COMP3141

Software System Design and Implementation

SAMPLE EXAM

Term 2, 2020

- Total Number of **Parts**: 5.
- Total Number of Marks: 125
- All parts **are** of equal value.
- Answer **all** questions.
- Excessively verbose answers may lose marks
- Failure to make the declaration or making a false declaration results in a 100% mark penalty.
- Ensure you are the person listed on the declaration.
- All questions must be attempted **individually** without assistance from anyone else.
- You must **save** your exam paper using the button below **before** time runs out.
- Late submissions will not be accepted.
- You may save multiple times before the deadline. Only your final submission will be considered.

□ I, Stefan Gao (5211215), declare that these answers are entirely my own, and that I did

Declaration

not complete this exam with assistance from anyone else.					
Part A (25 Marks)					
Answer the following questions in a couple of short sentences. No need to be verbose. 1. (3 Marks) What is the difference between a <i>partial function</i> and <i>partial application</i> ?					
2. (3 Marks) Name <i>two</i> methods of measuring program coverage of a test suite, and explain how they differ.					

3. (3 Marks) How are multi-argument functions typically modelled in Haskell?

	getChar:: IO Char
	getChar::IO Char
(3	Marks) What is a <i>functional correctness</i> specification?
(3	Marks) Under what circumstances is performance important for an abstract mode
(3	Marks) What is the relevance of termination for the Curry-Howard correspondence
`	Marks) Imagine you are working on some price tracking software for some comparocks. You have already got a list of stocks to track pre-defined.
	data Stock = GOOG MSFT APPL stocks = [GOOG, MSFT, APPL]
	data Stock = GOOG MSFT APPL stocks = [GOOG, MSFT, APPL]
	our software is required to produce regular reports of the stock prices of these ompanies. Your co-worker proposes modelling reports simply as a list of prices:
	type Report = [Price]
	type Report = [Price]
po	There each price in the list is the stock price of the company in the corresponding osition of the <i>stocks</i> list. How is this approach potentially unsafe? What would be a after representation?

Part B (25 Marks)

The following questions pertain to the given Haskell code:

	$foldr :: (a \rightarrow b \rightarrow b) \rightarrow b \rightarrow [a] \rightarrow b$						
	foldr f z (x : xs) = f x (foldr f z xs) (1)						
	foldr f z [] = z (2)						
	foldr:: $(a \to b \to b) \to b \to [a] \to b$ foldr $fz(x:xs) = fx(\text{foldr} fz(xs)) (1)$ foldr $fz[] = z$ (2)						
1.	(3 Marks) State the type, if one exists, of the expression $foldr$ (:) ([] :: [Bool]) foldr (:) ([]:: [Bool]).						
2.	(4 Marks) Show the evaluation of $foldr$ (:) [] [1, 2] foldr (:) [] [1, 2] via equational reasoning.						
3.	(2 Marks) In your own words, describe what the function $foldr$ (:) [] foldr (:) [] does						

4. (12 Marks) We shall prove by induction on lists that, for all lists xsxs and ysys:

$$foldr$$
 (:) $xs ys = ys ++ xs$
foldr (:) $xs ys = ys ++ xs$

i. (3 Marks) First show this for the base case where ys = []ys = [] using equational reasoning. You may assume the left identity property for +++++, that is, for all ls1s:

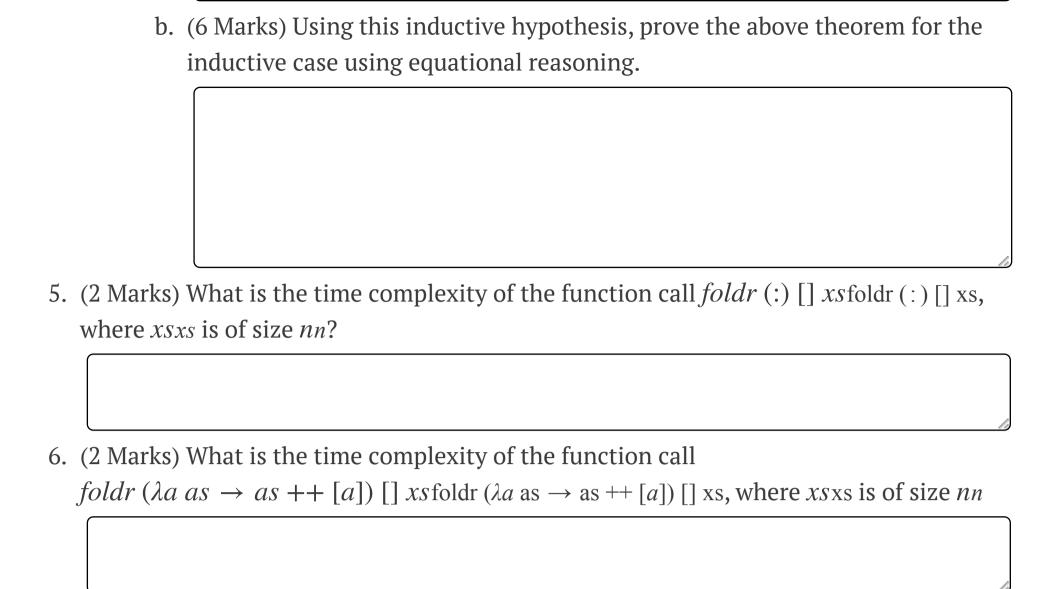
$$ls = [] ++ ls$$

 $ls = [] ++ ls$

ii (9 Marks) Next we have the case where $vs = (k \cdot ks)vs = (k \cdot ks)$ for some item kk

ii. (9 Marks) Next, we have the case where ys = (k : ks)ys = (k : ks) for some item kk and list ksks.

a. (3 Marks) What is the *inductive hypothesis* about ksks?



Part C (25 Marks)

A *sparse vector* is a vector where a lot of the values in the vector are zero. We represent a sparse vector as a list of position-value pairs, as well as an IntInt to represent the overall length of the vector:

We can convert a sparse vector back into a dense representation with this *expand* expand function:

```
expand :: SVec \rightarrow [Float]

expand (SV \ n \ vs) = map \ check \ [0..n-1]

where

check \ x = \mathbf{case} \ lookup \ x \ vs \ \mathbf{of}
Nothing \rightarrow 0
Just \ v \rightarrow v
expand :: SVec \rightarrow [Float]
expand (SV \ n \ vs) = map \ check \ [0..n-1]
where

check \ x = \mathbf{case} \ lookup \ x \ vs \ \mathbf{of}
Nothing \rightarrow 0
Just \ v \rightarrow v
```

For example, the SVecSVec value SV 5 [(0, 2.1), (4, 10.2)]SV 5 [(0, 2.1), (4, 10.2)] is

expanded	into [2.1, 0, 0, 0, 10.2][2.1, 0, 0, 0, 10.2]				
1. (16 Marks) There are a number of $SVec$ SVec values that do not correspond to a					
meaningful vector - they are invalid.					
	(6 Marks) Which two <i>data invariants</i> must be maintained to ensure validity of an $SVec$ SVec value? Describe the invariants in informal English.				
,	S v cos v co varae. Beserve ene invariantes in informar English.				
ii.	(4 Marks) Give two examples of $SVec$ SVec values which violate these invariants.				
	(6 Marks) Define a Haskell function $well formed :: SVec \rightarrow Bool$				
	wellformed:: SVec → Bool which returns TrueTrue iff the data invariants hold for				
	the input <i>SVecvalue</i> SVec <i>value</i> . Your Haskell doesn't have to be syntactically				
•	perfect, so long as the intention is clear.				
	You may find the function $nub :: (Eq a) \Rightarrow [a] \rightarrow [a] nub :: (Eq a) \Rightarrow [a] \rightarrow [a]$				
	useful, which removes duplicates from a list.				
2. (9 Ma	rks) Here is a function to multiply a $SVec$ SVec vector by a scalar:				
	$vsm :: SVec \rightarrow Float \rightarrow SVec$				
	$vsm (SV n vs) s = SV n (map (\lambda(p, v) \rightarrow (p, v * s)) vs)$				
	$vsm :: SVec \rightarrow Float \rightarrow SVec$				
	$vsm (SV n vs) s = SV n (map (\lambda(p, v) \rightarrow (p, v * s)) vs)$				
	(3 Marks) Define a function $vsmAvsmA$ that performs the same operation, but for dense vectors (i.e. lists of FloatFloat).				
ii.	(6 Marks) Write a set of properties to specify functional correctness of this function.				
	Hint: All the other functions you need to define the properties have already been				
1	mentioned in this part. It should maintain data invariants as well as refinement				

from the abstract model.

art D (25 Ma	arks)
,	ne you are working for a company that maintains this library for a nal records, about their customers, their staff, and their suppliers.
	$newtype Person = \dots$
	$name :: Person \rightarrow String$ $salary :: Person \rightarrow Maybe String$ $fire :: Person \rightarrow IO ()$ $company :: Person \rightarrow Maybe String$
	newtype Person =
	name:: Person → String salary:: Person → Maybe String fire:: Person → IO () company:: Person → Maybe String
member of compagiven person is a solution of the solution of t	function returns Nothing Nothing if given a person who is not a any staff. The <i>fire</i> fire function will also perform no-op unless the member of company staff. The <i>company</i> company function will returnless the given person is a supplier. It is a supplier type signatures to enforce the distinction between the different statically, within Haskell's type system. The function <i>name</i> name must sof people as input.

2. (15 Marks) Consider the following two types in Haskell:

data List a where

Nil :: List a

Cons :: $a \rightarrow List \ a \rightarrow List \ a$

data Nat = Z | S Nat

data Vec(n :: Nat) a where

VNil :: Vec Z a

VCons :: $a \rightarrow Vec \ n \ a \rightarrow Vec \ (S \ n) \ a$

data List a where

Nil :: List a

Cons :: $a \rightarrow \text{List } a \rightarrow \text{List } a$

 $data Nat = Z \mid S Nat$

data Vec (n:: Nat) a where

VNil :: Vec Z a

VCons :: $a \rightarrow \text{Vec } n \ a \rightarrow \text{Vec } (S \ n) \ a$

What is the difference between these types? In which circumstances would VecVec be the better choice, and in which ListList?

i. (5 Marks)

ii. (5 Marks) Here is a simple list function:

$$zip :: List \ a \to List \ b \to List \ (a, b)$$
 $zip \quad Nil \qquad ys \qquad = \quad Nil$
 $zip \quad xs \qquad Nil \qquad = \quad Nil$
 $zip \quad (Cons \ x \ xs) \quad (Cons \ y \ ys) \qquad = \quad Cons \ (x, y) \ (zip \ xs \ ys)$
 $zip :: List \ a \to List \ b \to List \ (a, b)$
 $zip \quad Nil \qquad ys \qquad = \quad Nil$
 $zip \quad xs \qquad Nil \qquad = \quad Nil$
 $zip \quad xs \qquad Nil \qquad = \quad Nil$
 $zip \quad (Cons \ x \ xs) \quad (Cons \ y \ ys) \qquad = \quad Cons \ (x, y) \ (zip \ xs \ ys)$

Define a new version of zipzip which operates on VecVec instead of ListList wherever possible. You can constrain the lengths of the input.

iii. (5 Marks) Here is another list function:

filter ::
$$(a \rightarrow \mathsf{Bool}) \rightarrow List \ a \rightarrow List \ a$$

filter $p \ \mathsf{Nil} = \mathsf{Nil}$

filter $p \ (\mathsf{Cons} \ x \ xs)$
 $| \ p \ x \ | \ \mathsf{Cons} \ x \ (filter \ p \ xs)$
 $| \ otherwise \ | \ filter \ p \ \mathsf{xs}$

filter :: $(a \rightarrow \mathsf{Bool}) \rightarrow \mathsf{List} \ a \rightarrow \mathsf{List} \ a$

filter $p \ \mathsf{Nil} = \mathsf{Nil}$

filter $p \ (\mathsf{Cons} \ x \ \mathsf{xs})$
 $| \ p \ x \ | \ \mathsf{Cons} \ x \ (\mathsf{filter} \ p \ \mathsf{xs})$
 $| \ p \ x \ | \ \mathsf{Cons} \ x \ (\mathsf{filter} \ p \ \mathsf{xs})$
 $| \ \mathsf{otherwise} \ | \ \mathsf{otherwise} \ | \ \mathsf{filter} \ p \ \mathsf{xs}$

Define a new version of *filter* filter which operates on *Vec* Vec instead of *List*List wherever possible.

Part E (25 Marks)

1. (10 Marks) An applicative functor is called *commutative* iff the order in which actions are sequenced does not matter. In addition to the normal applicative laws, a *commutative* applicative functor satisfies:

$$f \langle \$ \rangle u \langle * \rangle v = flip f \langle \$ \rangle v \langle * \rangle u$$
$$f \langle \$ \rangle u \langle * \rangle v = flip f \langle \$ \rangle v \langle * \rangle u$$

i. (2 Marks) Is the Maybe Applicative instance *commutative*? Explain your answer.

ii.	(3 Marks) We have seen two different Applicative Applicative instances for lists. Which of these instances, if any, are <i>commutative</i> ? Explain your answer.			
iii.	(5 Marks) A <i>commutative</i> monad is the same as a commutative applicative, only specialised to monads. Express the commutativity laws above in terms of monads, using either dodo notation or the raw pure/bind functions.			
`	Marks) Translate the following logical formulae into types, and provide Haskell			
V _	s that correspond to proofs of these formulae, if one exists. If not, explain why not. (2 Marks) $(A \lor B) \to (B \lor A)(A \lor B) \to (B \lor A)$			
ii.	$(2 \text{ Marks}) (A \lor A) \to A(A \lor A) \to A$			
iii.	$(3 \text{ Marks}) (A \land (B \lor C)) \rightarrow ((A \land B) \lor (A \land C))$ $(A \land (B \lor C)) \rightarrow ((A \land B) \lor (A \land C))$			
iv.	(3 Marks) $\neg ((A \rightarrow \bot) \lor A) \neg ((A \rightarrow \bot) \lor A)$			
(arks) Horo is a Haskell data type:			

3. (5 Marks) Here is a Haskell data type:

2.

$\mathbf{data}\ X$	=	First () A					
		Second () Void					
		Third (Either B ())					
$\operatorname{data} X$	=	First () A					
		Second () Void					
		Third (Either B ())					
Using known type isomorphisms, simplify this type as much as possible.							

END OF SAMPLE EXAM

(don't forget to save!)

Time Remaining

2h 9m 33s

Save