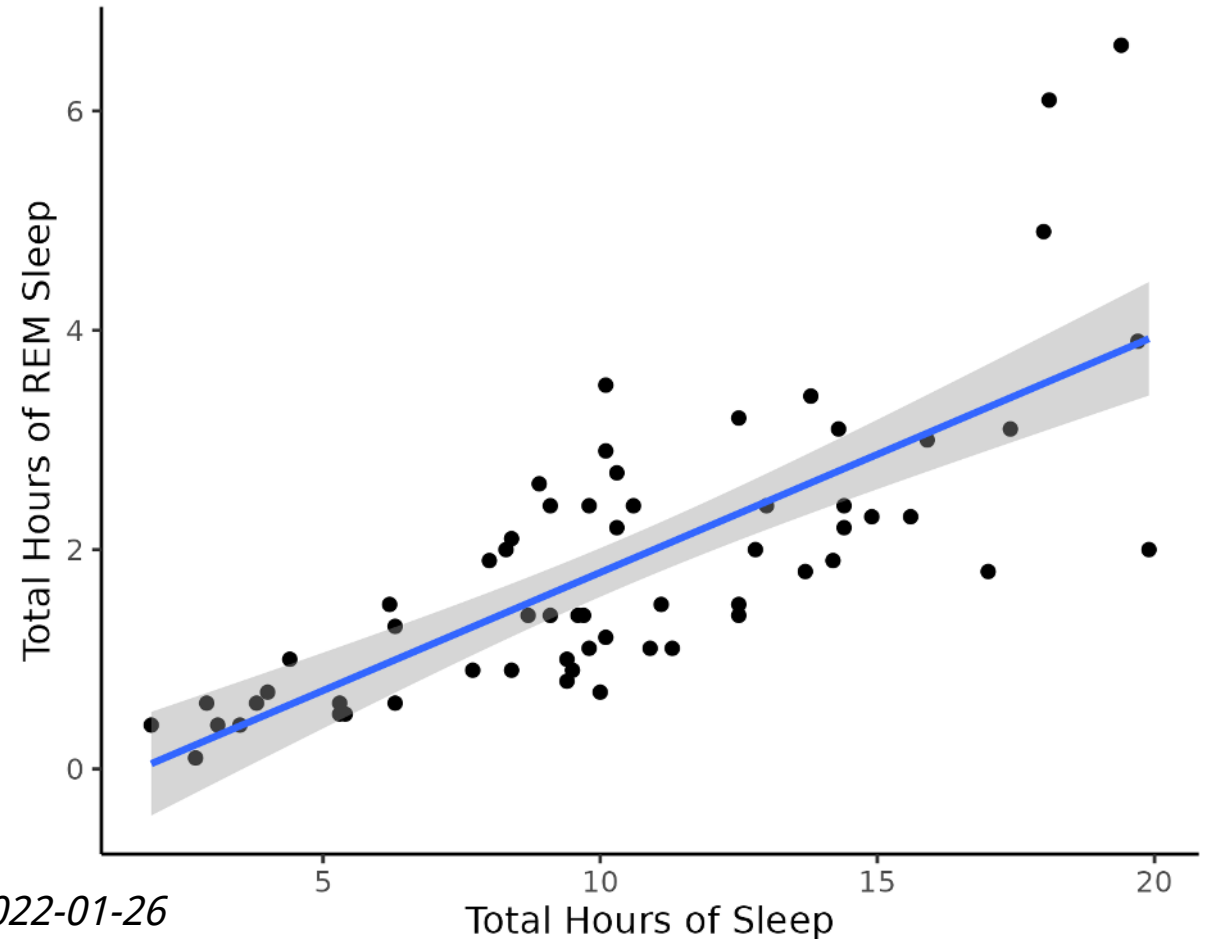


Workshop: Dealing with Data in R

# Statistics in R

Now that your data are ready



# Basic Statistics







# Looking at your data

```
library(skimr)
skim(mtcars)
```

```
## — Data Summary —————
```

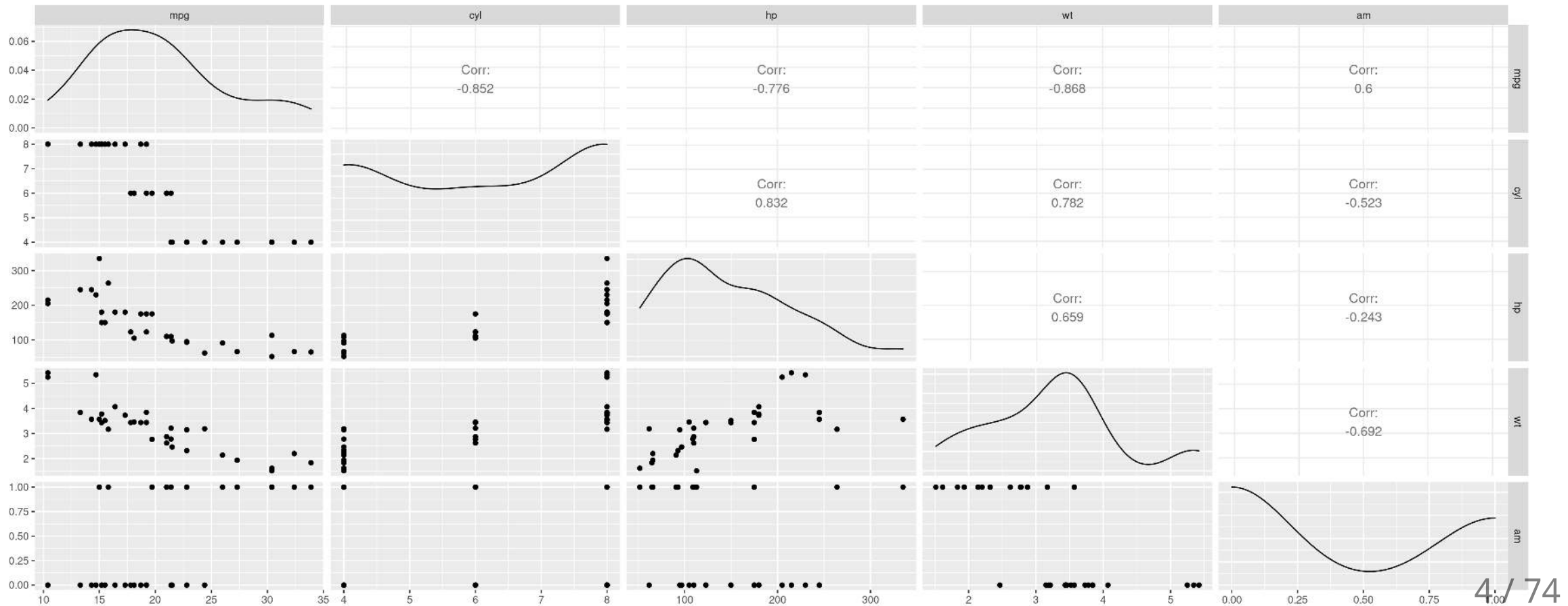
```
##                               Values
## Name                          mtcars
## Number of rows                 32
## Number of columns              11
## -----
## Column type frequency:
##   numeric                      11
## -----
## Group variables                 None
##
```

```
## — Variable type: numeric —————
```

##	skim_variable	n_missing	complete_rate	mean	sd	p0	p25	p50	p75	p100	hist
##	1 mpg	0	1	20.1	6.03	10.4	15.4	19.2	22.8	33.9	
##	2 cyl	0	1	6.19	1.79	4	4	6	8	8	
##	3 disp	0	1	231.	124.	71.1	121.	196.	326	472	
##	4 hp	0	1	147.	68.6	52	96.5	123	180	335	
##	5 drat	0	1	3.60	0.535	2.76	3.08	3.70	3.92	4.93	
##	6 wt	0	1	3.22	0.978	1.51	2.58	3.32	3.61	5.42	

# Looking at your data

```
library(GGally)
ggpairs(dplyr::select(mtcars, mpg, cyl, hp, wt, am))
```



# T-Tests

## Comparing two samples

```
t.test(values ~ group, data = data)
```

- **values** are measurements from the two populations
- **group** is the column that differentiates the two groups

OR

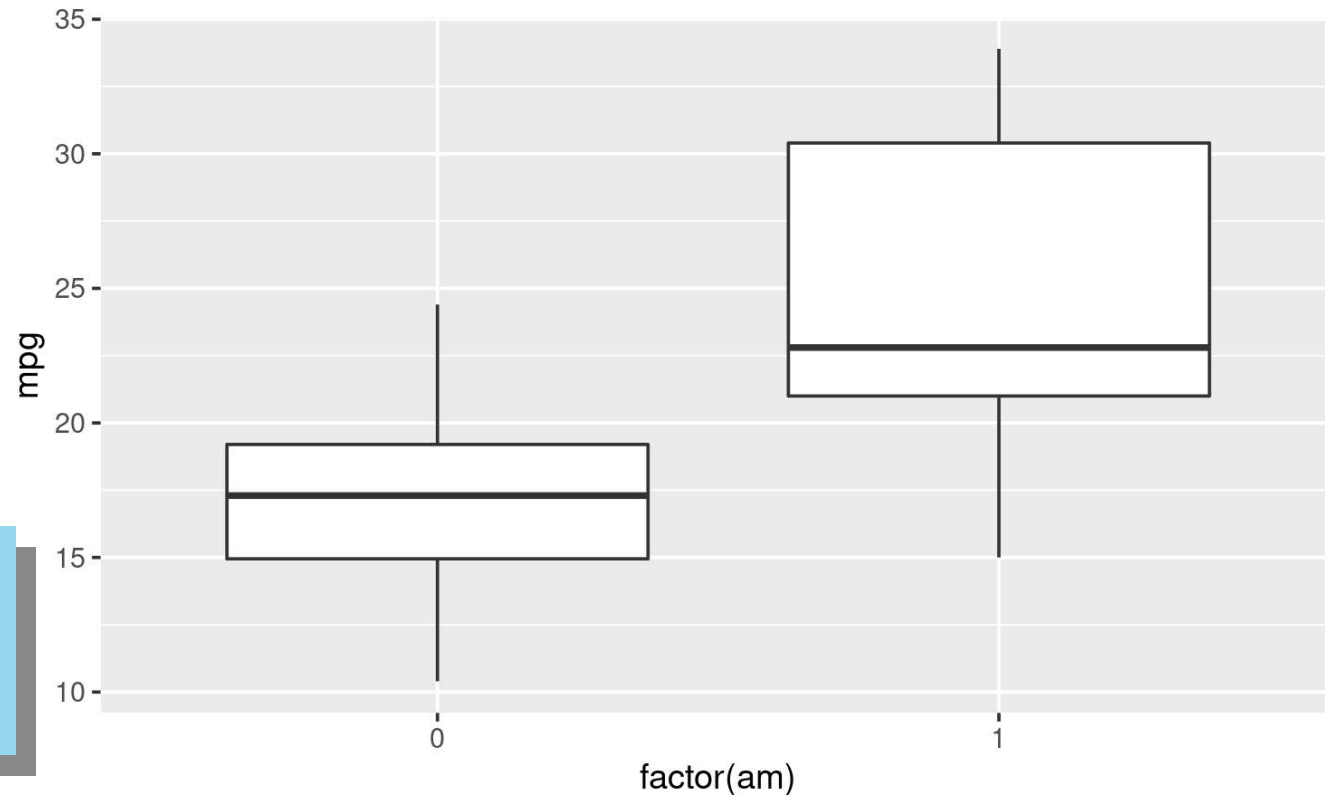
```
t.test(sample1, sample2)
```

- **sample1** and **sample2** are the two samples to be compared

# T-Tests

## Miles-per-gallon significantly different between Automatic and Manual cars?

```
ggplot(mtcars, aes(x = factor(am), y = mpg)) +  
  geom_boxplot()
```



?**mtcars** shows  
0 = automatic  
1 = manual

# T-Tests

## Miles-per-gallon significantly different between Automatic and Manual cars?

```
t.test(mpg ~ am, data = mtcars)
```

```
##  
##      Welch Two Sample t-test  
##  
## data:  mpg by am  
## t = -3.7671, df = 18.332, p-value = 0.001374  
## alternative hypothesis: true difference in means between group 0 and group 1 is not equal to 0  
## 95 percent confidence interval:  
##  -11.280194  -3.209684  
## sample estimates:  
## mean in group 0 mean in group 1  
##      17.14737      24.39231
```

P = 0.00137, so yes!  
Manual cars (1) get more miles per gallon  
than Automatic cars (0)

# Other tests

- Fisher's Exact Test - **`fisher.test()`**
- Chi-Square Test - **`chisq.test()`**

Here it's mostly about getting your data into a matrix



# Getting data into matrix for Chi-Square

## Example Data

```
my_data <- data.frame(expected = c(10, 10),  
                      observed = c(16, 4),  
                      site = c("A", "B"))  
  
my_data
```

```
##   expected observed site  
## 1         10        16   A  
## 2         10         4   B
```

## As a matrix (only expected and observed)

```
my_matrix <- dplyr::select(my_data, expected, observed)  
my_matrix <- as.matrix(my_matrix)  
  
my_matrix
```

```
##      expected observed  
## [1,]         10        16  
## [2,]         10         4
```

# Getting data into matrix for Chi-Square

## Example Data

```
my_data <- data.frame(expected = c(10, 10),  
                      observed = c(16, 4),  
                      site = c("A", "B"))  
  
my_data
```

```
##   expected observed site  
## 1         10        16   A  
## 2         10         4   B
```

## As a matrix (only expected and observed)

```
my_matrix <- dplyr::select(my_data, expected, observed)  
my_matrix <- as.matrix(my_matrix)  
  
my_matrix
```

```
##      expected observed  
## [1,]         10        16  
## [2,]         10         4
```

## Chi-Square Test

```
chisq.test(my_matrix)
```

```
##  
##      Pearson's Chi-squared test with Yates'  
## continuity correction  
##  
## data:  my_matrix  
## X-squared = 2.7473, df = 1, p-value = 0.09742
```

# **Non-parametric Statistics**

# Non-parametric Statistics

## Wilcoxon Rank Sum (Mann-Whitney) Test

```
air <- filter(airquality, Month %in% c(5, 8))
```

Is there a difference in air quality between May (5th month) and August (8th month)?

```
wilcox.test(Ozone ~ Month, data = air, exact = FALSE)
```

```
##  
##      Wilcoxon rank sum test with continuity correction  
##  
## data:  Ozone by Month  
## W = 127.5, p-value = 0.0001208  
## alternative hypothesis: true location shift is not equal to 0
```

Yes!

# Non-parametric Statistics

## Kruskal-Wallis Rank Sum Test

Is there a difference in air quality among months?

```
kruskal.test(Ozone ~ Month, data = airquality)
```

```
##  
##      Kruskal-Wallis rank sum test  
##  
## data:  Ozone by Month  
## Kruskal-Wallis chi-squared = 29.267, df = 4, p-value = 6.901e-06
```

Yes, there is at least one month that is different from the rest.

# Linear Models

# Linear Models

## Running models in R

```
lm(y ~ x1 + x2, data = data)
```

- **y** is **dependent** variable
- **x1** and **x2** are **independent** variables

# Linear Models

## Running models in R

```
lm(y ~ x1 + x2, data = data)
```

- **y** is **dependent** variable
- **x1** and **x2** are **independent** variables

## Different types of models

- If both **x**'s are continuous, this is a **linear regression**
- If both **x**'s are categorical, this is an **ANOVA**
- If **x1** is continuous and **x2** is categorical, this is an **ANCOVA**



# Linear Models

## Running models in R

```
lm(y ~ x1 + x2, data = data)
```

- **y** is **dependent** variable
- **x1** and **x2** are **independent** variables

## Different types of models

- If both **x**'s are continuous, this is a **linear regression**
- If both **x**'s are categorical, this is an **ANOVA**
- If **x1** is continuous and **x2** is categorical, this is an **ANCOVA**

R will figure it out for you

# Linear Models: Interactions

## Main effects only

```
m <- lm(y ~ x1 + x2, data = data)
```

# Linear Models: Interactions

## Main effects only

```
m <- lm(y ~ x1 + x2, data = data)
```

## Main effects and interaction

```
m <- lm(y ~ x1 + x2 + x1:x2, data = data)
```

# Linear Models: Interactions

## Main effects only

```
m <- lm(y ~ x1 + x2, data = data)
```

## Main effects and interaction

```
m <- lm(y ~ x1 + x2 + x1:x2, data = data)
```

## Main effects and interaction

```
m <- lm(y ~ x1 * x2, data = data)
```

# Linear Models: Interactions

## Main effects only

```
m <- lm(y ~ x1 + x2, data = data)
```

## Main effects and interaction

```
m <- lm(y ~ x1 + x2 + x1:x2, data = data)
```

## Main effects and interaction

```
m <- lm(y ~ x1 * x2, data = data)
```

**`x1 * x2` equivalent to `x1 + x2 + x1:x2`**

# Linear Regression

## Example with msleep

```
lm(sleep_cycle ~ bodywt, data = msleep)
```

```
##
```

```
## Call:
```

```
## lm(formula = sleep_cycle ~ bodywt, data = msleep)
```

```
##
```

```
## Coefficients:
```

```
## (Intercept)      bodywt
```

```
##      0.38549      0.00107
```

# Linear Regression

## Example with msleep

```
lm(sleep_cycle ~ bodywt, data = msleep)
```

```
##
```

```
## Call:
```

```
## lm(formula = sleep_cycle ~ bodywt, data = msleep)
```

```
##
```

```
## Coefficients:
```

```
## (Intercept)
```

```
##      0.38549
```

Intercept

# Linear Regression

## Example with msleep

```
lm(sleep_cycle ~ bodywt, data = msleep)
```

```
##
```

```
## Call:
```

```
## lm(formula = sleep_cycle ~ bodywt, data = msleep)
```

```
##
```

```
## Coefficients:
```

```
## (Intercept)      bodywt
```

```
##      0.38549      0.00107
```



Slope



# Linear Regression

## Example with msleep

```
lm(sleep_cycle ~ bodywt, data = msleep)
```

```
##  
## Call:  
## lm(formula = sleep_cycle ~ bodywt, data = msleep)  
##  
## Coefficients:  
## (Intercept)      bodywt  
##      0.38549      0.00107
```

Hmm, not a lot of detail

# Linear Regression

## Assign model to m

```
m <- lm(sleep_cycle ~ bodywt, data = msleep)
```

**m** is a model object

```
class(m)
```

```
## [1] "lm"
```

This contains all the information about the model

# Linear Regression

```
summary(m)
```

```
##
## Call:
## lm(formula = sleep_cycle ~ bodywt, data = msleep)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -0.36081 -0.20228 -0.08506  0.03564  1.04817
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)  0.3854937   0.0623726   6.180 8.43e-07 ***
## bodywt       0.0010700   0.0004248   2.519  0.0173 *
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.3313 on 30 degrees of freedom
## (51 observations deleted due to missingness)
## Multiple R-squared:  0.1746,    Adjusted R-squared:  0.147
## F-statistic: 6.344 on 1 and 30 DF,  p-value: 0.01734
```

# Linear Regression

```
summary(m)
```

```
##
## Call:
## lm(formula = sleep_cycle ~ bodywt, data = msleep)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -0.36081 -0.20228 -0.08506  0.03564  1.04817
##
## Coefficients:
##              Estimate Std. Error
## (Intercept)  0.3854937   0.06237
## bodywt       0.0010700   0.00042
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.3313 on 30 degrees of freedom
## (51 observations deleted due to missingness)
## Multiple R-squared:  0.1746,    Adjusted R-squared:  0.147
## F-statistic: 6.344 on 1 and 30 DF,  p-value: 0.01734
```

**Wait!**

Shouldn't interpret until we know the  
model is solid

# Model Diagnostics

## Model Assumptions

- Normality (of residuals)
- Constant Variance (no heteroscedasticity)

## Other cautions

- Influential variables (Cook's D)
- Multiple collinearity (with more than one **x** or explanatory variables)

# Model Diagnostics

## Diagnostics by Hand

- Depending on model, different diagnostic functions (e.g., `plot()`)
- But you can check any model by hand if you pull out the right data

First let's get our relevant variables, **residuals** and **fitted values**:

```
d <- data.frame(residuals = residuals(m),      # Residuals
               fitted = fitted(m),           # Fitted values
               cooks = cooks.distance(m))    # Cook's D

d <- mutate(d, observation = 1:nrow(d))      # Observation number
```

# Model Diagnostics

## Diagnostics by Hand

- Depending on model, different diagnostic functions (e.g., `plot()`)
- But you can check any model by hand if you pull out the right data

First let's get our relevant variables, **residuals** and **fitted values**:

```
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                fitted = fitted(m),          # Fitted values
                cooks = cooks.distance(m))    # Cook's D

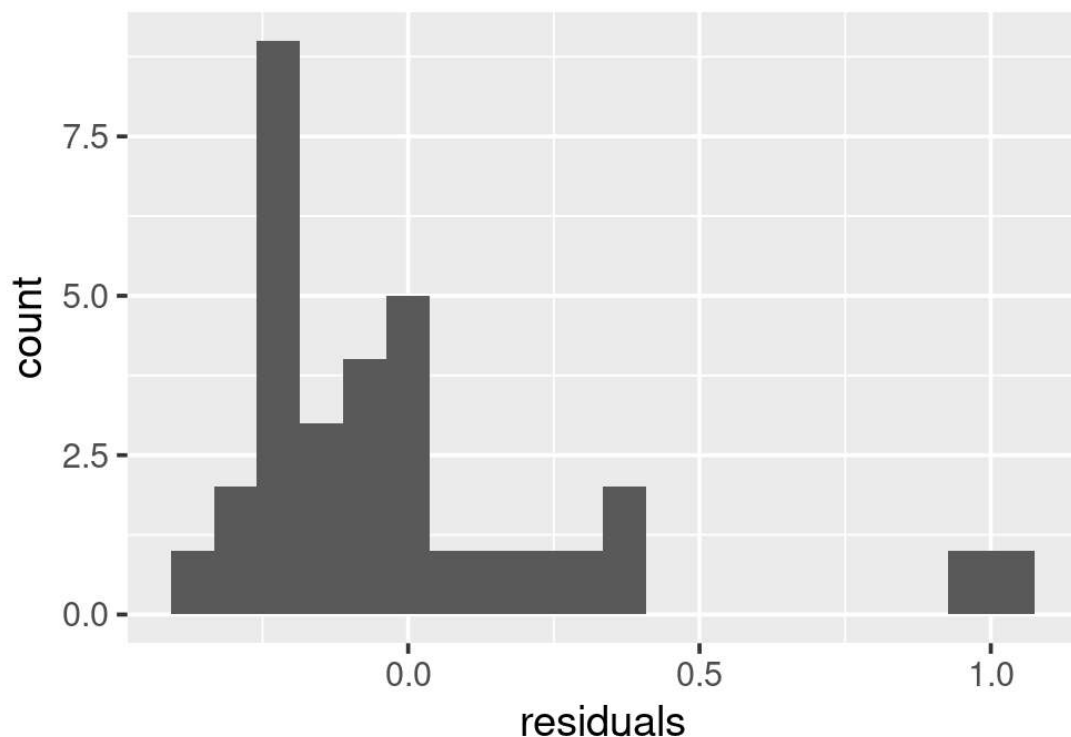
d <- mutate(d, observation = 1:nrow(d))      # Observation number
```

```
##      residuals      fitted      cooks observation
## 4 -0.25218072 0.3855141 1.104107e-02          1
## 5 -0.36081280 1.0274795 1.403343e+00          2
## 6  0.37705353 0.3896131 2.422542e-02          3
## 7 -0.02408421 0.4074175 9.247658e-05          4
## 9 -0.06714006 0.4004734 7.353601e-04          5
```

# Normality

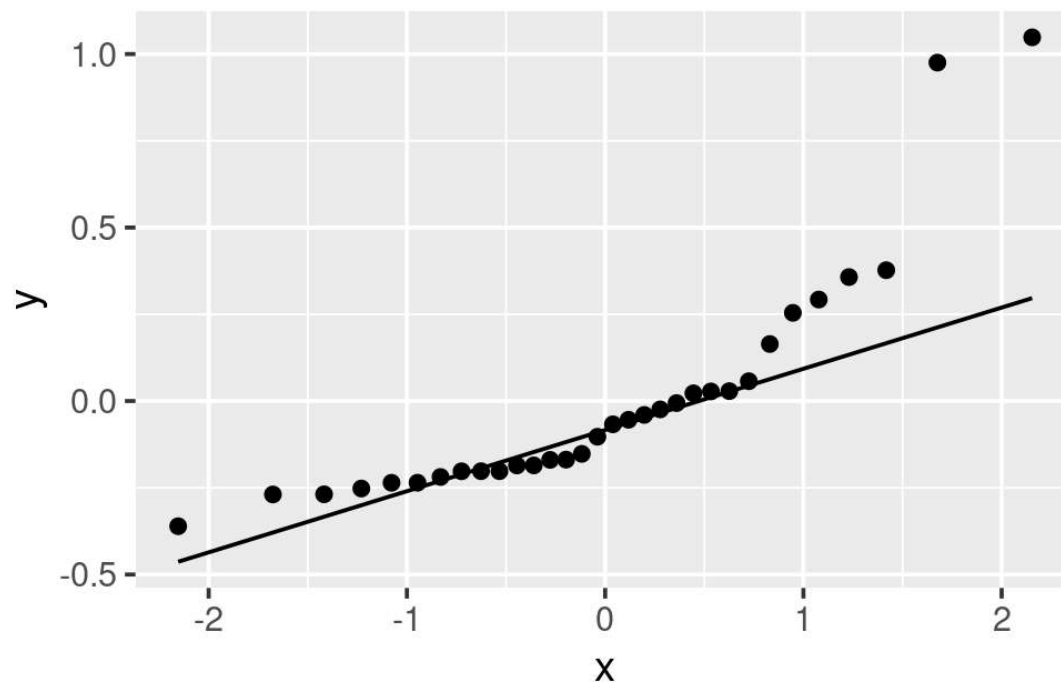
## Histogram of residuals

```
ggplot(data = d, aes(x = residuals)) +  
  geom_histogram(bins = 20)
```



## QQ Normality plot of residuals

```
ggplot(data = d, aes(sample = residuals)) +  
  stat_qq() +  
  stat_qq_line()
```

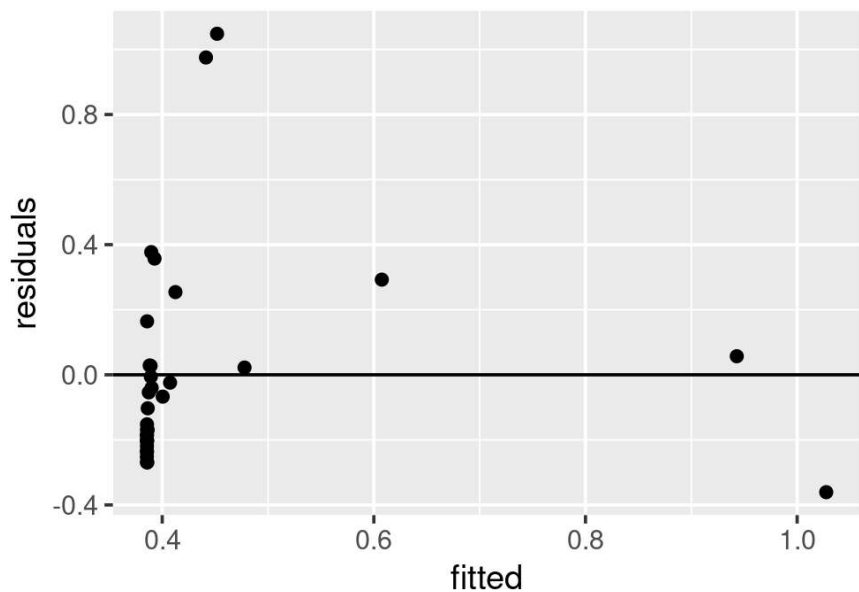




# Variance and Influence

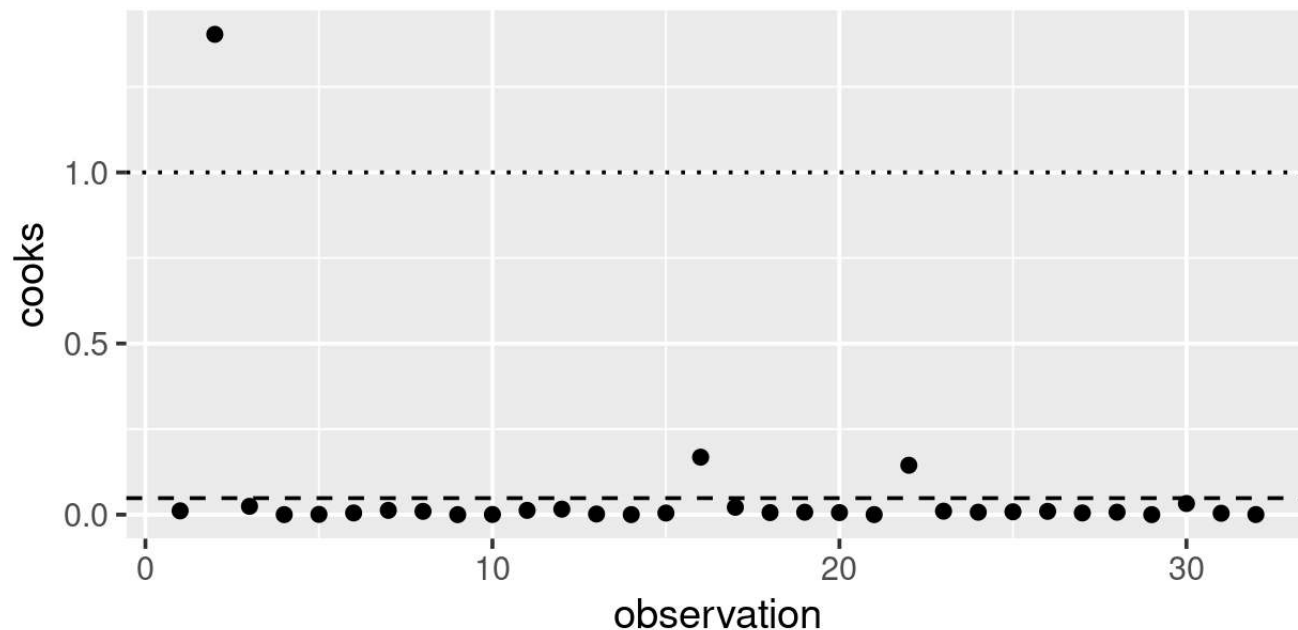
## Check heteroscedasticity

```
ggplot(d, aes(x = fitted, y = residuals)) +  
  geom_point() +  
  geom_hline(yintercept = 0)
```



## Cook's D

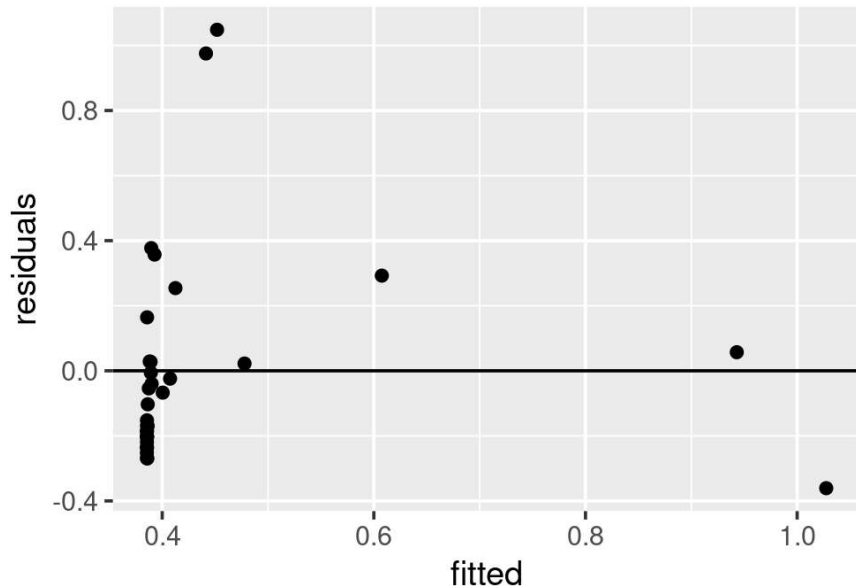
```
ggplot(d, aes(x = observation, y = cooks)) +  
  geom_point() +  
  geom_hline(yintercept = 1, linetype = "dotted") +  
  geom_hline(yintercept = 4/nrow(msleep), linetype = "dashed")
```



# Variance and Influence

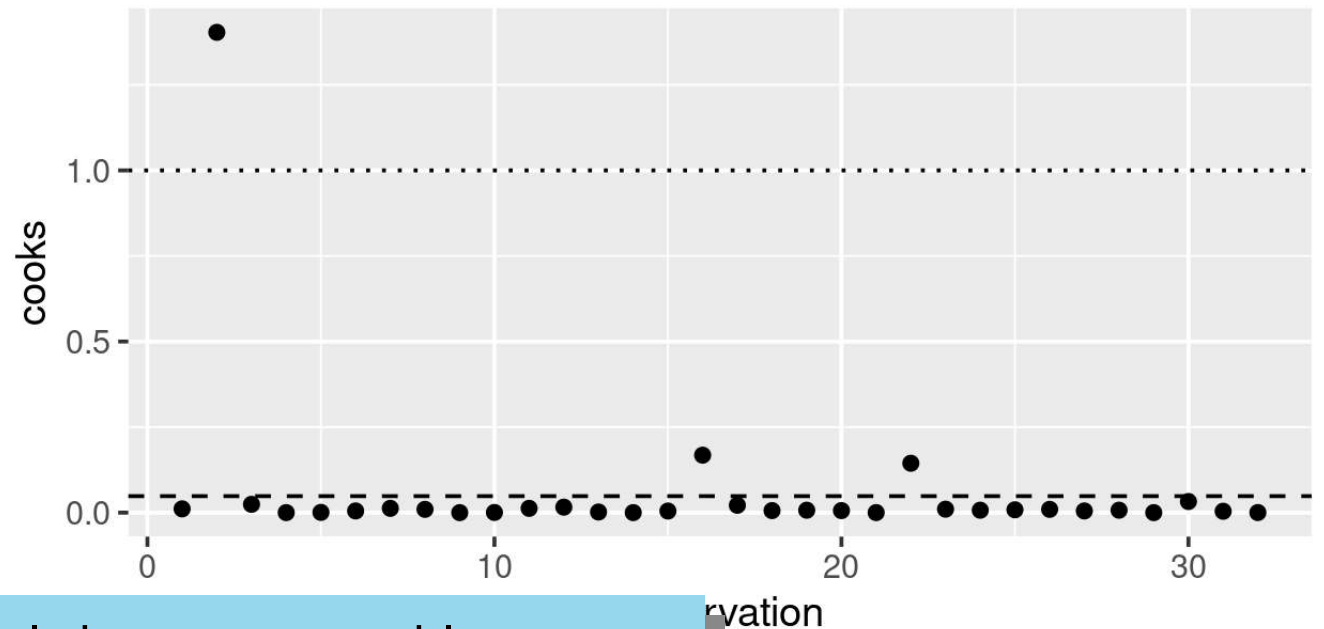
## Check heteroscedasticity

```
ggplot(d, aes(x = fitted, y = residuals)) +  
  geom_point() +  
  geom_hline(yintercept = 0)
```



## Cook's D

```
ggplot(d, aes(x = observation, y = cooks)) +  
  geom_point() +  
  geom_hline(yintercept = 1, linetype = "dotted") +  
  geom_hline(yintercept = 4/nrow(msleep), linetype = "dashed")
```

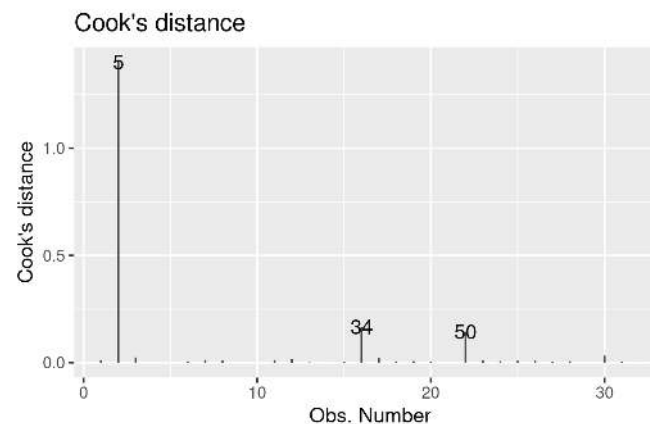
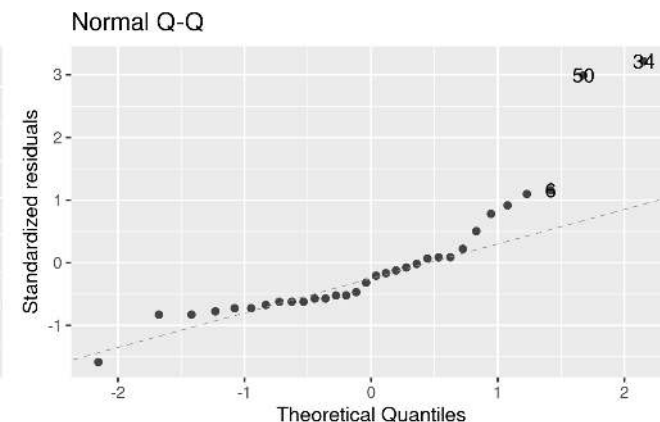
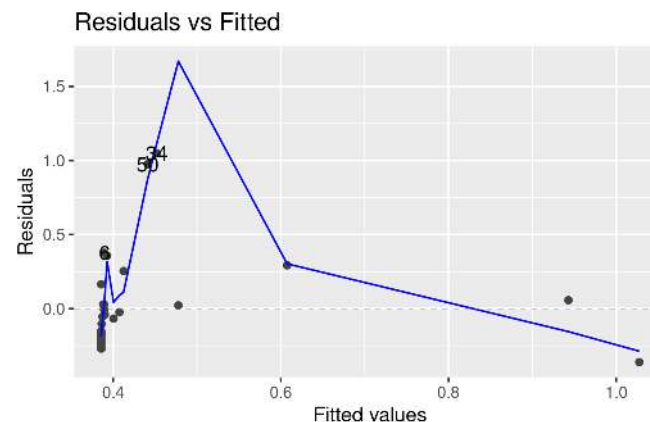


Definitely have some problems

# Diagnostics with ggfortify

- Uses **autoplot**
- Choose **which** plots to show
  - 1 = Residuals vs. fitted
  - 2 = QQ Norm
  - 4 = Cook's Distance
  - Others available

```
library(ggfortify)
autoplot(m, which = c(1, 2, 4))
```



# Transformations

## Let's try a log transformation

- Normally you would only transform the **y** value
- But mass data often works best with log10 or ln transformations (isometry)
- So we'll transform both x and y here

```
msleep_log <- mutate(msleep,  
                      sleep_cycle = log10(sleep_cycle),  
                      bodywt = log10(bodywt),  
                      brainwt = log10(brainwt))  
  
m_log <- lm(sleep_cycle ~ bodywt, data = msleep_log)
```

### Note:

- By default **log()** takes the ln. Use **log10()** if you want base 10

# Multicollinearity (collinearity)

Only relevant with more than one explanatory variable

```
m_mult <- lm(sleep_cycle ~ bodywt + brainwt, data = msleep_log)
```

# Multicollinearity (collinearity)

Only relevant with more than one explanatory variable

```
m_mult <- lm(sleep_cycle ~ bodywt + brainwt, data = msleep_log)
```

Use the **car** package to get the **vif()** function

```
library(car)
vif(m_mult)
```

```
##    bodywt  brainwt
## 13.30615 13.30615
```

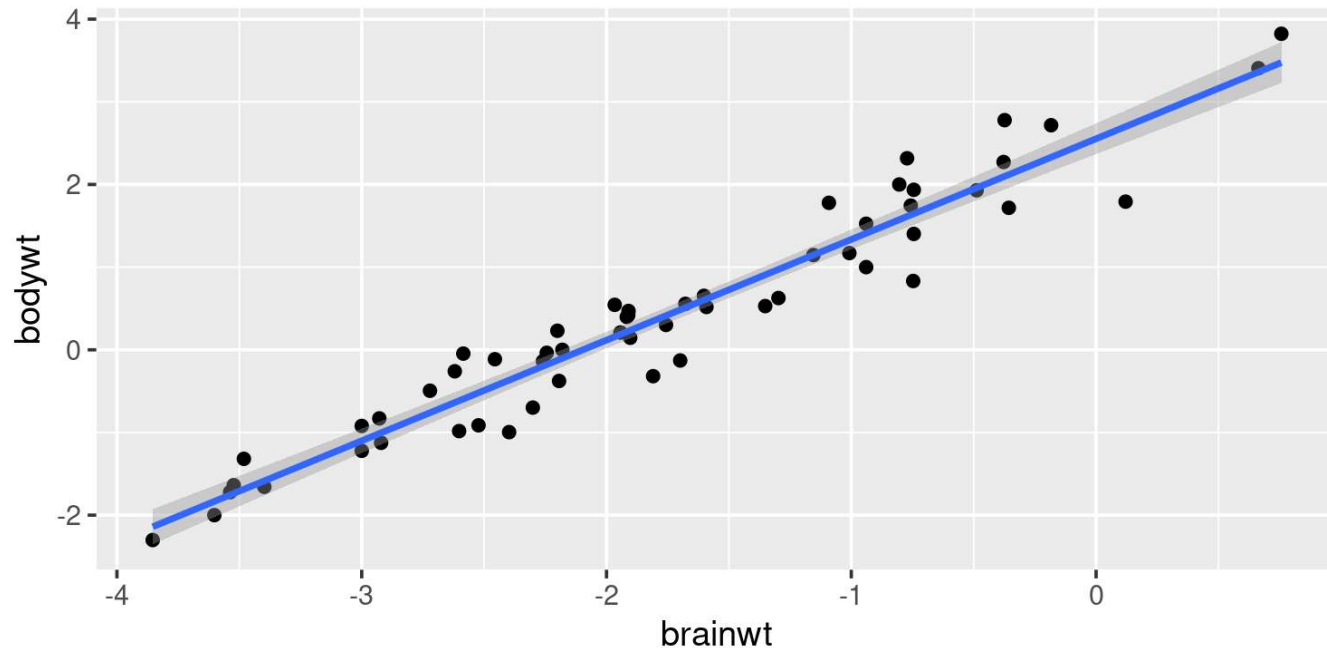
Hmm, that's pretty high (looking for  $< 10$ )

# Multicollinearity (collinearity)

Look at our two explanatory variables:

```
ggplot(data = msleep_log, aes(x = brainwt, y = bodywt)) +  
  geom_point() +  
  stat_smooth(method = "lm")
```

```
## `geom_smooth()` using formula 'y ~ x'
```

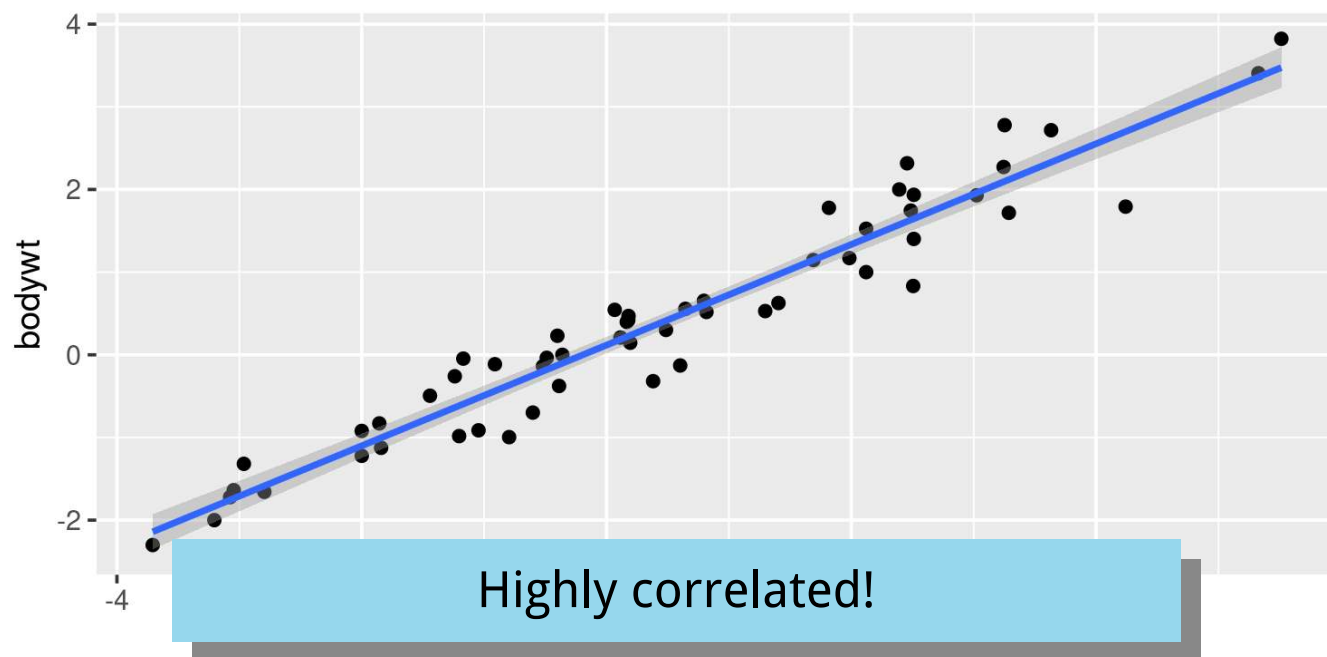


# Multicollinearity (collinearity)

Look at our two explanatory variables:

```
ggplot(data = msleep_log, aes(x = brainwt, y = bodywt)) +  
  geom_point() +  
  stat_smooth(method = "lm")
```

```
## `geom_smooth()` using formula 'y ~ x'
```





# Interpreting linear models

```
summary(m_log)
```

```
##
## Call:
## lm(formula = sleep_cycle ~ bodywt, data = msleep_log)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -0.36819 -0.13517 -0.01879  0.05897  0.36550
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept) -0.49439     0.03074 -16.082 2.72e-16 ***
## bodywt       0.18705     0.02197   8.515 1.68e-09 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.1734 on 30 degrees of freedom
## (51 observations deleted due to missingness)
## Multiple R-squared:  0.7073,    Adjusted R-squared:  0.6976
## F-statistic: 72.51 on 1 and 30 DF,  p-value: 1.679e-09
```

# Interpreting linear models

```
summary(m_log)
```

```
##
## Call:
## lm(formula = sleep_cycle ~ bodywt, data = msleep_log)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -0.36819 -0.13517 -0.01879  0.05897  0.36550
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## (Intercept) -0.49439     0.03074 -16.082 2.72e-16 ***
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## (51 observations deleted due to missingness)
## Multiple R-squared:  0.7073,    Adjusted R-squared:  0.6976
## F-statistic: 72.51 on 1 and 30 DF,  p-value: 1.679e-09
```

Model

# Interpreting linear models

```
summary(m_log)
```

```
##
## Call:
## lm(formula = sleep_cycle ~ bodywt, data = msleep_log)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -0.36819 -0.13517 -0.01879  0.05897  0.36550
##
## Coefficients:
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## F-statistic: 72.51 on 1 and 30 DF,  p-value: 1.679e-09
```

Effects!

# Interpreting linear models

```
summary(m_log)
```

```
##  
## Call:  
## lm(formula = sleep_cycle ~ bodywt, data = msleep_log)  
##  
## Residuals:  
##      Min       1Q   Median       3Q      Max   
## -0.36819 -0.13517 -0.01879  0.05897  0.36550   
##  
## Coefficients:  
##              Estimate Std. Error t value Pr(>|t|)      
## (Intercept) -0.49439      0.00000    2e-16 ***      
## bodywt       0.18705      0.00000    3e-09 ***      
## ---  
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1  
##  
## Residual standard error: 0.1734 on 30 degrees of freedom  
## (51 observations deleted due to missingness)  
## Multiple R-squared:  0.7073,    Adjusted R-squared:  0.6976   
## F-statistic: 72.51 on 1 and 30 DF,  p-value: 1.679e-09
```

Intercept

# Interpreting linear models

```
summary(m_log)
```

```
##
## Call:
## lm(formula = sleep_cycle ~ bodywt, data = msleep_log)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -0.36819 -0.13517 -0.01879  0.05897  0.36550
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)  -0.49439      0.00000  2e-16
## bodywt        0.18705      0.00000  3e-09
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.1734 on 30 degrees of freedom
## (51 observations deleted due to missingness)
## Multiple R-squared:  0.7073,    Adjusted R-squared:  0.6976
## F-statistic: 72.51 on 1 and 30 DF,  p-value: 1.679e-09
```

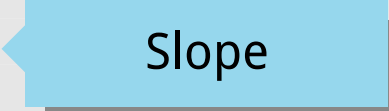
Intercept

For **bodywt** of 0 kg (log10 units),  
species has sleep cycle of -0.494 hours (log10 units)

# Interpreting linear models

```
summary(m_log)
```

```
##
## Call:
## lm(formula = sleep_cycle ~ bodywt, data = msleep_log)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -0.36819 -0.13517 -0.01879  0.05897  0.36550
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept) -0.49439    0.03074  -16.082 2.72e-16 ***
## bodywt       0.18705    0.00333   56.238 3e-09 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.1734 on 30 degrees of freedom
## (51 observations deleted due to missingness)
## Multiple R-squared:  0.7073,    Adjusted R-squared:  0.6976
## F-statistic: 72.51 on 1 and 30 DF,  p-value: 1.679e-09
```



# Interpreting linear models

```
summary(m_log)
```

```
##
## Call:
## lm(formula = sleep_cycle ~ bodywt, data = msleep_log)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -0.36819 -0.13517 -0.01879  0.05897  0.36550
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept) -0.49439    0.03074  -16.082 2.72e-16
## bodywt       0.18705    0.00333   56.233 3e-09
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.1734 on 30 degrees of freedom
## (51 observations deleted due to missingness)
## Multiple R-squared:  0.7073,    Adjusted R-squared:  0.6976
## F-statistic: 72.51 on 1 and 30 DF, p-value: 1.679e-09
```

Slope

For each 1 kg (log10 units) increase in **bodywt** sleep cycle increases by 0.187 hours (log10 units)

# Interpreting linear models

```
summary(m_log)
```

```
##
## Call:
## lm(formula = sleep_cycle ~ bodywt, data = msleep_log)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -0.36819 -0.13517 -0.01879  0.05897  0.36550
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept) -0.49439    0.03074  -16.082 2.72e-16 ***
## bodywt       0.18705    0.02197   8.515 1.68e-09 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.1734 on 30 degrees of freedom
## (51 observations deleted due to missingness)
## Multiple R-squared:  0.7073,    Adjusted R-squared:  0.6976
## F-statistic: 72.51 on 1 and 30 DF,  p-value: 1.679e-09
```

$$y = mx + b$$



# Interpreting linear models

```
summary(m_log)
```

```
##
## Call:
## lm(formula = sleep_cycle ~ bodywt, data = msleep_log)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -0.36819 -0.13517 -0.01879  0.05897  0.36550
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept) -0.49439    0.03074  -16.082 2.72e-16 ***
## bodywt       0.18705    0.02197   8.515 1.68e-09 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.1734 on 30 degrees of freedom
## (51 observations deleted due to missingness)
## Multiple R-squared:  0.7073,    Adjusted R-squared:  0.6976
## F-statistic: 72.51 on 1 and 30 DF,  p-value: 1.679e-09
```

$$y = 0.187x - 0.494$$

# Interpreting linear models

```
summary(m_log)
```

```
##
## Call:
## lm(formula = sleep_cycle ~ bodywt, data = msleep_log)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -0.36819 -0.13517 -0.01879  0.05897  0.36550
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept) -0.49439    0.03074  -16.082 2.72e-16 ***
## bodywt       0.18705    0.02197   8.515 1.68e-09 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.1734 on 30 degrees of freedom
## (51 observations deleted due to missingness)
## Multiple R-squared:  0.7073,    Adjusted R-squared:  0.6976
## F-statistic: 72.51 on 1 and 30 DF, p-value: 1.679e-09
```

Variability in the estimate

# Interpreting linear models

```
summary(m_log)
```

```
##
## Call:
## lm(formula = sleep_cycle ~ bodywt, data = msleep_log)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -0.36819 -0.13517 -0.01879  0.05897  0.36550
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept) -0.49439     0.03074  -16.082 2.72e-16 ***
## bodywt       0.18705     0.02197   8.515 1.68e-09 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.1734 on 30 degrees of freedom
## (51 observations deleted due to missingness)
## Multiple R-squared:  0.7073,    Adjusted R-squared:  0.6976
## F-statistic: 72.51 on 1 and 30 DF,  p-value: 1.679e-09
```

Significance of the results

# Interpreting linear models

```
summary(m_log)
```

```
##
## Call:
## lm(formula = sleep_cycle ~ bodywt, data = msleep_log)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -0.36819 -0.13517 -0.01879  0.05897  0.36550
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept) -0.49439     0.03074  -16.082 2.72e-16 ***
## bodywt       0.18705     0.02197   8.515 1.68e-09 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.1734 on 30 degrees of freedom
## (51 observations deleted due to missingness)
## Multiple R-squared:  0.7073,    Adjusted R-squared:  0.6976
## F-statistic: 72.51 on 1 and 30 DF,  p-value: 1.679e-09
```

Is the **intercept** significantly different from zero?  
(Yes,  $P < 0.0001$ )

# Interpreting linear models

```
summary(m_log)
```

```
##
## Call:
## lm(formula = sleep_cycle ~ bodywt, data = msleep_log)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -0.36819 -0.13517 -0.01879  0.05897  0.36550
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept) -0.49439     0.03074 -16.082 2.72e-16 ***
## bodywt       0.18705     0.02197   8.515 1.68e-09 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1
##
## Residual standard error: 0.1734 on 30 degrees of freedom
## (51 observations deleted due to missingness)
## Multiple R-squared:  0.7073,    Adjusted R-squared:  0.6976
## F-statistic: 72.51 on 1 and 30 DF,  p-value: 1.679e-09
```

Is the **slope** significantly different from zero?  
(Yes,  $P < 0.0001$ )

# Interpreting linear models

```
summary(m_log)
```

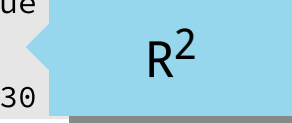
```
##
## Call:
## lm(formula = sleep_cycle ~ bodywt, data = msleep_log)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -0.36819 -0.13517 -0.01879  0.05897  0.36550
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept) -0.49439     0.03074 -16.082 2.72e-16 ***
## bodywt       0.18705     0.02197   8.515 1.68e-09 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1
##
## Residual standard error: 0.1734 on 30 degrees of freedom
## (51 observations deleted due to missingness)
## Multiple R-squared:  0.7073,    Adjusted R-squared:  0.6976
## F-statistic: 72.51 on 1 and 30 DF,  p-value: 1.679e-09
```

Is there a significant relationship between our variables? **(Yes)**

# Interpreting linear models

```
summary(m_log)
```

```
##
## Call:
## lm(formula = sleep_cycle ~ bodywt, data = msleep_log)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -0.36819 -0.13517 -0.01879  0.05897  0.36550
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept) -0.49439     0.03074 -16.082 2.72e-16 ***
## bodywt       0.18705     0.02197   8.515 1.68e-09 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.1734 on 30 degrees of freedom
## (51 observations deleted due to missingness)
## Multiple R-squared:  0.7073, Adjusted R-squared:  0.6976
## F-statistic: 72.51 on 1 and 30 df, value = 72.51, prob = 1.679e-09
```



# Interpreting linear models

```
summary(m_log)
```

```
##
## Call:
## lm(formula = sleep_cycle ~ bodywt, data = msleep_log)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -0.36819 -0.13517 -0.01879  0.05897  0.36550
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept) -0.49439     0.03074 -16.082 2.72e-16 ***
## bodywt       0.18705     0.02197   8.515 1.68e-09 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.1734 on 30 degrees of freedom
## (51 observations deleted due to missingness)
## Multiple R-squared:  0.7073,    Adjusted R-squared:  0.6976
## F-statistic: 72.51 on 1 and 30 DF,  p-value: 1.679e-09
```

$R^2$  Adjusted for the number of variables



# ANOVAs

**Same as before, but now with categorical variables (vore & conservation)**

```
m <- lm(sleep_total ~ vore + conservation, data = msleep)
```

# ANOVAs

Same as before, but now with categorical variables (vore & conservation)

```
m <- lm(sleep_total ~ vore + conservation, data = msleep)
```

What are these variables?

```
count(msleep, vore)
```

```
## # A tibble: 5 × 2
##   vore      n
##   <chr>  <int>
## 1 carni    19
## 2 herbi    32
## 3 insecti   5
## 4 omni     20
## 5 <NA>      7
```

```
count(msleep, conservation)
```

```
## # A tibble: 7 × 2
##   conservation      n
##   <chr>          <int>
## 1 cd              2
## 2 domesticated   10
## 3 en              4
## 4 lc             27
## 5 nt              4
## 6 vu              7
## 7 <NA>          29
```

cd = conservation dependent, lc = least concern, vu = vulnerable, nt = non-threatened, en = endangered, etc.

# ANOVAs

Same as before, but now with categorical variables (vore & conservation)

```
m <- lm(sleep_total ~ vore + conservation, data = msleep)
```

## What are these variables?

```
count(msleep, vore)
```

```
## # A tibble: 5 × 2
##   vore      n
##   <chr> <int>
## 1 carni    19
## 2 herbi    32
## 3 insecti   5
## 4 omni     20
## 5 <NA>      7
```

```
count(msleep, conservation)
```

```
## # A tibble: 7 × 2
##   conservation      n
##   <chr>          <int>
## 1 cd              2
## 2 domesticated   10
## 3 en              4
## 4 lc             27
## 5 nt              4
```

**Note:** This makes no sense!  
Why would conservation status ever predict sleep?

cd = conservation  
endangered, etc.

# Interpreting ANOVA *summaries*

```
summary(m)
```

```
##
## Call:
## lm(formula = sleep_total ~ vore + conservation, data = msleep)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -7.1632 -2.7702  0.2547  2.8866  6.4368
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)      3.851      3.041   1.266  0.21231
## voreherbi        -3.101      1.431  -2.167  0.03585 *
## voreinsecti       1.853      2.800   0.662  0.51174
## voreomni         -1.401      1.945  -0.720  0.47525
## conservationdomesticated  6.040      3.265   1.850  0.07121 .
## conservationen    10.262      3.688   2.783  0.00797 **
## conservationlc     9.414      3.141   2.997  0.00452 **
## conservationnt    11.450      3.638   3.147  0.00299 **
## conservationvu     4.407      3.353   1.314  0.19575
## ---
```

# Interpreting ANOVA *summaries*

```
summary(m)
```

```
##
## Call:
## lm(formula = sleep_total ~ vore + conservation, data = msleep)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -7.1632 -2.7702  0.2547  2.8866  6.4368
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)      3.851      3.041   1.266  0.21231
## voreherbi        -3.101      1.431  -2.167  0.03585 *
## voreinsecti       1.853      2.800   0.662  0.51174
## voreomni         -1.401      1.945  -0.720  0.47525
## conservationdomesticated  6.040      3.265   1.850  0.07121 .
## conservationen    10.262      3.688   2.783  0.00797 **
## conservationlc     9.414      3.141   2.997  0.00452 **
## conservationnt    11.450      3.638   3.147  0.00299 **
## conservationvu     4.407      3.353   1.314  0.19575
## ---
```

Treatment Contrasts

Effect of **vore** categories, each compared to first category (**carni**)

# Interpreting ANOVA *summaries*

```
summary(m)
```

```
##
## Call:
## lm(formula = sleep_total ~ vore + conservation, data = msleep)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -7.1632 -2.7702  0.2547  2.8866  6.4368
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)      3.851      3.041   1.266  0.21231
## voreherbi        -3.101      1.431  -2.167  0.03585 *
## voreinsecti       1.853      2.800   0.662  0.51174
## voreomni         -1.401      1.945  -0.720  0.47525
## conservationdomesticated  6.040      3.265   1.850  0.07121 .
## conservationen    10.262      3.688   2.783  0.00797 **
## conservationlc     9.414      3.141   2.997  0.00452 **
## conservationnt    11.450      3.638   3.147  0.00299 **
## conservationvu     4.407      3.353   1.314  0.19575
## ---
```

## Treatment Contrasts

### For example

Total sleep in herbivores (**herbi**) is significantly ( $P = 0.03585$ ) lower (Est = -3.101) than in carnivores (**carni**, baseline category)

# Interpreting ANOVA *summaries*

```
summary(m)
```

```
##
## Call:
## lm(formula = sleep_total ~ vore + conservation, data = msleep)
##
## Residuals:
```

	Min	1Q	Median	3Q	Max
	-7.1632	-2.7702	0.2547	2.8866	6.4368

```
##
## Coefficients:
```

	Estimate	Std. Error	t value	Pr(> t )
(Intercept)	3.851	3.041	1.266	0.21231
voreherbi	-3.101	1.431	-2.167	0.03585 *
voreinsecti	1.853	2.800	0.662	0.51174
voreomni	-1.401	1.945	-0.720	0.47525
conservationdomesticated	6.040	3.265	1.850	0.07121 .
conservationen	10.262	3.688	2.783	0.00797 **
conservationlc	9.414	3.141	2.997	0.00452 **
conservationnt	11.450	3.638	3.147	0.00299 **
conservationvu	4.407	3.353	1.314	0.19575

```
## ---
```

Treatment Contrasts

Effect of **conservation**  
categories, each compared to first  
category (**cd**)

# Interpreting ANOVA *tables*

```
anova(m)
```

```
## Analysis of Variance Table
```

```
##
```

```
## Response: sleep_total
```

```
##           Df Sum Sq Mean Sq F value    Pr(>F)
```

```
## vore          3  167.57   55.856    3.1960 0.032757 *
```

```
## conservation  5  342.97   68.595    3.9249 0.005095 **
```

```
## Residuals    43  751.51   17.477
```

```
## ---
```

```
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```



# Interpreting ANOVA *tables*

```
anova(m)
```

```
## Analysis of Variance Table
```

```
##
```

```
## Response: sleep_total
```

```
##           Df Sum Sq Mean Sq F value    Pr(>F)
```

```
## vore          3  167.57   55.856    3.1960 0.032757 *
```

```
## conservation  5  342.97   68.595    3.9249 0.005095 **
```

```
## Residuals    43  751.51   17.477
```

```
## ---
```

```
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

Overall differences among categories of  
**vore**

# Interpreting ANOVA *tables*

```
anova(m)
```

```
## Analysis of Variance Table
```

```
##
```

```
## Response: sleep_total
```

```
##           Df Sum Sq Mean Sq F value    Pr(>F)
```

```
## vore          3  167.57   55.856    3.1960 0.032757 *
```

```
## conservation  5  342.97   68.595    3.9249 0.005095 **
```

```
## Residuals    43  751.51   17.477
```

```
## ---
```

```
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

Overall differences among categories of  
**conservation**

# Interpreting ANOVA *tables*

```
anova(m)
```

```
## Analysis of Variance Table
```

```
##
```

```
## Response: sleep_total
```

```
##           Df Sum Sq Mean Sq F value    Pr(>F)
```

```
## vore           3  167.57   55.856    3.1960 0.032757 *
```

```
## conservation   5  342.97   68.595    3.9249 0.005095 **
```

```
## Residuals     43  751.51   17.477
```

```
## ---
```

```
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

This is a **Type I ANOVA**

# Interpreting ANOVA *tables*

## Type II ANOVA

```
library(car)
Anova(m, type = "2")
```

```
## Anova Table (Type II tests)
##
## Response: sleep_total
##
```

	Sum Sq	Df	F value	Pr(>F)	
vore	121.75	3	2.3220	0.088502	.
conservation	342.97	5	3.9249	0.005095	**
Residuals	751.51	43			
---					

```
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*'
0.05 '.' 0.1 ' ' 1
```

## Type III ANOVA

```
library(car)
Anova(m, type = "3")
```

```
## Anova Table (Type III tests)
##
## Response: sleep_total
##
```

	Sum Sq	Df	F value	Pr(>F)	
(Intercept)	28.01	1	1.6029	0.212313	
vore	121.75	3	2.3220	0.088502	.
conservation	342.97	5	3.9249	0.005095	**
Residuals	751.51	43			
---					

```
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*'
0.05 '.' 0.1 ' ' 1
```

# **ANOVAs and Post-Hoc Tests**

# Chicks and Diet

## Prep data

```
chicks <- filter(ChickWeight,  
                 Time == 21,  
                 !(Chick %in% 1:7))  
head(chicks)
```

```
## Grouped Data: weight ~ Time | Chick  
##   weight Time Chick Diet  
## 1     98   21     9    1  
## 2    124   21    10    1  
## 3    175   21    11    1  
## 4    205   21    12    1  
## 5     96   21    13    1  
## 6    266   21    14    1
```

## How many chicks per diet?

```
count(chicks, Diet)
```

```
## Grouped Data: weight ~ Time | Chick  
##   Diet  n  
## 1     1  9  
## 2     2 10  
## 3     3 10  
## 4     4  9
```

# Chicks and Diet

4 different diets, how do chicks gain weight on each diet?

```
m <- lm(weight ~ Diet, data = chicks)
```

# Chicks and Diet

4 different diets, how do chicks gain weight on each diet?

```
m <- lm(weight ~ Diet, data = chicks)
```

```
anova(m)
```

```
## Analysis of Variance Table
##
## Response: weight
##           Df Sum Sq Mean Sq F value    Pr(>F)
## Diet         3  68673 22891.0   5.5334 0.003331 **
## Residuals   34 140654   4136.9
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.'
0.1 ' ' 1
```



# Chicks and Diet

4 different diets, how do chicks gain weight on each diet?

```
m <- lm(weight ~ Diet, data = chicks)
```

```
anova(m)
```

```
## Analysis of Variance Table
##
## Response: weight
##           Df Sum Sq Mean Sq F value    Pr(>F)
## Diet        3  68673 22891.0   5.5334 0.003331 **
## Residuals  34 140654   4136.9
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.'
0.1 ' ' 1
```

```
summary(m)
```

```
##
## Call:
## lm(formula = weight ~ Diet, data = chicks)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -140.700  -39.414   -1.056   40.908  116.300
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)    153.33     21.44    7.152 2.87e-08 ***
## Diet2           61.37     29.55    2.077 0.045472 *
## Diet3          116.97     29.55    3.958 0.000365 ***
## Diet4           85.22     30.32    2.811 0.008143 **
## ---
```

# Chicks and Diet

4 different diets, how do chicks gain weight on each diet?

```
m <- lm(weight ~ Diet, data = chicks)
```

```
anova(m)
```

```
## Analysis of Variance Table
##
## Response: weight
##           Df Sum Sq Mean Sq F value    Pr(>F)
## Diet        3  68673 22891.0   5.5334 0.003331 **
## Residuals  34 140654   4136.9
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.'
0.1 ' ' 1
```

Need post-hoc tests to  
test each Diet against the others

```
summary(m)
```

```
##
## Call:
## lm(formula = weight ~ Diet, data = chicks)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -140.700  -39.414   -1.056   40.908  116.300
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)    153.33     21.44    7.152 2.87e-08 ***
## Diet2           61.37     29.55    2.077 0.045472 *
## Diet3          116.97     29.55    3.958 0.000365 ***
## Diet4           85.22     30.32    2.811 0.008143 **
## ---
```

# Post-Hoc Tests

```
library(multcomp)
mult_pairwise <- glht(m, linfct = mcp(Diet = "Tukey")) # All Pair-wise comparisons
```

- Package **multcomp**
- Function **glht()** (general linear hypothesis testing)
- Model of interest (here, **m**)
- Argument **linfct** (linear function, i.e., Which post-hoc tests?)
- Function **mcp()** (multiple comparisons)
- Specify the variable you want to compare (Here, **Diet**)
- Specify the way the categories should be compared:
  - **"Tukey"** reflects **Tukey Contrasts** (i.e., all pairwise comparisons)
  - **"Dunnett"** reflects **Dunnett's comparison with a control**

# Post-Hoc Tests

## All pair-wise comparisons

```
summary(mult_pairwise)
```

```
##      Simultaneous Tests for General Linear Hypotheses
##
## Multiple Comparisons of Means: Tukey Contrasts
##
##
## Fit: lm(formula = weight ~ Diet, data = chicks)
##
## Linear Hypotheses:
##              Estimate Std. Error t value Pr(>|t|)
## 2 - 1 == 0      61.37      29.55   2.077  0.18124
## 3 - 1 == 0     116.97      29.55   3.958  0.00186 **
## 4 - 1 == 0      85.22      30.32   2.811  0.03873 *
## 3 - 2 == 0      55.60      28.76   1.933  0.23359
## 4 - 2 == 0      23.86      29.55   0.807  0.85056
## 4 - 3 == 0     -31.74      29.55  -1.074  0.70723
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## (Adjusted p values reported -- single-step method)
```

Each group compared to each other  
 $2 - 1 == 0$  reflects hypothesis that  
Diet 2 - Diet 1 is equal to 0  
(i.e., no difference)

# Post-Hoc Tests

## All pair-wise comparisons

```
summary(mult_pairwise)
```

```
##      Simultaneous Tests for General Linear Hypotheses
##
## Multiple Comparisons of Means: Tukey Contrasts
##
##
## Fit: lm(formula = weight ~ Diet, data = chicks)
##
## Linear Hypotheses:
##              Estimate Std. Error t value Pr(>|t|)
## 2 - 1 == 0      61.37      29.55   2.077  0.18124
## 3 - 1 == 0     116.97      29.55   3.958  0.00186 **
## 4 - 1 == 0      85.22      30.32   2.811  0.03873 *
## 3 - 2 == 0      55.60      28.76   1.933  0.23359
## 4 - 2 == 0      23.86      29.55   0.807  0.85056
## 4 - 3 == 0     -31.74      29.55  -1.074  0.70723
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## (Adjusted p values reported -- single-step method)
```

Each group compared to each other  
 $2 - 1 == 0$  reflects hypothesis that  
Diet 2 - Diet 1 is equal to 0  
(i.e., no difference)

# Post-Hoc Tests

## Specify the P-Value adjustment

```
summary(mult_pairwise, test = adjusted("BH"))
```

```
##      Simultaneous Tests for General Linear Hypotheses
##
## Multiple Comparisons of Means: Tukey Contrasts
##
##
## Fit: lm(formula = weight ~ Diet, data = chicks)
##
## Linear Hypotheses:
##              Estimate Std. Error t value Pr(>|t|)
## 2 - 1 == 0      61.37      29.55   2.077  0.09094 .
## 3 - 1 == 0     116.97      29.55   3.958  0.00219 **
## 4 - 1 == 0      85.22      30.32   2.811  0.02443 *
## 3 - 2 == 0      55.60      28.76   1.933  0.09241 .
## 4 - 2 == 0      23.86      29.55   0.807  0.42515
## 4 - 3 == 0     -31.74      29.55  -1.074  0.34837
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## (Adjusted p values reported -- BH method)
```

"BH" = Benjamini-Hochberg,  
also known as FDR test  
(see [here for more details](#))

# Post-Hoc Tests

Argument	P-Value Adjustment
single-step	Adjusted p values based on the joint normal or t distribution of the linear function
Shaffer	<a href="#"><u>Shaffer Test</u></a>
Westfall	<a href="#"><u>Westfall Test</u></a>
free	<a href="#"><u>Multiple testing procedures under free combinations</u></a>
holm	<a href="#"><u>Holm Test</u></a>
hochberg	<a href="#"><u>Hochberg Test</u></a>
hommel	<a href="#"><u>Hommel Test</u></a>
bonferroni	Bonferroni Correction
BH or fdr	<a href="#"><u>Benjamini-Hochberg Test or False Discovery Rate Test</u></a>
BY	<a href="#"><u>Benjamini-Yekutieli Test</u></a>
none	No P-Value Adjustment

# Data Transformations



# Transformations

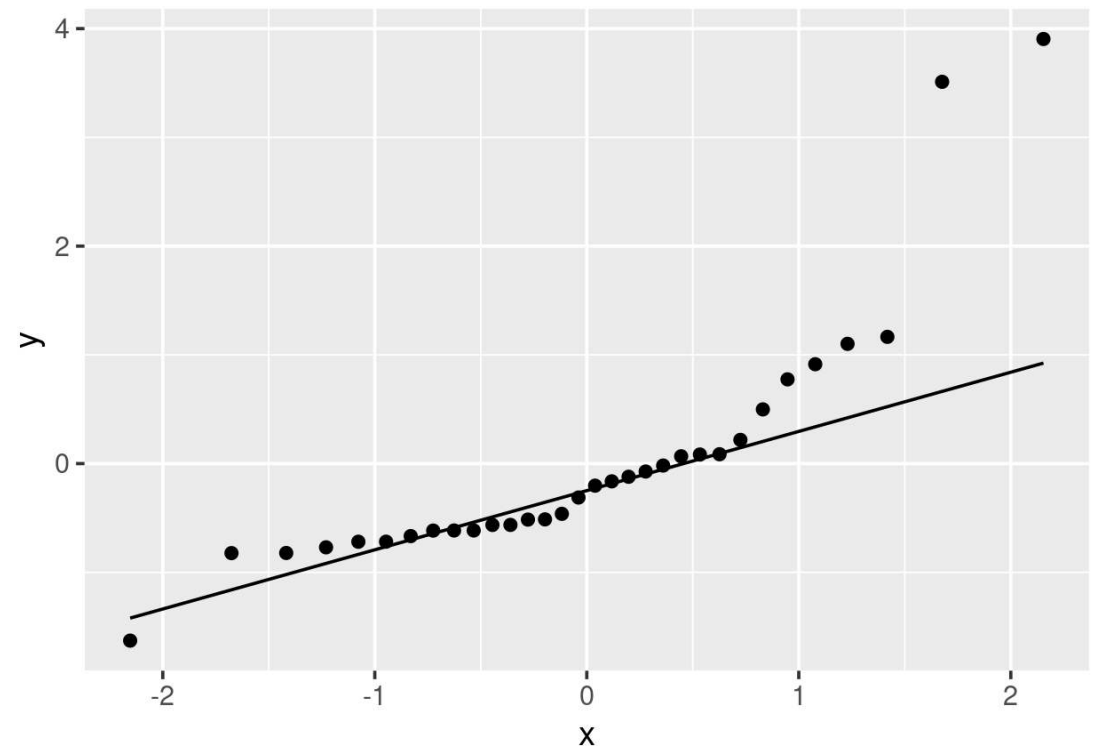
```
m <- lm(sleep_cycle ~ bodywt, data = msleep)

d <- data.frame(residuals = residuals(m),
               std_residuals = rstudent(m),
               fitted = fitted(m),
               cooks = cooks.distance(m))

d <- mutate(d, observation = 1:nrow(d))
```

Good for addressing non-normality of residuals,  
and problems with variance

```
ggplot(data = d, aes(sample = std_residuals)) +  
  stat_qq() +  
  stat_qq_line()
```



# Transformations

## Order of Operations

1. See the need (e.g., non-normal residuals, heteroscedacity)
2. Figure out which transformation
3. Apply the transformation
4. Check model assumptions
5. Rinse and repeat as needed

# Transformations: Common options

## Table of transformations in R

```
data_trans <- mutate(data, y_trans = 1/y^2)
data_trans <- mutate(data, y_trans = 1/y)
data_trans <- mutate(data, y_trans = 1/sqrt(y))
data_trans <- mutate(data, y_trans = log(y))
data_trans <- mutate(data, y_trans = log10(y))
data_trans <- mutate(data, y_trans = sqrt(y))
data_trans <- mutate(data, y_trans = y^2)
data_trans <- mutate(data, y_trans = asin(sqrt(y/100)))
data_trans <- mutate(data, y_trans = (y^lambda - 1)/lambda)
```

Transformation	R Code
Inverse square	$1/y^2$
Reciprocal	$1/y$
Inverse square root	$1/\sqrt{y}$
Natural log (ln)	$\log(y)$
Log base 10	$\log_{10}(y)$
Square root	$\sqrt{y}$
Square	$y^2$
Box Cox	$(y^\lambda - 1) / \lambda$
Arcsine-square-root	$\text{asin}(\sqrt{y/100})$

**data\_trans** is the NEW data frame, **y\_trans** is your TRANSFORMED y-value

# Transformations: How to choose?

- Based on what you know (often discipline specific standards for certain data types)
- Based on what you see (does it look exponential or logarithmic?)
- Based on trial and error (try different transformations and see how it goes)
- Based on Box-Cox lambda ( $\lambda$ )

**Can EITHER apply  $\lambda$  through Box-Cox transformation OR use it to indicate best transformation**

Best $\lambda$	Equation	Name
-2.5 to -1.5	$1/y^2$	inverse square
-1.5 to -0.75	$1/y$	reciprocal
-0.75 to -0.25	$1/\sqrt{y}$	inverse square root
-0.25 to 0.25	$\ln(y)$	natural log
0.25 to 0.75	$\sqrt{y}$	square root
0.75 to 1.5	$y$	none
1.5 to 2.5	$y^2$	square

# Transformations: Find $\lambda$

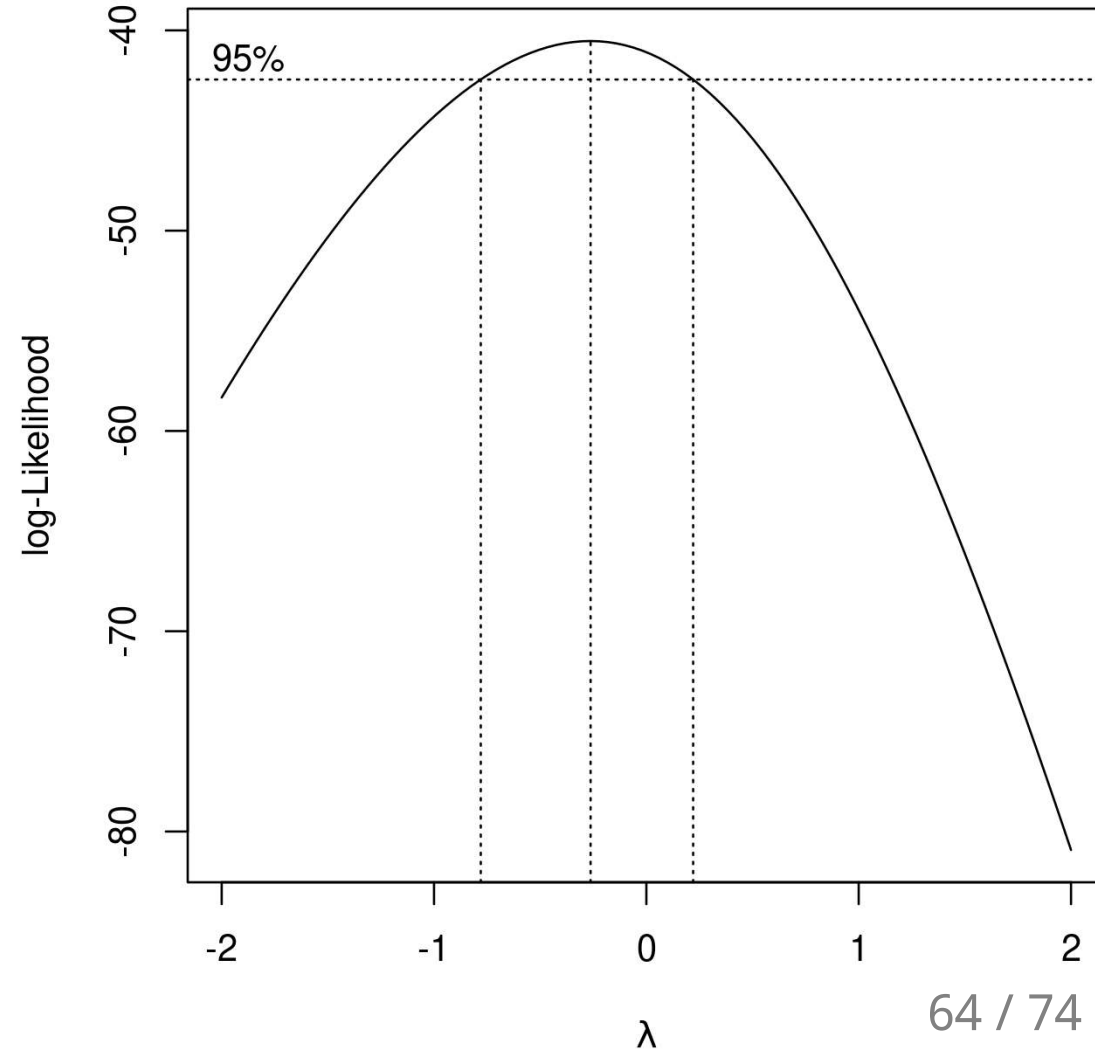
## Plot of $\lambda$

```
library(MASS)
b <- boxcox(m)
```

## Exact $\lambda$

```
b$x[b$y == max(b$y)]
```

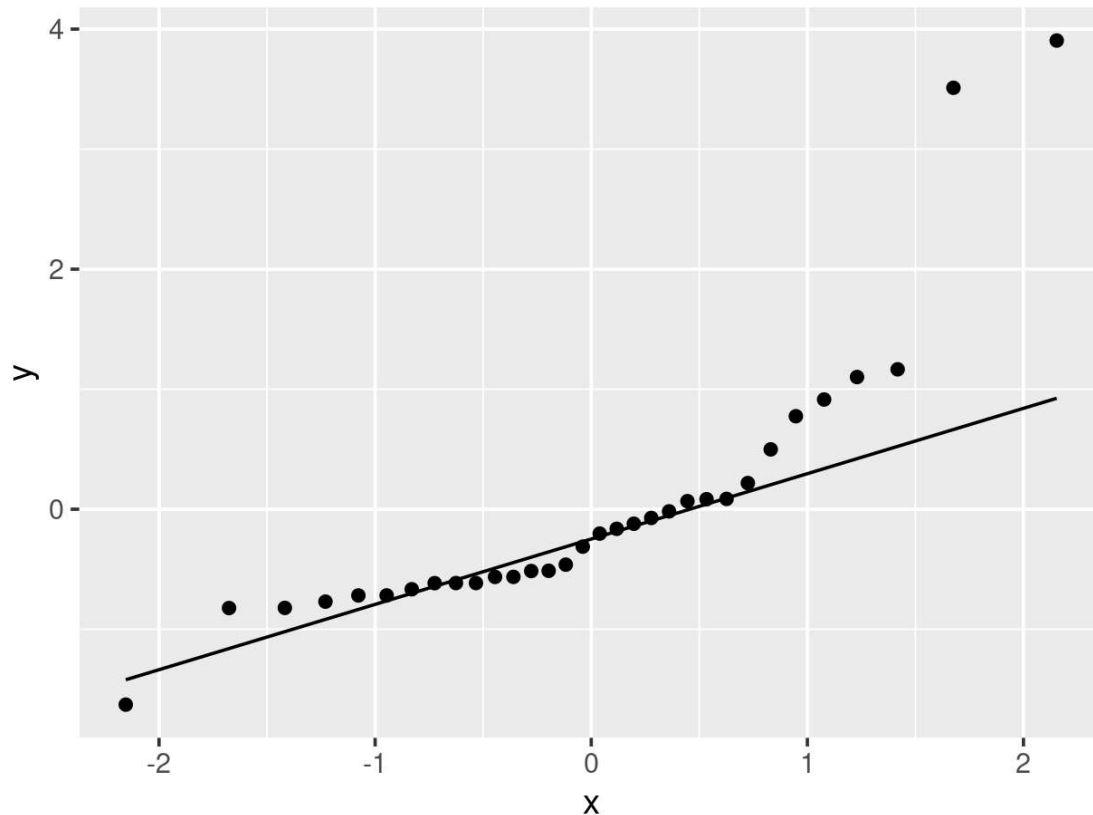
```
## [1] -0.2626263
```



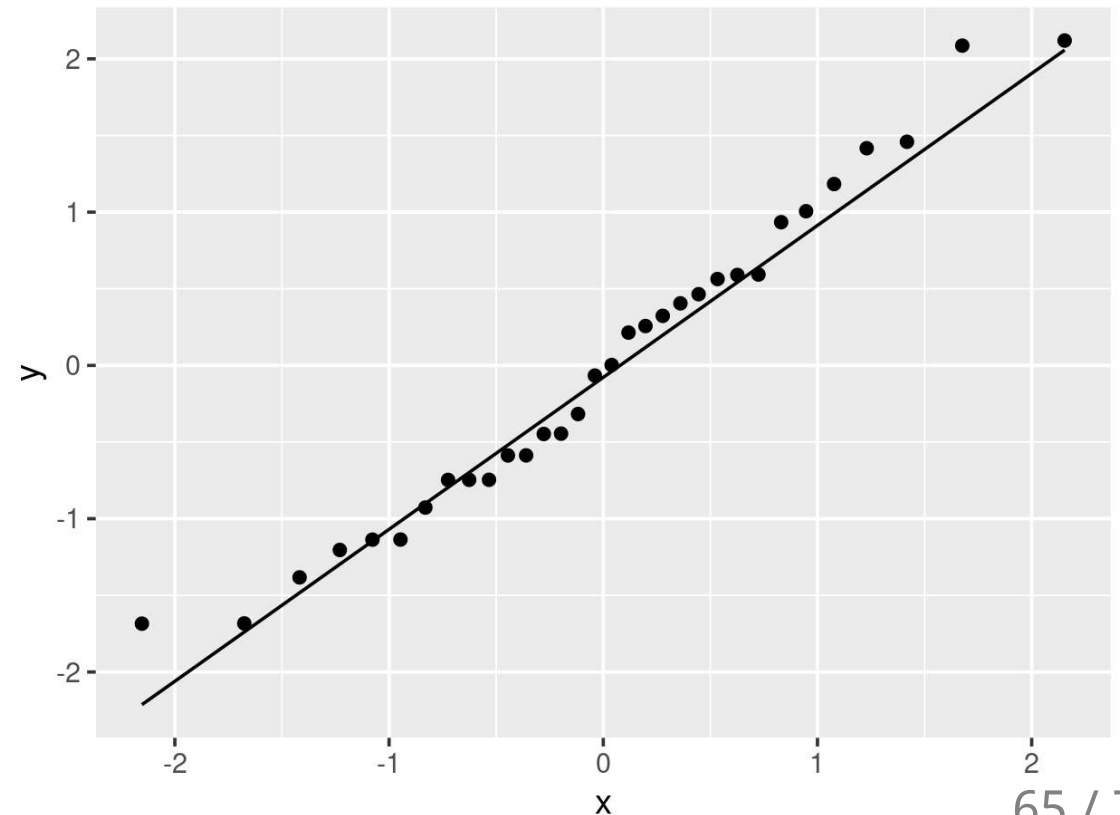
# Apply the transformation

```
msleep_trans <- mutate(msleep, sleep_cycle = (sleep_cycle^(-0.26) - 1) / -0.26)  
m_trans <- lm(sleep_cycle ~ bodywt, data = msleep_trans)
```

Q-Q Normality Plot: No transformation



Q-Q Normality Plot: Box-Cox transformation



# Generalized Linear Models

# Generalized Linear Models

## Normal distribution - Gaussian Distribution

```
lm(y ~ x1 * x2, data = my_data)
```

## Count data - Poisson Family

```
glm(counts ~ x1 * x2, family = "poisson", data = my_data)
```

## Binary (0/1, Logistic Regression) - Binomial Distribution

```
glm(y ~ x1 * x2, family = "binomial", data = my_data)
```

## Proportion with binary outcomes (10 yes, 5 no) - Binomial Distribution

```
glm(cbind(Yes, No) ~ x1 * x2, family = "binomial", data = my_data)
```



# Poisson - Run

## Download data

```
p <- read.csv("https://stats.idre.ucla.edu/stat/data/poisson_sim.csv")
p <- mutate(p, program = factor(prog, levels = 1:3,
                                labels = c("General", "Academic", "Vocational")))
head(p)
```

##	id	num_awards	prog	math	program
## 1	45	0	3	41	Vocational
## 2	108	0	1	41	General
## 3	15	0	3	44	Vocational
## 4	67	0	3	42	Vocational
## 5	153	0	3	40	Vocational
## 6	51	0	1	42	General

## Run model

```
m <- glm(num_awards ~ program + math, family = "poisson", data = p)
```

# Poisson - Evaluate

```
summary(m)
```

```
## glm(formula = num_awards ~ program + math, family = "poisson",
##      data = p)
##
## Deviance Residuals:
##      Min        1Q    Median        3Q        Max
## -2.2043   -0.8436   -0.5106    0.2558    2.6796
##
## Coefficients:
##              Estimate Std. Error z value Pr(>|z|)
## (Intercept)   -5.24712    0.65845  -7.969 1.60e-15 ***
## programAcademic    1.08386    0.35825   3.025 0.00248 **
## programVocational  0.36981    0.44107   0.838 0.40179
## math            0.07015    0.01060   6.619 3.63e-11 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for poisson family taken to be 1)
##
##      Null deviance: 287.67  on 199  degrees of freedom
## Residual deviance: 189.45  on 196  degrees of freedom
```

Look at deviance vs. df:

```
deviance(m)
```

```
## [1] 189.4496
```

```
df.residual(m)
```

```
## [1] 196
```

```
deviance(m) / df.residual(m)
```

```
## [1] 0.9665797
```

Nice! (should be close to 1)

# Binary (0/1 - Logistic Regression)

## Data

```
binary <- read.csv("https://stats.idre.ucla.edu/stat/data/binary.csv")  
head(binary)
```

##	admit	gre	gpa	rank
## 1	0	380	3.61	3
## 2	1	660	3.67	3
## 3	1	800	4.00	1
## 4	1	640	3.19	4
## 5	0	520	2.93	4
## 6	1	760	3.00	2

## Run model

```
m <- glm(admit ~ gpa, family = "binomial", data = binary)
```

# Binary (0/1 - Logistic Regression)

## Check results

```
summary(m)
```

```
## Call:
## glm(formula = admit ~ gpa, family = "binomial", data = binary)
##
## Deviance Residuals:
##      Min       1Q   Median       3Q      Max
## -1.1131  -0.8874  -0.7566   1.3305   1.9824
##
## Coefficients:
##              Estimate Std. Error z value Pr(>|z|)
## (Intercept)  -4.3576     1.0353  -4.209 2.57e-05 ***
## gpa           1.0511     0.2989   3.517 0.000437 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
##      Null deviance: 499.98  on 399  degrees of freedom
## Residual deviance: 486.97  on 398  degrees of freedom
```

## Convert to Odd's Ratios

```
exp(coef(m))
```

```
## (Intercept)          gpa
##  0.01280926  2.86082123
```

e.g., The odds of being admitted increase by a factor of 2.86 (x2.86 times more likely) for every unit increase in GPA.

# Binary Outcomes

Proportion with binary outcomes (e.g., 10 yes, 5 no)

## Get the data

```
admissions <- as.data.frame(UCBAdmissions)
admissions <- spread(admissions, Admit, Freq)
head(admissions)
```

##	Gender	Dept	Admitted	Rejected
## 1	Male	A	512	313
## 2	Male	B	353	207
## 3	Male	C	120	205
## 4	Male	D	138	279
## 5	Male	E	53	138
## 6	Male	F	22	351

## Run model

```
m <- glm(cbind(Admitted, Rejected) ~ Gender, family = "binomial", data = admissions)
```

# Binary Outcomes

## Check results

```
summary(m)
```

```
## Call:
## glm(formula = cbind(Admitted, Rejected) ~ Gender, family = "binomial",
##      data = admissions)
##
## Deviance Residuals:
##      Min       1Q   Median       3Q      Max
## -16.7915   -4.7613   -0.4365    5.1025   11.2022
##
## Coefficients:
##              Estimate Std. Error z value Pr(>|z|)
## (Intercept)  -0.22013    0.03879  -5.675 1.38e-08 ***
## GenderFemale -0.61035    0.06389  -9.553 < 2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
##      Null deviance: 877.06  on 11  degrees of freedom
## Residual deviance: 783.61  on 10  degrees of freedom
```

```
deviance(m)
```

```
## [1] 783.607
```

```
df.residual(m)
```

```
## [1] 10
```

```
deviance(m) / df.residual(m)
```

```
## [1] 78.3607
```

Oops, over-dispersed

# Binary Outcomes

## Try again with 'quasibinomial' family

```
m <- glm(cbind(Admitted, Rejected) ~ Gender, family = "quasibinomial", data = admissions)
summary(m)
```

```
## Call:
## glm(formula = cbind(Admitted, Rejected) ~ Gender, family = "quasibinomial",
##      data = admissions)
##
## Deviance Residuals:
##      Min       1Q   Median       3Q      Max
## -16.7915   -4.7613   -0.4365    5.1025   11.2022
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)   -0.2201     0.3281  -0.671   0.517
## GenderFemale  -0.6104     0.5404  -1.129   0.285
##
## (Dispersion parameter for quasibinomial family taken to be 71.52958)
##
##      Null deviance: 877.06  on 11  degrees of freedom
## Residual deviance: 783.61  on 10  degrees of freedom
```