

1. (1 point) Solve the following system of equations.

$$\begin{aligned}x + 3y &= 17 \\ 5x &= 25\end{aligned}$$

Write your answer in point notation: e.g., for $x = 4, y = -3$ write $(4, -3)$.

Answer: _____

2. (1 point) Solve the following system of equations. Your answer must be a point. If there is no solution, type *None* and if there are infinitely many solutions, type x for x , and an expression in terms of x for the y -coordinate.

$$\begin{aligned}4x + 3y &= -2 \\ -2x - y &= -2\end{aligned}$$

Answer: _____

3. (1 point)

Solve the system of equations by graphing. Choose the graph that represents the two given line equations, and then enter the solution.

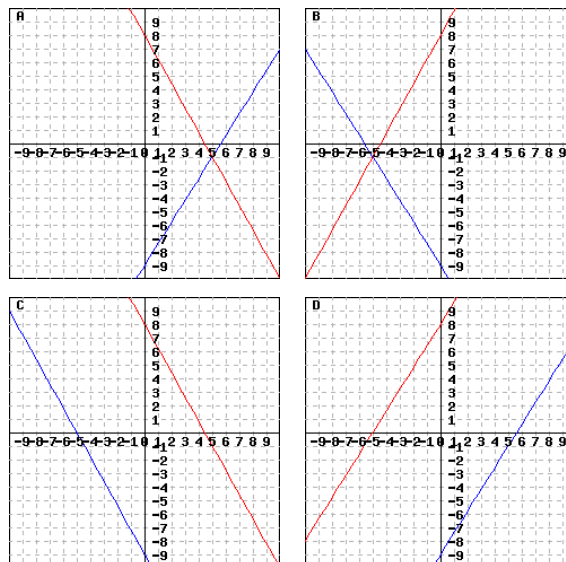
$$\begin{cases} y = -\frac{9}{5}x + 8 \\ 9x + 5y = -45 \end{cases}$$

The correct graph is graph

- A
- B
- C
- D

The solution of this system, written as an ordered pair, is _____.

(If these two lines don't intersect, type **no solution**.
If these two lines overlap each other, type **infinitely many solutions**.)



4. (1 point) For each system, determine whether it has a unique solution (in this case, find the solution), infinitely many solutions, or no solutions.

(1)
$$\begin{cases} -7x - 4y = 0 \\ 8x - 9y = 0 \end{cases}$$

- A. Unique solution: $x = 9, y = -7$
- B. Infinitely many solutions
- C. No solutions
- D. Unique solution: $x = -11, y = -1$
- E. Unique solution: $x = 0, y = 0$
- F. None of the above

(2)
$$\begin{cases} 3x + 4y = -2 \\ -5x + 9y = -28 \end{cases}$$

- A. Unique solution: $x = 0, y = 0$
- B. No solutions
- C. Infinitely many solutions
- D. Unique solution: $x = -2, y = 2$
- E. Unique solution: $x = 2, y = -2$
- F. None of the above

(3)
$$\begin{cases} 4x + 6y = 38 \\ -12x - 18y = -113 \end{cases}$$

- A. No solutions
- B. Unique solution: $x = 0, y = 0$
- C. Infinitely many solutions
- D. Unique solution: $x = 38, y = -113$
- E. Unique solution: $x = -113, y = 38$

- F. None of the above

$$(4) \begin{cases} -2x + 5y = 14 \\ 6x - 15y = -42 \end{cases}$$

- A. Unique solution: $x = 0, y = 0$
- B. Infinitely many solutions
- C. Unique solution: $x = -7, y = 0$
- D. Unique solution: $x = 14, y = -42$
- E. No solutions
- F. None of the above

5. (1 point) Solve the system using row operations (or elementary matrices).

$$\begin{cases} -6x + 5y + 5z = -8 \\ -3x - 4y + 6z = 2 \\ -5x - 5y + 6z = 8 \end{cases}$$

$x =$ _____

$y =$ _____

$z =$ _____

6. (1 point) Determine all values of h and k for which the system

$$\begin{cases} 9x - 9y = h \\ 6x + ky = -10 \end{cases}$$

has no solution.

$k =$ _____

$h \neq$ _____

7. (1 point) Determine if the following statement is true or false:

If a linear system has four equations and seven variables, then it must have infinitely many solutions.

If the answer is true, then type **true**. If the answer is false, type **false**.

Answer: _____

8. (1 point) Let $A = \begin{bmatrix} 1 & 0 & 1 & 0 & 1 \\ 0 & 1 & 3 & 0 & -3 \\ 0 & 0 & 0 & 1 & 2 \\ 0 & 0 & 0 & 0 & 0 \end{bmatrix}$

Is the matrix in echelon form? (input Yes or No) _____

Is the matrix in reduced echelon form? (input Yes or No) _____

If this matrix were the augmented matrix for a system of linear equations, would the system be consistent or inconsistent? _____

9. (1 point) Determine whether the following matrices are in echelon form, reduced echelon form or not in echelon form.

- Choose
- Echelon Form
- Reduced Echelon Form
- Not in Echelon Form

$$(1) \begin{bmatrix} 1 & 0 & 5 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & -8 \\ 0 & 0 & 1 & 0 \end{bmatrix}$$

- Choose
- Echelon Form
- Reduced Echelon Form
- Not in Echelon Form

$$(2) \begin{bmatrix} 0 & 1 & 0 & 9 \\ 0 & 0 & 1 & -10 \end{bmatrix}$$

- Choose
- Echelon Form
- Reduced Echelon Form
- Not in Echelon Form

$$(3) \begin{bmatrix} 1 & 0 & 0 & -7 \\ 0 & 1 & 0 & -4 \\ 0 & 0 & 1 & -2 \end{bmatrix}$$

- Choose
- Echelon Form
- Reduced Echelon Form
- Not in Echelon Form

$$(4) \begin{bmatrix} 1 & 0 & 1 \\ 0 & 1 & 1 \\ 0 & 0 & -8 \end{bmatrix}$$

10. (1 point) Reduce the matrix

$$A = \begin{bmatrix} 3 & -1 & 4 & -4 \\ 3 & 0 & -3 & -21 \\ -2 & 3 & -2 & 14 \end{bmatrix}$$

to reduced row-echelon form.

$$\begin{bmatrix} _ & _ & _ & _ \\ _ & _ & _ & _ \\ _ & _ & _ & _ \end{bmatrix}$$

11. (1 point)

Solve the system

$$\begin{cases} x_1 + 4x_3 + 4x_4 = -20 \\ x_2 - 3x_3 - 2x_4 = 7 \\ 3x_1 - 3x_2 + 23x_3 + 18x_4 = -85 \\ -x_2 + 3x_3 + 6x_4 = -15 \end{cases}$$

$x_1 =$ _____

$x_2 =$ _____

$x_3 =$ _____

$x_4 =$ _____

12. (1 point)

If the linear system

$$-4x - 6y + 7z = 3$$

$$-6x - 3y + 3z = -2$$

$$24x + 24y + hz = k$$

has infinitely many solutions, then $k =$ ____ and $h =$ ____.