# Manual: Performance of wafer-fused VECSEL under high power operation

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## Abstract

This document explains the basics to measure and evaluate VECSEL performance, using the software provided through  $\tt github.com/stefantkeller/VECSELsetup.$ 

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## 0 Refresher

This section is for if your computer is already set up, the measurement routine is adapted to your needs, and you simply want to refresh your memory how to get (re)started.

- record a measurement with routine\_measurement.py
   adjust the variables samplename, path\_to\_meas\_folder, heatsink\_start, pump\_end, use\_spectrometer, shuffle\_pump
   (as explained in section 2)
- 2. calibrate the setup with routine\_calibration.py
  If you still have a valid calibration you can skip this. But if you didn't measure for a while, you probably want to recalibrate! (as explained in section 3)
- 3. evaluate the measurement with light\_light\_to\_file.py specify the path to the measurement logfile logfile and the path to the calibration data calib\_folder. This script returns a file that you can open for example with Excel; the top row states all sorts of information, what were the measurement conditions, and what the columns mean at all.

## 1 Introduction

#### 1.1 Installation

Find this documentation and the scripts it refers to at github.com/stefantkeller/VECSELsetup. From within the EPFL network find a VECSEL starter-kit with the relevant manuals and publications to start with at wiki.epfl.ch/vecsel-lpn/documents/VECSEL-starterkit.zip.

This is a Python library. If you don't have Python installed yet, I recommend you install "Anaconda" (http://continuum.io/downloads) for Python 2.7 (it's free!). Also, you have to have installed the drivers from National Instrument (ni.com), in order to communicate with GPIB (etc...(NI drivers are a mess, what exactly you need, you have to figure out yourself)).

To install this library from github,

- 1. click on "Download ZIP",
- 2. extract the .zip
- 3. copy the folder to where ever you want it
- 4. adjust the PYTHONPATH

(at least, that's the proper way to do it, I guess). And, if you are familliar with git ... you know what to do.

If you don't care about "proper" and you simply want it to work (I don't know though what this breaks along the way...): after extracting the .zip, copy the folder to (something like; if you work with Anaconda as recommended above)

- Windows: C:\Anaconda\Lib\site-packages
- Mac: /Users/yourusername/anaconda/Lib/python2.7/site-packages

this path is already in the Pythonpath, and Python will find it.

For measurements (the stuff in meas/) you need pyvisa (https://pyvisa.readthedocs.org/en/master/).

For evaluation (the stuff in eval/) you need to also install errorvalues

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Figure 1.1: PyScripter is a convenient tool to work with python scripts. When you have opened one of the examples from the folder exp/ you can simply click on the launch button, the scripts starts and writes the output in one of the subwindows – try it out, should be selfexplanatory. The stop button lets you to interrupt the script if required. For example, exp/meas/temp\_logger.py logs the heat sink temperature in an infinite loop; in order to stop the logging you have to interrupt it. This interruption raises a KeyboardInterrupt error. This is supposed to happen.

(https://github.com/stefantkeller/errorvalues).

Install it with the same procedure as listed above. If you intend to use the calibration in exp/eval/calibration.py as it is, this is going to write an automated report (tuck together some plots) as a pdf; ready for print. This relys on IATEX(pdflatex) to be installed on your system.

If measurement and evaluation happens on two different computers (recommended) you probably install only those dependencies that you need. That's ok, the error handling in <code>\_\_init\_\_.py</code> catches <code>ImportErrors</code> and ignores them. However, if nothing happens at all, you might want to check whether you have installed, what you're supposed to have installed (maybe everything is caught and subsequentially ignored?).

## 1.2 File hierarchy

The different folders have different purposes:

- meas, setup control to record measurements
- eval, scripts for evaluation of measurements
- exp, examples of working measurement routines (using meas), and evaluation (using eval)
- doc, documentation

#### 1.3 Usage

Copy the files stored from the folder exp in your working directory. The example exp/meas/routine\_measurement.py is the most exhaustive for setup control / recording measurements. While exp/eval/light\_light.py highlights the evaluation part.

There is not graphical user interface (GUI), as one might know from LabView. Instead, with this library you have full controll over what the software does. But this comes with the price to actually having to read the lines of code – instead of looking at obscure icons. There are only few lines of code to read, in order to understand what's going on; and those are accompanied with comments. So go ahead and read it. You best start with the example scripts in the folder exp.

These lines of code you can read with any text editor of your choosing. On Windows I recommend PyScripter (https://code.google.com/p/pyscripter/). It brings in some simple GUI features, so you can edit and launch your measurement routines easily, see Fig. 1.1.

Additionally: consider TeamViewer teamviewer.com as a means to access the lab computer remotely from your office.

## 1.4 Disclaimer

Some paragraphs in this documentation are copy-paste from the master project report, during whose period the presented scripts have established themselves. A back-up copy of said report you will find at

github.com/stefantkeller/VECSELMasterProjectReport.

## 2 Measurement Routine

The routine is written in Python. This brings in several advantages: First of all we can actually look through the code and comment on it, where clarification is needed. The Python syntax is simple enough – basically, English with peculiar grammar – so if you can read this documentation, you will understand the program just as well. LabView for example fails at exactly this point; it's very hard to maintain, and the different sections of the script are difficult to interpret (let alone the litteral spaghetti code). And lastly, with Python we don't depend on a third party license. Again, LabView and Matlab fail at this point.

#### 2.1 The routine

You either look at the example given in exp/eval/routine\_measurement.py and read it through, or you continue to read here. The following long text covers the same.

We choose a set of values corresponding to a) the current of the pump laser, and b) the temperatures of the heat sink. We specify further, a path where to store the results. And lastly, we choose on how often every power current is ought to be measured – repeated measurements in order to obtain the errorbars that inform us on the reliability of the results.

At each temperature, we set the power source to the requested currents, and read out the power meters. The results of each power meter is written in its own file. Each of these files starts with a header line, that contains the state of the relevant settings of the device in question. Consequentially, if we doubt the integrity of the measurements we can look at this header line and at least know what state the device has reported to be in. The information about the power source are also written to its own file, containing the set and actual current. Hence, at each temperature we generate one file for the power source, plus one for each power meter.

At the end of these measurements we write a line in a logfile: The set temperature, the actually reached temperature, the filenames of the files with the results of the different devices, along with a timestamp so we know which measurement took how long. The timestamp also allows us to connect certain effects to the time of the day it was measured. The approach with a logfile and the separate files of each device (whose names are automatically stored in the logfile), facilitates the analysis; all the information a analysis-script needs is specified in the logfile.

At each heat sink temperature we irradiate the sample with different pump powers. Each pump is repeated N times over all. The pump order is selected at random, as illustrated in Fig. 2.1. Thanks to the random sampling the measurement results are detached from the lab environment – most notably time-independent. The heat sink cannot control its temperature with absolute precision. Figure 2.2 illustrates this issue: It shows the actually present heat sink temperature for six set temperatures. In the left column the temperatures are plotted in chronological order. We can identify, the temperature drifts. The right column shows the same temperatures, but corresponding to the set pump. The repeated measurements see a spread of different temperatures but the temporal drifts can not be resolved.

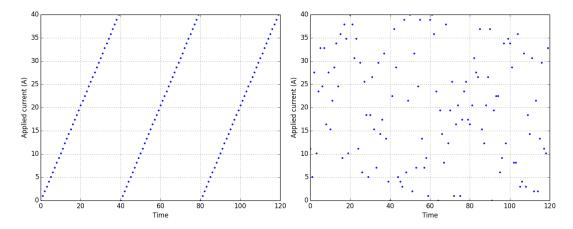


Figure 2.1: Two examples to apply various pump settings, with a repetition rate of 3. Left: A ramp. Right: Random sampling.

In contrast, Fig. 2.3 shows the heat sink temperature during a measurement without the random pump selection. In this case, clearly, we cannot talk about a single heat sink temperature for all the pump settings for this specific set heat sink temperature. The resulting measurements are highly repeatable, but only given the same pump order. This pseudo-stability we exploit during the calibration process of the different beam samplers and detectors: During the calibration we don't care about reproducibility but solely about the repeatability of two consecutive measurements.

The power meter average each measurement point over 200 samples, of which each one sample takes approx. 3 ms [1].

The order of heat sink temperature is still a ramp: I expect the setting of a new temperature to be somewhat time consuming. Therefore, we want to make use of the previously set temperature. The measurement routine looks at the specified temperature range, picks the one closest to room temperature, and increases to every second entry. Once the highest temperature is reached, the residual temperatures are picked, in descending order, until the lowest temperature is reached. From there we heat back up to room temperature. This routine is illustrated in Fig. 2.4.

As mentioned already, we repeated the measurement of each pump setting N times. With this repetition we obtain a measure for how well we know the underlying true value. We are hence interested in the mean of these single measurements and the resulting unbiased standard error [2]

$$\Delta x = \sqrt{\frac{1}{N(N-1)} \sum_{i=1}^{N} (x_i - \frac{1}{N} \sum_{i=1}^{N} x_i)^2}.$$
 (2.1)

For the uncertainties attached to quantities obtained through fits, I use a so-called Jackknife [3] approach: In a nutshell, this method allows to estimate the influence of the single measurement points on the fit parameters without working through the covariance matrix of the fit. The resulting error value is directly related with the unbiased standard error (2.1), used for the rest of the report.

Working with errorbars on data is tedious. Not only do you have to manipulate the data themselves, you always have to carry with you the uncertainty value associated with each of the data points. This is why the evaluation scripts rely heavily on errorvalues; a python library designed for lazy people who don't want to keep track of the uncertainties by hand (https://github.com/stefantkeller/errorvalues).

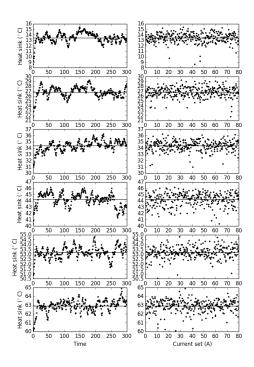


Figure 2.2: The heat sink temperature fluctuates over time (left). Thanks to the random sampling addressed in Fig. 2.1 the measurements don't see these drifts (right).

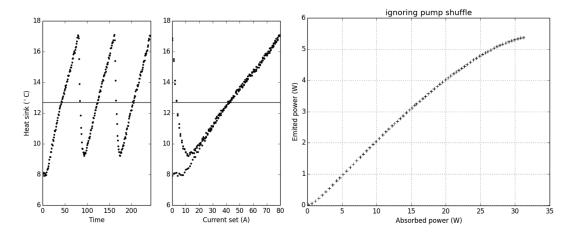


Figure 2.3: In contrast to Fig. 2.2, when we ignore the random pump sampling highlighted in Fig. 2.1, the temperature seen by the single pump settings differ strongly from the average heat sink temperature (left). The resulting LL-characteristic has very little noise on its data points (right). But these small error bars dismiss the fact that the underlying points were measured under very different conditions; eroding the significance of this low noise.

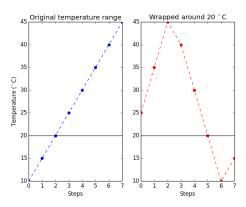


Figure 2.4: An example of how a given temperature range is wrapped around the room temperature (here assumed to be 20 °C).

## 2.2 Safety precautions

The goal of this script is to automate as much as possible. Ideally, we want to install a new VECSEL, align the output coupler, press start, and return some time later to a complete data set for this specific VECSEL under test. For this we need to be sure our measurement routine handles potential errors appropriately.

For this we must not rely on software. Instead, we have to implement the safety precautions on hardware side. In software we can try to mitigate potential problems through proper error handling. I don't know how this would be done in LabView. In Matlab and Python this is performed through so-called try/catch and try/except handles, respectively. With it I have implemented that if anything goes wrong software side, the power source is shut down (This order itself is so low-level, that it should always work.). For example, one of the devices could send an unexpected answer, the heat sink doesn't reach its requested temperature within reasonable time, etc. For the unlikely event that even the power source shut down doesn't work, we have to implement the safety precautions on hardware side.

Our power source has two ways to be shut down: We can disable the current, or we can set the current to zero. In order to disable the current, we first have to ask the power source, whether the current is currently applied. If it is, we toggle it like a light-switch to shut off. However, querying the current state is error-prone. Hence, if an error is caught we leave the shutter to be in what ever state it is and only set the current to zero. Potentially it is still applied. But the light output at 0 A is barely detectable – but there still is a leak flow of photons. Writing to the power source should not cause any new problems, so simply writing 0 A should go through.

On the hardware side, the "laser on" light in front of the lab is controlled by a logic tied to the power source: As soon as the power source applies a certain specified voltage the laser warning turns on. During the measurements this safety sign therefore is always on. Our setup is not fit for an inter-lock solution, hence the safety responsibility lies solely on you, the operator. This means, you have to wear you safety goggles, and the setup is to be closed up, Fig. 2.5.

As a second safety precaution exp/meas/VECSELSetupFake.py allows us to test modifications on the measurement routine with fake devices. In order to connect the measurement routine with the measurement devices we have to specify a protocol. In the new script we do this by selecting an external file that contains the initiation details. By specifying the fake protocol we can modify the routine without the real devices. This separation in code is, for one, good practice, and secondly convenient if we cannot use one of the devices due to a revision or whatever. To be detached from the physical devices

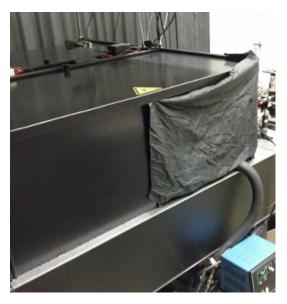


Figure 2.5: During operation the setup has to protect the Along the primary beam line we use a beam dump. None the less, there is a lot of scattered light and reflections from everywhere. To cope with that, close the walls and cover. The curtain allows you to reach into the setup, in order to align the xyz-stage during high power operation.

was not possible with the old script – which is one of the reasons why it was possible to toggle the power source shutter while setting the wavelength of the power meter.

## 3 Calibration

## 3.1 Principle

Figure 3.1 shows a photograph of the setup. Before we can use it to characterize samples, we have to characterize the setup first. Following the beam path, we start with the lens system indicated as *pump*. This input beam is targeted at the sample. Part of this pump beam is sampled by a beam sampler (BS), a glas plate with high damage threshold and anti reflective coating on one side. This sampled light is directed towards a detector. The pump light is reflected off the sample, collimated by a lens, and again sampled as for the input. The lasing output passes the output coupler (OC), a collimating lens, and another beam sampler (coated for the emission wavelength). This beam sampler we eventually use to record the spectrum of the emission.

In order to calibrate this setup we need to know how to correlate the readings of the single detectors with the actually present powers. For this we place the thermal power meter at the four indicated positions. With the thermal power meter we can validate the setup up to  $40\,\mathrm{W}$ , in principle.

Position 1 requires to remove the sample. We're interested in the correlation between the readings of the detector after the beam sampler and the measurements at the sample position. From this same measurement we can also extract a look-up-table what current setting of the pump laser corresponds to what output power.

On position 2 we measure the beam power present after the collimating lens. This we relate with the readings of the detector after the beam sampler, gathered during the measurements at position 3 (below). Make sure (IR-viewer) you capture all of the reflected light within the aperture of the power meter. Clipping during the calibration renders everything else useless.

At position 3 we need two measurements: once with and once without the beam

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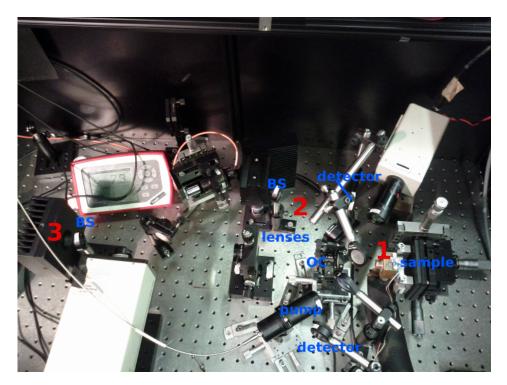


Figure 3.1: In order to calibrate the setup we have to measure the actually present power at the indicated positions 1–3.

sampler. The difference between these two measurements lets us correct for the fraction of light the beam sampler directs away.

The pump order during calibration is a ramp (not random sampling as for the measurement routine, section 2). As shown in Fig. 2.3 this way we arrive in a highly repeatable situation, using the same exact ramp.

#### 3.2 Implementation

The routine in exp/meas/routine\_calibration.py needs the following 4 files. The calibration evaluation routine in exp/eval/calibration.py should also clear things up, what the following comments mean.

Between these measurements you move only the thermal power meter to the different positions indicated in Fig. 3.1. Do not touch the other equipment! With this procedure we gauge the photo detectors (after beam splitters to protect from high power) to the thermal power meter. When placing the thermal power meter, you have to make sure the exposure is below its damage threshold. A Thorlabs thermal power meter S314C, for example, has a power range limited up to 40W.

### 1\_pump\_calib.csv

Place the thermal power meter at the sample position; position 1. Choose the variable pump\_end equal to the pump current corresponding to the maximally allowed pump power (or less, to be on the safe side). (Note: pump\_end will be a lower value than during actual operation. This is made possible because there is a linear relation between pump current and the power seen at position 1. We're going to extrapolate based on this linear relationship. Ensure yourself, this is actually linear! (Otherwise you have to find a new solution how to do the job.))

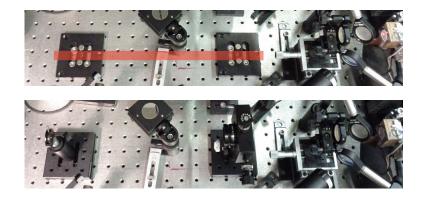


Figure 4.1: Top: Removeable posts to define the beamline. Bottom: HeNe beam has to be directed through the two irises. With these two irises the position of the HeNe source is detached from the beam line.

#### 2\_refl\_calib.csv :

Thermal power meter goes in the reflection channel, between collimating lens and beam sampler; position 2. Variable pump\_end now determines up to what power you can calibrate the setup over all. Make sure the power exposure at this point doesn't exceed the power range of the power meter. Caveat: If you replace the sample under test without changing the alignment, you can – in principle – use an old calibration. But, if this sample has a higher reflectivity, you run the risk of entering an uncalibrated range.

#### 3\_emission\_calib.csv :

Thermal power meter goes at its final position in the laser emission path – position 3 – without the spectrometer beam sampler.

#### 4\_emission\_calib.csv :

Thermal power meter goes at its final position in the laser emission path – position 3 – with the spectrometer beam sampler in place. Measurement 3 and 4 allow you to find the influence of said beam sampler.

In practice you will probably gather these four measurement in reverse order. After you have conducted the measurements (e.g. with routine\_measurement.py), you run this script for 4, remove the spectrometer beam sampler and measure 3, and so on. This way you're sure to account for the actual alignment present during the measurements.

#### 3.3 Evaluation

The example routine exp/eval/calibration.py works with these mentioned files. It is easiest to look at the code and learn based on the comments provided alongside. The main() function in these scripts you can use to calibrate one of the specific parts manually.

# 4 Measurement alignment process, description of

The alignment process comes in two steps: a rough base alignment and a fine tuning. For the first step align the optical elements along the emission path to be orthogonal to it. With the equipment orthogonal to the beam path we arrive at a well-defined state, which is easy to reproduce.

First we define the beam line. It is defined by two removable magnetic posts, Fig. 4.1. These posts allow us to remove and replace a mount reproducible. Two irises define the



Figure 4.2: First, we remove / flip all components along the beam line except the sample. In this configuration we align the sample surface orthogonal to the HeNe.

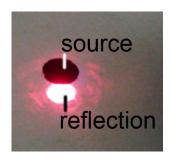


Figure 4.3: By arranging the reflected beam to coincide with the HeNe source position we ensure the orthogonality of the component. The orthogonality is an easily obtainable well-defined state, it thus helps for reproducibility.

beam line height. This height is arbitrary, but in order to have a reproducible setup pick a height and use this iris as a reference tool. Use the HeNe laser for the rough alignment: place it anywhere on the table. Send its beam through the two irises; using mirrors. The two irises are all we need in order to define the beam line. With them the setup is detached from the rest of the table.

Place the sample on the heat sink and align it orthogonal to the aforementioned beam line: Remove – or flip, Fig. 4.2 – all other components along the beam line and leave only the sample. Adjust the orientation of the sample such that the back-reflection is directed at the HeNe, Fig. 4.3, now it is in a well-defined configuration. Once the sample is aligned, place the output coupler back in the beam path. Repeat the same procedure. Careful: since the output coupler is curved you will find two reflections. One looks like in Fig. 4.3. This you can align by tilting the output coupler; like a regular mirror. The second reflection is divergent. Bring it to the center using the xyz-translation-stage.

The last equipment in this beam line is the lens after the output coupler. It - in combination with the output coupler - images the sample onto the camera you'll use later. Align the lens orthogonal and choose its position with appropriate distance from the output couper and camera. Appropriate means the picture on the camera is in focus and there is enough room for all the equipment.

For the fine tuning we need the pump light and look at the photoluminescence of the sample. The camera along the emission beam line, mentioned above, sees the photoluminescence resulting from the pump on the sample. Attach a long-pass filter to the camera in order to see only the photoluminescence and not the pump light. With this camera – initially, thanks to the rough alignment – we see two spots corresponding to pump and reflection from the output coupler, Fig. 4.4. If you don't see two spots the rough alignment with the HeNe was not precise enough; repeat. Don't forget to test whether the sample really is in focus of the camera. Otherwise, of course you won't see

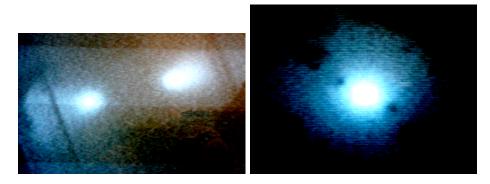


Figure 4.4: After the pre-alignment with the HeNe, the two spots – originating from the pump and the output coupler reflection – are close by (left). By optimizing the alignment of the output coupler, these two spots have to be brought to overlap (right). Given this configuration, we have to increase the pump power, and at threshold we obtain laser emission. For the fine-alignment we have to replace the camera with a power meter and adjust for maximum output power.

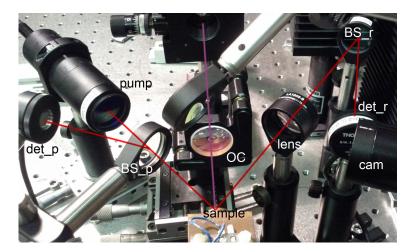


Figure 4.5: Overview of the different components incorporated for the cavity.

anything. Bring these two spots to overlap, using the xyz-stage of the output coupler. Once the two spots do overlap, and the pump is above threshold, the sample starts lasing. Congratulations, the setup is aligned.

Now you have to make sure the beam sampler for the pump and reflection detectors actually send off the sampled beam towards the aperture of the detectors. If you move the pump beam sampler, the spot moves on the sample, detuning the alignment just described; repeat. An additional reminder about some obvious alignment necessities: The distance between output coupler and sample has to be smaller than the radius of curvature of the output coupler. The distance between pump and sample has to match the focal length of the pump lens (provided the light is collimated after the first lens).

Figure 4.5 shows an overview of the different components. The pump light is directed via fiber to a lens system that images the light onto the sample. With beam sampler  $BS_p$  we extract a fraction of the pump and direct it to detector  $\det_p$ . This way we have a realtime reading of the pumped power. A considerable part of the pump light is reflected off the sample. This light diverges. First, we thus have to collimate it. For this we install a lens with appropriate focal length and distance from the sample. Of this reflected beam we again sample a fraction with  $BS_r$ , and direct this to detector  $\det_r$ . The largest fraction of the reflected beam is directed to the beam dump. By sampling pump and reflection in this geometry we avoid high power readings on the detectors.

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Before you record a measurement you want to optimize the alignment once more: place the power meter in the emission path, set the pump to a value above threshold, and optimize for maximum output power. Don't move the sample, only adjust the xyz-stage of the output coupler, and the distance between pump and sample. For measurements that record the spectral information, place also the assigned beam sampler in the emission path.

The fiber delivering the light to the spectrometer is at a distance from the sample similar to the camera; in the focus of the emission. In order to have access to both the camera and the spectrometer within the same setup, several mirrors are flippable to use the equipment needed for the alignment step you are at. Coupling the emission into the fiber is straight forward; but can be frustrating, because this alignment is delicate. You have to hit the position of the fiber core and you have to hit with normal incidence. The angular component is tricky. We use a multimode fiber, those allow for a larger margin of error. Use the IR-viewer or an IR-card to visualize the emission beam, mount the fiber such that is along this beam line, and direct the beam onto the fiber. Once you have a reading on the spectrometer adjust the alignment for maximum signal.

A general note on optimizing based on a reading on a power meter: when you optimize the output coupler along the cavity axis be prepared to find more than one maximum. Depending on the exact setting different modes are realized. The global maximum performes a lot better than the local ones, but it's easy to miss. The heat sink temperature may increase when you optimize for too long (and thus irradiate the pump beam for a long time). As a result the VECSEL performance decreases and you are likely to chase a value that isn't possible anymore, given the new temperature. This may lead you to find the "maximum" off center, i.e. not at the maximum. As a remedy, take short breaks during the alignment, or actively modify the temperature: the maximum should be maximal also for other temperatures. The emission power fluctuates. This noise can pile up; and since you scan along one parameter axis this may also fake a wrong maximum. In order to have a picture in mind how that might look like, google for "random walk". You can't do anything against these error sources. Be aware of them and with experience in alignment you will develop a sense for their impact.

# 5 Sample surface microscopy

Take a picture of the non-radiative defects of the sample under the microscope. For this connect the pump light with the microscope illumination, and place the camera, including a long-pass filter so we see only the photoluminescence and block the pump, as illustrated in Fig. 5.1.

Note: Whenever you change the fiber connected to the pump diode, ensure the fiber is intact – to avoid damages portrayed in Fig. 5.2 – and make sure to have the best possible diode-to-fiber coupling. For the first task use the fiber inspection microscope. For the latter (see diode manual!) apply a certain pump, unscrew the fiber connection at the pump diode module, and turn the fiber end while observing the change in output power. Lock it for the maximum configuration.

With a microscope magnification of  $5\times$ , take a picture of all four corners. For this you can use the fully equiped NI-MAX, which came along with the other NI drivers, see Fig. 5.3. The overlapping parts of these images allow you to staple together the whole photograph.

## References

[1] Thorlabs, Power meter operation manual,

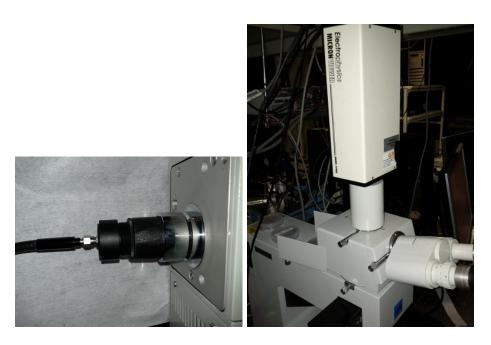


Figure 5.1: Direct the pump light to the microscope for illumination. With this light source, and a long-pass filter on the camera, the non-radiative defects are directly visible.

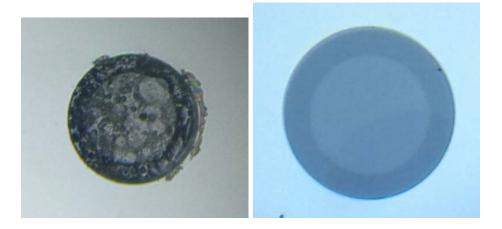


Figure 5.2: Left: This fiber end is burnt; it delivers a beam of bad quality. Rigth: This is how all fiber interfaces are supposed like; it is intact.

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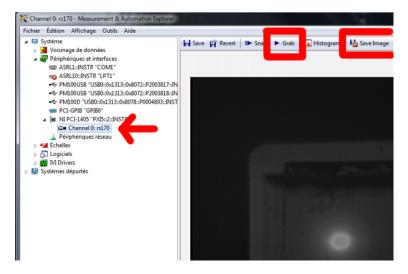


Figure 5.3: National Instrument's measurement and automation explorer (NI MAX) allows us to control the camera. With "Grab" you activate the real-time image feed. Once the sample is placed as wished, click "Grab" again to stop the broadcast, and save the image. To find this software, open the start menu and type "ni max".

http://www.thorlabs.de/thorcat/19500/PM100USB-Manual.pdf

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