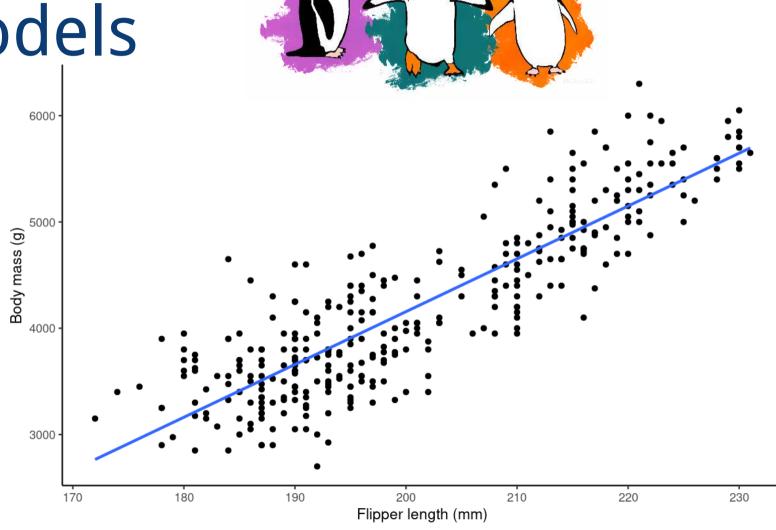
Regressions, ANOVAs, and Model assumptions



ADELIE

GENTOO!

CHINSTRAPI

### **Getting started (again)**

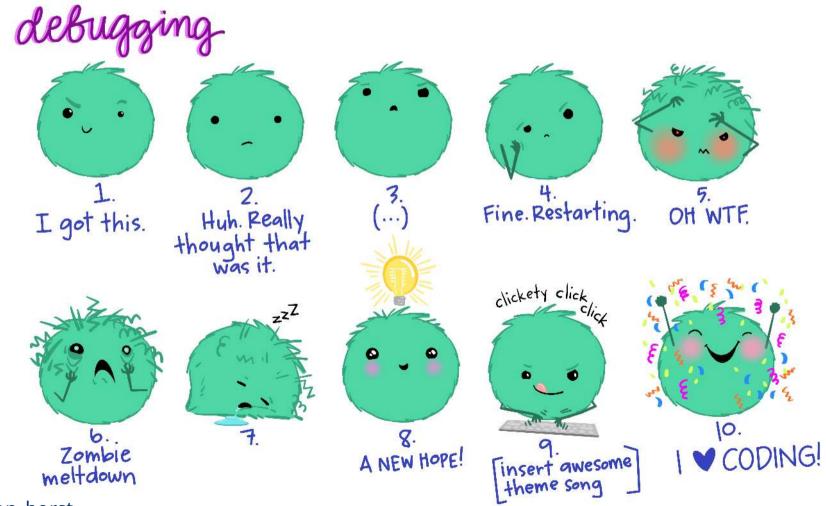
Open RStudio
Open your NRI project
Open a **new** script for today:

File > New File > R Script

Make sure to load packages at the top:

library(tidyverse)
library(palmerpenguins)

### How Are we Doing?



### **Running models in R**

```
lm(y \sim x1 + x2, data = data)
```

- y is the response variable (dependent)
- x are the explanatory variables (independent, predictor)

Here we're assuming a **continuous y** 

#### **Running models in R**

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lm(y \sim x1 + x2, data = data)
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Here we're assuming a **continuous y** 

#### Different types of models

- If we only have one x which is continuous, this is a simple linear regression
- If both x are continuous, this is a multiple linear regression
- If both x are categorical, this is an ANOVA
- If x1 is continuous and x2 is categorical, this is an ANCOVA

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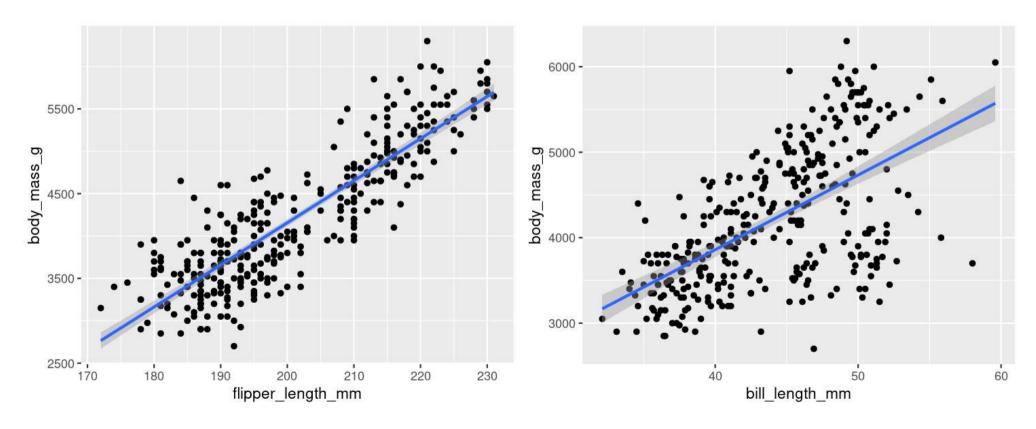
#### Different types of models

- If we only have one x which is continuous, this is a simple linear regression
- If both x are continuous, this is a multiple linear regression
- If both x are categorical, this is an ANOVA
- If x1 is continuous and x2 is categorical, this is an ANCOVA

R will figure it out for you

### **Real example**

- Is penguin body mass a function of skeletal size?
- Can it be predicted by flipper length and bill length?



#### **Real example**

```
lm(body_mass_g ~ flipper_length_mm + bill_length_mm, data = penguins)

##
## Call:
## lm(formula = body_mass_g ~ flipper_length_mm + bill_length_mm,
## data = penguins)
##
## Coefficients:
## (Intercept) flipper_length_mm bill_length_mm
## -5736.897 48.145 6.047
```

#### **Real example**

```
lm(body_mass_g ~ flipper_length_mm + bill_length_mm, data = penguins)

##
## Call:
## lm(formula = body_mass_g ~ flipper_length_mm + bill_length_mm,
## data = penguins)
##
## Coefficients:
## (Intercept) flipper_length_mm bill_length_mm
## -5736.897 48.145 6.047
```

```
Hmm, not a lot of detail...
Only Intercept and Slopes
(flipper_length_mm and bill_length_mm)
```

### Assign model to m (or any other name you want to give it)

```
m <- lm(body_mass_g ~ flipper_length_mm + bill_length_mm, data = penguins)
m is a model object

class(m)
## [1] "lm"</pre>
```

This contains all the information about the model

#### Use **summary()** to show summary table:

```
summary(m)
```

```
##
## Call:
## lm(formula = body_mass_g ~ flipper_length_mm + bill_length_mm,
## data = penguins)
##
```

#### Your turn!

Create a model with your response variable by two of your *continuous* predictors.

#### Look at the output of **summary()**

```
## bill_length_mm 6.047 5.180 1.168 0.244

## ---

## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1

##

## Residual standard error: 394.1 on 339 degrees of freedom

## (2 observations deleted due to missingness)

## Multiple R-squared: 0.76, Adjusted R-squared: 0.7585

## F-statistic: 536.6 on 2 and 339 DF, p-value: < 2.2e-16
```

\*\*\*

Use **summary()** to show summary table:

```
##
summary(m)
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                           ##
                                              Your turn!
                       Create a model with your response variable by two of
                                     your continuous predictors.
                                  Look at the output of summary()
                                                                                    ***
                           ## bill_length_mm
                                                   6.047
                                                             5.180
                                                                     1.168
                                                                              0.244
                                                                              .' 0.1 ' ' 1
                                                 Wait!
                                Shouldn't interpret until we know the
                                                                              Freedom
                                             model is solid
                                                                                0.7585
                           ## F-statistic: 536.6 on 2 and 339 DF,
                                                                 p-value: < 2.2e-16
```

### Model Diagnostics

#### **Model Assumptions**

- Normality (of residuals)
- Constant Variance (no heteroscedasticity)

#### Other cautions

- Influential observations (Cook's D)
- Multiple collinearity (with more than one x or explanatory variables)

## **Model Diagnostics**

First let's get our relevant variables into a diagnostic data frame:

- residuals (regular and standardized)
- fitted values
- cooks distance
- obs number

### Model Diagnostics

First let's get our relevant variables into a diagnostic data frame:

- residuals (regular and standardized)
- fitted values
- cooks distance
- obs number

```
head(d)

## residuals std_residuals fitted cooks obs
## 1 536.220898 1.368529806 3213.779 5.539153e-03 1
## 2 343.077607 0.873050231 3456.922 1.609402e-03 2
## 3 -645.064115 -1.644516798 3895.064 3.797384e-03 3
## 5 -327.003441 -0.833002736 3777.003 1.992863e-03 4
## 6 1.707668 0.004338503 3648.292 3.338060e-08 5
## 7 412.430396 1.051400111 3212.570 3.272886e-03 6
```

## Side Note: tidyverse functions

• From **dplyr** package (part of **tidyverse**)

```
d <- mutate(d, obs = 1:n())
```

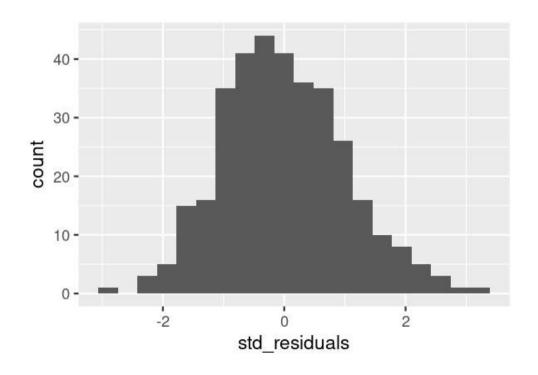
#### mutate()

- tidyverse functions always start with the data, followed by other arguments
- mutate() adds new columns to your data
- Also note: 1:5 is the same as c(1,2,3,4,5)

### Normality

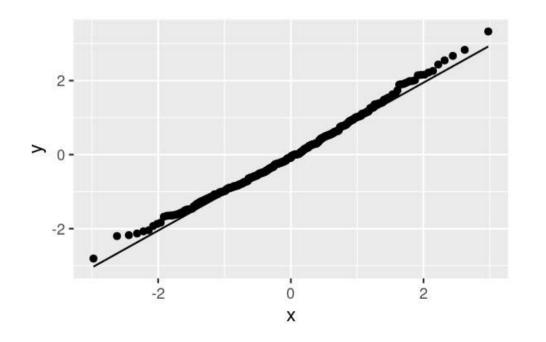
#### **Histogram of residuals**

```
ggplot(data = d, aes(x = std_residuals)) +
  geom_histogram(bins = 20)
```



### **QQ Normality plot of residuals**

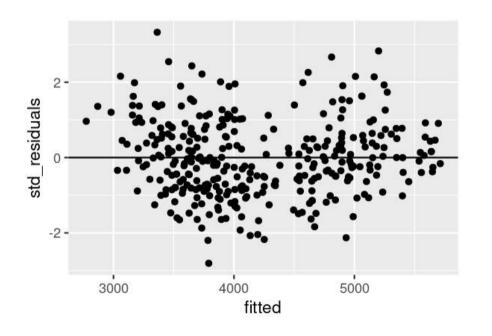
```
ggplot(data = d, aes(sample = std_residuals)) +
  stat_qq() +
  stat_qq_line()
```



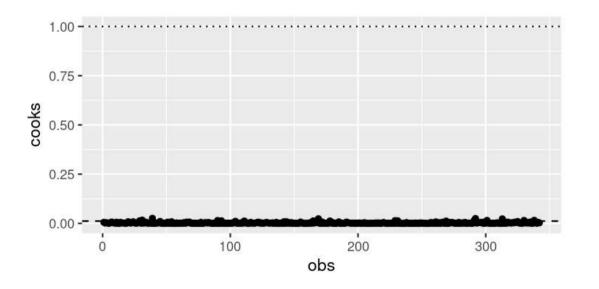
### Variance and Influence

#### **Check heteroscedasticity**

```
ggplot(d, aes(x = fitted, y = std_residuals)) +
  geom_point() +
  geom_hline(yintercept = 0)
```



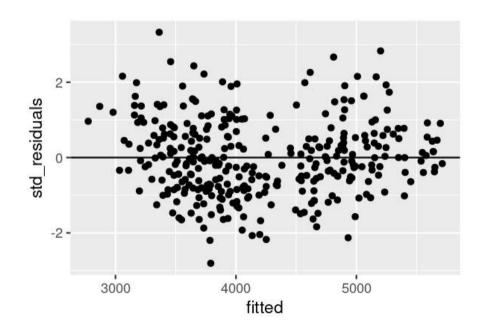
#### Cook's D



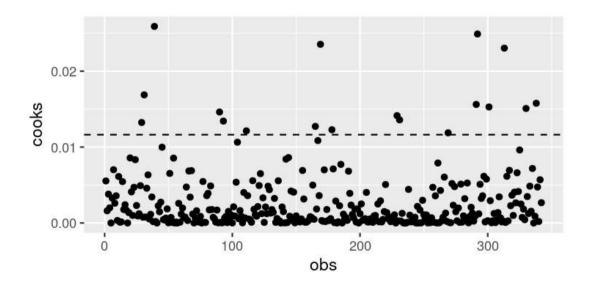
### Variance and Influence

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ggplot(d, aes(x = fitted, y = std_residuals)) +
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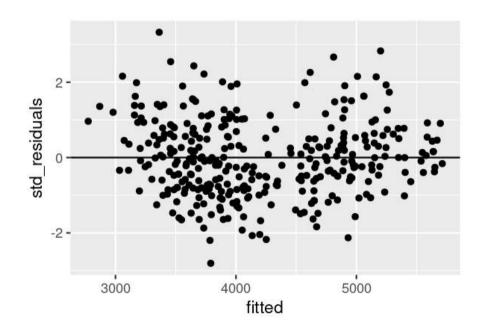
#### Cook's D



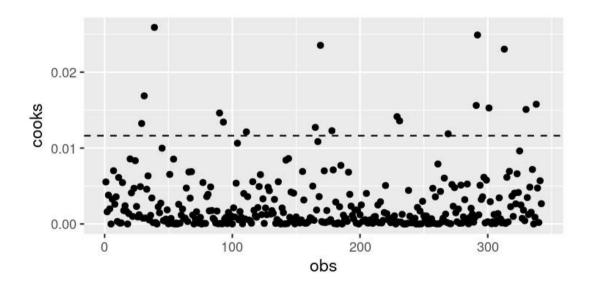
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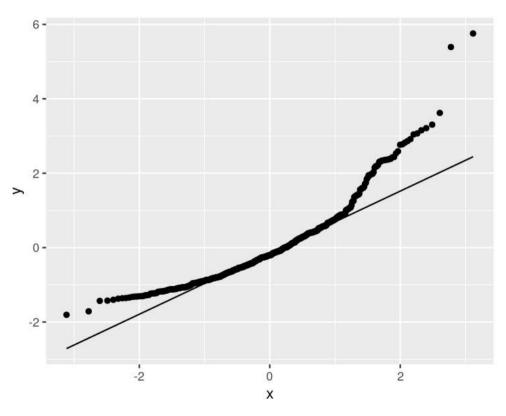


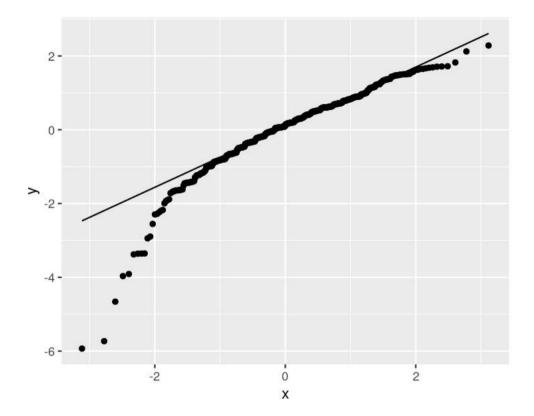
#### Cook's D



# What is a 'Good' Normality Plot?

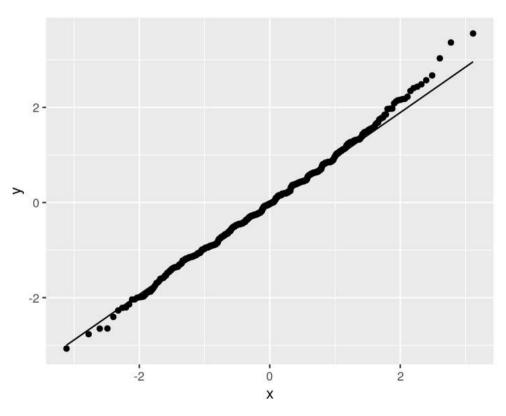
### **Problematic**

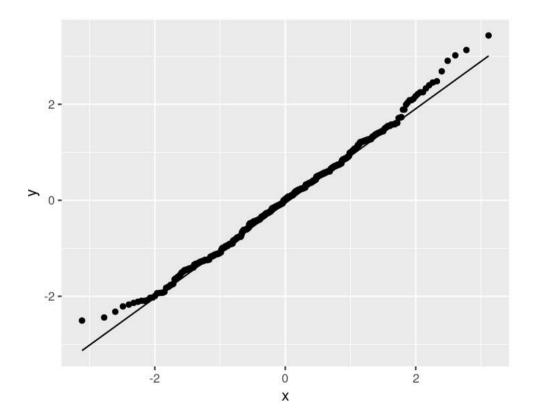




# What is a 'Good' Normality Plot?

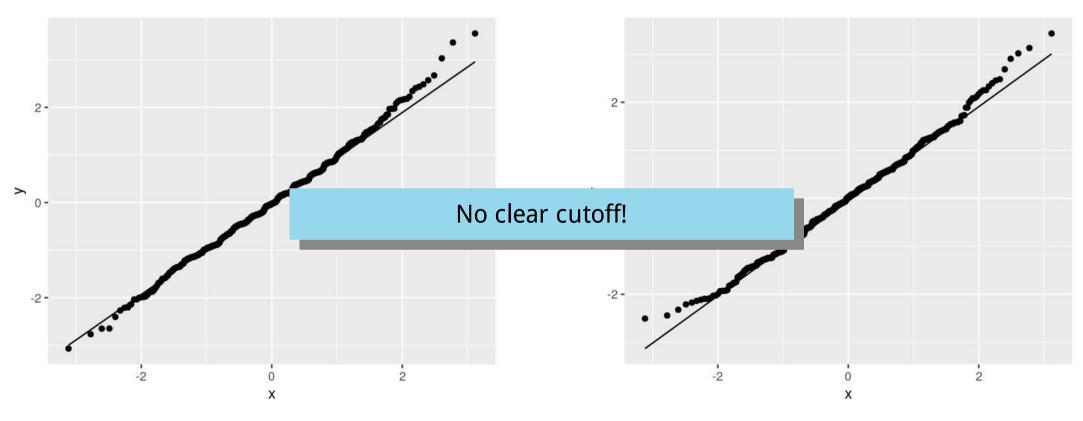
### Good





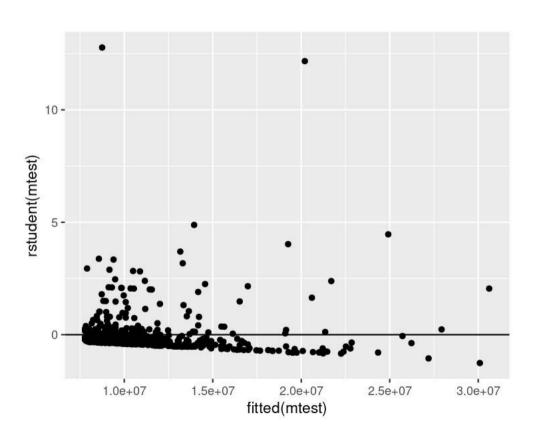
# What is a 'Good' Normality Plot?

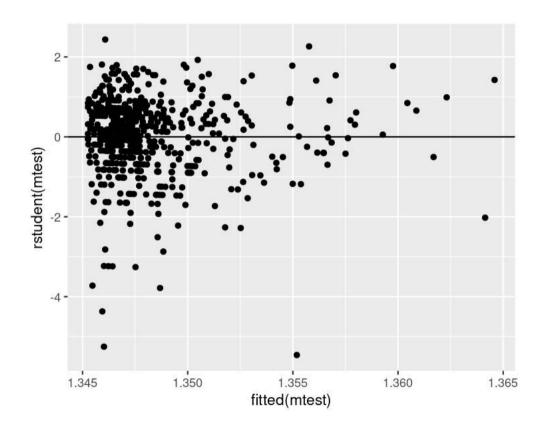
### Good



## What is a 'Good' Heteroscedasticity Plot?

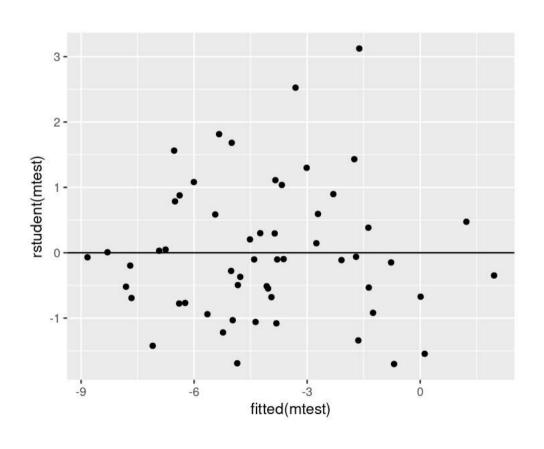
### **Problematic**

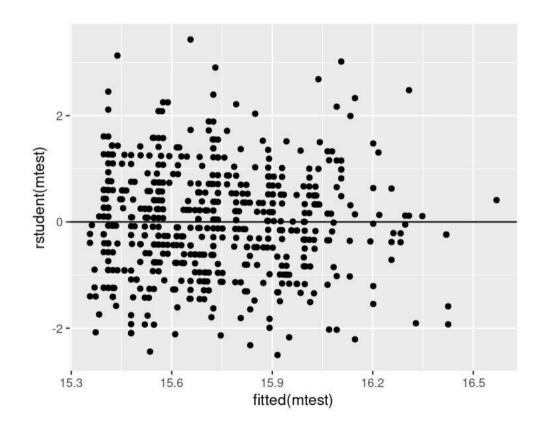




## What is a 'Good' Heteroscedasticity Plot?

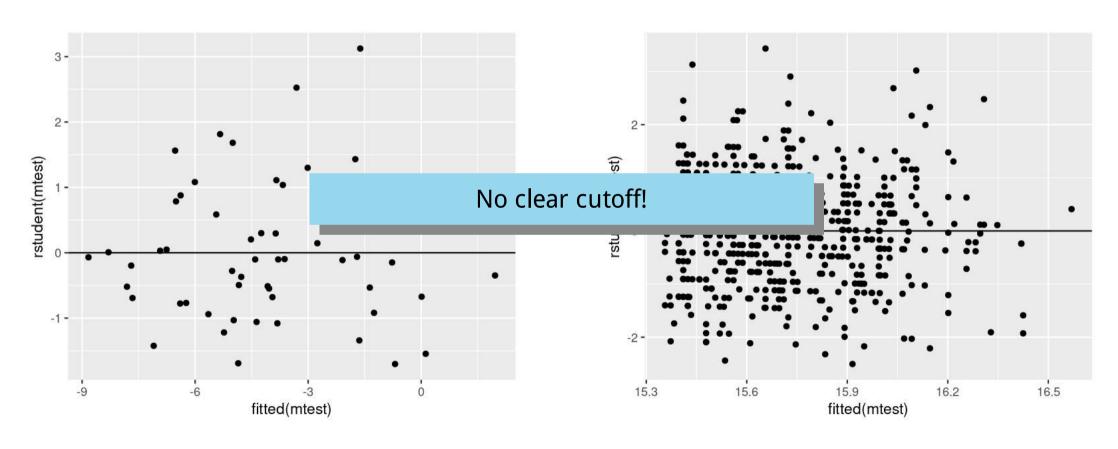
### Good





## What is a 'Good' Heteroscedasticity Plot?

#### Good

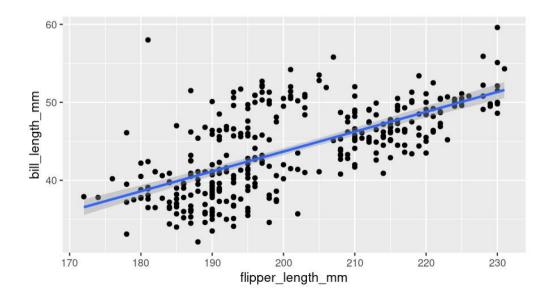


- Only relevant with more than one explanatory variable
- If explanatory variables too correlated, can interfere with model interpretation

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#### Look at our two explanatory variables

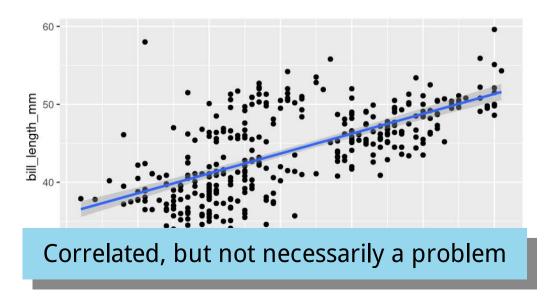
```
ggplot(data = penguins, aes(x = flipper_length_mm, y = bill_length_mm)) +
  geom_point() +
  stat_smooth(method = "lm")
```



- Only relevant with more than one explanatory variable
- If explanatory variables too correlated, can interfere with model interpretation

#### Look at our two explanatory variables

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ggplot(data = penguins, aes(x = flipper_length_mm, y = bill_length_mm)) +
  geom_point() +
  stat_smooth(method = "lm")
```



- Only relevant with more than one explanatory variable
- If explanatory variables too correlated, can interfere with model interpretation
- Correlations between variables *might* be problematic (but not necessarily)

#### Use vif() function from car package (vif = variance inflation factor\*)

Hmm, that's pretty good (looking for < 10)

```
m <- lm(body_mass_g ~ flipper_length_mm + bill_length_mm, data = penguins)</pre>
```

```
summary(m)
```

```
##
## Call:
## lm(formula = body mass g ~ flipper length mm + bill length mm,
      data = penguins)
##
##
## Residuals:
     Min 10 Median 30
##
                                   Max
## -1090.5 -285.7 -32.1 244.2 1287.5
##
## Coefficients:
##
                   Estimate Std. Error t value Pr(>|t|)
## (Intercept) -5736.897 307.959 -18.629 <2e-16 ***
## flipper_length_mm 48.145 2.011 23.939 <2e-16 ***
## bill_length_mm 6.047
                                5.180 1.168 0.244
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 394.1 on 339 degrees of freedom
    (2 observations deleted due to missingness)
## Multiple R-squared: 0.76, Adjusted R-squared: 0.7585
## F-statistic: 536.6 on 2 and 339 DF, p-value: < 2.2e-16 23/58
```

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m <- lm(body_mass_g ~ flipper_length_mm + bill_length_mm, data = penguins)</pre>
```

```
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```

#### Model

```
##
## Call:
## lm(formula = body_mass_g ~ flipper_length_mm + bill_length_mm,
##
      data = penguins)
##
## Residuals:
     Min 10 Median 30
##
                                   Max
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```

```
m <- lm(body_mass_g ~ flipper_length_mm + bill_length_mm, data = penguins)</pre>
```

```
summary(m)
```

#### **Effects**

```
##
## Call:
## lm(formula = body mass g ~ flipper length mm + bill length mm,
      data = penguins)
##
##
## Residuals:
     Min 10 Median 30
##
                                  Max
## -1090.5 -285.7 -32.1 244.2 1287.5
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## Coefficients:
##
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```

```
m <- lm(body_mass_g ~ flipper_length_mm + bill_length_mm, data = penguins)</pre>
```

```
summary(m)
```

#### **Missing observations**

```
##
## Call:
## lm(formula = body mass g ~ flipper length mm + bill length mm,
##
      data = penguins)
##
## Residuals:
     Min 10 Median 30
                                   Max
## -1090.5 -285.7 -32.1 244.2 1287.5
##
## Coefficients:
##
                   Estimate Std. Error t value Pr(>|t|)
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```

```
m <- lm(body_mass_g ~ flipper_length_mm + bill_length_mm, data = penguins)</pre>
```

```
summary(m)
```

### R<sup>2</sup> and adjusted R<sup>2</sup>

Adjusted for the number of parameters

```
##
## Call:
## lm(formula = body mass g ~ flipper length mm + bill length mm,
##
      data = penguins)
##
## Residuals:
      Min 10 Median 30
                                   Max
## -1090.5 -285.7 -32.1 244.2 1287.5
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## Coefficients:
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                   Estimate Std. Error t value Pr(>|t|)
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```

```
m <- lm(body_mass_g ~ flipper_length_mm + bill_length_mm, data = penguins)</pre>
```

```
summary(m)
```

### **Specific Details**

- Estimate
  - Slope of the effect
- Std. Error
  - Variability in the estimates
- t value
  - Test statistic
  - Think of it as a holistic combination of estimate and variability
- Pr(>|t|)
  - o **P-value**, significance of the results
  - Probability of getting t-value by chance

```
##
## Call:
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##
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##
## Residuals:
      Min 10 Median 30
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## bill length mm 6.047
                                 5.180 1.168 0.244
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 394.1 on 339 degrees of freedom
    (2 observations deleted due to missingness)
## Multiple R-squared: 0.76, Adjusted R-squared: 0.7585
## F-statistic: 536.6 on 2 and 339 DF, p-value: < 2.2e-16 28/58
```

```
m <- lm(body_mass_g ~ flipper_length_mm + bill_length_mm, data = penguins)</pre>
```

```
summary(m)
```

### **Specific Details**

#### **Intercept**

- Significant (P < 2e<sup>-16</sup>\*)
- Penguins with a flipper length of 0 mm are predicted to have a body mass of -5736.9g
  - Not useful!

```
##
## Call:
## lm(formula = body mass g ~ flipper length mm + bill length mm,
##
      data = penguins)
##
## Residuals:
      Min
              10 Median 30
                                   Max
## -1090.5 -285.7 -32.1 244.2 1287.5
##
## Coefficients:
##
                    Estimate Std. Error t value Pr(>|t|)
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m <- lm(body_mass_g ~ flipper_length_mm + bill_length_mm, data = penguins)</pre>
```

```
summary(m)
```

### **Specific Details**

#### Effect of Flipper Length

- Significant (P < 2e<sup>-16</sup>\*)
- For each 1 mm increase in flipper length, body mass is predicted to increase by 48.14g

```
##
## Call:
## lm(formula = body mass g ~ flipper length mm + bill length mm,
##
      data = penguins)
##
## Residuals:
      Min 10 Median 30
                                   Max
## -1090.5 -285.7 -32.1 244.2 1287.5
##
## Coefficients:
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```

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```

```
summary(m)
```

### **Specific Details**

#### Effect of Flipper Length

- Significant (P < 2e<sup>-16</sup>\*)
- For each 1 mm increase in flipper length, body mass is predicted to increase by 48.14g

- Non-significant (P = 0.244, i.e. P < 0.05)
- Therefore no effect (in this model)
   (and no interpretation of estimate)

```
##
## Call:
## lm(formula = body_mass_g ~ flipper_length_mm + bill_length_mm,
##
      data = penguins)
##
## Residuals:
      Min
              10 Median 30
                                   Max
## -1090.5 -285.7 -32.1 244.2 1287.5
##
## Coefficients:
##
                    Estimate Std. Error t value Pr(>|t|)
## (Intercept) -5736.897 307.959 -18.629
                                               <2e-16 ***
## flipper_length_mm 48.145
                                2.011 23.939 <2e-16 ***
## bill_length_mm 6.047
                                5.180 1.168
                                               0.244
## ---
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## Multiple R-squared: 0.76, Adjusted R-squared: 0.7585
## F-statistic: 536.6 on 2 and 339 DF, p-value: < 2.2e-16 31/58
```

m <- lm(boo

#### **Therefore**

There is a significant relationship between flipper length and body mass But not between bill length and body mass (when including flipper length)

length mm,

### Specific Details

#### Effect of Flipper Length

- Significant (P < 2e<sup>-16</sup>\*)
- For each 1 mm increase in flipper length, body mass is predicted to increase by 48.14g

- Non-significant (P = 0.244, i.e. P < 0.05)
- Therefore no effect (in this model)
   (and no interpretation of estimate)

```
data = penguins)
##
## Residuals:
      Min
               10 Median
                              30
                                     Max
## -1090.5 -285.7 -32.1 244.2 1287.5
##
## Coefficients:
##
                     Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                   -5736.897
                               307.959 -18.629
                                                  <2e-16 ***
## flipper_length_mm 48.145
                                  2.011 23.939
                                                  <2e-16 ***
## bill_length_mm
                       6.047
                                  5.180
                                          1.168
                                                   0.244
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 394.1 on 339 degrees of freedom
    (2 observations deleted due to missingness)
## Multiple R-squared: 0.76, Adjusted R-squared: 0.7585
## F-statistic: 536.6 on 2 and 339 DF, p-value: < 2.2e-16
```

```
m <- lm(body_mass_g ~ flipper_length_mm + bill_length_mm, data = penguins)</pre>
```

```
summary(m)
```

### **Specific Details**

#### Effect of Flipper Length

- Significant (P < 2e<sup>-16</sup>\*)
- For each 1 mm increase in flipper length, body mass is predicted to increase by 48.14g

- Non-significant (P = 0.244, i.e. P < 0.05)</li>
- Therefore no effect (and no interpretation of estimate)

```
(2 observations deleted due to missingness)
```

```
##
## Call:
## lm(formula = body_mass_g ~ flipper_length_mm + bill_length_mm,
##
      data = penguins)
##
                         y = mx + b
## Residuals:
      Min
              iv Median
## -1090.5 -285.7 -32.1 244.2 1287.5
##
## Coefficients:
                    Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
              -5736.897
                              307.959 -18.629
                                                <2e-16 ***
## flipper_length_mm 48.145
                                 2.011 23.939 <2e-16 ***
## bill_length_mm 6.047
                                 5.180 1.168
                                                0.244
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
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```

```
m <- lm(body_mass_g ~ flipper_length_mm + bill_length_mm, data = penguins)</pre>
```

##

## Call:

```
summary(m)
```

### **Specific Details**

#### Effect of Flipper Length

- Significant (P < 2e<sup>-16</sup>\*)
- For each 1 mm increase in flipper length, body mass is predicted to increase by 48.14g

#### Effect of Bill Length

- Non-significant (P = 0.244, i.e. P < 0.05)
- Therefore no effect (and no interpretation of estimate)

```
## lm(formula = body_mass_g ~ flipper_length_mm + bill_length_mm,
##
      data = penguins)
##
                    y = m_1x_1 + m_2x_2 + b
## Residuals:
      Min
##
## -1090.5 -285.7 -32.1 244.2 1287.5
##
## Coefficients:
                    Estimate Std. Error t value Pr(>|t|)
##
               -5736.897
## (Intercept)
                               307.959 -18.629
                                                 <2e-16 ***
## flipper_length_mm 48.145
                                 2.011 23.939 <2e-16 ***
## bill_length_mm 6.047
                                  5.180 1.168
                                                 0.244
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 394.1 on 339 degrees of freedom
    (2 observations deleted due to missingness)
## Multiple R-squared: 0.76, Adjusted R-squared: 0.7585
## F-statistic: 536.6 on 2 and 339 DF, p-value: < 2.2e-16 32/58
```

```
m <- lm(body_mass_g ~ flipper_length_mm + bill_length_mm, data = penguins)</pre>
```

```
summary(m)
```

### **Specific Details**

#### Effect of Flipper Length

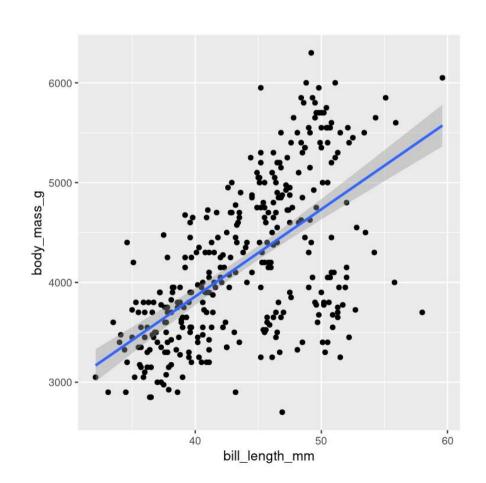
- Significant (P < 2e<sup>-16</sup>\*)
- For each 1 mm increase in flipper length, body mass is predicted to increase by 48.14g

- Non-significant (P = 0.244, i.e. P < 0.05)
- Therefore no effect (and no interpretation of estimate)

```
##
## Call:
## lm(formula = body_mass_g ~ flipper_length_mm + bill_length_mm,
##
      data = penguins)
##
              y = 48.14x_1 + 6.05x_2 + (-5736.9)
## Residuals:
      Min
##
## -1090.5 -285.7 -32.1 244.2 1287.5
##
## Coefficients:
                    Estimate Std. Error t value Pr(>|t|)
##
## (Intercept) -5736.897
                              307.959 -18.629
                                                <2e-16 ***
## flipper_length_mm 48.145
                                 2.011 23.939 <2e-16 ***
## bill_length_mm 6.047
                                 5.180 1.168
                                                0.244
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 394.1 on 339 degrees of freedom
    (2 observations deleted due to missingness)
## Multiple R-squared: 0.76, Adjusted R-squared: 0.7585
## F-statistic: 536.6 on 2 and 339 DF, p-value: < 2.2e-16 32/58
```

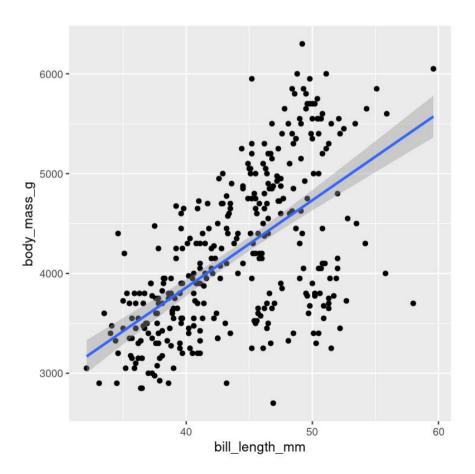
# Extra

### Why no effect of Bill Length?



### Extra

#### Why no effect of Bill Length?



```
m <- lm(body_mass_g ~ bill_length_mm, data = penguins)
summary(m)</pre>
```

```
##
## Call:
## lm(formula = body_mass_g ~ bill_length_mm, data = penguins)
##
## Residuals:
       Min
                10 Median
                                  30
                                          Max
## -1762.08 -446.98 32.59
                              462.31 1636.86
##
## Coefficients:
##
                 Estimate Std. Error t value Pr(>|t|)
## (Intercept)
               362.307
                            283.345
                                      1.279
                                              0.202
## bill_length_mm 87.415
                              6.402 13.654 <2e-16 ***
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 645.4 on 340 degrees of freedom
    (2 observations deleted due to missingness)
## Multiple R-squared: 0.3542, Adjusted R-squared: 0.3523
## F-statistic: 186.4 on 1 and 340 DF, p-value: < 2.2e-16
```

### Extra

#### Why no effect of Bill Length?

- Hypothesis of *causation* but really just correlation
- Flipper length is the 'better' predictor of body mass
- When flipper length in the model, no extra variation explained by bill length
- When flipper length not in the model, some variation left to be explained

```
m <- lm(body_mass_g ~ bill_length_mm, data = penguins)
summary(m)</pre>
```

```
##
## Call:
## lm(formula = body mass_g ~ bill_length_mm, data = penguins)
##
## Residuals:
       Min
                     Median
                                  30
                                          Max
## -1762.08 -446.98 32.59 462.31 1636.86
##
## Coefficients:
                 Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                 362.307
                                              0.202
                            283,345
                                      1,279
## bill_length_mm 87.415
                              6.402 13.654 <2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 645.4 on 340 degrees of freedom
    (2 observations deleted due to missingness)
## Multiple R-squared: 0.3542, Adjusted R-squared: 0.3523
## F-statistic: 186.4 on 1 and 340 DF, p-value: < 2.2e-16
```

# Homework (Practice)\*

Consider **bill depth** your response and **bill length** your predictor

- 1. Plot the relationship
- 2. Create a linear regression model
- 3. Check your model diagnostics
  - Normality
  - Heteroscedasticity
  - Influential variables (i.e. Cook's distance)
- 4. Interpret the results of your model

<sup>\*</sup> Not to be handed in, answers posted in these slides next week

# **ANOVAs**

### Linear Models

### **Running models in R**

```
lm(y \sim x1 + x2, data = data)
```

- y is the response variable (dependent)
- x are the explanatory variables (independent, predictor)

Here we're assuming a **continuous y** 

### Linear Models

### **Running models in R**

```
lm(y \sim x1 + x2, data = data)
```

- y is the response variable (dependent)
- x are the explanatory variables (independent, predictor)

Here we're assuming a **continuous y** 

### Different types of models

- If we only have one x which is continuous, this is a simple linear regression
- If both x are continuous, this is a multiple linear regression
- If both x are categorical, this is an ANOVA
- If x1 is continuous and x2 is categorical, this is an ANCOVA

### Linear Models

### **Running models in R**

```
lm(y \sim x1 + x2, data = data)
```

- y is the response variable (dependent)
- x are the explanatory variables (independent, predictor)

Here we're assuming a **continuous y** 

### Different types of models

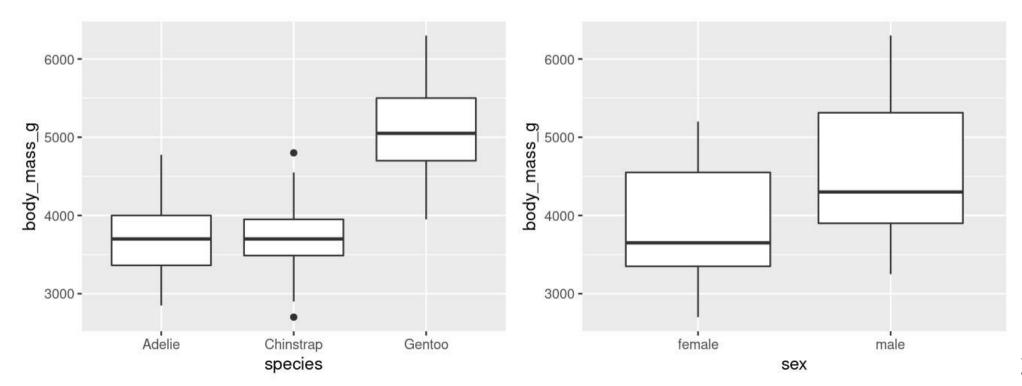
- If we only have one x which is continuous, this is a simple linear regression
- If both **x** are continuous, this is a **multiple linear regression**
- If both x are categorical, this is an ANOVA
- If x1 is continuous and x2 is categorical, this is an ANCOVA

R will figure it out for you

### **ANOVAs**

### **Real example**

- Are male penguins larger than female penguins?
- Are different species different sizes?
- Can body mass be predicted by species and sex?



### **ANOVAS**

### **Real example**

```
m <- lm(body_mass_g ~ species + sex, data = penguins)
```

As we have two **categorical** predictors, this is an ANOVA

#### Your turn!

Create a model with your response variable by your one categorical predictor.

Look at the output of summary() and anova()

### **ANOVAS**

### **Real example**

```
m <- lm(body_mass_g ~ species + sex, data = penguins)</pre>
```

As we have two **categorical** predictors, this is an ANOVA

#### Your turn!

Create a model with your response variable by your one categorical predictor.

Look at the output of **summary()** and **anova()** 

#### Wait!

Shouldn't interpret until we know the model is solid

# **Model Diagnostics**

Same as before! Let's get our relevant variables into a diagnostic data frame:

- residuals (regular and standardized)
- fitted values
- cooks distance
- obs number

# **Model Diagnostics**

Same as before! Let's get our relevant variables into a diagnostic data frame:

- residuals (regular and standardized)
- fitted values
- cooks distance
- obs number

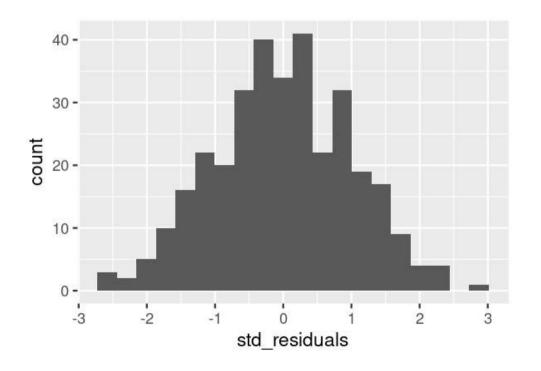
```
head(d)

## residuals std_residuals fitted cooks obs
## 1 -289.94196    -0.9201062 4039.942 0.0021071103    1
## 2 427.61319     1.3590567 3372.387 0.0045831843    2
## 3 -122.38681    -0.3879729 3372.387 0.0003754346    3
## 5 77.61319     0.2460043 3372.387 0.0001509858    4
## 6 -389.94196    -1.2387413 4039.942 0.0038112292    5
## 7 252.61319     0.8013974 3372.387 0.0015994740    6
```

# Normality

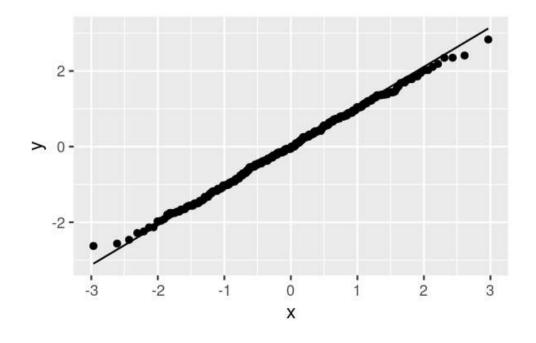
### Histogram of residuals

```
ggplot(data = d, aes(x = std_residuals)) +
  geom_histogram(bins = 20)
```



### QQ Normality plot of residuals

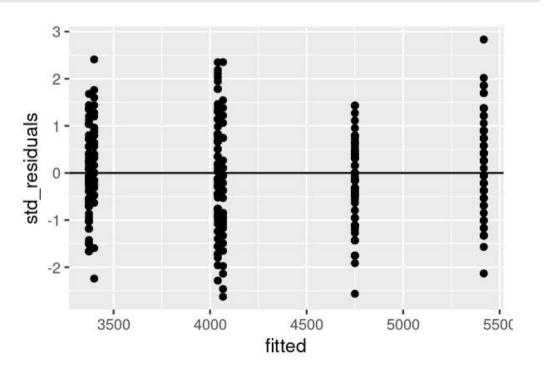
```
ggplot(data = d, aes(sample = std_residuals)) +
  stat_qq() +
  stat_qq_line()
```



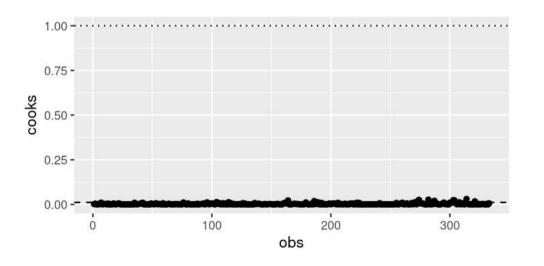
### Variance and Influence

#### Check heteroscedasticity

```
ggplot(d, aes(x = fitted, y = std_residuals)) +
  geom_point() +
  geom_hline(yintercept = 0)
```



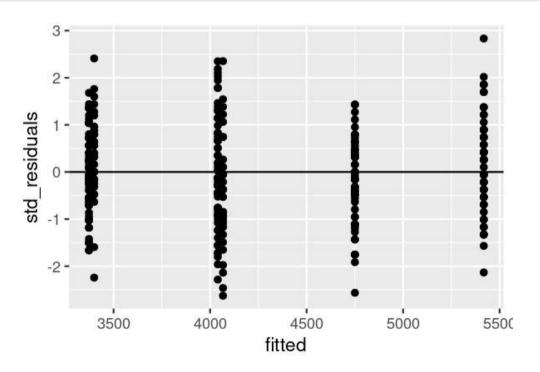
#### Cook's D



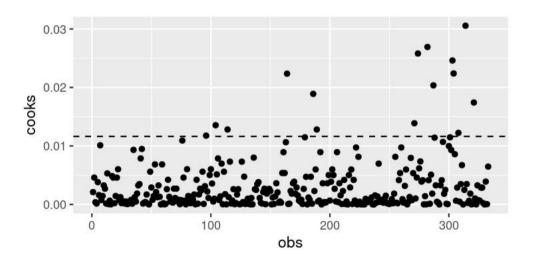
### Variance and Influence

### Check heteroscedasticity

```
ggplot(d, aes(x = fitted, y = std_residuals)) +
  geom_point() +
  geom_hline(yintercept = 0)
```



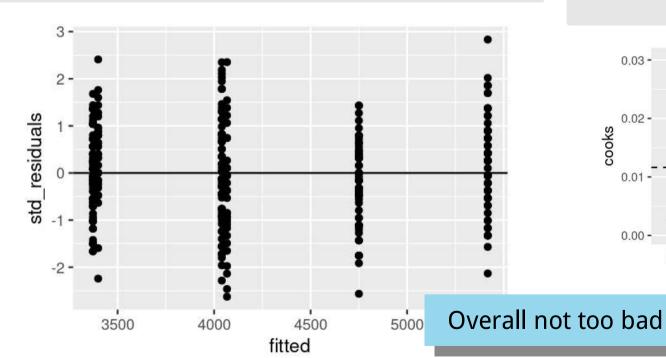
#### Cook's D



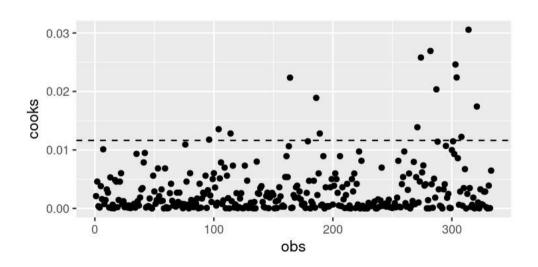
### Variance and Influence

### Check heteroscedasticity

```
ggplot(d, aes(x = fitted, y = std_residuals)) +
  geom_point() +
  geom_hline(yintercept = 0)
```



#### Cook's D



# Multicollinearity (collinearity)

### vif() function from car package

Here we consider the **GVIF^(1/2\*Df))** value\* Looks good!

<sup>\*</sup> See ?vif and the reference therein: Fox, J. and Monette, G. (1992) Generalized collinearity diagnostics. JASA, 87, 178-483/58

```
m <- lm(body_mass_g ~ species + sex, data = penguins)
```

```
summary(m)
```

```
##
## Call:
## lm(formula = body mass g ~ species + sex, data = penguins)
##
## Residuals:
     Min 10 Median 30
                                   Max
## -816.87 -217.80 -16.87 227.61 882.20
##
## Coefficients:
                 Estimate Std. Error t value Pr(>|t|)
##
## (Intercept) 3372.39 31.43 107.308 <2e-16 ***
## speciesChinstrap 26.92 46.48 0.579 0.563
## speciesGentoo 1377.86 39.10 35.236 <2e-16 ***
## sexmale 667.56 34.70 19.236 <2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 316.6 on 329 degrees of freedom
    (11 observations deleted due to missingness)
## Multiple R-squared: 0.8468, Adjusted R-squared: 0.8454
## F-statistic: 606.1 on 3 and 329 DF, p-value: < 2.2e-16 45/58
```

```
m <- lm(body_mass_g ~ species + sex, data = penguins)

summary(m)

##</pre>
```

#### Model

```
## Call:
## lm(formula = body_mass_g ~ species + sex, data = penguins)
##
## Residuals:
     Min 10 Median 30
                                  Max
## -816.87 -217.80 -16.87 227.61 882.20
##
## Coefficients:
                 Estimate Std. Error t value Pr(>|t|)
##
## (Intercept) 3372.39 31.43 107.308 <2e-16 ***
## speciesChinstrap 26.92 46.48 0.579 0.563
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## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 316.6 on 329 degrees of freedom
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## Multiple R-squared: 0.8468, Adjusted R-squared: 0.8454
## F-statistic: 606.1 on 3 and 329 DF, p-value: < 2.2e-16 46/58
```

```
m <- lm(body_mass_g ~ species + sex, data = penguins)
summary(m)
##</pre>
```

#### **Effects**

```
## Call:
## lm(formula = body_mass_g ~ species + sex, data = penguins)
##
## Residuals:
      Min
              10 Median 30
                                   Max
## -816.87 -217.80 -16.87 227.61 882.20
##
## Coefficients:
                  Estimate Std. Error t value Pr(>|t|)
##
## (Intercept) 3372.39 31.43 107.308 <2e-16 ***
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## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 316.6 on 329 degrees of freedom
    (11 observations deleted due to missingness)
## Multiple R-squared: 0.8468, Adjusted R-squared: 0.8454
## F-statistic: 606.1 on 3 and 329 DF, p-value: < 2.2e-16 47/58
```

```
m <- lm(body_mass_g ~ species + sex, data = penguins)

summary(m)

##</pre>
```

#### **Missing observations**

```
## Call:
## lm(formula = body_mass_g ~ species + sex, data = penguins)
##
## Residuals:
     Min 10 Median 30
                                  Max
## -816.87 -217.80 -16.87 227.61 882.20
##
## Coefficients:
                 Estimate Std. Error t value Pr(>|t|)
##
## (Intercept) 3372.39 31.43 107.308 <2e-16 ***
## speciesChinstrap 26.92 46.48 0.579 0.563
## speciesGentoo 1377.86 39.10 35.236 <2e-16 ***
## sexmale 667.56 34.70 19.236 <2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 316.6 on 329 degrees of freedom
  (11 observations deleted due to missingness)
## Multiple R-squared: 0.8468, Adjusted R-squared: 0.8454
## F-statistic: 606.1 on 3 and 329 DF, p-value: < 2.2e-16 48/58
```

```
m <- lm(body_mass_g ~ species + sex, data = penguins)
```

```
summary(m)
```

### R<sup>2</sup> and adjusted R<sup>2</sup>

Adjusted for the number of parameters

```
##
## Call:
## lm(formula = body_mass_g ~ species + sex, data = penguins)
##
## Residuals:
     Min 10 Median 30
                                  Max
## -816.87 -217.80 -16.87 227.61 882.20
##
## Coefficients:
                 Estimate Std. Error t value Pr(>|t|)
##
## (Intercept) 3372.39 31.43 107.308 <2e-16 ***
## speciesChinstrap 26.92 46.48 0.579 0.563
## speciesGentoo 1377.86 39.10 35.236 <2e-16 ***
## sexmale
           667.56 34.70 19.236 <2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 316.6 on 329 degrees of freedom
    (11 observations deleted due to missingness)
## Multiple R-squared: 0.8468, Adjusted R-squared: 0.8454
## F-statistic: 606.1 on 3 and 329 DF, p-value: < 2.2e-16 49/58
```

```
m <- lm(body_mass_g ~ species + sex, data = penguins)
```

```
summary(m)
```

#### **Specific Details**

- Estimate
  - Treatment contrasts
  - Average differences among categories compared to the base category
- Std. Error
  - Variability in the estimates
- t value
  - Test statistic
- Pr(>|t|)
  - **P-value**, significance of the *differences*
  - Probability of getting t-value by chance

```
##
## Call:
## lm(formula = body_mass_g ~ species + sex, data = penguins)
##
## Residuals:
      Min
              10 Median
                             30
                                    Max
## -816.87 -217.80 -16.87 227.61 882.20
##
## Coefficients:
                  Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                  3372.39
                               31.43 107.308 <2e-16 ***
## speciesChinstrap 26.92 46.48 0.579 0.563
## speciesGentoo 1377.86 39.10 35.236 <2e-16 ***
## sexmale
              667.56 34.70 19.236 <2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 316.6 on 329 degrees of freedom
    (11 observations deleted due to missingness)
## Multiple R-squared: 0.8468, Adjusted R-squared: 0.8454
## F-statistic: 606.1 on 3 and 329 DF, p-value: < 2.2e-16 50/58
```

```
m <- lm(body_mass_g ~ species + sex, data = penguins)
```

```
summary(m)
```

### **Specific Details**

- Estimate
  - Treatment contrasts
  - Average difference Easier to interpret estimates if we consider a simpler model compared to transfer to interpret estimates if we consider a simpler model

##

##

## Call:

## Residuals:

Min

- Std. Error
  - Variability in the estimates
- t value
  - Test statistic
- Pr(>|t|)
  - **P-value**, significance of the *differences*
  - Probability of getting **t-value** by chance

```
Estimate Sto. Error t value Pr(>|t|)
## (Intercept)
                   3372.39
                               31.43 107.308 <2e-16 ***
## speciesChinstrap 26.92 46.48 0.579 0.563
## speciesGentoo 1377.86 39.10 35.236 <2e-16 ***
## sexmale
              667.56
                          34.70 19.236 <2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 316.6 on 329 degrees of freedom
    (11 observations deleted due to missingness)
## Multiple R-squared: 0.8468, Adjusted R-squared: 0.8454
## F-statistic: 606.1 on 3 and 329 DF, p-value: < 2.2e-16 50/58
```

## lm(formula = body\_mass\_g ~ species + sex, data = penguins)

30

Max

10 Median

## -816.87 -217.80 -16.87 227.61 882.20

```
m <- lm(body_mass_g ~ species, data = penguins)</pre>
```

```
summary(m)
```

```
##
## Call:
## lm(formula = body mass g ~ species, data = penguins)
##
## Residuals:
       Min 10 Median
##
                                30
                                       Max
## -1126.02 -333.09 -33.09 316.91 1223.98
##
## Coefficients:
                  Estimate Std. Error t value Pr(>|t|)
##
## (Intercept) 3700.66 37.62 98.37 <2e-16 ***
## speciesChinstrap 32.43 67.51 0.48 0.631
## speciesGentoo 1375.35 56.15 24.50 <2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 462.3 on 339 degrees of freedom
    (2 observations deleted due to missingness)
## Multiple R-squared: 0.6697, Adjusted R-squared: 0.6677
## F-statistic: 343.6 on 2 and 339 DF, p-value: < 2.2e-16
```

```
m <- lm(body_mass_g ~ species, data = penguins)
```

#### Effect of **Species**

summary(m)

- (Intercept) represents base category (i.e. Adelie penguins)
- Adelie have mean body mass of 3700.66 g
- On average, Chinstrap penguins are 32.43 g heavier than Adelie penguins
- On average, Gentoo penguins are 1375.35 g heavier than Adelie penguins

```
##
## Call:
## lm(formula = body_mass_g ~ species, data = penguins)
##
## Residuals:
       Min
                     Median
                                  30
                                         Max
## -1126.02 -333.09
                     -33.09
                              316.91 1223.98
##
## Coefficients:
                  Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                   3700.66
                                37.62
                                       98.37 <2e-16 ***
## speciesChinstrap
                     32.43
                                               0.631
                                67.51
                                        0.48
## speciesGentoo
                   1375.35
                               56.15
                                       24.50 <2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 462.3 on 339 degrees of freedom
    (2 observations deleted due to missingness)
## Multiple R-squared: 0.6697, Adjusted R-squared: 0.6677
## F-statistic: 343.6 on 2 and 339 DF, p-value: < 2.2e-16
```

GENTOO!

CHINSTRAP!

```
m <- lm(body_mass_g ~ species, data = penguins)</pre>
```

```
Effect of Species
```

summary(m)

- (Intercept) represents base category (i.e. Adelie penguins)
- Adelie have mean body mass of 3700.
- On average, Chinstrap penguins are 32.43 g heavier than Adelie penguins
- On average, Gentoo penguins are 1375.35 g heavier than Adelie penguins

```
##
## Call:
## lm(formula = body_mass_g ~ species, data = penguins)
##
## Residuals:
## Min 1Q Median 3Q Max
## -1126.02 -333.09 -33.09 316.91 1223.98
```

CHINSTRAP!

GENTOO!

#### Back to original model

```
ESTIMATE Std. Error t value Pr(>|t|)
##
## (Intercept)
                   3700.66
                               37.62
                                       98.37 <2e-16 ***
## speciesChinstrap
                                               0.631
                     32.43
                               67.51
                                       0.48
## speciesGentoo
                   1375.35
                               56.15
                                      24.50 <2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 462.3 on 339 degrees of freedom
    (2 observations deleted due to missingness)
## Multiple R-squared: 0.6697, Adjusted R-squared: 0.6677
## F-statistic: 343.6 on 2 and 339 DF, p-value: < 2.2e-16
```

```
m <- lm(body_mass_g ~ species + sex, data = penguins)
```

```
summary(m)
```

#### Effect of **Species** and **Sex**

- (Intercept) represents base category but is a combination of factors
- Much more complicated to interpret
- Comparisons are often not of interest anyway (unless you've set up contrasts, which are advanced stats but awesome!)

```
##
## Call:
## lm(formula = body_mass_g ~ species + sex, data = penguins)
##
## Residuals:
      Min
              10 Median
                             30
                                   Max
## -816.87 -217.80 -16.87 227.61 882.20
##
## Coefficients:
                  Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                 3372.39
                              31.43 107.308 <2e-16 ***
## speciesChinstrap 26.92 46.48 0.579 0.563
## speciesGentoo 1377.86 39.10 35.236 <2e-16 ***
## sexmale
             667.56 34.70 19.236 <2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 316.6 on 329 degrees of freedom
    (11 observations deleted due to missingness)
## Multiple R-squared: 0.8468, Adjusted R-squared: 0.8454
## F-statistic: 606.1 on 3 and 329 DF, p-value: < 2.2e-16 52/58
```

```
m <- lm(body_mass_g ~ species + sex, data = penguins)
```

```
summary(m)
```

#### Effect of **Species** and **Sex**

- (Intercept) represents base category but is a combination of factors
- Much more complicated to interpret
- Comparisons are often not of interest anyway (unless you've set up contrasts, which are advanced stats but awesome!)

So let's look at ANOVA tables instead

```
##
## Call:
## lm(formula = body_mass_g ~ species + sex, data = penguins)
##
## Residuals:
      Min
              10 Median
                             30
                                    Max
## -816.87 -217.80 -16.87 227.61 882.20
##
## Coefficients:
                  Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                   3372.39
                               31.43 107.308 <2e-16 ***
## speciesChinstrap 26.92 46.48 0.579 0.563
## speciesGentoo 1377.86 39.10 35.236 <2e-16 ***
## sexmale
              667.56 34.70 19.236 <2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 316.6 on 329 degrees of freedom
    (11 observations deleted due to missingness)
## Multiple R-squared: 0.8468, Adjusted R-squared: 0.8454
## F-statistic: 606.1 on 3 and 329 DF, p-value: < 2.2e-16 52/58
```

### Type I

```
m <- lm(body_mass_g ~ species + sex, data = penguins)</pre>
```

anova(m)

### Type I

```
m <- lm(body_mass_g ~ species + sex, data = penguins)
```

```
anova(m)
```

#### Overall effects of **Species** and **Sex**

- Yes there are differences among Species (P < 2.2e<sup>-16</sup>)
- Yes there are differences between Sexes (P < 2.2e<sup>-16</sup>)

```
## Analysis of Variance Table
##
## Response: body_mass_g
                  Sum Sq Mean Sq F value
                                            Pr(>F)
## species
             2 145190219 72595110 724.21 < 2.2e-16
***
## sex
              1 37090262 37090262 370.01 < 2.2e-16
***
## Residuals 329 32979185
                          100241
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05
'.' 0.1 ' ' 1
```

### Type I

anova(m)

```
m <- lm(body_mass_g ~ species + sex, data = penguins)</pre>
```

#### Overall effects of **Species** and **Sex**

- Yes there are differences among Species (P < 2.2e<sup>-16</sup>)
- Yes there are differences between **Sexes** (P < 2.2e<sup>-16</sup>)

Not a whole lot of information...
Stay tuned for **Post-Hoc** tests next week!

### Type I

```
m1 <- lm(body_mass_g ~ species + sex, data =
penguins)
anova(m1)</pre>
```

```
## Analysis of Variance Table
##
## Response: body_mass_g
##
                   Sum Sq Mean Sq F value
                                              Pr(>F)
## species
              2 145190219 72595110 724.21 < 2.2e-16
***
              1 37090262 37090262 370.01 < 2.2e-16
## sex
***
## Residuals 329 32979185
                            100241
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05
'.' 0.1 ' ' 1
```

```
m2 <- lm(body_mass_g ~ sex + species, data =
penguins)
anova(m2)</pre>
```

```
## Analysis of Variance Table
##
## Response: body_mass_g
                   Sum Sq Mean Sq F value
                                              Pr(>F)
##
## sex
              1 38878897 38878897 387.86 < 2.2e-16
***
## species
              2 143401584 71700792 715.29 < 2.2e-16
***
## Residuals 329 32979185
                            100241
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05
'.' 0.1 ' ' 1
```

- For Type I ANOVAs, order matters with unbalanced samples
  - See that **Sum sq, Mean Sq** and **F value** all differ between the models
- Here, pretty minor, but important to remember with greater unbalances

#### Type III

```
m <- lm(body_mass_g ~ species + sex, data = penguins)</pre>
```

```
library(car)
Anova(m, type = "3")
```

#### Type III

```
m1 <- lm(body_mass_g ~ species + sex, data =
penguins)
Anova(m1, type = "3")</pre>
```

```
m2 <- lm(body_mass_g ~ sex + species, data =
penguins)
Anova(m2, type = "3")</pre>
```

• Type III and unbalanced samples: Not dependent on variable order

# Homework (Practice)\*

Consider flipper length your response variable and species and sex your predictor variables

- 1. Plot the relationship between flipper length and species and between flipper length and sex
- 2. Create an ANOVA model of flipper length and species
- 3. Check diagnostics
- 4. Interpret the **summary table**
- 5. Interpret the **ANOVA Table**
- 6. Create an ANOVA model of flipper length and species and sex
- 7. Check diagnostics
- 8. Interpret the **ANOVA Table**