

Unsupervised Learning of Disentangled and Interpretable Representations from Sequential Data

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Talk by Stefan Wezel

Explainable Machine Learning

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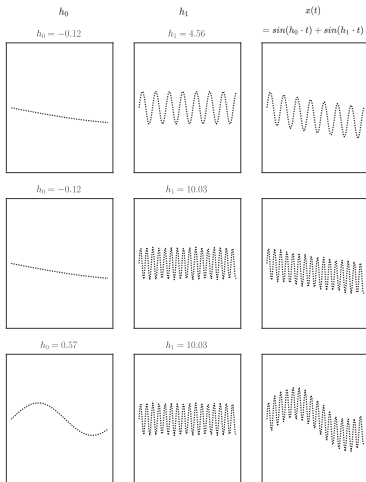
- Introduction
- What are disentangled representations (intuition)
- Why disentangled representations
- Formal description of disentangled representations
- SequentialVAE
- Did they achieve disentanglement?
- Other approaches and challenges

- Using Sequential VAE (-> Unsupervised representation learning)
- Represent information from different temporal scales in corresponding latent subspaces
- Claim that they achieve disentanglement with respect to sequence (speaker) and segment (content) information
- would mean that those latent variables then can be used separately
 - speaker verification
 - denoising
 - ...

What is disentanglement?

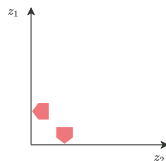
Intuition

- encode distinct generating factors in separate subsets of latent space dimensions

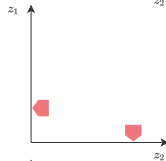


Encoder
 $f: Z \mapsto X, Z \in \mathbb{R}^2$

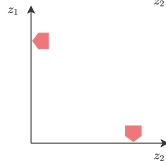
$f(x)$
 $\rightarrow Z$



$f(x)$
 $\rightarrow Z$



$f(x)$
 $\rightarrow Z$



Why learn disentangled representations?

Motivation

- Gives us an exact idea, of what variables were used, to come to a result
 - Fairness in ML (exact)
 - Explainability/Interpretability
 - Overall, a model just becomes more usable if latent variables carry semantic meaning

Disentangled Representations Formally

A field-trip to group theory: important concepts

- Group
 - tuple of operation and set
 - set is closed under operation, there is identity element, and inverse for every element, associativity
- Symmetry group
 - Group action, that leaves object (defined through set/sets) invariant
- Group action
 - Actions are results of symmetry transformations of set (i.e. set of changed order)
- Direct product
 - $G = G_1 \times \dots \times G_n$
 - Group conditions must hold for group and each subgroup

Disentangled Representations Formally

A field-trip to group theory: What is disentanglement in terms of group theory?

- Disentangled group actions
 - Result of transformations that only change certain aspect of world, but leave others invariant
- Assuming G can be decomposed into direct product symmetry subgroups G_i
- We want mapping $f : W \mapsto Z$
- Symmetry G on W should be preserved in Z , $G \times Z \mapsto Z$
 - $g \cdot f(w) = f(g \cdot w) \rightarrow$ equivariant map

Disentangled Representations Formally

A field-trip to group theory: What is disentanglement in terms of group theory?

- Representation is disentangled if
 - equivariant map $f : W \mapsto Z, g \cdot f(w) = f(g \cdot w) \forall g \in G, w \in W$
 - such a map would split Z into independent subspaces, thus satisfying:
 - Decomposition $Z = Z_1 \times \dots \times Z_n$
 - where Z_i is only affected by transformations G_i in W
 - and Z_i invariant to all $G_{j \neq i}$ in W
 - Thus each subspace Z_i can be transformed ONLY by the corresponding symmetry of W

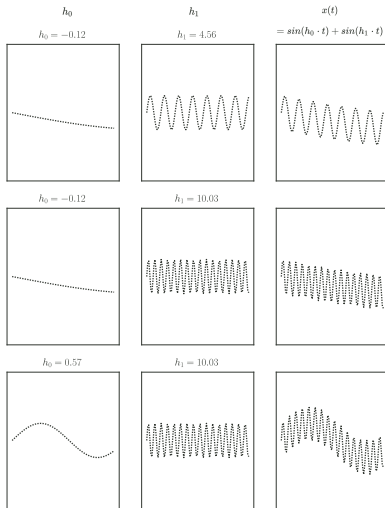
Disentangled Representations Formally

A field-trip to group theory: Disentangle our example formally

- signal $x(t) = \sin(h_0 \cdot t) + \sin(h_1 \cdot t)$ with $h_0 \sim \mathcal{N}(0, 1)$, $h_1 \sim \mathcal{N}(5, 1)$;
- The set of possible values for h_0, h_1 make up our W
- The group of symmetries acting on this W decompose into
$$G = G_{h_0} \times G_{h_1}$$
- We want to find an equivariant map $f : W \mapsto Z$ with $Z \in \mathbb{Z}^2$
- so that changes of h_0 result ONLY in changes in z_0 and changes of h_1 ONLY in z_2
- Note, that this requires prior knowledge of generating factors in our world

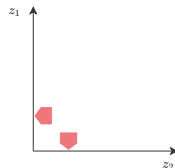
Disentangled Representations Formally

A field-trip to group theory: Disentangle our example formally

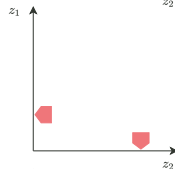


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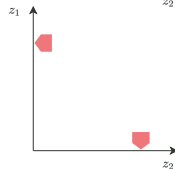
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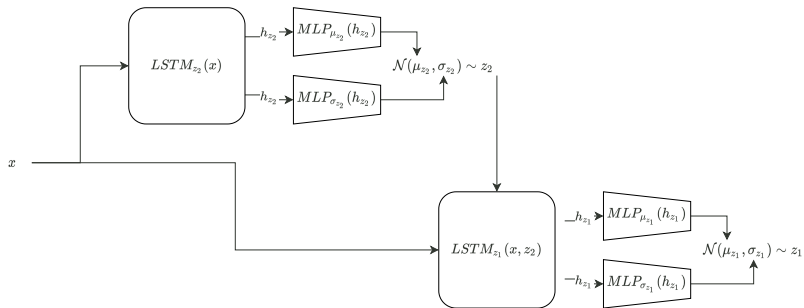
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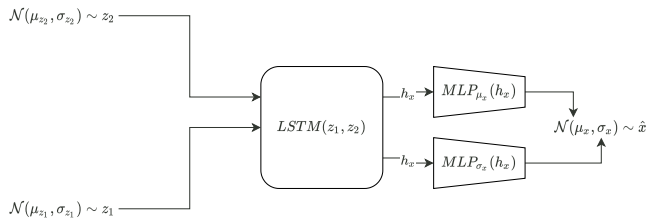


Back to the paper

Did they achieve disentanglement?

- Disentangled with respect to what decomposition?
- Assuming there is a decomposition $G = G_{sequence} \times G_{segment}$
- This should be reflected in $Z = (z_1, z_2)$
- They propose to store sequence information in z_2 and segment information in z_1
- Thus, they need to find an equivariant map $f : W \mapsto Z$, so that z_1 is only affected by actions on $G_{sequence}$ and vice versa





Back to the paper

How did they do it?

- regularize z_2 by sequence dependent prior (lookup table of s-vectors)
- and z_1 by sequence independent prior
- optimize latent space at segment level

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Disentangled Representations Formally

A field-trip to group theory: Disentangle our example formally

- Signal can get shifted or warped
- the set of these transformations make up a symmetry group
- This can be decomposed into shifts and warps/subsets of original set (all shifted \times all warped)
- Either content is preserved, or speaker is preserved
- the resulting set of transformed signals are the actions of the symmetry group on the world state

Disentangled Representations Formally

A field-trip to group theory

- This symmetry group can be decomposed into symmetry subgroups
- One affects location
- the other affects frequency

What are disentangled representations formally?

Disentangled Group Action

- Group action $G \times X \mapsto X$
- Group decomposes into direct product $G = G_{shifts} \times G_{warps}$
- Is disentangled with respect to decomposition of G
 - if there is decomposition $X = X_{shifted} \times X_{warped}$
 - and actions $G_{shifts} \times X_{shifted} \mapsto X_{shifted}$
 - and actions $G_{warps} \times X_{warped} \mapsto X_{warped}$

What are disentangled representations formally?

Disentangled Representation

- Let W be the set of world states (all shifts and warps of signal)
- Generative process $b : W \mapsto O$ (voice to audio processing unit)
- Inference process $h : O \mapsto Z$ (observation to latent space)
- $f : W \mapsto Z, f = h \circ b$
- Now, we know, there is a symmetry group acting on W
($G \times W \mapsto W$)
- We want to find corresponding $G \times Z \mapsto Z$ to reflect symmetry structure of W in Z
- More formal: $g \cdot f(w) = f(g \cdot w)$
- This is what's called an equivariant map (famous example: convnet)

What are disentangled representations formally?

Disentangled Representation

- Assume symmetry transformations G of W decompose into direct product $G = G_1 \times \dots \times G_n$
- Representation is disentangled if
 - equivariant map $f : W \mapsto Z, g \cdot f(w) = f(g \cdot w) \forall g \in G, w \in W$
 - such a map would split Z into independent subspaces, thus satisfying:
 - Decomposition $Z = Z_{shifted} \times Z_{warped}$
 - where $Z_{shifted}$ is only affected by shifts in W (G_{shifts})
 - and Z_{warped} is only affected by warps in W (G_{warps})
 - Thus each subspace can be transformed by the corresponding symmetry (like shift or warp independently)
- There may be more criteria (preserving group structure, isomorphisms, ...) but for the intuition this is sufficient

Did they achieve disentanglement

...

- With respect to a decomposition into two
- Setting: 10 sentences, 630 speakers
- How can we formulate this in group theory terms?

How did they do it?

Intuition

- With respect to a decomposition into two
- regularize z_2 by sequence dependant prior (lookup table of s-vectors)
- and z_1 by sequence independant prior

How did they do it?

Methods

- Sample batch at segment level (instead of sequence level)
- Maximize segment variational lower bound
- (Force z_2 to be close to μ_2)
- approximation of μ_2 is closed form equation (concave function, set derivative to 0)

- If we really think about it, it is hard for us to define what a disentangled representation should actually be
- Precise biases of what the latent space should be decomposed into can be helpful as well as biases towards the 'form' of these latent subspaces