the same action,
- $r(x,\pi(x))$ is the reward gained when taking action based on policy π in state x,
- $P(x,\pi(x),y)$ is the probability of ending in state y when taking action under policy π while in state x,
- $V^{\pi}(y)$ is the value of the state y under policy π ,

 γ∈ [0,1] is a discount factor defining the relative importance of long term rewards over short term ones (the closer to 0, the more the agent focuses on immediate rewards).

When using Q, the Bellman Expectation Equation with deterministic policy π for Q becomes:

$$Q^{\pi}(x,u) = r(x,u) + \gamma \sum_{y \in S} P(x,u,y) Q^{\pi}(y,\pi(y)).$$

The policy can then be updated as follows:

$$\pi^{(t+1)}(x) = \arg \max_{u} Q^{\pi^{(t)}}(x, u).$$

3.2.1 Intermediate functions

In order to facilitate the coding of policy iteration algorithms, we will first define a set of useful functions. The code for all the functions below should be given in your report.

Question 4: In dynamic_programming.py, code a function $get_policy_from_q(q)$, where q is the state-action value function. The more complicated function $get_policy_from_v(v)$, where v is the state value function, is given.

Question 5: Code a function improve_policy_from_v(mdp, v, policy), where mdp is a given MDP, v is some value function in this MDP and policy is some policy.

Question 6: The functions evaluate_one_step_v(mdp,v,policy), where mdp is a given MDP, v is some value function in this MDP and policy is some policy and the function evaluate_v(mdp,policy) are given. These functions give the value function V^{π} corresponding to policy π . By drawing inspiration on them, code a function evaluate_one_step_q(mdp,q,policy), where q is some action value function, and a function evaluate_q(mdp,policy).

3.2.2 Policy Iteration functions

Question 7: By using the above functions, fill the code of the policy_iteration_q(mdp) function, run it and visualize it. Include a picture of the final configuration in your report.

Question 8: By using the above functions, fill the code of the policy_iteration_v(mdp) function, run it and visualize it. Include a picture of the final configuration in your report.

3.3 Comparisons

Question 9: Compare the various dymanic programming functions in terms of iterations, elementary operations and time taken. To answer the question, add counters on the number of updates and iterations to the above codes and use a timer (with the time.time() function), run them again and get the results by printing counters and time. Discuss the relative computational efficiency of these methods (give a table with various measures).

3.3.1 Generalized Policy Iteration

The GENERALIZED POLICY ITERATION (GPI) algorithm² draws a continuum between value iteration and policy iteration.

Question 10: (**OPTIONAL and more difficult**) Code the GPI algorithm and parametrize it to obtain the value iteration regime, the policy iteration regime, and something intermediate. Report the performance of the various regimes.

4 Reinforcement learning functions

Reinforcement Learning is about finding the optimal policy in an MDP which is initially unknown to the agent. More precisely, the state and action spaces are known, but the agent does not know the transition and reward functions. Generally speaking, the agent has to explore the MDP to figure out which action in which state leads to which other state and reward. The model-free case is about finding this optimal policy just through very local updates, without storing any information about previous interactions with the environment. Principles of these local updates can already be found in the Temporal Difference (TD) algorithm, which iteratively computes optimal values for all state using local updates. The most widely used model-free RL algorithms are Q-LEARNING, SARSA and actor-critic algorithms. In the reinforcement_learning. py file, we focus on the first two.

4.1 TD learning

Given a state and an action spaces as well as a policy, TD(0) computes the state value of this policy based on the following equations:

$$\delta_t = r(x_t, u_t) + \gamma V^{(t)}(x_{t+1}) - V^{(t)}(x_t)$$
$$V^{(t+1)}(x_t) = V^{(t)}(x_t) + \alpha \delta_t$$

where δ is the TD error and α is a parameter called "learning rate".

The code is provided in reinforcement_learning.py, so that you can take inspiration later on. The important part is the computation of δ , and the update of the values of V.

²https://link.springer.com/content/pdf/10.1007/BF00933260.pdf

To run TD learning, a policy is needed as input. Such a policy can be retreived by using the policy iteration method defined in the dynamic_programming.py file.

Question 11: Fill the code of the temporal_difference(...) function and run it. Put into your report the corresponding code and a picture of the final configuration.

4.2 Q-learning

The Q-LEARNING algorithm accounts for an agent exploring an MDP and updating at each step a model of the state action-value function stored into a Q-table. It is updated as follows:

$$\begin{split} \delta_t &= r(x_t, u_t) + \gamma \max_{u_{t+1} \in A} Q^{(t)}(x_{t+1}, u_{t+1}) - Q^{(t)}(x_t, u_t) \\ Q^{(t+1)}(x_t, u_t) &= Q_{(t)}(x_t, u_t) + \alpha \delta_t. \end{split}$$

The Q-LEARNING function in reinforcement_learning.py gives the code of Q-LEARNING.

Question 12: Fill the code of the q_learning(...) function and run it. Put into your report the corresponding code and a picture of the final configuration.

4.2.1 Learning dynamics

If you watch carefully the values while the agent is learning, you will see that the agent favors certains paths over others which have a strictly equivalent value. This can be explained easily: as the agent chooses a path for the first time, it updates the values along that path, these values get higher than the surrounding values, and the agent will choose the same path again and again, increasing the phenomenon. Only steps of random exploration can counterbalance this effect, but they do so extremely slowly.

4.2.2 Exploration

In Q-LEARNING function, action selection is based on a *softmax* policy. Instead, it could have relied on ε -greedy.

Question 13: Copy-paste the Q-LEARNING function and do the replacement in the copy. The softmax and egreedy functions are available in toolbox.py. Put the corresponding code into your report. Then compare the behavior of Q-LEARNING using *softmax* and ε-*greedy* and comment the results in your report.

4.3 SARSA

The SARSA algorithm is very similar to Q-learning. At first glance, the only difference is in the update rule. However, to perform the update in SARSA, one needs to know the

action the agent will take when it will be at the next state, even if the agent is taking a random action.

This implies that the next state action is determined in advance and stored for being played at the next time step.

Question 14: By taking inspiration from the above Q-LEARNING function, fill the code of the sarsa(...) function that implements the corresponding algorithm, then run it. Put the corresponding code into your report. Again, compare the behavior of SARSA using *softmax* and ε -greedy and comment the results in your report.

4.4 Comparisons and hyper-parameters

Question 15: Compare in your report the number of steps needed by Q-LEARNING and SARSA to converge on the given MDP. To figure out, run your algorithm for a given number of steps (for instance, 10.000) and watch the corresponding Q-table: can you determine if one was updated more than another? Eventually, do so with much smaller mazes...

Question 16: When using *softmax*, the three main hyper-parameters of Q-LEARNING and SARSA are α , τ and γ . By varying the values of these hyper-parameters and watching the learning process, explain in your report their impact on the algorithm.

5 Going further

These lab instructions are taken from a richer set of labs available here: https://github.com/osigaud/rl_labs_notebooks

Note that studying actor-critic algorithms is a must if you want to study deep RL afterwards, because several state-of-the-art deep RL algorithms are actor-critic.

Trying to perform these further labs and putting the answers in your final report will result in a bonus on your final grade.