

$$TSS = ESS + RSS$$

$$\sum_{i=1}^n (y_i - \bar{y})^2 = \sum_{i=1}^n (\hat{y}_i - \bar{y})^2 + \sum_{i=1}^n (\hat{y}_i - y_i)^2$$

$$R^2 = \frac{ESS}{TSS} = \text{prop. of ES explained}$$

$$\in (0, 1)$$

$$\underline{\text{cov}(\mathbf{e})} = \text{cov}(\mathbf{y} - \hat{\mathbf{y}}) = \text{cov}(\mathbf{y} - \mathbf{H}\mathbf{y})$$

$$= \text{cov}(\underbrace{(\mathbf{I} - \mathbf{H})}_{\mathbf{C}} \cdot \mathbf{y}) = (\mathbf{I} - \mathbf{H}) \cdot \underbrace{\text{cov}(\mathbf{y})}_{\sigma^2 \cdot \mathbf{I}} (\mathbf{I} - \mathbf{H})^T$$

$$= \sigma^2 (\mathbf{I} - \mathbf{H})(\mathbf{I} - \mathbf{H}^T) = \sigma^2 (\mathbf{I} - \mathbf{H} - \underbrace{\mathbf{H}^T}_{\mathbf{H}} + \underbrace{\mathbf{H}\mathbf{H}^T}_{\mathbf{H}})$$

$$\underline{\sigma^2 (\mathbf{I} - \mathbf{H})}$$