**A** Random up-matching  $\mathcal{V}'$  **B** Projection of s and  $\phi_{\mathcal{V}'}\psi_{\mathcal{V}'}s$  on the Hodge decomposition



