

# Supplementary Material

## EGAD: Evolving Graph Representation Learning with Self-Attention and Knowledge Distillation for Live Video Streaming Events

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Table 1. Effect on RMSE when varying the representation size  $d$  of the examined models for LiveStream-4K. We report average RMSE over the graph snapshots during the live video streaming event. Bold values denote the best configuration for each examined model.

Representation size $d$	DynVGAE	EvolveGCN	DySAT	DMTKG- $\mathcal{T}$	DMTKG- $\mathcal{S}$	EGAD- $\mathcal{T}$	EGAD- $\mathcal{S}$
16	0.23 $\pm$ 0.14	0.27 $\pm$ 0.09	0.18 $\pm$ 0.07	0.28 $\pm$ 0.14	0.27 $\pm$ 0.15	0.17 $\pm$ 0.09	<b>0.13 <math>\pm</math> 0.09</b>
32	0.21 $\pm$ 0.12	<b>0.25 <math>\pm</math> 0.12</b>	0.16 $\pm$ 0.10	0.26 $\pm$ 0.13	<b>0.23 <math>\pm</math> 0.17</b>	0.16 $\pm$ 0.05	0.15 $\pm$ 0.10
64	<b>0.19 <math>\pm</math> 0.13</b>	0.26 $\pm$ 0.18	<b>0.15 <math>\pm</math> 0.09</b>	<b>0.25 <math>\pm</math> 0.16</b>	0.24 $\pm$ 0.12	<b>0.14 <math>\pm</math> 0.08</b>	0.16 $\pm$ 0.06
128	0.20 $\pm$ 0.17	0.26 $\pm$ 0.12	0.17 $\pm$ 0.08	0.26 $\pm$ 0.17	0.25 $\pm$ 0.16	0.15 $\pm$ 0.06	0.16 $\pm$ 0.08
256	0.21 $\pm$ 0.15	0.27 $\pm$ 0.15	0.18 $\pm$ 0.05	0.27 $\pm$ 0.19	0.26 $\pm$ 0.14	0.16 $\pm$ 0.07	0.17 $\pm$ 0.06

Table 2. Effect on RMSE when varying the representation size  $d$  of the examined models for LiveStream-6K

Representation size $d$	DynVGAE	EvolveGCN	DySAT	DMTKG- $\mathcal{T}$	DMTKG- $\mathcal{S}$	EGAD- $\mathcal{T}$	EGAD- $\mathcal{S}$
16	0.48 $\pm$ 0.16	0.47 $\pm$ 0.12	0.41 $\pm$ 0.15	0.48 $\pm$ 0.18	0.48 $\pm$ 0.14	0.41 $\pm$ 0.12	<b>0.36 <math>\pm</math> 0.06</b>
32	0.46 $\pm$ 0.16	<b>0.44 <math>\pm</math> 0.11</b>	0.40 $\pm$ 0.17	0.47 $\pm$ 0.18	<b>0.41 <math>\pm</math> 0.12</b>	0.39 $\pm$ 0.09	0.37 $\pm$ 0.09
64	<b>0.45 <math>\pm</math> 0.18</b>	0.45 $\pm$ 0.13	<b>0.39 <math>\pm</math> 0.18</b>	<b>0.43 <math>\pm</math> 0.16</b>	0.43 $\pm$ 0.15	<b>0.37 <math>\pm</math> 0.10</b>	0.39 $\pm$ 0.10
128	0.46 $\pm$ 0.17	0.45 $\pm$ 0.14	0.41 $\pm$ 0.16	0.45 $\pm$ 0.14	0.44 $\pm$ 0.16	0.38 $\pm$ 0.11	0.40 $\pm$ 0.08
256	0.46 $\pm$ 0.18	0.46 $\pm$ 0.18	0.42 $\pm$ 0.14	0.46 $\pm$ 0.12	0.46 $\pm$ 0.18	0.38 $\pm$ 0.11	0.42 $\pm$ 0.07

Table 3. Effect on RMSE when varying the representation size  $d$  of the examined models for LiveStream-16K

Representation size $d$	DynVGAE	EvolveGCN	DySAT	DMTKG- $\mathcal{T}$	DMTKG- $\mathcal{S}$	EGAD- $\mathcal{T}$	EGAD- $\mathcal{S}$
16	0.36 $\pm$ 0.13	0.35 $\pm$ 0.18	0.29 $\pm$ 0.16	0.39 $\pm$ 0.15	0.39 $\pm$ 0.12	0.27 $\pm$ 0.10	<b>0.23 <math>\pm</math> 0.07</b>
32	0.35 $\pm$ 0.14	<b>0.33 <math>\pm</math> 0.19</b>	0.29 $\pm$ 0.14	0.37 $\pm$ 0.14	0.36 $\pm$ 0.11	0.26 $\pm$ 0.09	0.25 $\pm$ 0.09
64	<b>0.33 <math>\pm</math> 0.12</b>	0.34 $\pm$ 0.11	<b>0.27 <math>\pm</math> 0.14</b>	0.36 $\pm$ 0.15	<b>0.33 <math>\pm</math> 0.11</b>	<b>0.24 <math>\pm</math> 0.09</b>	0.26 $\pm$ 0.06
128	0.34 $\pm$ 0.11	0.35 $\pm$ 0.13	0.28 $\pm$ 0.13	<b>0.35 <math>\pm</math> 0.12</b>	0.35 $\pm$ 0.15	0.25 $\pm$ 0.10	0.26 $\pm$ 0.08
256	0.34 $\pm$ 0.17	0.36 $\pm$ 0.11	0.29 $\pm$ 0.12	0.38 $\pm$ 0.13	0.36 $\pm$ 0.18	0.26 $\pm$ 0.10	0.27 $\pm$ 0.10

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Table 4. Impact of the window size  $l$  on the performance of each examined model in terms of RMSE for LiveStream-4K

Window size $l$	DynVGAE	EvolveGCN	DySAT	DMTKG- $\mathcal{T}$	DMTKG- $\mathcal{S}$	EGAD- $\mathcal{T}$	EGAD- $\mathcal{S}$
1	0.32 $\pm$ 0.16	0.35 $\pm$ 0.19	0.21 $\pm$ 0.12	N/A	N/A	0.18 $\pm$ 0.06	0.16 $\pm$ 0.05
2	<b>0.19 <math>\pm</math> 0.13</b>	<b>0.25 <math>\pm</math> 0.12</b>	<b>0.15 <math>\pm</math> 0.09</b>	N/A	N/A	0.16 $\pm$ 0.09	0.14 $\pm$ 0.06
3	0.24 $\pm$ 0.18	0.28 $\pm$ 0.14	0.19 $\pm$ 0.14	N/A	N/A	<b>0.14 <math>\pm</math> 0.08</b>	<b>0.13 <math>\pm</math> 0.09</b>
4	0.29 $\pm$ 0.12	0.32 $\pm$ 0.16	0.20 $\pm$ 0.12	N/A	N/A	0.17 $\pm$ 0.10	0.16 $\pm$ 0.04
5	0.36 $\pm$ 0.17	0.42 $\pm$ 0.19	0.24 $\pm$ 0.14	N/A	N/A	0.20 $\pm$ 0.09	0.19 $\pm$ 0.06

Table 5. Impact of the window size  $l$  on the performance of each examined model in terms of RMSE for LiveStream-6K

Window size $l$	DynVGAE	EvolveGCN	DySAT	DMTKG- $\mathcal{T}$	DMTKG- $\mathcal{S}$	EGAD- $\mathcal{T}$	EGAD- $\mathcal{S}$
1	0.48 $\pm$ 0.16	0.56 $\pm$ 0.11	0.42 $\pm$ 0.14	N/A	N/A	0.41 $\pm$ 0.11	0.39 $\pm$ 0.07
2	<b>0.45 <math>\pm</math> 0.18</b>	<b>0.44 <math>\pm</math> 0.11</b>	<b>0.39 <math>\pm</math> 0.18</b>	N/A	N/A	0.38 $\pm$ 0.08	0.37 $\pm$ 0.09
3	0.46 $\pm$ 0.14	0.49 $\pm$ 0.13	0.41 $\pm$ 0.16	N/A	N/A	<b>0.37 <math>\pm</math> 0.10</b>	<b>0.36 <math>\pm</math> 0.06</b>
4	0.52 $\pm$ 0.19	0.51 $\pm$ 0.12	0.43 $\pm$ 0.12	N/A	N/A	0.40 $\pm$ 0.09	0.39 $\pm$ 0.04
5	0.54 $\pm$ 0.12	0.54 $\pm$ 0.18	0.49 $\pm$ 0.15	N/A	N/A	0.43 $\pm$ 0.12	0.40 $\pm$ 0.05

Table 6. Impact of the window size  $l$  on the performance of each examined model in terms of RMSE for LiveStream-16K

Window size $l$	DynVGAE	EvolveGCN	DySAT	DMTKG- $\mathcal{T}$	DMTKG- $\mathcal{S}$	EGAD- $\mathcal{T}$	EGAD- $\mathcal{S}$
1	0.42 $\pm$ 0.12	0.38 $\pm$ 0.16	0.33 $\pm$ 0.16	N/A	N/A	0.31 $\pm$ 0.10	0.29 $\pm$ 0.06
2	<b>0.33 <math>\pm</math> 0.12</b>	<b>0.33 <math>\pm</math> 0.19</b>	<b>0.27 <math>\pm</math> 0.14</b>	N/A	N/A	0.29 $\pm$ 0.11	0.27 $\pm$ 0.08
3	0.37 $\pm$ 0.11	0.36 $\pm$ 0.17	0.29 $\pm$ 0.12	N/A	N/A	<b>0.24 <math>\pm</math> 0.09</b>	<b>0.23 <math>\pm</math> 0.07</b>
4	0.39 $\pm$ 0.18	0.39 $\pm$ 0.19	0.31 $\pm$ 0.16	N/A	N/A	0.30 $\pm$ 0.07	0.29 $\pm$ 0.09
5	0.46 $\pm$ 0.14	0.41 $\pm$ 0.15	0.39 $\pm$ 0.14	N/A	N/A	0.38 $\pm$ 0.10	0.24 $\pm$ 0.10

Table 7. Effect on RMSE when varying the number of heads  $h$  of the self-attention mechanisms of DySAT, EGAD- $\mathcal{T}$  and EGAD- $\mathcal{S}$  for LiveStream-4K

Number of heads $h$	DynVGAE	EvolveGCN	DySAT	DMTKG- $\mathcal{T}$	DMTKG- $\mathcal{S}$	EGAD- $\mathcal{T}$	EGAD- $\mathcal{S}$
1	N/A	N/A	0.19 $\pm$ 0.06	N/A	N/A	0.16 $\pm$ 0.05	<b>0.13 <math>\pm</math> 0.09</b>
2	N/A	N/A	0.17 $\pm$ 0.07	N/A	N/A	0.15 $\pm$ 0.04	0.14 $\pm$ 0.10
3	N/A	N/A	<b>0.15 <math>\pm</math> 0.09</b>	N/A	N/A	<b>0.14 <math>\pm</math> 0.08</b>	0.16 $\pm$ 0.08
4	N/A	N/A	0.16 $\pm$ 0.08	N/A	N/A	0.16 $\pm$ 0.07	0.17 $\pm$ 0.09
5	N/A	N/A	0.18 $\pm$ 0.08	N/A	N/A	0.17 $\pm$ 0.09	0.20 $\pm$ 0.03

Table 8. Effect on RMSE when varying the number of heads  $h$  of the self-attention mechanisms of DySAT, EGAD- $\mathcal{T}$  and EGAD- $\mathcal{S}$  for LiveStream-6K.

Number of heads $h$	DynVGAE	EvolveGCN	DySAT	DMTKG- $\mathcal{T}$	DMTKG- $\mathcal{S}$	EGAD- $\mathcal{T}$	EGAD- $\mathcal{S}$
1	N/A	N/A	0.47 $\pm$ 0.12	N/A	N/A	0.42 $\pm$ 0.07	<b>0.36 <math>\pm</math> 0.06</b>
2	N/A	N/A	0.45 $\pm$ 0.15	N/A	N/A	0.40 $\pm$ 0.12	0.38 $\pm$ 0.06
3	N/A	N/A	<b>0.39 <math>\pm</math> 0.18</b>	N/A	N/A	<b>0.37 <math>\pm</math> 0.10</b>	0.41 $\pm$ 0.04
4	N/A	N/A	0.41 $\pm$ 0.14	N/A	N/A	0.38 $\pm$ 0.10	0.43 $\pm$ 0.09
5	N/A	N/A	0.46 $\pm$ 0.17	N/A	N/A	0.39 $\pm$ 0.11	0.43 $\pm$ 0.08

Table 9. Effect on RMSE when varying the number of heads  $h$  of the self-attention mechanisms of DySAT, EGAD- $\mathcal{T}$  and EGAD- $\mathcal{S}$  for LiveStream-16K

Number of heads $h$	DynVGAE	EvolveGCN	DySAT	DMTKG- $\mathcal{T}$	DMTKG- $\mathcal{S}$	EGAD- $\mathcal{T}$	EGAD- $\mathcal{S}$
1	N/A	N/A	$0.32 \pm 0.17$	N/A	N/A	$0.28 \pm 0.08$	<b><math>0.23 \pm 0.07</math></b>
2	N/A	N/A	$0.29 \pm 0.18$	N/A	N/A	$0.26 \pm 0.10$	$0.25 \pm 0.05$
3	N/A	N/A	$0.28 \pm 0.15$	N/A	N/A	<b><math>0.24 \pm 0.09</math></b>	$0.26 \pm 0.09$
4	N/A	N/A	<b><math>0.27 \pm 0.14</math></b>	N/A	N/A	$0.25 \pm 0.06$	$0.26 \pm 0.10$
5	N/A	N/A	$0.29 \pm 0.12$	N/A	N/A	$0.27 \pm 0.07$	$0.27 \pm 0.08$