Note that the filtering distributions does not specify a valid joint distribution for the states, but the smoothing does.