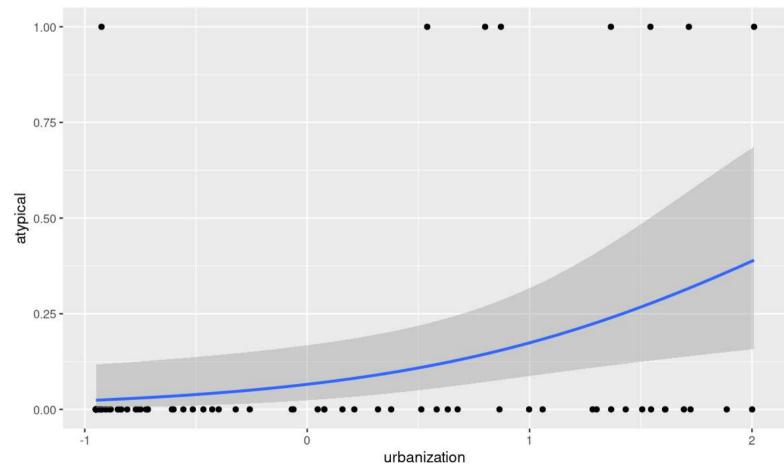
Even more stats...

Generalized linear models, Other advanced models, Non-parametric stats



Getting started (again)

Open RStudio
Open your NRI project
Open a **new** script for today:

File > New File > R Script

Make sure to load packages at the top:

library(tidyverse)
library(DHARMa)

Reference Material

This lecture covers A HUGE subject area

It is not comprehensive

It is a place to start, with references to guide you later on

Diagnostics for complex models

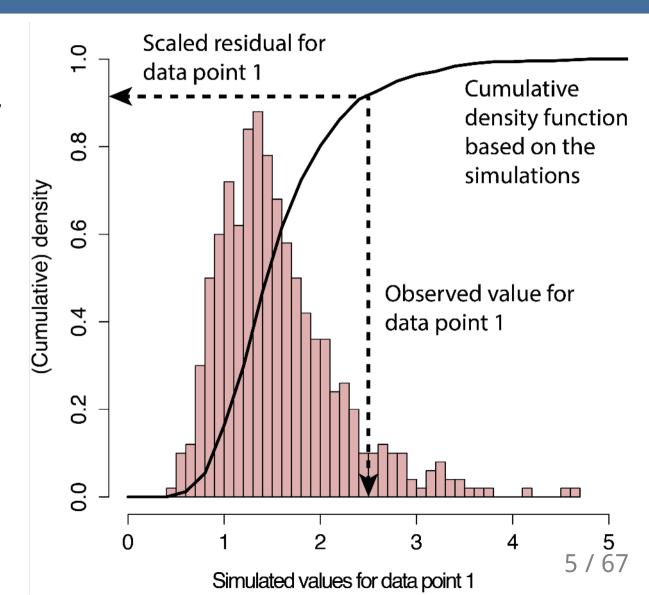
Introducing DHARMa

DHARMa Tutorial

(Many great examples of model checking)

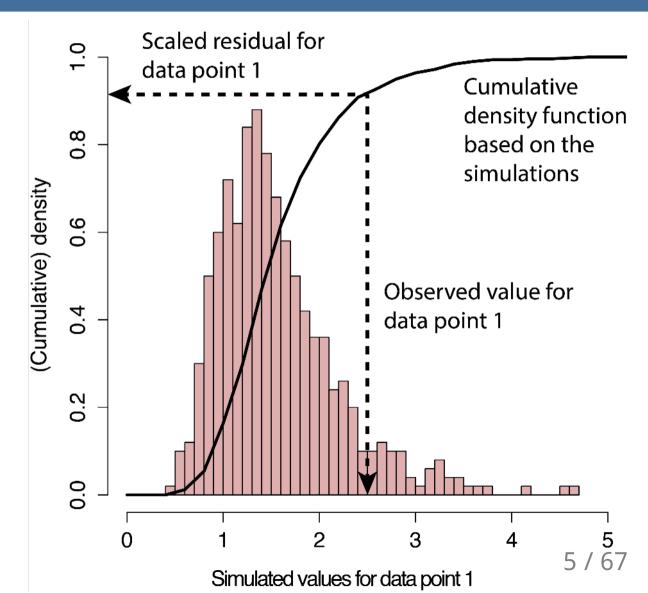
Simulated Residuals

- **If** your data perfectly matched your model, what would the values look like?
 - Pink histogram values show repeatedly simulated values



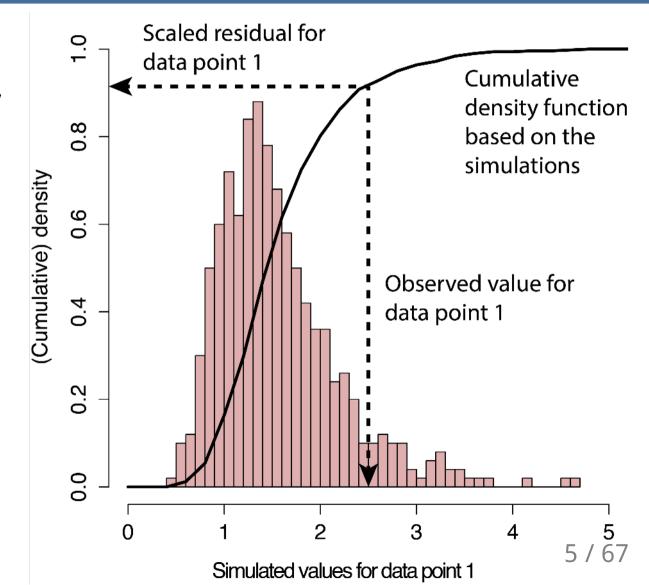
Simulated Residuals

- **If** your data perfectly matched your model, what would the values look like?
 - Pink histogram values show repeatedly simulated values
- How do your *actual* values compare?
 - Black arrow on x-axis shows actual value
 - Black arrow on y-axis shows residual: how actual value compares to distribution of simulated values



Simulated Residuals

- **If** your data perfectly matched your model, what would the values look like?
 - Pink histogram values show repeatedly simulated values
- How do your *actual* values compare?
 - Black arrow on x-axis shows actual value
 - Black arrow on y-axis shows residual: how actual value compares to distribution of simulated values
- Residuals are scaled (0 to 1)
 - If data fits model perfectly, expect all = 0.5
 - Good fit *always* = flat/uniform distribution

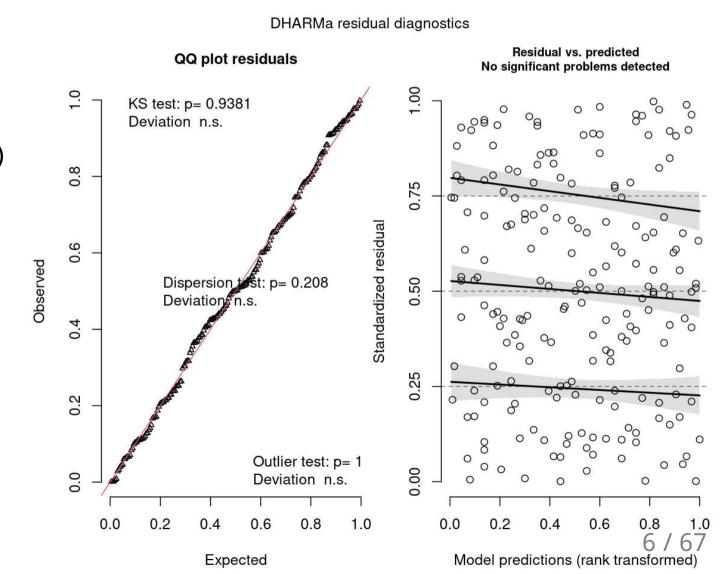


If data fits the model

Residuals follow a flat (uniform)
 distribution (no matter what model!)

If data fits the model

- Residuals follow a flat (uniform)
 distribution (no matter what model!)
- Expect: Straight line on QQ plot of uniform distribution
 (similar to QQ Normal plot)
- Expect: No patterns between residuals and model predictions (similar to heteroscedasticity plot, resid vs. fitted)



If data fits the model

Residuals follow a flat (uniform)
 distribution (no matter what model!)

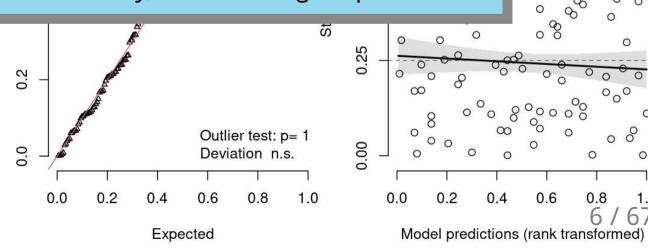
• Expect: !
uniforn
(similar to C

These aren't the same kinds of plots we did in the last couple of labs.

Note

BUT you can interpret them the same way, when looking for problems

 Expect: No patterns between residuals and model predictions (similar to heteroscedasticity plot, resid vs. fitted)



DHARMa residual diagnostics

QQ plot residuals

KS test: p= 0.9381

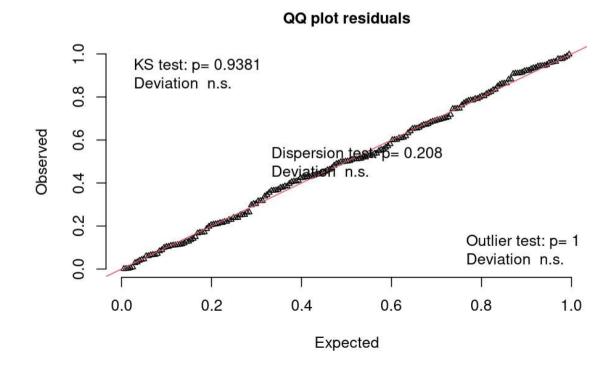
Deviation n.s.

Residual vs. predicted

No significant problems detected

QQ Plot

- Tests **Uniformity** with Kolmogorov-Smirnov (KS) test
 (do the residuals match a Uniform distribution?)
- Tests for **Over/Underdispersion** with Dispersion Test
- Tests for more **Outliers** than expected with Outlier test



QQ Plot

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 (do the residuals match a Uniform distribution?)
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- Tests for more **Outliers** than expected with Outlier test

QQ plot residuals KS test: p= 0.9381 Deviation n.s. 0.8 Observed 9.0 Dispersion test p= 0.208 Deviation n.s. 0.4 0.2 Outlier test: p= 1 Deviation n.s. 0.0 0.0 0.2 0.4 0.6 8.0 1.0 Expected

Residuals vs. Predicted

- Check distribution of residuals (visually and with quantiles)
- Dotted lines show expected quantiles
- Black lines show simulated quantiles (want straight lines)
- Outliers would show up as red stars

Usage

```
library(DHARMa)

m <- lm(body_mass_g ~ flipper_length_mm, data = penguins)

r <- simulateResiduals(m, n = 1000, plot = TRUE)</pre>
```

- simulateResiduals() function from
- Use **plot** = **TRUE** to produce diagnostic plots to see if simulated match expectation
- n = 1000 isn't strictly necessary but runs more simulations to produce more stable results

Usage

```
library(DHARMa)

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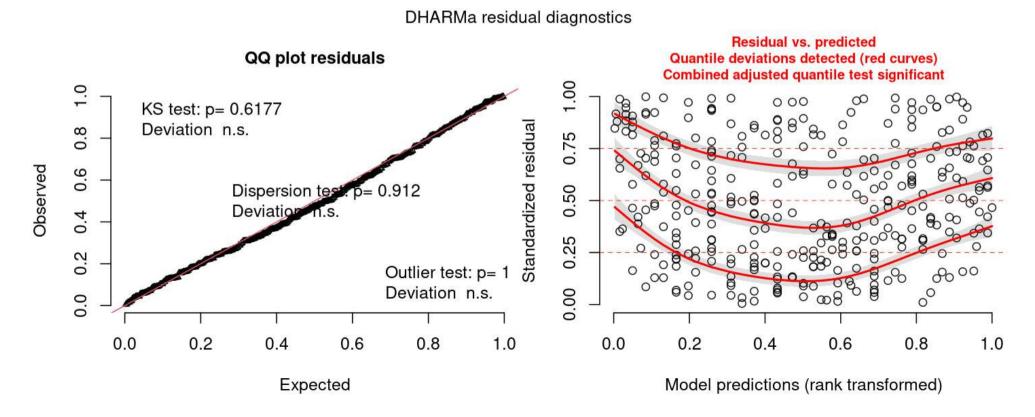
- simulateResiduals() function from
- Use **plot** = **TRUE** to produce diagnostic plots to see if simulated match expectation
- n = 1000 isn't strictly necessary but runs more simulations to produce more stable results

Applies to any model

- REMEMBER! Not assessing normality of residuals or heteroscedacity...
- Assessing whether data fits the model
- This includes assumptions, but also includes general fit, etc.
- So, we can use this to see if our model could be improved...

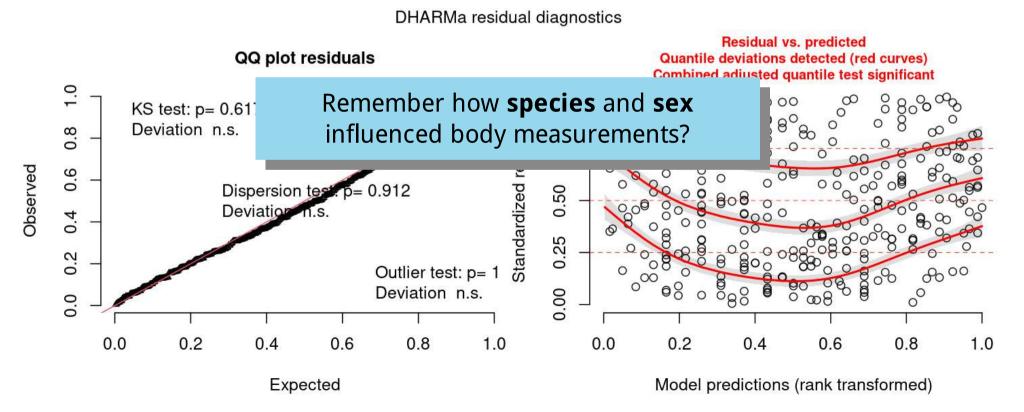
Check a previous model

```
m <- lm(body_mass_g ~ flipper_length_mm, data = penguins)
r <- simulateResiduals(m, n = 1000, plot = TRUE)</pre>
```



Check a previous model

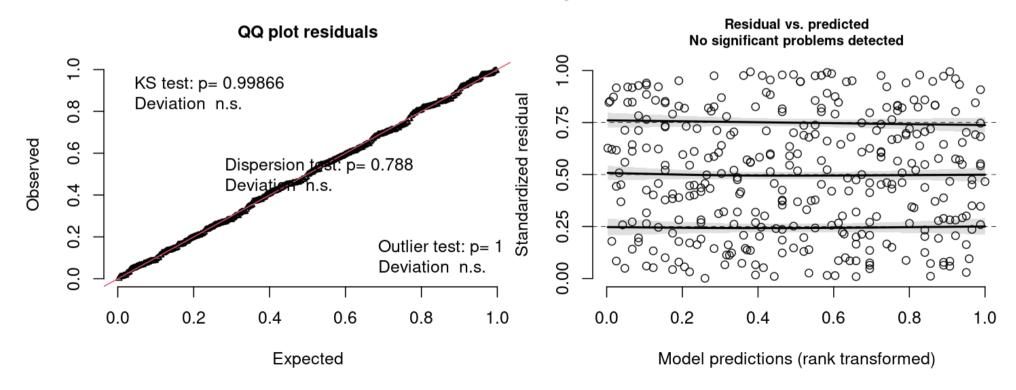
```
m <- lm(body_mass_g ~ flipper_length_mm, data = penguins)
r <- simulateResiduals(m, n = 1000, plot = TRUE)</pre>
```



Improve the fit...

```
m <- lm(body_mass_g ~ flipper_length_mm + species * sex, data = penguins)
r <- simulateResiduals(m, n = 1000, plot = TRUE)</pre>
```

DHARMa residual diagnostics



Comparing Models

Model Selection

How do I know which model to use?

- 1. Check your diagnostics
 - Generally speaking, pick the model which has good diagnostics

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All models have reasonably good diagnostics?

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All models have reasonably good diagnostics?

- 2. Check model fit (how good is model at explaining data?)
 - Analysis of Variance/Deviance anova()
 - Information Theoretic Approach (AIC) model.sel() (MuMIn package)
 - (covered in class Nov 17th)

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 - (covered in class Nov 17th)

Many other methods, functions, packages

Very common in R

- Sequential analysis of variance for lm()
- Analysis of deviance for glm()

```
p <- na.omit(penguins) # Must have exact same dataset for each model
m1 <- lm(body_mass_g ~ flipper_length_mm, data = p)
m2 <- lm(body_mass_g ~ flipper_length_mm + species + sex, data = p)
m3 <- lm(body_mass_g ~ flipper_length_mm + species * sex, data = p)
anova(m1, m2, m3)</pre>
```

```
anova(m1, m2, m3)
## Analysis of Variance Table
##
## Model 1: body_mass_g ~ flipper_length_mm
## Model 2: body_mass_g ~ flipper_length_mm + species + sex
## Model 3: body_mass_g ~ flipper_length_mm + species * sex
##
    Res.Df RSS Df Sum of Sq F Pr(>F)
## 1 331 51211963
## 2 328 28653568 3 22558395 91.082 < 2.2e-16 ***
## 3 326 26913579 2 1739989 10.538 3.675e-05 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

```
anova(m1, m2, m3)
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## Model 1: body_mass_g ~ flipper_length_mm
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Models being compared

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```

- Models being compared
- How the models compare

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## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
```

- Models being compared
- How the models compare
 - m2 has significantly (P < 0.05) lower Sums Squares than m1

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## Model 1: body_mass_g ~ flipper_length_mm
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## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

- Models being compared
- How the models compare
 - m2 has significantly (P < 0.05) lower Sums Squares than m1
 - m3 has significantly (P < 0.05) lower Sums Squares than m2

```
anova(m1, m2, m3)
## Analysis of Variance Table
##
## Model 1: body_mass_g ~ flipper_length_mm
## Model 2: body_mass_g ~ flipper_length_mm + species + sex
## Model 3: body_mass_g ~ flipper_length_mm + species * sex
                                        Pr(>F)
##
    Res.Df RSS Df Sum of Sq F
## 1 331 51211963
                                                                    Therefore
## 2 328 28653568 3 22558395 91.082 < 2.2e-16 ***
                                                                  m3 > m2 > m1
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## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

- Models being compared
- How the models compare
 - m2 has significantly (P < 0.05) lower Sums Squares than m1
 - m3 has significantly (P < 0.05) lower Sums Squares than m2

model.sel() - AIC model selection

- m3 is the best (lowest AICc, and much lower than the others)
- For more specifics on how to use/interpret this table, stay tuned for Nicky's lecture

model.sel() - AIC model selection

- m3 is the best (lowest AICc, and much lower than the others)
- For more specifics on how to use/interpret this table, stay tuned for Nicky's lecture

Always, remember that your 'best' model is only the best of what you've compared...

Chapter 13, "The R Book" by Michael J. Crawley

(Freely available online through University of Manitoba Library)

Simple Linear Models

General Linear Models

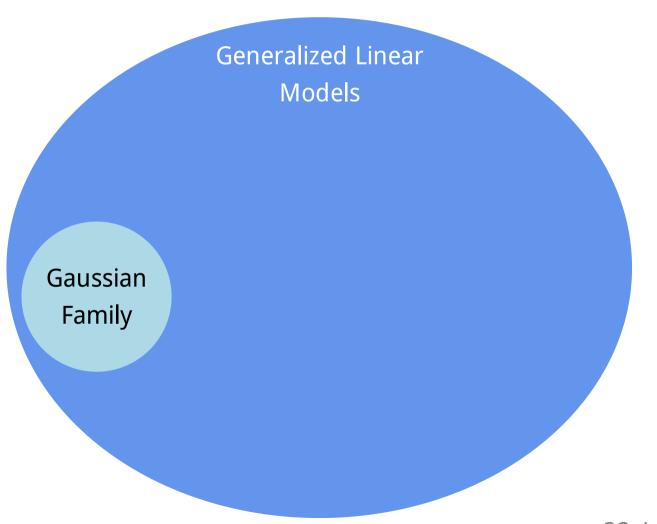
- Residuals are normally distributed
- Normally distributed also known as "Gaussian" distribution

General Linear Models

- Residuals are normally distributed
- Normally distributed also known as "Gaussian" distribution



• One type of Generalized linear model



• One type of Generalized linear model Generalized Linear • So what if your residuals are *not* normal? Models • ie. they don't follow a Gaussian distribution Gaussian Family

• One type of Generalized linear model

• So what if your residuals are *not* normal?

• ie. they don't follow a Gaussian distribution

• Try a different family!

Generalized Linear Models

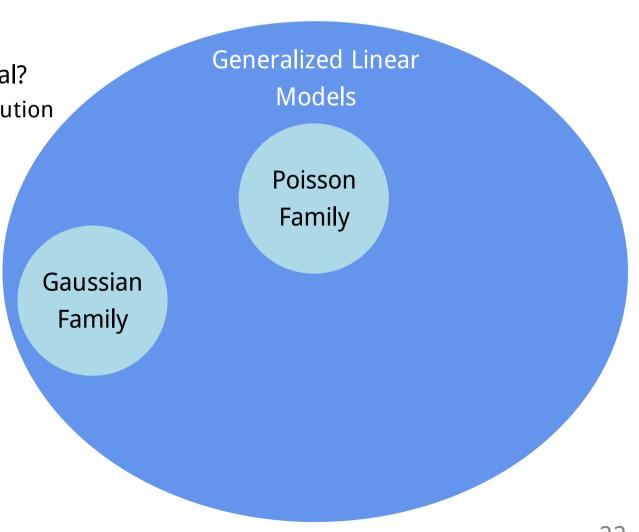
Gaussian Family

• One type of Generalized linear model

• So what if your residuals are *not* normal?

• ie. they don't follow a Gaussian distribution

• Try a different family!

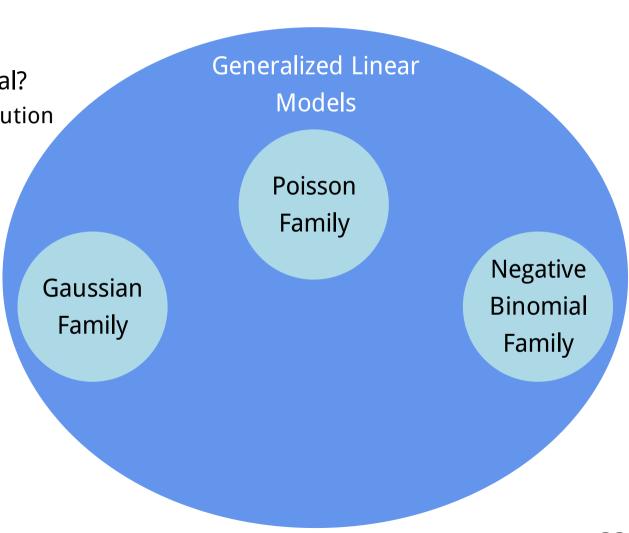


• One type of Generalized linear model

• So what if your residuals are *not* normal?

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• Try a different family!

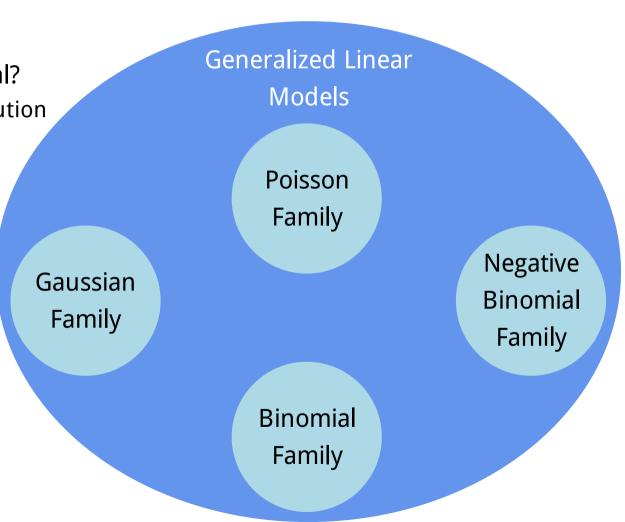


• One type of Generalized linear model

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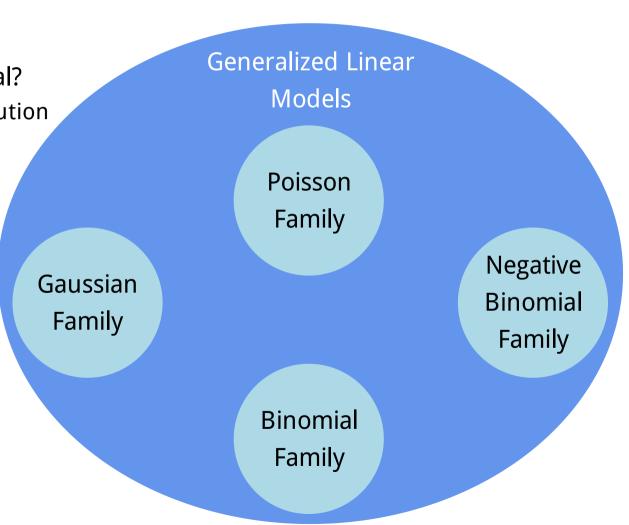
• One type of Generalized linear model

• So what if your residuals are *not* normal?

• ie. they don't follow a Gaussian distribution

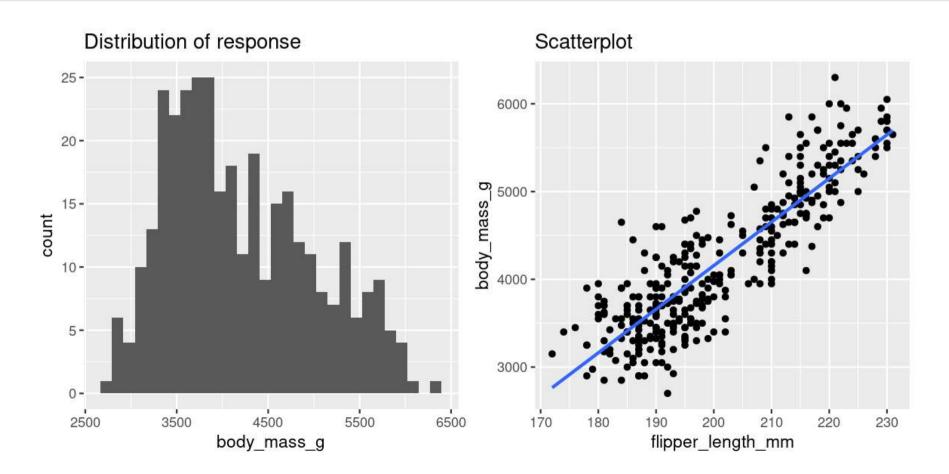
• Try a different family!

• Etc.



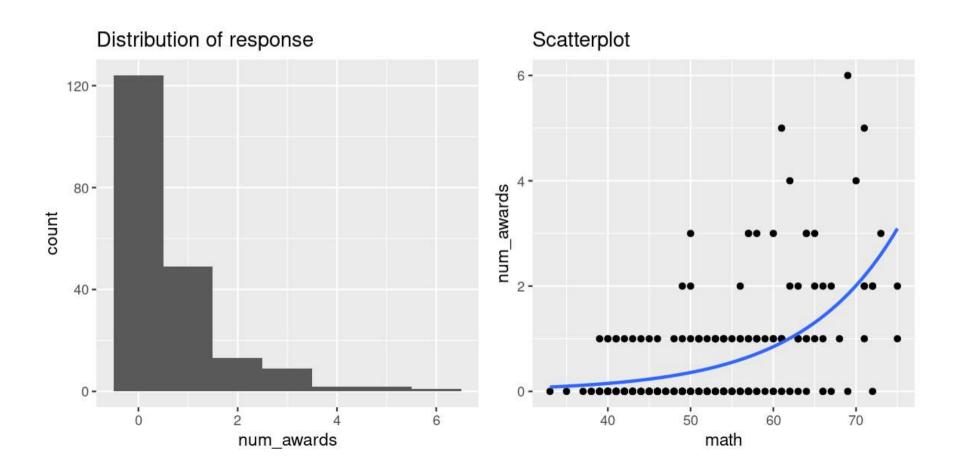
Gaussian Family (Normal data)

 $lm(y \sim x1 * x2, data = my_data)$



Poisson Family (Count data)

```
glm(counts ~ x1 * x2, family = "poisson", data = my_data)
```



Negative Binomial Family (Overdispersed Count data)

```
MASS::glm.nb(counts ~ x1 * x2, data = my_data)
```

- Do Poisson model first
- Check diagnostics, if necessary, you'll do a negative binomial model

Binomial Family (Binary data)

• TRUE/FALSE, 0/1, Logistic Regression

```
glm(y ~ x1 * x2, family = "binomial", data = my_data)
```

Binomial Family (Binary data)

• TRUE/FALSE, 0/1, Logistic Regression

```
glm(y ~ x1 * x2, family = "binomial", data = my_data)
```

Binomial Family (Proportion data)

- Two responses (binary outcomes), each in it's own column
 - (e.g., number of Yes, vs. No; Number of songs, vs. calls)

```
glm(cbind(yes, no) ~ x1 * x2, family = "binomial", data = my_data)
```

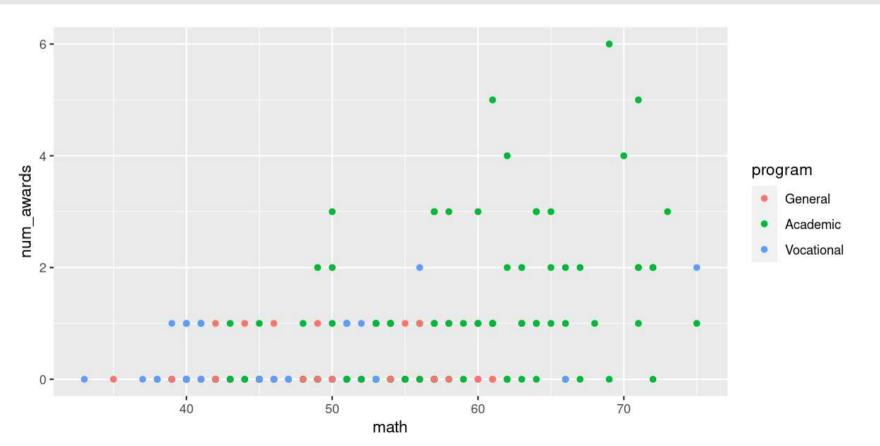
Examples

Get the data

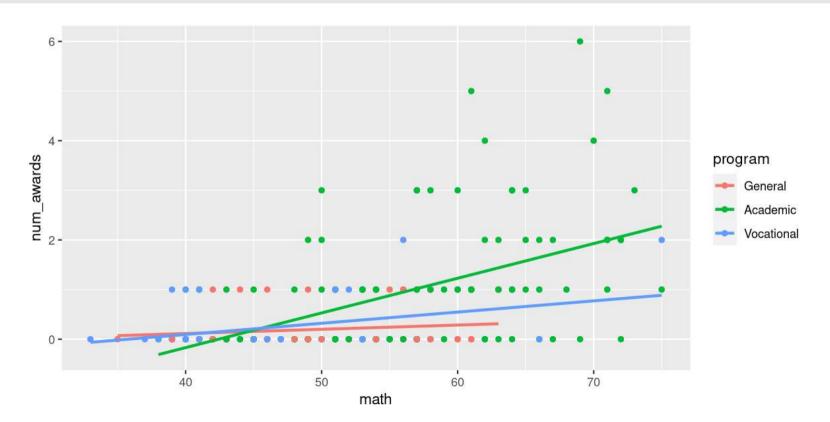
```
## # A tibble: 200 × 5
       id num awards prog math program
    <dbl> <dbl> <dbl> <dbl> <fct>
                         41 Vocational
                  1 41 General
  2 108
          0 3 44 Vocational
  3 15
                0 3 42 Vocational
  4 67
                0 3 40 Vocational
  5 153
                         42 General
     51
      164
                         46 Vocational
                0 3 40 Vocational
      133
                  3 33 Vocational
                   3 46 Vocational
  # ... with 190 more rows
```

How do marks in **math** as well as **program** of study influence the number of awards a student receives (**num_awards**)?

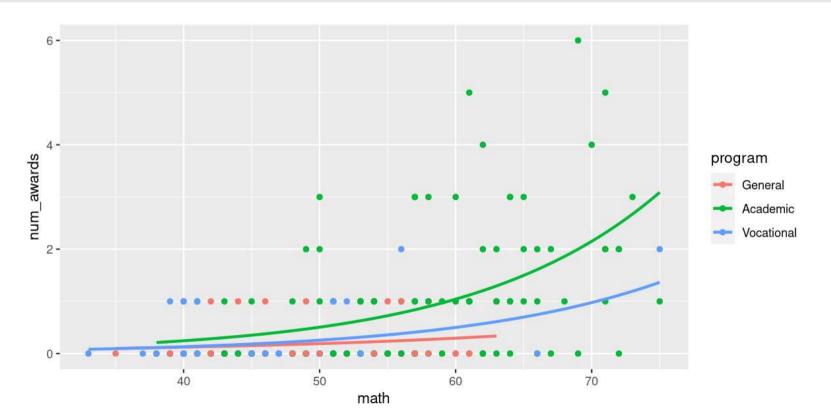
```
ggplot(data = p, aes(x = math, y = num_awards, colour = program)) +
  geom_point()
```



```
ggplot(data = p, aes(x = math, y = num_awards, colour = program)) +
  geom_point() +
  stat_smooth(method = "glm", se = FALSE)
```



```
ggplot(data = p, aes(x = math, y = num_awards, colour = program)) +
  geom_point() +
  stat_smooth(method = "glm", method.args = list(family = "poisson"), se = FALSE)
```



Run the model

```
m <- glm(num_awards ~ math + program, family = "poisson", data = p)
```

Diagnostics

##

```
summary(m)
## Call:
## glm(formula = num_awards ~ math + program, family = "poisson",
##
      data = p)
##
## Coefficients:
                   Estimate Std. Error z value Pr(>|z|)
##
  (Intercept)
                   -5.24712 0.65845 -7.969 1.60e-15 ***
## math
              0.07015 0.01060 6.619 3.63e-11 ***
## programAcademic 1.08386 0.35825 3.025 0.00248 **
  programVocational 0.36981
                            0.44107
                                        0.838 0.40179
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
   (Dispersion parameter for poisson family taken to be 1)
##
      Null deviance: 287.67 on 199 degrees of freedom
## Residual deviance: 189.45 on 196 degrees of freedom
## AIC: 373.5
```

Overdispersion

- Dispersion = Residual Deviance / DF
- Expected to be 1 for Poisson
- Overdispersion > 1; Underdispersion < 1

Diagnostics

```
summary(m)
## Call:
## glm(formula = num_awards ~ math + program, family = "poisson",
##
      data = p)
## Coefficients:
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##
```

Overdispersion

- Dispersion = Residual Deviance / DF
- Expected to be 1 for Poisson
- Overdispersion > 1; Underdispersion < 1

Traditional check:

Residual Deviance (189.45) vs. DF (196)

```
deviance(m) / df.residual(m)
```

```
## [1] 0.9665797
```

• Almost 1 (which it is good)

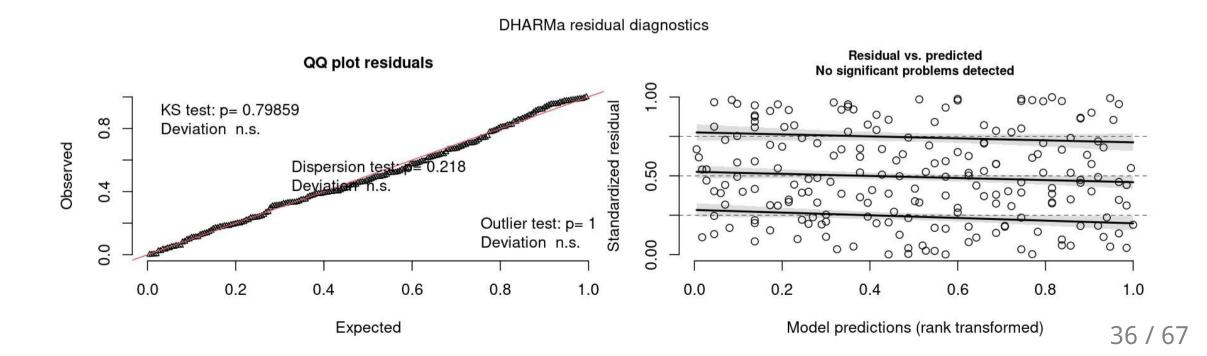
```
## [1] 0.6182274
```

Test shows no significant overdispersion
 (p = 0.62)

Diagnostics

- Residuals are complicated to assess in GLMs
- Therefore, use **DHARMa** package!

```
r <- simulateResiduals(m, n = 1000, plot = TRUE)
```

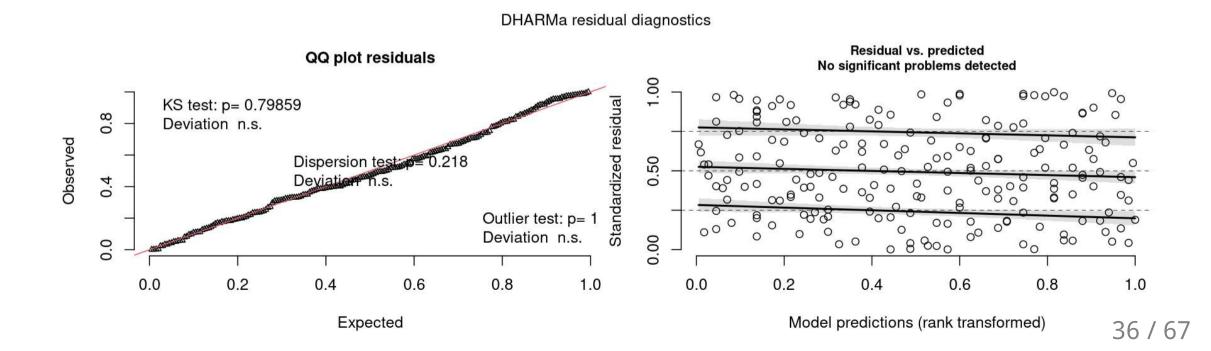


Diagnostics

- Residuals are complicated to assess in GLMs
- Therefore, use **DHARMa** package!

```
r <- simulateResiduals(m, n = 1000, plot = TRUE)
```

Also shows no overdispersion (See Dispersion test)



Count Data - Poisson Family - Model Diagnostics

Zero-inflation (More zeros than expected)

- Will often pop up as iffy residuals
- Overdispersion can lead to false positives
- Here not a problem (non-significant P-value)

```
##
## DHARMa zero-inflation test via comparison to expected zeros with simulation under H0 =
## fitted model
##
## data: simulationOutput
## ratioObsSim = 1.0131, p-value = 0.832
## alternative hypothesis: two.sided
```

Interpretation

```
summary(m)
## Call:
  glm(formula = num_awards ~ math + program, family = "poisson",
##
      data = p)
##
  Coefficients:
                    Estimate Std. Error z value Pr(>|z|)
##
  (Intercept)
                    -5.24712
                                0.65845 -7.969 1.60e-15 ***
## math
                    0.07015
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##
   (Dispersion parameter for poisson family taken to be 1)
##
      Null deviance: 287.67 on 199 degrees of freedom
  Residual deviance: 189.45 on 196 degrees of freedom
## AIC: 373.5
##
```

Effects

- Significantly more awards received with higher marks in math
 - i.e. Number of awards increases by 0.07
 log-counts per 1 unit increase in Math mark
- Significantly more awards received in Academic Program compared to General
 - i.e. Number of awards greater by 1.08 logcounts for Academic compared to General
- No difference in amount of awards received in Vocational vs. General Program

Interpretation

```
summary(m)
## Call:
  glm(formula = num_awards ~ math + program, family = "poisson",
##
      data = p)
##
## Coefficients:
##
                    Estimate Std. Error z value Pr(>|z|)
  (Intercept)
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  Residual deviance: 189.45 on 196 degrees of freedom
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##
```



OH WTF.

Interpretation

```
summary(m)
## Call:
  glm(formula = num_awards ~ math + program, family = "poisson",
##
      data = p)
##
## Coefficients:
                  Estimate Std. Error z value Pr(>|z|)
##
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                          0.65845 -7.969 1.60e-15 ***
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##
```

Interpreting Results

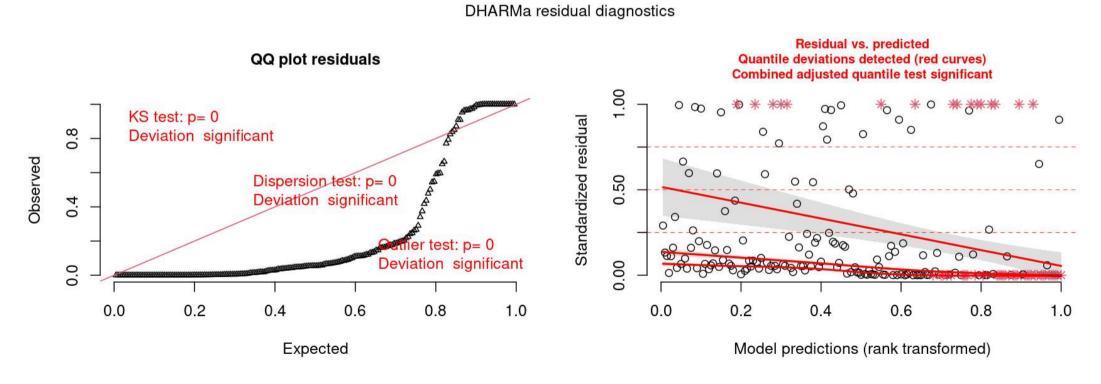
• Convert to ratios with $e^{\rm est}$ (exp())

```
## (Intercept) -5.2471244 0.00526263
## math 0.0701524 1.07267164
## programAcademic 1.0838591 2.95606545
## programVocational 0.3698092 1.44745846
```

- No. awards increases by 1.07 times per 1 unit increase in Math mark (7%)
- No. awards received by Academic is 2.96
 times greater than in General program

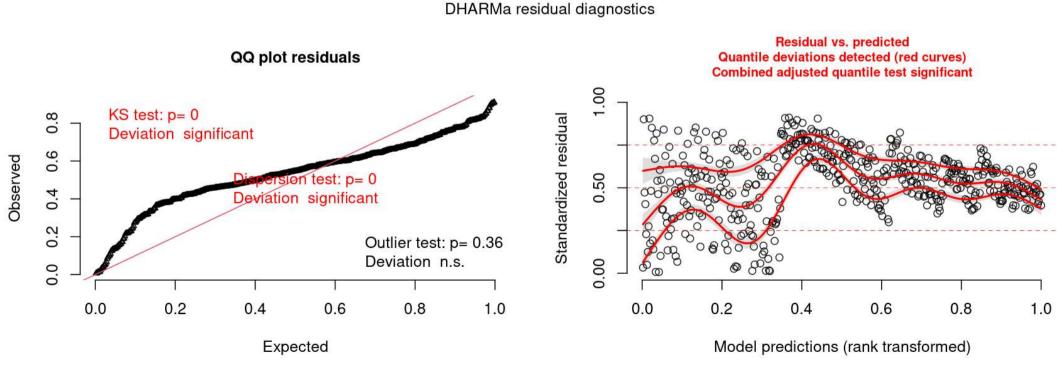
Overdispersion

- Overdispersion when data is spread out more than distribution would be (longer tails)
- Results in **highly** significant findings that are **not** valid!!
- Simulated residuals run from 0 to 1, but here more residuals around 0 and 1 (longer tails)



Underdispersion

- Underdispersion is less common
- When data is gathered towards the centre more than distribution would be (shorter tails)
- These simulated residuals run from 0 to 1
- Here, more residuals around 0.5 (shorter tails)



```
quine <- MASS::quine
```

Poisson GLM

```
m1 <- glm(Days ~ Sex, data = quine, family =
"poisson")
summary(m1)
## Coefficients:
              Estimate Std. Error z value Pr(>|z|)
## (Intercept) 2.72294
                          0.02865 95.030 < 2e-16
***
        0.16490 0.04080 4.041 5.31e-05
## SexM
***
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05
'.' 0.1 ' ' 1
##
## (Dispersion parameter for poisson family taken to
be 1)
##
      Null deviance: 2073.5 on 145 degrees of
freedom
```

```
m2 <- MASS::glm.nb(Days ~ Sex, data = quine)</pre>
summary(m2)
## Coefficients:
              Estimate Std. Error z value Pr(>|z|)
## (Intercept) 2.7229
                           0.1116 24.395
                                          <2e-16
***
## SexM
        0.1649 0.1656
                                    0.996
                                             0.319
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05
'.' 0.1 ' ' 1
##
## (Dispersion parameter for Negative Binomial(1.0741)
family taken to be 1)
##
      Null deviance: 169.50 on 145 degrees of
freedom
## Residual deviance: 168.51 on 144 degrees of
freedom
```

```
quine <- MASS::quine
```

Poisson GLM

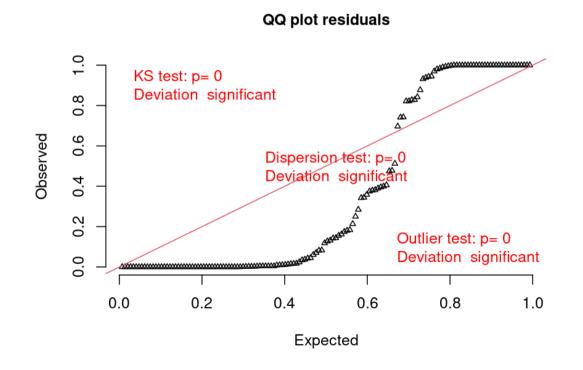
```
m1 <- glm(Days ~ Sex, data = quine, family =
"poisson")
summary(m1)
## Coefficients:
              Estimate Std. Error z value Pr(>|z|)
## (Intercept) 2.72294
                          0.02865 95.030 < 2e-16
***
## SexM
        0.16490 0.04080 4.041 5.31e-05
***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05
'.' 0.1 ' ' 1
##
## (Dispersion parameter for poisson family taken to
be 1)
##
      Null deviance: 2073.5 on 145 degrees of
freedom
```

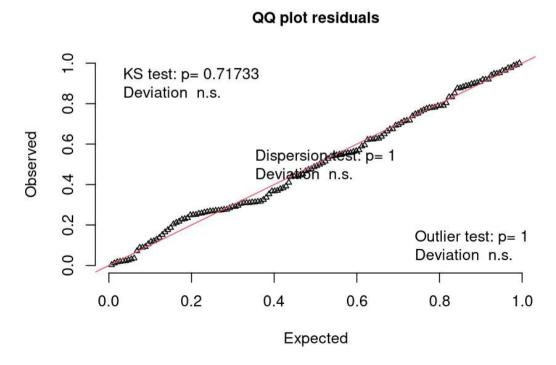
```
m2 <- MASS::glm.nb(Days ~ Sex, data = quine)</pre>
summary(m2)
## Coefficients:
              Estimate Std. Error z value Pr(>|z|)
## (Intercept) 2.7229
                           0.1116 24.395
                                            <2e-16
***
## SexM
                0.1649
                           0.1656
                                    0.996
                                             0.319
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05
'.' 0.1 ' ' 1
##
## (Dispersion parameter for Negative Binomial(1.0741)
family taken to be 1)
##
      Null deviance: 169.50 on 145 degrees of
freedom
## Residual deviance: 168.51 on 144 degrees of
freedom
```

Poisson GLM

```
r <- simulateResiduals(m1)
plotQQunif(r) # Just the first Uniformity Plot</pre>
```

```
r <- simulateResiduals(m2)
plotQQunif(r) # Just the first Uniformity Plot</pre>
```

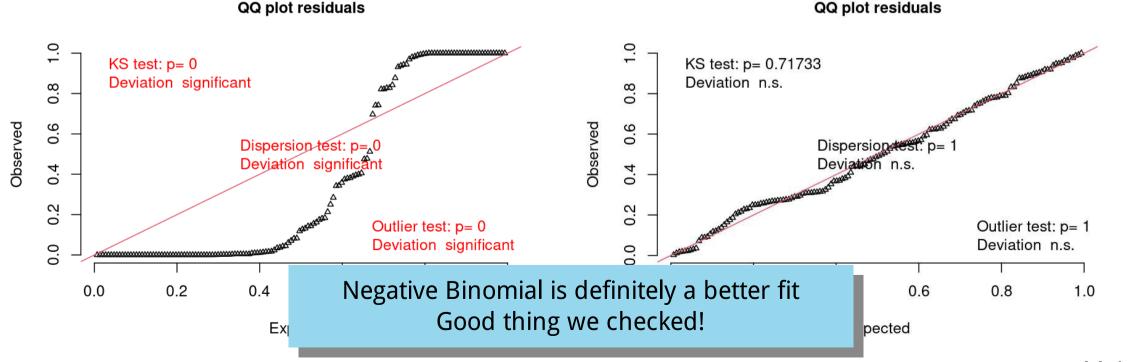




Poisson GLM

```
r <- simulateResiduals(m1)
plotQQunif(r) # Just the first Uniformity Plot</pre>
```

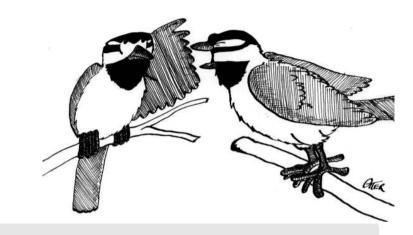
```
r <- simulateResiduals(m2)
plotQQunif(r) # Just the first Uniformity Plot</pre>
```



Binary Data (0/1) - Binomial Family (logistic regression)

Get the data

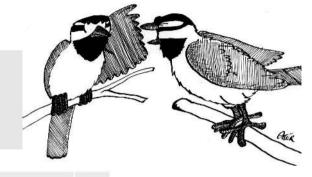
- Mountain chickadees atypical songs by urbanization
- Negative **urbanization** more rural
- Positive urbanization more urban
- atypical_c atypical singer (1) or 'normal' singer (0)

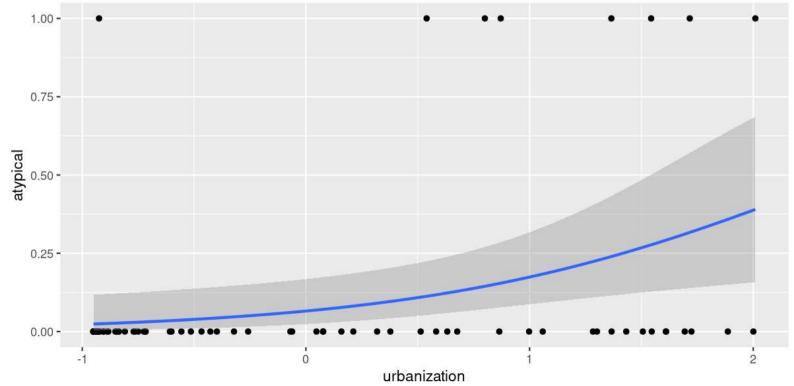


```
atypical <- read_csv("https://steffilazerte.ca/NRI_7350/data/atypical.csv")
atypical</pre>
```

Binary Data (0/1) - Binomial Family (logistic regression)

```
ggplot(data = atypical, aes(x = urbanization, y = atypical)) +
  geom_point() +
  stat_smooth(method = "glm", method.args = list(family = "binomial"))
```

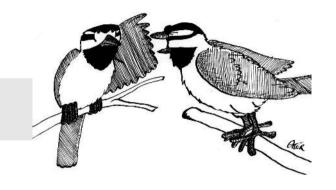




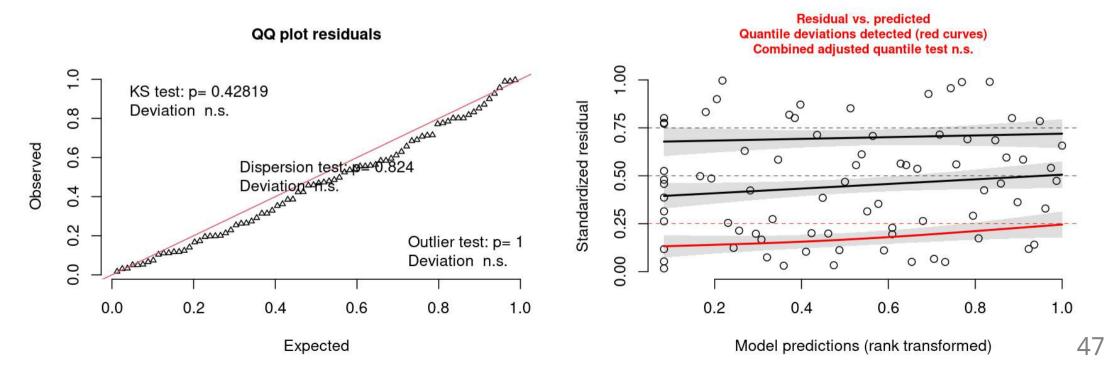
Binary Data (0/1) - Binomial Family (logistic regresion)

Run model and check diagnostics

```
m <- glm(atypical ~ urbanization, family = "binomial", data = atypical)
r <- simulateResiduals(m, plot = TRUE)</pre>
```



DHARMa residual diagnostics



Binary Data (0/1) - Binomial Family (logistic regression)

```
summary(m)
```

```
##
## Call:
## glm(formula = atypical ~ urbanization, family = "binomial",
data = atypical)
##
  Deviance Residuals:
               10 Median 30
      Min
                                        Max
  -0.9907 -0.4460 -0.2500 -0.2210 2.7201
##
  Coefficients:
              Estimate Std. Error z value Pr(>|z|)
  (Intercept) -2.6572 0.5380 -4.939 7.85e-07 ***
## urbanization 1.1000
                       0.4209 2.613 0.00897 **
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
  (Dispersion parameter for binomial family taken to be 1)
##
      Null deviance: 51.586 on 77 degrees of freedom
  Residual deviance: 43.203 on 76 degrees of freedom
## AIC: 47.203
```

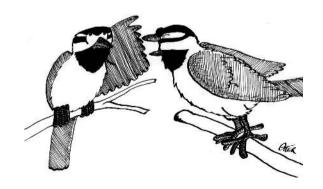
Interpreting Results

```
exp(coef(m))

## (Intercept) urbanization

## 0.07014254 3.00406665
```

E.g., The odds of being an atypical singer increase by a factor of 3 (x3 times more likely) for every unit increase in Habit Urbanization.



Binary Outcomes - Binomial Family

Proportion with binary outcomes (e.g., 10 yes, 5 no)

Get the data

```
## # A tibble: 12 × 4
##
    Gender Dept Admitted Rejected
##
   <fct> <fct>
                 <dbl> <dbl>
  1 Male A
                  512
                          313
  2 Female A
            89
                      19
  3 Male
            353
                          207
            17
  4 Female B
 5 Male
            120
                         205
  6 Female C
                  202
                          391
  7 Male
                  138
                          279
```

Binary Outcomes - Binomial Family

Diagnostics

```
## Call:
## glm(formula = cbind(Admitted, Rejected) ~ Gender, family =
"binomial",
     data = admissions)
##
## Coefficients:
       Estimate Std. Error z value Pr(>|z|)
## (Intercept) -0.22013 0.03879 -5.675 1.38e-08 ***
## GenderFemale -0.61035 0.06389 -9.553 < 2e-16 ***
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
  (Dispersion parameter for binomial family taken to be 1)
##
      Null deviance: 877.06 on 11 degrees of freedom
## Residual deviance: 783.61 on 10 degrees of freedom
## AIC: 856.55
```

Overdispersion

Traditional check:

• Look at resid deviance (783.61) vs. df (10)

```
deviance(m) / df.residual(m)
## [1] 78.3607
```

• Very large (definitely not close to 1)

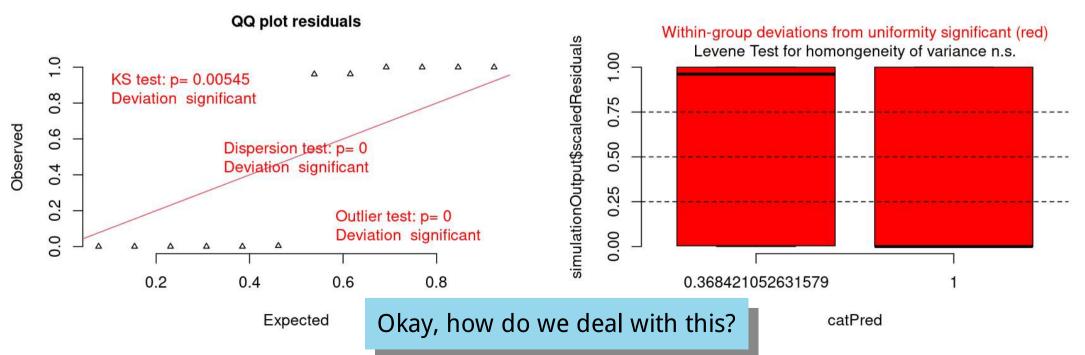
```
## [1] 6.892992e-162
```

• Test shows significant overdispersion

Binary Outcomes - Binomial Family

Check with DHARMa

```
plotQunif(m)
plotResiduals(m, asFactor = TRUE) # to ensure Gender is treated as category
```



Binary Outcomes - Quasi-binomial Family for overdispersion

```
m quasi <- glm(cbind(Admitted, Rejected) ~ Gender, family = "quasibinomial", data = admissions)
summary(m quasi)
```

```
##
## Call:
## glm(formula = cbind(Admitted, Rejected) ~ Gender, family = "quasibinomial",
      data = admissions)
##
##
## Deviance Residuals:
       Min 1Q Median 3Q
##
                                           Max
## -16.7915 -4.7613 -0.4365 5.1025 11.2022
##
## Coefficients:
##
       Estimate Std. Error t value Pr(>|t|)
  (Intercept) -0.2201 0.3281 -0.671
                                           0.517
## GenderFemale -0.6104 0.5404 -1.129
                                          0.285
##
  (Dispersion parameter for quasibinomial family taken to be 71.52958)
##
      Null deviance: 877.06 on 11 degrees of freedom
## Residual deviance: 783.61 on 10 degrees of freedom
## AIC: NA
```

Binary Outcomes - Quasi-binomial Family for overdispersion

```
m quasi <- glm(cbind(Admitted, Rejected) ~ Gender, family = "quasibinomial", data = admissions)
summary(m_quasi)
```

```
##
## Call:
## glm(formula = cbind(Admitted, Rejected) ~ Gender, family = "quasibinomial",
      data = admissions)
##
##
  Deviance Residuals:
                                                                    Much more appropriate
                 10 Median 30
##
       Min
                                             Max
## -16.7915 -4.7613 -0.4365 5.1025 11.2022
                                                               But 'quasi' families don't always work with
##
                                                                     other functions/packages,
  Coefficients:
                                                                           like DHARMa!
##
         Estimate Std. Error t value Pr(>|t|)
  (Intercept) -0.2201 0.3281 -0.671
                                            0.517
## GenderFemale -0.6104 0.5404 -1.129
                                            0.285
##
  (Dispersion parameter for quasibinomial family taken to be 71.52958)
##
      Null deviance: 877.06 on 11 degrees of freedom
## Residual deviance: 783.61 on 10 degrees of freedom
## AIC: NA
```

Binary Outcomes - Mixed models for overdispersion

• Observation-level random effects (i.e assign each observation an ID number)

```
library(lme4)
admissions <- mutate(admissions, ID = 1:n())
m_glmm <- glmer(cbind(Admitted, Rejected) ~ Gender + (1|ID), family = "binomial", data = admissions)</pre>
```

Binary Outcomes - Overdispersion

Either way, fixing overdispersion remove the 'significance'

Original

```
coef(summary(m))

## Estimate Std. Error z value Pr(>|z|)
## (Intercept) -0.2201340 0.03878810 -5.675297 1.384479e-08
## GenderFemale -0.6103524 0.06389305 -9.552720 1.263352e-21
```

Quasi fix

coef(summary(m_quasi)) ## Estimate Std. Error t value Pr(>|t|) ## (Intercept) -0.2201340 0.3280510 -0.6710359 0.5173966 ## GenderFemale -0.6103524 0.5403765 -1.1294947 0.2850545

GLMM fix

coef(summary(m glmm))

```
## Estimate Std. Error z value
Pr(>|z|)
## (Intercept) -0.6508845 0.4932596 -1.319558
0.1869827
## GenderFemale 0.1747094 0.7016048 0.249014
0.8033499
```

Your Turn!

We have the **crabs** dataset

```
crabs <-
read_csv("https://steffilazerte.ca/NRI_7350/data/crabs.csv")</pre>
```

Background

- Horseshoe crabs form pairs for spawning (mating)
- But extra, unattached males crowd around and try to get involved (Satellite males)

Your Job

You're interested in the effect of female size (width) on the number of male satellites

- Look at your data (make a plot)
- Run a **glm()** for count data
- Check your diagnostics. Do you have a problem? Check for overdispersion and zero-inflation
- Apply an overdispersion fix
- Check your diagnostics. Do you have a problem? Check for zero-inflation

- glmmTMB() function from glmmTMB package
- Allows modeling zero-inflation (ziformula says zeros are a function of the variable weight)

```
crabs <- read_csv("https://steffilazerte.ca/NRI_7350/data/crabs.csv")
library(glmmTMB)
m <- glmmTMB(satellites ~ weight, ziformula = ~ weight , family = "nbinom2", data = crabs)
summary(m)</pre>
```

```
## Dispersion parameter for nbinom2 family (): 4.96
##

## Conditional model:
## Estimate Std. Error z value Pr(>|z|)
## (Intercept) 0.8979 0.3051 2.943 0.00325 **
## weight 0.2171 0.1118 1.942 0.05217 .
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Zero-inflation model:
## Estimate Std. Error z value Pr(>|z|)
## (Intercept) 3.7546 0.9837 3.817 0.000135 ***
## weight -1.9123 0.4320 -4.426 9.59e-06 ***
## ---
```

- glmmTMB() function from glmmTMB package
- Allows modeling zero-inflation (ziformula says zeros are a function of the variable weight)

```
crabs <- read_csv("https://steffilazerte.ca/NRI_7350/data/crabs.csv")
library(glmmTMB)
m <- glmmTMB(satellites ~ weight, ziformula = ~ weight , family = "nbinom2", data = crabs)
summary(m)
## Dispersion parameter for nbinom2 family (): 4.96</pre>
```

```
## Conditional model:

## Conditional model:

## Estimate Std. Error z value Pr(>|z|)

## (Intercept) 0.8979 0.3051 2.943 0.00325 **

## weight 0.2171 0.1118 1.942 0.05217 .

## ---

## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.'

##

## Zero-inflation model:

## Estimate Std. Error z value Pr(>|z|)

## (Intercept) 3.7546 0.9837 3.817 0.000135 ***

## weight -1.9123 0.4320 -4.426 9.59e-06 ***
```

"Regular" effects Heavier females have more satellite males (P = 0.052)

- glmmTMB() function from glmmTMB package
- Allows modeling zero-inflation (ziformula says zeros are a function of the variable weight)

```
crabs <- read_csv("https://steffilazerte.ca/NRI_7350/data/crabs.csv")
library(glmmTMB)
m <- glmmTMB(satellites ~ weight, ziformula = ~ weight , family = "nbinom2", data = crabs)
summary(m)</pre>
```

```
## Dispersion parameter for nbinom2 family (): 4.96
##

## Conditional model:
## Estimate Std. Error z value Pr(>|z|)
## (Intercept) 0.8979 0.3051 2.943 0.00325 **
## weight 0.2171 0.1118 1.942 0.05217.
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.'
##

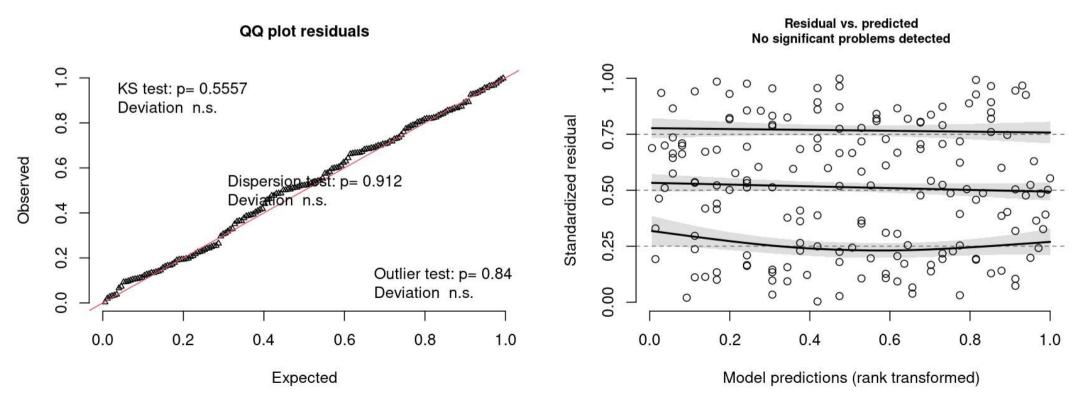
## Zero-inflation model:
## Estimate Std. Error z value Pr(>|z|)
## (Intercept) 3.7546 0.9837 3.817 0.000135 ***
## weight -1.9123 0.4320 -4.426 9.59e-06 ***
```

"Zero-inflation" effects more zeros counts as weight decreases What we expected!

r <- simulateResiduals(m, plot = TRUE)</pre>



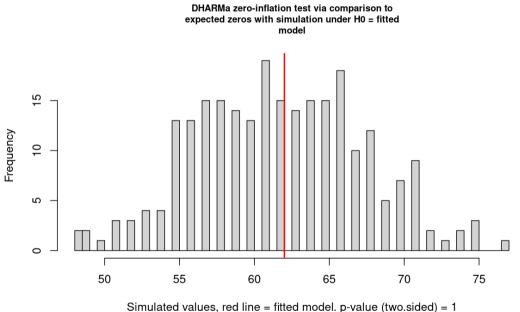




testZeroInflation(m)

```
##
##
       DHARMa zero-inflation test via comparison to
expected zeros with simulation under H0 =
       fitted model
##
##
  data: simulationOutput
  ratioObsSim = 1.0016, p-value = 1
## alternative hypothesis: two.sided
```





Packages and References for Other Advanced Models

Packages and References

(Generalized) Linear Mixed Models (LMM, GLMM)

- Also called generalized linear mixed effects models (GLME, LME)
- lme4 More advanced, crossed-random factors, Generalized (glmer()) and Gaussian (lmer())
- nlme Older but can specify auto-correlation structures, only Gaussian (lme())
- glmmTMB Zero-inflated models and other distribtions

References

- Ben Bolker's GLMM FAQ
- Chapter 19, "The R Book" by Michael J. Crawley

(Freely available online through University of Manitoba Library)

Mixed Effects Models and Extensions in Ecology with R by Alain Zuur

(Freely available online through University of Manitoba Library)

• <u>Generalized linear mixed models: a practical guide for ecology and evolution</u>, 2009, Trends in ecology and evolution

Packages and References

General Additive Models (GAM)

- mgcv package (gam(), gamm())
- gamm4 package (gamm4())

References

• Chapter 19, "The R Book" by Michael J. Crawley

(Freely available online through University of Manitoba Library)

• "Generalized Additive Models: An Introduction with R" by Simon N. Wood

(Hard-copy available from University of Manitoba Library)

Packages and References

Generalized Estimating Equations (GEE)

- gee package (gee())
- geepack package (geeglm())

References

- The R package geepack for Generalized Estimating equations, Journal of Statistical Software, 2005
- geepack Manual

Non-parametric Statistics

Non-parametric Statistics

Wilcoxon Rank Sum (Mann-Whitney) Test

```
air <- filter(airquality, Month %in% c(5, 8))
```

Is there a difference in air quality between May (5th month) and August (8th month)?

```
wilcox.test(Ozone ~ Month, data = air, exact = FALSE)

##

## Wilcoxon rank sum test with continuity correction

##

## data: Ozone by Month

## W = 127.5, p-value = 0.0001208

## alternative hypothesis: true location shift is not equal to 0
```

Yes!

Non-parametric Statistics

Kruskal-Wallis Rank Sum Test

Is there a difference in air quality among months?

```
kruskal.test(Ozone ~ Month, data = airquality)

##

##

Kruskal-Wallis rank sum test

##

## data: Ozone by Month

## Kruskal-Wallis chi-squared = 29.267, df = 4, p-value = 6.901e-06
```

Yes, there is at least one month that is different from the rest.