

# Optimal regulation of oligopolistic markets under discrete choice models of demand

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# Outline

- 1 Introduction
- 2 Modelling framework
- 3 Numerical experiments

# Regulated competitive markets in transportation

- Actors:
  - Demand: people as utility maximizers.
  - Supply: operators as profit maximizers.
  - Regulation: government as welfare maximizer.
- Issues:
  - Product differentiation
  - Fair treatment of market players
  - Externalities



# Case study: intercity travel



# Case study: alternatives

Alternative	0	1	2	3	4	5	6	7	8	9
Mode	Car	Air	Air	IC	HSR	HSR	HSR	HSR	HSR	HSR
Endogenous	No	No	No	No	Yes	Yes	Yes	Yes	Yes	Yes
Operator	-	-	-	-	1	1	1	2	2	2
Dep	-	7:10	8:10	2:00	5:45	6:15	6:45	5:35	6:05	6:35
Arr	-	8:20	9:20	10:00	8:45	9:15	9:45	8:55	9:25	9:55
TT	6h	1h10'	1h10'	8h	3h	3h	3h	3h20'	3h20'	3h20'
WT	-	1h	1h	-	-	-	-	-	-	-
Access	-	30-60'	30-60'	0-60'	0-60'	0-60'	0-60'	0-60'	0-60'	0-60'
Egress	-	30-60'	30-60'	0-30'	0-30'	0-30'	0-30'	0-30'	0-30'	0-30'
Price	100 €	60 €	60 €	30 €	$p_4$	$p_5$	$p_6$	$p_7$	$p_8$	$p_9$

Table: Attributes of all scheduled services for problem instance 1.

# Case study: alternatives

Alternative	0	1	2	3	4	5	6	7	8	9
Mode	Car	Air	Air	IC	HSR	HSR	HSR	HSR	HSR	HSR
Endogenous	No	No	No	No	Yes	Yes	Yes	Yes	Yes	Yes
Operator	-	-	-	-	1	1	1	2	2	2
Dep	-	8:40	10:40	22:00	5:10	6:10	7:10	5:00	6:00	7:00
Arr	-	10:10	12:10	10:00	10:40	11:40	12:40	11:00	12:00	13:00
TT	<b>8h30'</b>	<b>1h30'</b>	<b>1h30'</b>	<b>12h</b>	<b>5h30'</b>	<b>5h30'</b>	<b>5h30'</b>	<b>6h</b>	<b>6h</b>	<b>6h</b>
WT	-	1h	1h	-	-	-	-	-	-	-
Access	-	30-60'	30-60'	0-60'	0-60'	0-60'	0-60'	0-60'	0-60'	0-60'
Egress	-	30-60'	30-60'	0-30'	0-30'	0-30'	0-30'	0-30'	0-30'	0-30'
Price	110 €	60 €	60 €	40 €	$p_4$	$p_5$	$p_6$	$p_7$	$p_8$	$p_9$

**Table:** Attributes of all scheduled services for problem instance 2.

- 1 Introduction
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## Demand: discrete choice

- Discrete choice models allow to model choices of customers with different tastes and socioeconomic characteristics.
- Linearization: simulation is used to draw  $R$  times from the distribution of the error term of the utility function [Pacheco et al., 2017].

$$U_{inr} = V_{in} + \xi_{inr}.$$

- In each scenario, customers choose the alternative with the highest utility:

$$P_{inr} = \begin{cases} 1 & \text{if } U_{inr} = \max_{j \in I} U_{jnr}, \\ 0 & \text{otherwise.} \end{cases}$$

- Over  $R$  scenarios, the probability of customer  $n$  choosing alternative  $i$  is

$$P_{in} = \frac{\sum_{r \in R} P_{inr}}{R}.$$



## Case study: demand

$\beta$	Business travelers			Other purpose travelers	
$\mu_{Air}$		1.086		1.106	
$\mu_{HSR1}$		1.190		1.333	
$\mu_{HSR2}$		1.134		1.299	
Travel time (min)		-0.0133		-0.0054	
Access/egress time (min)		-0.00555		-0.0103	
Early schedule delay (min)		-0.00188		-0.00677	
Late schedule delay (min)		-0.0130		-0.00617	
Dummy male car (1/0)		1.400		0.550	
	Reimbursed	High income	Low income	High income	Low income
Cost car (euro)	-0.0222*	-0.0296*	-0.0527	-0.0228*	-0.0405
Cost Air (euro)	-0.0109	-0.0113*	-0.0201	-0.0109*	-0.0194
Cost IC (euro)	-0.0158	-0.0212*	-0.0377	-0.0097*	-0.0172
Cost HSR (euro)	-0.0120	-0.0160*	-0.0284	-0.0144*	-0.0256
Value of Travel Time	Reimbursed	High income	Low income	High income	Low income
Car (euro/h)	35.88*	26.95*	15.14	14.24*	8.00
Air (euro/h)	73.21	70.67*	39.70	29.73*	16.70
IC (euro/h)	50.51	37.68*	21.17	33.54*	18.84
HSR (euro/h)	66.50	50.02*	28.10	22.53*	12.66

Table: Nested logit model parameters and VoTTs derived from Cascetta and Coppola [2012].

# Case study: demand

- Origin
- Purpose
- Income
- Desired arrival time

Trip purpose



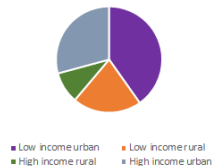
Trip origin



Income

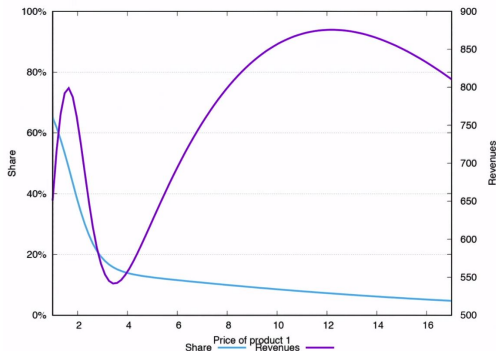


Income and trip origin



# Supply: optimization

- Each supplier  $k \in K$  chooses the strategy that maximizes its profits.
- Discrete choice models are embedded into the optimization problem of the suppliers.



From the MOOC Introduction to Discrete Choice Models (Michel Bierlaire and Virginie Lurkin)

# Choice-based optimization: MILP model

$$\max_{s=(p,X)} \pi_s = \frac{1}{|R|} \sum_{i \in I_k} \sum_{n \in N} \sum_{r \in R} p_{in} P_{inr} - c(X),$$

$$s.t. \quad U_{inr} = \beta_{p,in} p_{in} + \beta_{in} X_{in} + q_{in} + \xi_{inr}$$

$$U_{inr} \leq U_{nr}$$

$$U_{nr} \leq U_{inr} + M_{U_{nr}}(1 - P_{inr})$$

$$\sum_{i \in I} P_{inr} = 1$$

$$P_{inr} \in \{0, 1\}$$

$$\forall i \in I, \forall n \in N, \forall r \in R,$$

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# Regulation

- The utilities  $U_{inr}$  depend on the prices  $p_{in}$ .

$$p_{in} = r_{in} + t_{in} - s_{in},$$

where

- $r_{in}$  is the revenue made by the supplier in case of purchase,
  - $s_{in}$  is the subsidy given by the regulator to the consumer,
  - $t_{in}$  is the tax imposed by the regulator to the consumer.
- In case of purchase we have that
    - the consumer pays  $r_{in} + t_{in} - s_{in}$ ,
    - the supplier receives  $r_{in}$ ,
    - the regulator intervenes with  $t_{in} - s_{in}$ , i.e. it gives  $s_{in}$  to or receives  $t_{in}$  from the consumer, or does not intervene at all ( $s_{in} = t_{in} = 0$ ).

# Market equilibrium

- We look for  $\varepsilon$ -equilibrium solutions: stationary states of the system in which no competitor has an incentive to change its decision to increase profit by more than  $\varepsilon\%$ .
- Fixed-point iteration algorithm
- Fixed-point MIP model



# Fixed-point MIP model for the regulator

$$\max \quad \frac{1}{|N||R|} \sum_{i \in I_s} \sum_{n \in N} \sum_{r \in R} P_{inr}'$$

s.t. Equilibrium constraints:

$$\pi_k'' \leq (1 + \varepsilon) \pi_k' \quad \forall k \in K,$$

Regulator constraints:

$$\sum_{n \in N} \sum_{r \in R} \sum_{i \in I} P_{inr}' (s_{in} - t_{in}) \leq B,$$

$$s_{in} = s_{jn} \quad \forall i, j \in I_s, \forall n \in N,$$

$$s_{in} = 0 \quad \forall i \in I \setminus I_s, \forall n \in N,$$

$$t_{in} = t_{jn} \quad \forall i, j \in I_t, \forall n \in N,$$

$$t_{in} = 0 \quad \forall i \in I \setminus I_t, \forall n \in N,$$

Supplier and consumer constraints:

...

# Algorithmic approach

- ① Identify candidate equilibrium regions efficiently.
- ② Use exact method on restricted strategy sets derived from step 1 to find a subgame equilibrium: fixed-point MIP model.
- ③ Verify if best-response conditions are satisfied for the initial problem:

$$\pi_k^{BR} \leq (1 + \varepsilon)\pi_k^{FP} \quad \forall k \in K.$$

If they are not, modify the restricted problem (add/remove strategies) and go to step 2.

- Do multiple runs to search for different  $\varepsilon$ -equilibrium solutions.



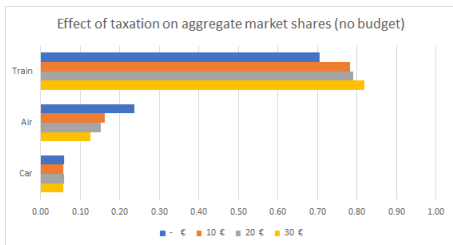
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# Regulation of an intercity travel market

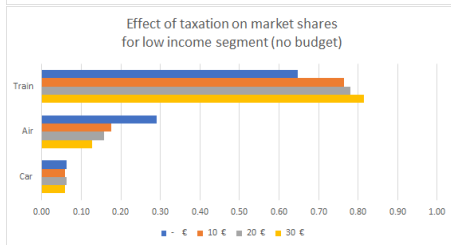
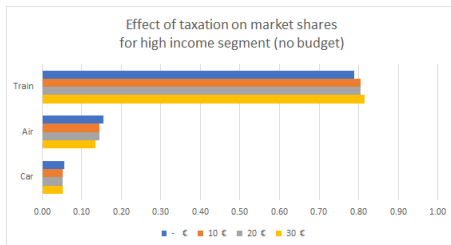
- The regulator wants to promote low-emission mobility.
- Subsidies or tax must satisfy some constraints.
- What are the optimal levels?
  - Competition analysis, e.g. how do supply pricing strategies change?
  - Demand analysis, e.g. what is the effect on choices and utilities on specific segments of the population?
  - Environmental analysis, e.g. what are the marginal abatement costs in different budget scenarios?



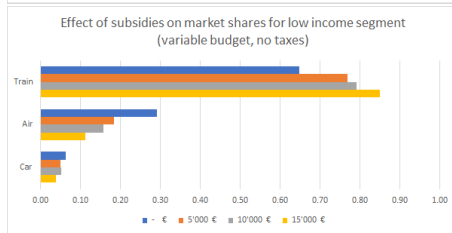
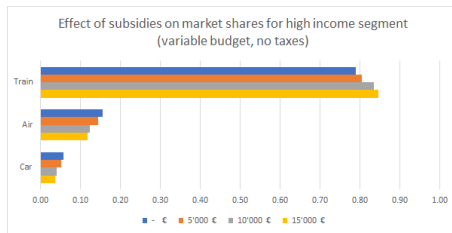
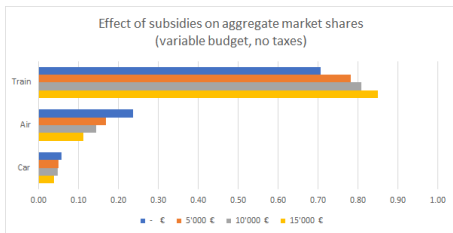
# Preliminary tests: 3h-3h30' train travel time



- Train subsidies are financed through taxation on air travel.
- More low income travellers are priced out of flying.

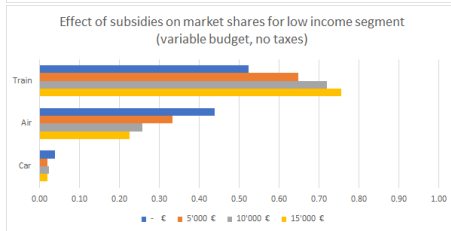
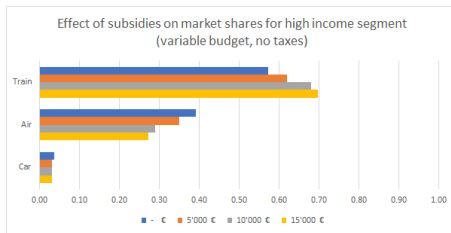
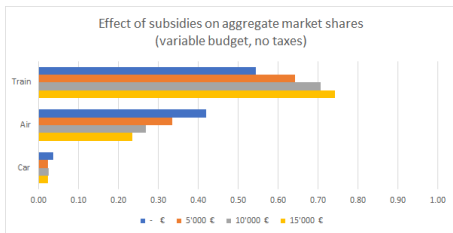


# Preliminary tests: 3h-3h30' train travel time



- Train subsidies are financed with a fixed budget.
- Higher modal shift.
- Cost-benefit analysis needed to compare with monetized benefits.

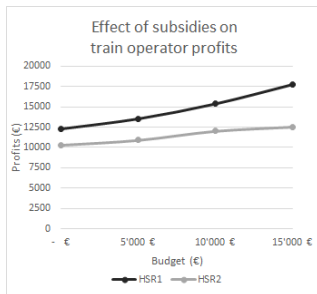
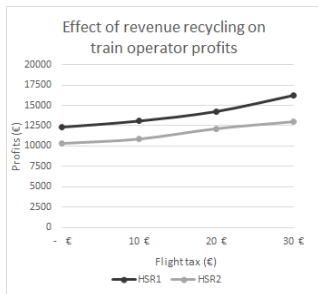
# Preliminary tests: 5h30'-6h train travel time



- Flying gives higher travel time savings.
- Higher initial modal share.
- Money "better spent" than in previous case.

# Preliminary tests: 5h30'-6h train travel time

- Part of the subsidies is cashed in by the train operators...
- ...but we are currently neglecting the competitive behaviour of airlines.



# Summary

- Discrete choice models are embedded in the optimization problems of the suppliers.
- We use an algorithmic approach to find market  $\varepsilon$ -equilibrium solutions.
- Subsidies or taxes are set by the regulator to maximize welfare or achieve other targets, subject to budget or market-specific constraints.
- The application to a realistic case study shows potential for various types of analysis.
- The framework is very general and can accommodate many complex discrete choice models.

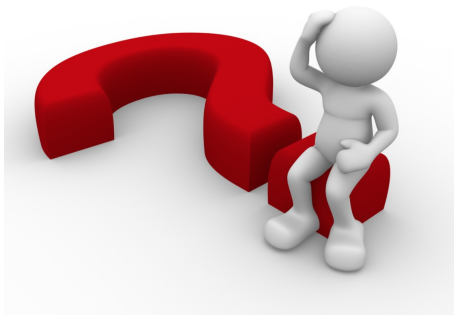
# Next steps

- Improve models and try to reduce computational times.
- Allow targeted measures on the regulator side.
- Do more experiments and refine case studies.





# Questions and discussion time



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