CS 476/676 (Spring 2021): Homework 1

Due: Feb 3, 2021 at 11:59pm EST

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Instructions: This homework requires some open-ended questions, short proofs, and programming. This is an individual assignment, not group work. Though you may discuss the problems with your classmates, you must solve the problems and write the solutions independently. As stated in the syllabus, copying code from a classmate or the internet (even with minor changes) constitutes plagiarism. You are required to submit your answers in pdf form (use LATEX) in a file called <your-JHED>-hw1.pdf to Gradescope. (Note: for those who not familiar with LATEX, you can visit https://www.overleaf.com to quickly start by using the provided .tex template file.) The code for the programming assignment will be handed in separately on github; see the instructions under Problem 8. Late submissions will be penalized, except in extenuating circumstances such as medical or family emergency. Submissions submitted 0-24 hours late will be penalized 10%, 24-48 hours late by 20%, 48-72 hours late by 30%, and later than 72 hours by 100%. Late days may be used (if available) to avoid these penalties. Problems 1 and 2 are worth 5 points each, Problem 3 is worth 10 points, and Problem 4 is worth 15 points, for a total of 35 points.

Problem 1

This is an open-ended question to get you a head start on thinking about what you would like to do for your final project. Write a brief description of the kinds of data you have worked with (if you have not worked with data before, it is ok to say so) and would like to work with in this course. What questions did you/would you like to answer with such data? There are no right or wrong answers; a paragraph or two is sufficient.

I've worked with assorted datasets in CS475: Machine Learning, but no par-
ticular one stands out in my memory. I did compile a small dataset of con-
sisting of song lyrics for Billboard's then-current Top 100 Songs for a per-
sonal project that was then put through some standard NLP pre-processing
steps.
In this class, I would like to work with some kind of social network data,
or perhaps more advanced listening analytics from a streaming service such
as Spotify or Apple Music. Generally, I am interested more in sociological,
cultural, or psychological data.

Problem 2

Prove that $X \perp\!\!\!\perp Y \mid Z$ implies that $\mathrm{OR}(X,Y \mid Z) = 1$ for all x,y,z.

Write your answer here.							

Problem 3

Consider three sets of random variables X, Y, and Z. Assume that X and Y are binary random variables and the relations between X, Y, and Z can be modeled

via a linear logistic regression (i.e., no interaction terms.) That is,

$$p(X = 1 \mid Y, Z) = \frac{1}{1 + \exp(-(\beta_0 + \beta_1 Y + \beta_2 Z))}.$$

Let the reference values of X and Y be $x_0 = 0$ and $y_0 = 0$ respectively. Prove

$$OR(X, Y \mid Z) = \begin{cases} exp(\beta_1), & \text{if } X = Y = 1\\ 1, & \text{otherwise.} \end{cases}$$

W	Write your answer here.								

Problem 4

Implement a method/function which takes data in the form of a comma separated file (csv) and returns a point estimate for the odds ratio via logistic regression, and confidence intervals via bootstrap for the same. We recommend using the statsmodels package in Python for fitting any regression models in this course – the reason for this is because sklearn does not allow you to (easily) turn off regularization. Regularization is useful when considering out-of-sample prediction, but will bias your estimate of the statistical parameters we are interested in computing.

Use your function to compute point estimates and confidence intervals for OR(Mortality, Opera) and $OR(Mortality, Opera \mid Income)$ from the data provided in data.txt. Set the number of bootstraps to 200 when computing your confidence intervals. Based on the numbers you have computed, would you say

- a) Mortality ⊥ Opera?
- b) Mortality ⊥ Opera | Income?

Provide a brief comment on how seriously the above numbers you computed and the implied dependence/independence relations should be interpreted causally.

Report the numbers you computed and answers to the above questions in the PDF that you turn in. Hand in your Python code separately. Please make sure your variables and functions are aptly named, and your code is clear and readable, with comments where appropriate. We may try to execute your code on a new dataset as a test case, but don't worry too much about making your code robust in terms of error checking and adversarial inputs – this new dataset will look very similar to the one we have provided.

A brief explanation of the data and the variables. The data is simulated, but heavily inspired by a longitudinal study on the health benefits of engaging in the arts – going to the opera, theatre, museum etc.

- age: individual's age at beginning of the study
- income: individual's income at beginning of the study
- college_degree: did the individual hold a college degree at the beginning of the study (1 = yes, 0 = no)
- opera: was the individual attending the opera regularly (once a month or more) at the beginning of the study (1 = yes, 0 = no)
- mortality: did the individual die during the 5-year period of the study $(1=yes,\,0=no)$

Write your answer here.				