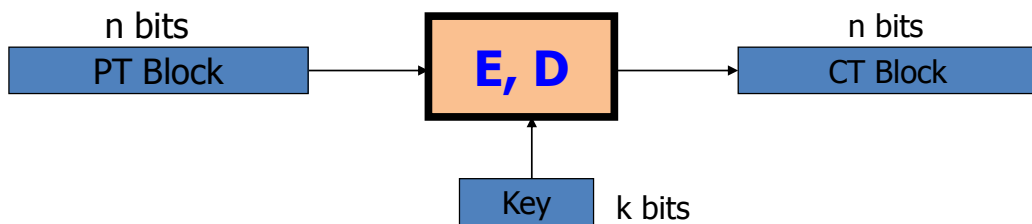




Block ciphers

What is a block cipher?

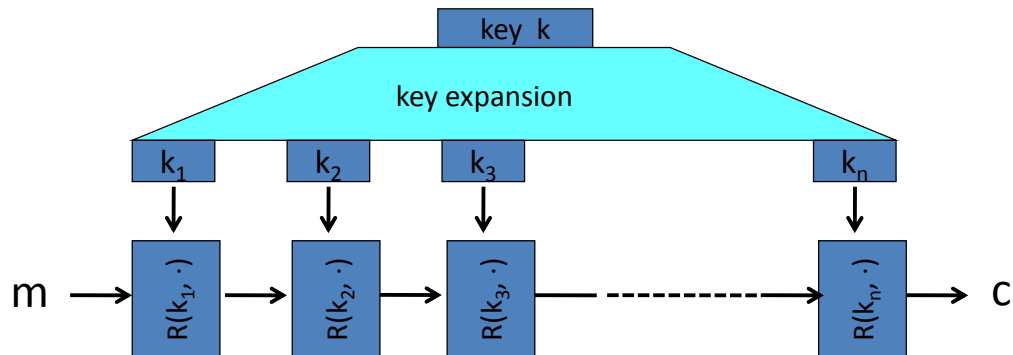
Block ciphers: crypto work horse



Canonical examples:

1. 3DES: $n = 64$ bits, $k = 168$ bits
2. AES: $n = 128$ bits, $k = 128, 192, 256$ bits

Block Ciphers Built by Iteration



$R(k, m)$ is called a round function

for 3DES ($n=48$), for AES-128 ($n=10$)

Dan Boneh

Performance:

Crypto++ 5.6.0 [Wei Dai]

AMD Opteron, 2.2 GHz (Linux)

	<u>Cipher</u>	<u>Block/key size</u>	<u>Speed (MB/sec)</u>
stream	RC4		126
	Salsa20/12		643
	Sosemanuk		727
block	3DES	64/168	13
	AES-128	128/128	109

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Abstractly: PRPs and PRFs

- Pseudo Random Function (**PRF**) defined over (K, X, Y) :

$$F: K \times X \rightarrow Y$$

such that exists “efficient” algorithm to evaluate $F(k, x)$

- Pseudo Random Permutation (**PRP**) defined over (K, X) :

$$E: K \times X \rightarrow X$$

such that:

1. Exists “efficient” deterministic algorithm to evaluate $E(k, x)$
2. The function $E(k, \cdot)$ is one-to-one
3. Exists “efficient” inversion algorithm $D(k, y)$

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Running example

- Example PRPs: 3DES, AES, ...

$$\text{AES: } K \times X \rightarrow X \quad \text{where} \quad K = X = \{0, 1\}^{128}$$

$$\text{3DES: } K \times X \rightarrow X \quad \text{where} \quad X = \{0, 1\}^{64}, \quad K = \{0, 1\}^{168}$$

- Functionally, any PRP is also a PRF.
 - A PRP is a PRF where $X=Y$ and is efficiently invertible.

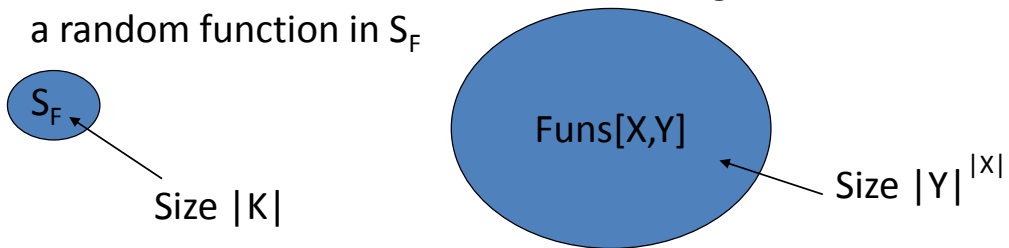
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Secure PRFs

- Let $F: K \times X \rightarrow Y$ be a PRF

$$\left\{ \begin{array}{l} \text{Funs}[X,Y]: \text{ the set of all functions from } X \text{ to } Y \\ S_F = \{ F(k, \cdot) \text{ s.t. } k \in K \} \subseteq \text{Funs}[X,Y] \end{array} \right.$$

- Intuition: a PRF is **secure** if a random function in $\text{Funs}[X,Y]$ is indistinguishable from a random function in S_F



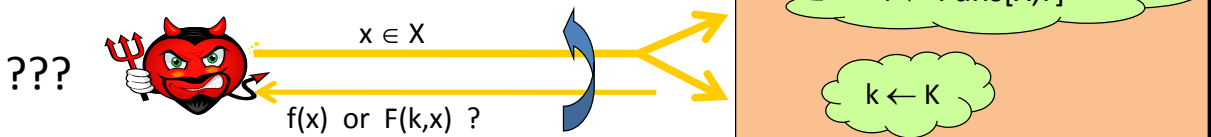
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Secure PRFs

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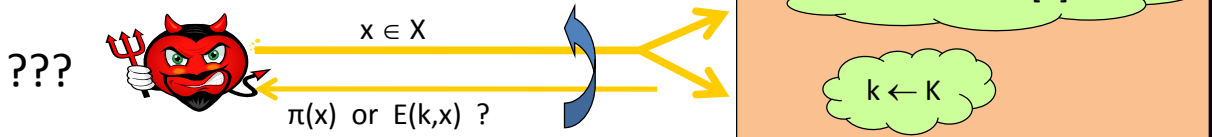


Secure PRPs (secure block cipher)

- Let $E: K \times X \rightarrow Y$ be a PRP

$$\left\{ \begin{array}{l} \text{Perms}[X]: \text{ the set of all } \underline{\text{one-to-one}} \text{ functions from } X \text{ to } Y \\ S_F = \{ E(k, \cdot) \text{ s.t. } k \in K \} \subseteq \text{Perms}[X, Y] \end{array} \right.$$

- Intuition: a PRP is **secure** if a random function in $\text{Perms}[X]$ is indistinguishable from a random function in S_F



Let $F: K \times X \rightarrow \{0,1\}^{128}$ be a secure PRF.

Is the following G a secure PRF?

$$G(k, x) = \begin{cases} 0^{128} & \text{if } x=0 \\ F(k, x) & \text{otherwise} \end{cases}$$

- ☐ No, it is easy to distinguish G from a random function
- ☐ Yes, an attack on G would also break F
- ☐ It depends on F

An easy application: $\text{PRF} \Rightarrow \text{PRG}$

Let $F: K \times \{0,1\}^n \rightarrow \{0,1\}^n$ be a secure PRF.

Then the following $G: K \rightarrow \{0,1\}^{nt}$ is a secure PRG:

$$G(k) = F(k,0) \parallel F(k,1) \parallel \dots \parallel F(k,t-1)$$

Key property: parallelizable

Security from PRF property: $F(k, \cdot)$ indist. from random function $f(\cdot)$

Dan Boneh

End of Segment