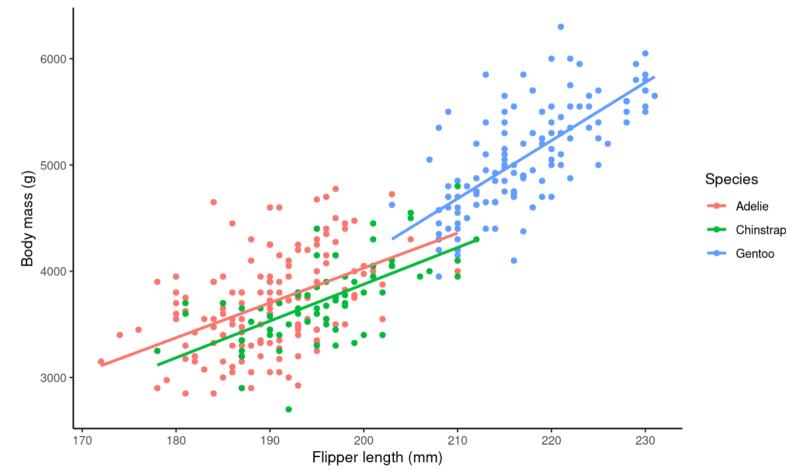


# Advanced Linear Models

Transformations, Interactions, and Post-hoc tests



Artwork by <u>@allison horst</u>

# **Getting started (again)**

Open RStudio
Open your NRI project
Open a **new** script for today:
File > New File > R Script

Make sure to load packages at the top:
 library(tidyverse)
 library(palmerpenguins)
 library(car)

# Messages vs. Warnings vs. Errors

- Not all coloured text is a problem
- Messages are just helpful information

```
ggplot(data = drop_na(penguins), aes(x = body_mass_g, y = flipper_length_mm)) +
  stat_smooth()
```

```
## `geom_smooth()` using method = 'loess' and formula 'y ~ x'
```

- Not all coloured text is a problem
- Messages are just helpful information
- Warnings should be considered **FYIs**. They might be a problem, but not always
  - Your code will run, even with a warning
  - Warnings always start with Warning:

```
ggplot(data = penguins, aes(x = sex, y = body_mass_g)) +
  geom_boxplot()
```

```
## Warning: Removed 2 rows containing non-finite values (stat_boxplot).
```

- Not all coloured text is a problem
- Messages are just helpful information
- Warnings should be considered **FYIs**. They might be a problem, but not always
  - Your code will run, even with a warning
  - Warnings always start with Warning:
- Errors are always problems :(
  - Your code will stop with an error
  - Errors always start with Error:

```
ggplot(data = Penguins, aes(x = sex, y = body_mass_g)) +
  geom_boxplot()
```

```
## Error in ggplot(data = Penguins, aes(x = sex, y = body_mass_g)): object 'Penguins' not found
```

- Not all coloured text is a problem
- Messages are just helpful information
- Warnings should be considered **FYIs**. They might be a problem, but not always
  - Your code will run, even with a warning
  - Warnings always start with Warning:
- Errors are always problems :(
  - Your code will stop with an error
  - Errors always start with Error:

**Messages < Warnings < Errors** 

```
ggplot(data = Penguins, aes(x = sex, y = body_mass_g)) +
    geom_boxplot()

## Error in ggplot(data = Penguins, aes(x = sex, y = body_mass_g)): object 'Penguins' not found
```

# **Data Transformations**

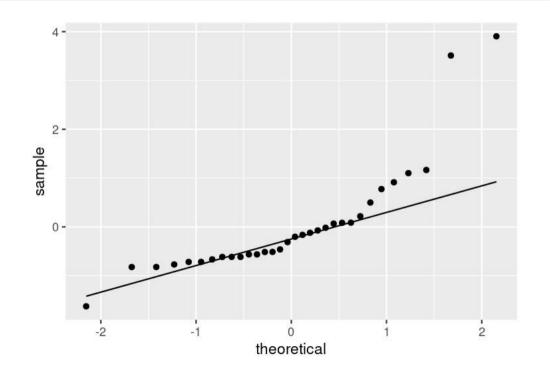
### Transformations

#### **Non-normal residuals**

Use a transformation!

Good for addressing non-normality of residuals,
and problems with variance

```
ggplot(data = d, aes(sample = std_residuals)) +
  stat_qq() +
  stat_qq_line()
```



### **Transformations**

### **Order of Operations**

- 1. See the need (i.e. non-normal residuals, heteroscedacity, etc.)
- 2. Figure out which transformation
- 3. Apply the transformation
- 4. Check model assumptions
- 5. Try again as needed

# Transformations: Common options

#### Table of transformations in R

```
data_trans <- mutate(data, y_trans = 1/y^2)</pre>
data_trans <- mutate(data, y_trans = 1/y)</pre>
data_trans <- mutate(data, y_trans = 1/sqrt(y))</pre>
data_trans <- mutate(data, y_trans = log(y))</pre>
data_trans <- mutate(data, y_trans = log10(y))</pre>
data_trans <- mutate(data, y_trans = sqrt(y))</pre>
data_trans <- mutate(data, y_trans = y^2)</pre>
data_trans <- mutate(data, y_trans = (y^lambda -</pre>
1)/lambda)
data trans <- mutate(data, y trans = asin(sqrt(y/100)))
```

Transformation	R Code	
Inverse square	1/y^2	
Reciprocal	1/y	
Inverse square root	1/sqrt(y)	
Naural log (ln)	log(y)	
Log base 10	log10(y)	
Square root	sqrt(y)	
Square	y^2	
Box Cox	(y^lambda - 1) / lambda	
Arcsine-sqare-root	asin(sqrt(y/100))	

### Transformations: How to choose?

- Based on what you know (often discipline specific standards for certain data types)
- Based on what you see (does it look exponential or logarithmic?)
- Based on trial and error (try different transformations and see how it goes)
- Based on Box-Cox lambda  $(\lambda)$

### 

Use it to indicate best transformation  $\rightarrow$ 

Dest A	Equation	Name
-2.5 to -1.5	$1/y^{2}$	inverse square
-1.5  to  -0.75	1/y	reciprocal
-0.75 to $-0.25$	$1/\sqrt{y}$	inverse square root
-0.25 to $0.25$	ln(y)	natural log
0.25  to  0.75	$\sqrt{y}$	square root
0.75  to  1.5	y	none
1.5  to  2.5	$y^2$	square

Faustion

Post 1

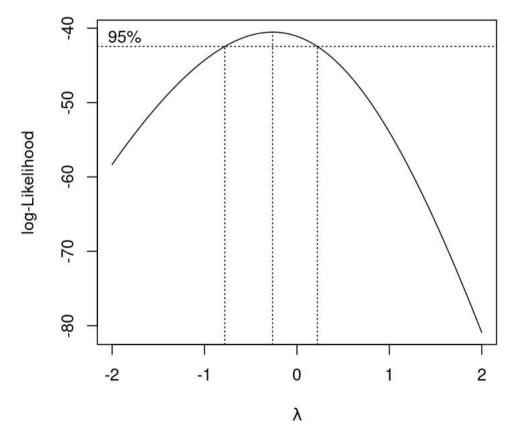
Namo

### Transformations: Box-Cox

### Finding $\lambda$

- Use a plot of  $\lambda$ 
  - boxcox() function from MASS package
  - Use boxcox() directly, otherwise MASS interferes with select()

```
b <- MASS::boxcox(m)</pre>
```



### Transformations: Box-Cox

### Finding $\lambda$

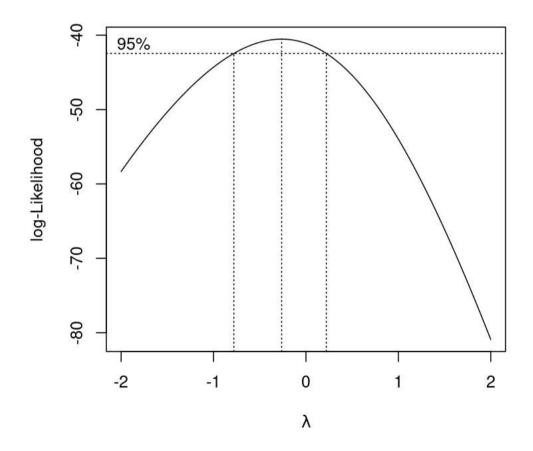
- Use a plot of  $\lambda$ 
  - boxcox() function from MASS package
  - Use boxcox() directly, otherwise MASS interferes with select()

```
b <- MASS::boxcox(m)
```

• Get the exact  $\lambda$ 

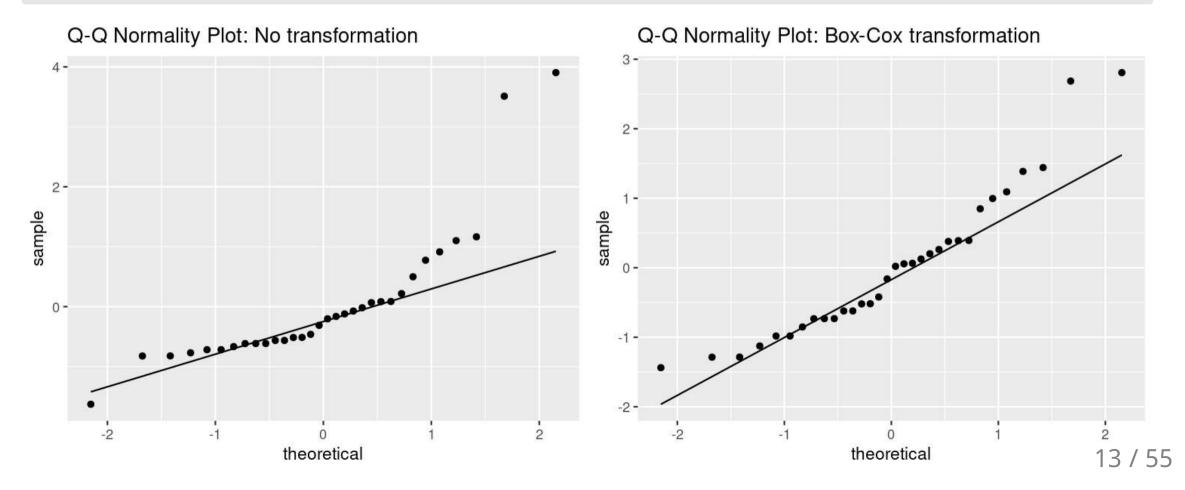
```
b$x[b$y == max(b$y)]
```

```
## [1] -0.2626263
```



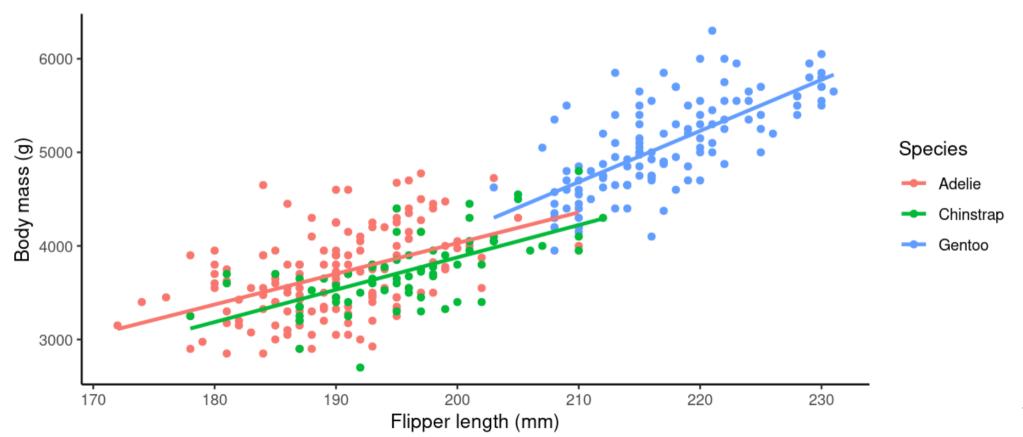
# Apply the transformation

```
msleep_trans <- mutate(msleep, sleep_cycle = (sleep_cycle^0.26 - 1) / 0.26)
m_trans <- lm(sleep_cycle ~ bodywt, data = msleep_trans)</pre>
```



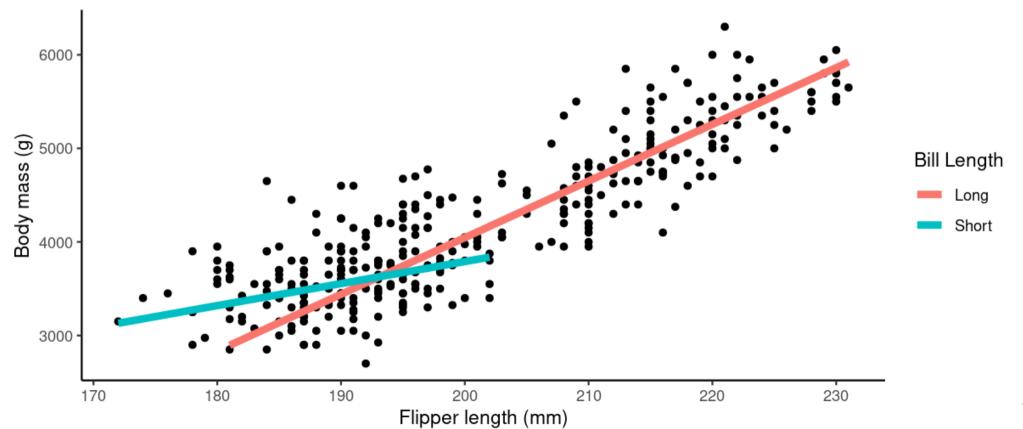
### **Interaction between Flipper Length and Species**

Does the effect of Flipper Length on Body Mass depend on Species? (i.e. Are the slopes different?)



### **Interaction between Flipper Length and Bill Length**

Does the effect of Flipper Length on Body Mass depend on Bill Length? (i.e. Does the slope of Flipper Length change with Bill Length?)



16 / 55

### **Main Effects only** +

```
m <- lm(body_mass_g ~ flipper_length_mm + bill_length_mm, data = penguins)</pre>
```

### Main Effects only +

```
m <- lm(body_mass_g ~ flipper_length_mm + bill_length_mm, data = penguins)</pre>
```

#### **Main Effects and Interaction +:**

### Main Effects only +

```
m <- lm(body_mass_g ~ flipper_length_mm + bill_length_mm, data = penguins)</pre>
```

#### **Main Effects and Interaction +:**

#### Shortcut: Main Effects and Interaction \*

```
m <- lm(body_mass_g ~ flipper_length_mm * bill_length_mm, data = penguins)</pre>
```

### Main Effects only +

```
m <- lm(body_mass_g ~ flipper_length_mm + bill_length_mm, data = penguins)</pre>
```

#### Main Effects and Interaction +:

#### **Shortcut: Main Effects and Interaction \***

```
m <- lm(body_mass_g ~ flipper_length_mm * bill_length_mm, data = penguins)</pre>
```

### Don't forget your diagnostic plots!

### **Including Correlation Tables**

```
summary(m, correlation = TRUE) # Showing bottom of the output only
```

```
## Coefficients:
##
                                   Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                                  5090.5088 2925.3007 1.740 0.082740 .
## flipper_length_mm
                                 -7.3085 15.0321 -0.486 0.627145
## bill_length_mm
                                -229.2424 63.4334 -3.614 0.000347 ***
## flipper length mm:bill length mm 1.1998 0.3224 3.721 0.000232 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 386.8 on 338 degrees of freedom
    (2 observations deleted due to missingness)
## Multiple R-squared: 0.7694, Adjusted R-squared: 0.7674
## F-statistic: 375.9 on 3 and 338 DF, p-value: < 2.2e-16
##
## Correlation of Coefficients:
##
                                  (Intercept) flipper_length_mm bill_length_mm
## flipper_length_mm
                                  -1.00
## bill_length_mm
                                -0.99
                                         0.98
## flipper length mm:bill length mm 0.99
                                             -0.99
                                                               -1.00
```

### **Including Correlation Tables**

```
summary(m, correlation = TRUE) # Showing bottom of the output only
```

```
## Coefficients:
##
                                   Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                                  5090.5088 2925.3007 1.740 0.082740 .
                                  -7.3085 15.0321 -0.486 0.627145
## flipper_length_mm
## bill_length_mm
                                -229.2424 63.4334 -3.614 0.000347 ***
## flipper_length_mm:bill_length_mm 1.1998 0.3224 3.721 0.000
                                                                    But for now we'll focus on
## ---
                                                                           the Estimates
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 386.8 on 338 degrees of freedom
    (2 observations deleted due to missingness)
## Multiple R-squared: 0.7694, Adjusted R-squared: 0.7674
## F-statistic: 375.9 on 3 and 338 DF, p-value: < 2.2e-16
##
## Correlation of Coefficients:
##
                                  (Intercept) flipper_length_mm bill_length_mm
## flipper_length_mm
                                  -1.00
## bill_length_mm
                                 -0.99
                                            0.98
## flipper_length_mm:bill_length_mm 0.99
                                             -0.99
                                                               -1.00
```

Effect of Flipper Length on Body Mass when Bill Length is 0 mm

Effect of Flipper Length on Body Mass when Bill Length is 0 mm

When Bill Length is 0 mm, Body mass decreases by 7.31 g for each 1 mm increase in Flipper Length

Effect of Flipper Length on Body Mass when Bill Length is 0 mm

Not meaningful! Do we ever have a Bill Length of 0 mm?

Do not interpret

Effect of Bill Length on Body Mass when Flipper Length is 0 mm

Effect of Bill Length on Body Mass when Flipper Length is 0 mm

When Flipper Length is 0 mm, Body Mass decreases by 229.24 g for each 1 mm increase in Bill Length

Effect of Bill Length on Body Mass when Flipper Length is 0 mm

Not meaningful! Do we ever have a Flipper Length of 0 mm?

Do not interpret

Change in the effect of **Flipper Length** on Body Mass for every 1 mm change in **Bill Length** 

Change in the effect of **Flipper Length** on Body Mass for every 1 mm change in **Bill Length** 

For every 1 mm increase in Bill Length, the effect of a 1 mm increase in Flipper Length on Body Mass increases by 1.2 g (i.e. the slope of the relationship between Body Mass and Flipper Length increases)

Change in the effect of **Flipper Length** on Body Mass for every 1 mm change in **Bill Length** 

For every 1 mm increase in Bill Length, the effect of a 1 mm increase in Flipper Length on Body Mass increases by 1.2 g (i.e. the slope of the relationship between Body Mass and Flipper Length increases)



OH WTF.

Artwork by <u>@allison horst</u> 22 / 55

# Plotting Interactions

#### Create new data frame with extremes

## Side Note: tidyverse functions

#### Create new data frame with extremes

### expand()

- from tidyr package (part of the tidyverse)
- tidyverse functions always start with the data, followed by other arguments
- you can reference any column from 'data'
- expand() creates a data frame with all possible combinations of new columns

#### Create new data frame with extremes

### Add predicted y values

- Use **predict()** function
  - predict() can be used on most statistical models
- Returns predicted body\_mass\_g values for new data

```
penguins_new <- mutate(penguins_new, body_mass_g = predict(m, newdata = penguins_new))</pre>
```

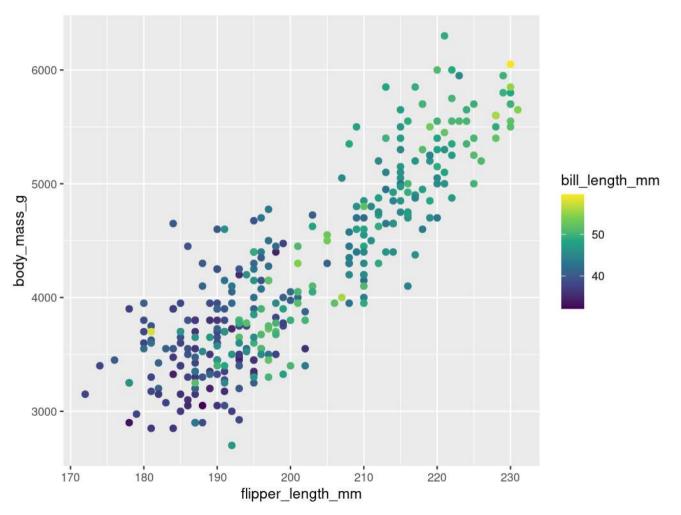
#### **Small data frame**

- With values predicted from model
- Can plot this to illustrate interactions

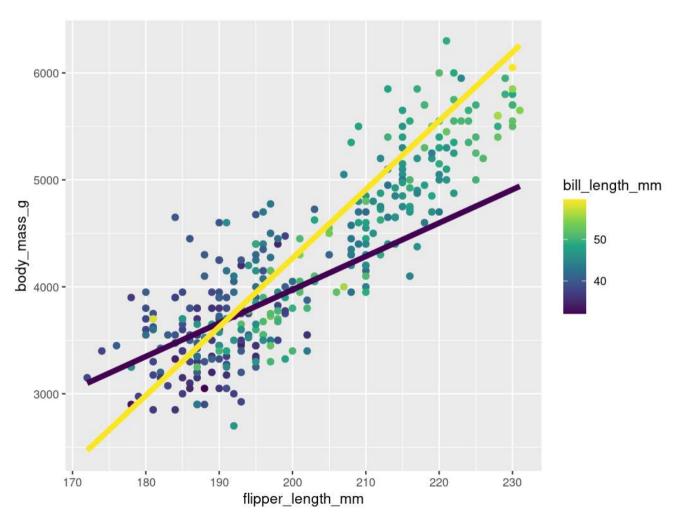
```
penguins_new
```

```
## # A tibble: 4 x 3
     flipper_length_mm bill_length_mm body_mass_g
##
                                  <dbl>
                                               <dbl>
##
                  <int>
## 1
                    172
                                   32.1
                                               3099.
                                              2470.
## 2
                    172
                                   59.6
## 3
                    231
                                   32.1
                                               4941.
## 4
                    231
                                   59.6
                                               6258.
```

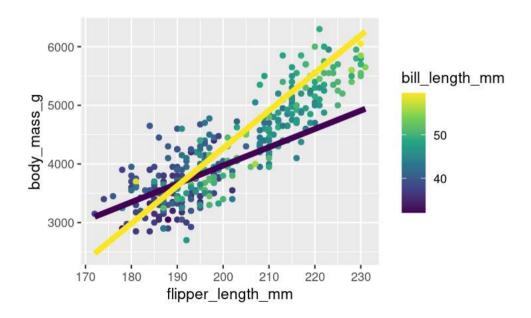
## Raw data (no model)



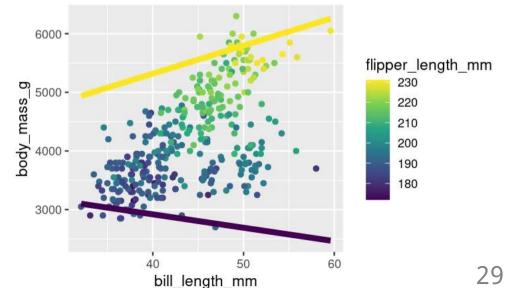
#### **Raw data + Model interaction**



#### From a Flipper Length perspective

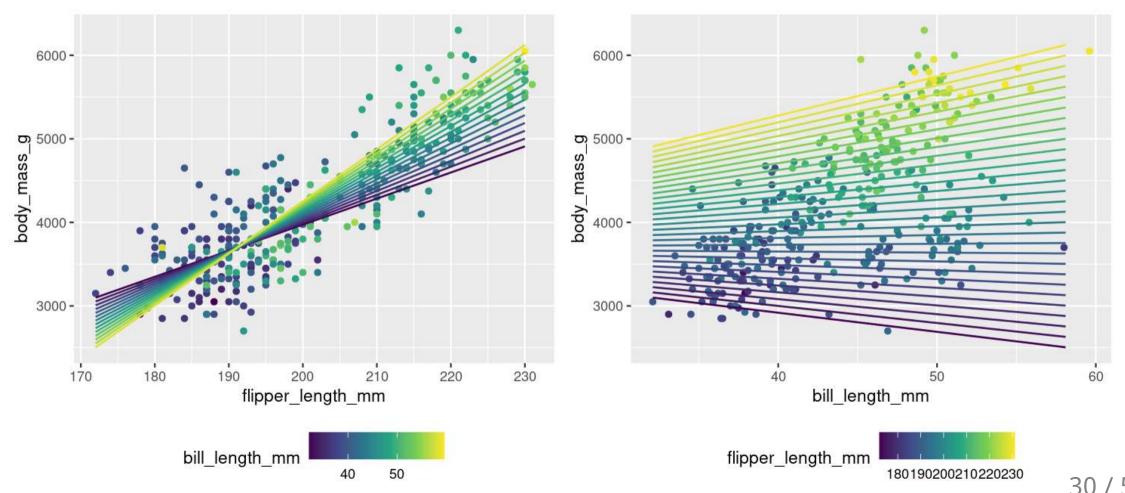


#### From a Bill Length perspective



# Visualizing Interactions

Not what you would present in a paper, but good to think about



# **ANOVAs and Post-Hoc Tests**

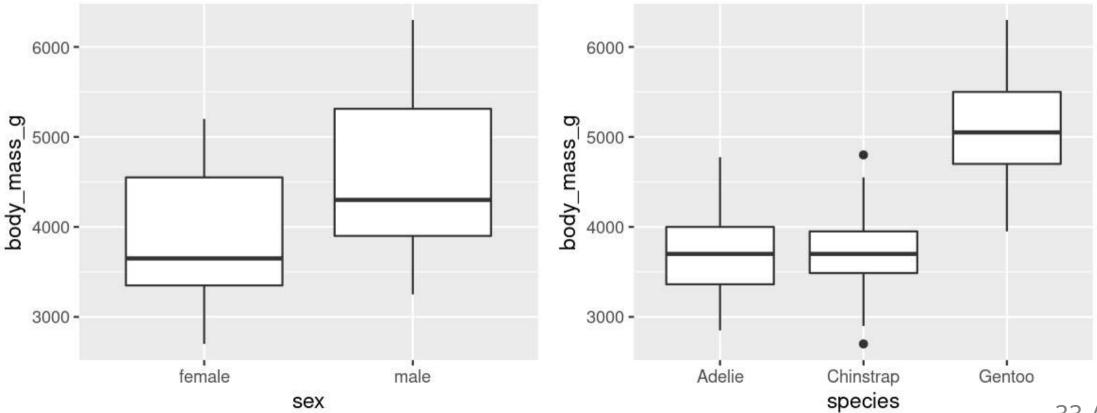
#### From last week...

```
m <- lm(body_mass_g ~ species + sex, data = penguins)</pre>
Anova(m, type = 3)
## Anova Table (Type III tests)
##
## Response: body_mass_g
   Sum Sq Df F value Pr(>F)
##
## species 143401584 2 715.29 < 2.2e-16 ***
## sex 37090262 1 370.01 < 2.2e-16 ***
## Residuals 32979185 329
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

Differences within groups, but how are they different?

- Males significantly bigger than females
- Only two groups, so we can use the figure

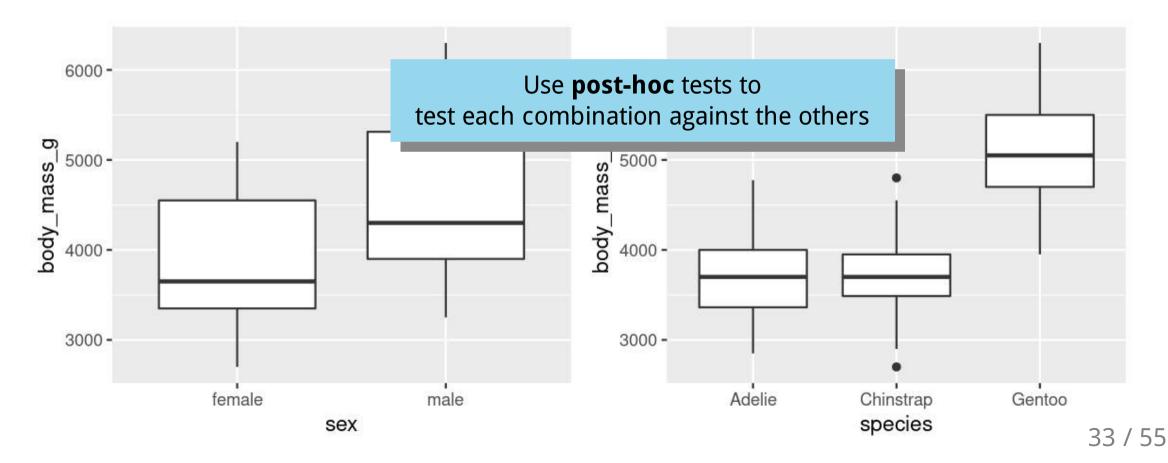
- Are Adelie and Chinstrap the same size?
- Looks like it, but no statistical support



33 / 55

- Males significantly bigger than females
- Only two groups, so we can use the figure

- Are Adelie and Chinstrap the same size?
- Looks like it, but no statistical support



# **Estimated Marginal Means**

### emmeans() function from emmeans package

- Calculates **estimated marginal means** (least-squares means)
- Mean response of each factor, adjusting for other factors
- Can think of this as a predicted mean response if sample sizes were equal (and controlling for other parameters)

```
library(emmeans)
emm sp <- emmeans(m, specs = "species")</pre>
emm sp
   species
              emmean SE df lower.CL upper.CL
   Adelie 3706 26.2 329
                                  3655
                                           3758
   Chinstrap 3733 38.4 329
                                          3809
                                 3658
   Gentoo
               5084 29.0 329
                                  5027
                                           5141
##
##
## Results are averaged over the levels of: sex
## Confidence level used: 0.95
```

### pairs() function from emmeans packages

Compare each combination

```
pairs(emm_sp)
```

### pairs() function from emmeans packages

Compare each combination

```
pairs(emm_sp)
```

#### **Differences in Body Mass**

 Adelie penguins are **not** different from Chinstrap penguins (P value = 0.831)

### pairs() function from emmeans packages

Compare each combination

```
pairs(emm_sp)
```

#### **Differences in Body Mass**

- Adelie penguins are **not** different from Chinstrap penguins (P value = 0.831)
- Adelie penguins are on average 1377.9 g lighter than Gentoo penguins (P value = < 0.0001)</li>

### pairs() function from emmeans packages

Compare each combination

```
pairs(emm_sp)
```

#### **Differences in Body Mass**

- Adelie penguins are **not** different from Chinstrap penguins (P value = 0.831)
- Adelie penguins are on average 1377.9 g lighter than Gentoo penguins (P value = < 0.0001)</li>
- Chinstrap penguins are on average 1350.9 g lighter than Gentoo penguins (P value < 0.0001)</li>

### pairs() function from emmeans packages

Compare each combination

```
pairs(emm_sp)
```

#### **Differences in Body Mass**

- Adelie penguins are **not** different from Chinstrap penguins (P value = 0.831)
- Adelie penguins are on average 1377.9 g lighter than Gentoo penguins (P value = < 0.0001)</li>
- Chinstrap penguins are on average 1350.9 g lighter than Gentoo penguins (P value < 0.0001)</li>

#### Therefore, on average

Gentoo penguins are the largest
Adelie and Chinstrap penguins are the
same size

## Post-Hoc Tests (Dunnett's)

### With contrast() function from emmeans package

- Dunnett's comparison is a type of contrast
- Each level compared to control
- Use method = "trt.vs.ctrl" OR method = "dunnett"

## Post-Hoc Tests (Dunnett's)

### With contrast() function from emmeans package

- Dunnett's comparison is a type of contrast
- Each level compared to control
- Use method = "trt.vs.ctrl" OR method = "dunnett"

#### Look familiar?

# Post-Hoc Tests (Dunnett's)

#### Dunnett's treatment vs. control contrasts with summary() table

```
## Coefficients:

## Estimate Std. Error t value Pr(>|t|)

## (Intercept) 3372.39 31.43 107.308 <2e-16 ***

## speciesChinstrap 26.92 46.48 0.579 0.563

## speciesGentoo 1377.86 39.10 35.236 <2e-16 ***

## sexmale 667.56 34.70 19.236 <2e-16 ***
```

#### **Dunnett's treatment vs. control contrasts with emmeans**

# Post-Hoc Tests and P-Value adjustments

#### No adjustment, too liberal?

## **Extremely conservative\***

In these examples, little difference, but can make a HUGE difference in other analyses

# Post-Hoc Tests and P-Value adjustments

## Middle of the road: Benjamini Hochberg (FDR, False Discovery Rate)\*

\* See this article 42 / 5

# Post-Hoc Tests and P-Value adjustments

## Middle of the road: Benjamini Hochberg (FDR, False Discovery Rate)\*

#### No one best method

What is your question? Are you more concerned about Type 1 or Type 2 error?

\* See this article 42 / !

## **Test options**

Argument	P-Value Adjustment
none	No P-Value Adjustment (essentially Fisher's LSD)
tukey	Tukey's HSD (Honestly significant difference), uses the Studentized range distribution with the number of means in the family.
fdr	Benjamini-Hochberg Test or False Discovery Rate Test
bonferroni	Bonferroni Correction
scheffe	Computes p values from F distribution
mvt	Adjusted p values based on the joint normal or t distribution of the linear function
holm	<u>Holm Test</u>
hochberg	<u>Hochberg Test</u>
hommel	<u>Hommel Test</u>

## Post-Hoc Tests with Interactions

## **Model: 2-way ANOVA**

```
m <- lm(body_mass_g ~ species * sex, data = penguins)</pre>
```

### **Estimated Marginal Means**

```
library(emmeans)
m_emms <- emmeans(m, specs = c("species", "sex"))
m_emms</pre>
```

```
species
                          SE df lower.CL upper.CL
                  emmean
            sex
   Adelie
            female 3369 36.2 327
                                    3298
                                            3440
   Chinstrap female
                   3527 53.1 327
                                 3423
                                        3632
   Gentoo
           female
                   4680 40.6 327
                                 4600
                                          4760
  Adelie male 4043 36.2 327
                                    3972
                                          4115
   Chinstrap male 3939 53.1 327
                                    3835
                                            4043
   Gentoo
            male
                5485 39.6 327
                                    5407
                                            5563
##
## Confidence level used: 0.95
```

### pairs() function from emmeans packages

Compare each combination

```
pairs(m_emms, adjust = "fdr")
```

```
contrast
                                    estimate SE df t.ratio p.value
   Adelie female - Chinstrap female
                                        -158 64.2 327 -2.465 0.0152
  Adelie female - Gentoo female
                                       -1311 54.4 327 -24.088 <.0001
  Adelie female - Adelie male
                                        -675 51.2 327 -13.174 <.0001
   Adelie female - Chinstrap male
                                        -570 64.2 327 -8.875 <.0001
   Adelie female - Gentoo male
                                       -2116 53.7 327 -39.425 <.0001
   Chinstrap female - Gentoo female
                                       -1153 66.8 327 -17.246 <.0001
   Chinstrap female - Adelie male
                                        -516 64.2 327 -8.037 <.0001
   Chinstrap female - Chinstrap male
                                        -412 75.0 327 -5.487 <.0001
   Chinstrap female - Gentoo male
                                       -1958 66.2 327 -29.564 <.0001
   Gentoo female - Adelie male
                                         636 54.4 327 11.691 <.0001
   Gentoo female - Chinstrap male
                                         741 66.8 327 11.085 <.0001
   Gentoo female - Gentoo male
                                        -805 56.7 327 -14.188 <.0001
   Adelie male - Chinstrap male
                                        105 64.2 327 1.627 0.1047
   Adelie male - Gentoo male
                                       -1441 53.7 327 -26.855 <.0001
   Chinstrap male - Gentoo male
                                       -1546 66.2 327 -23.345 <.0001
##
## P value adjustment: fdr method for 15 tests
```

### pairs() function from emmeans packages

Compare each combination

```
pairs(m_emms, adjust = "fdr")
```

#### **Differences in Body Mass**

 Female Adelie penguins are on average 158 g smaller than female Chinstrap penguins (P value = 0.015)

```
contrast
                                     estimate
                                                SE df t.ratio p.value
   Adelie female - Chinstrap female
                                         -158 64.2 327 -2.465 0.0152
   Adelie female - Gentoo female
                                        -1311 54.4 327 -24.088 <.0001
  Adelie female - Adelie male
                                         -675 51.2 327 -13.174 <.0001
   Adelie female - Chinstrap male
                                         -570 64.2 327 -8.875 <.0001
   Adelie female - Gentoo male
                                        -2116 53.7 327 -39.425 <.0001
   Chinstrap female - Gentoo female
                                        -1153 66.8 327 -17.246 <.0001
   Chinstrap female - Adelie male
                                         -516 64.2 327 -8.037 <.0001
   Chinstrap female - Chinstrap male
                                         -412 75.0 327 -5.487 <.0001
   Chinstrap female - Gentoo male
                                        -1958 66.2 327 -29.564 <.0001
   Gentoo female - Adelie male
                                          636 54.4 327 11.691 <.0001
   Gentoo female - Chinstrap male
                                          741 66.8 327 11.085 < .0001
   Gentoo female - Gentoo male
                                         -805 56.7 327 -14.188 <.0001
   Adelie male - Chinstrap male
                                          105 64.2 327 1.627 0.1047
   Adelie male - Gentoo male
                                        -1441 53.7 327 -26.855 <.0001
   Chinstrap male - Gentoo male
                                        -1546 66.2 327 -23.345 <.0001
##
## P value adjustment: fdr method for 15 tests
```

### pairs() function from emmeans packages

• Compare each combination

```
pairs(m_emms, adjust = "fdr")
```

#### **Differences in Body Mass**

- Female Adelie penguins are on average 158 g smaller than female Chinstrap penguins (P value = 0.015)
- Male Adelie penguins are **not** different from male Chinstrap penguins (P value = 0.105)

```
contrast
                                     estimate
                                               SE df t.ratio p.value
   Adelie female - Chinstrap female
                                          -158 64.2 327 -2.465 0.0152
   Adelie female - Gentoo female
                                        -1311 54.4 327 -24.088 <.0001
  Adelie female - Adelie male
                                         -675 51.2 327 -13.174 <.0001
   Adelie female - Chinstrap male
                                         -570 64.2 327 -8.875 <.0001
   Adelie female - Gentoo male
                                        -2116 53.7 327 -39.425 <.0001
   Chinstrap female - Gentoo female
                                        -1153 66.8 327 -17.246 <.0001
   Chinstrap female - Adelie male
                                         -516 64.2 327 -8.037 <.0001
   Chinstrap female - Chinstrap male
                                         -412 75.0 327 -5.487 <.0001
   Chinstrap female - Gentoo male
                                        -1958 66.2 327 -29.564 <.0001
   Gentoo female - Adelie male
                                           636 54.4 327 11.691 <.0001
   Gentoo female - Chinstrap male
                                          741 66.8 327 11.085 < .0001
   Gentoo female - Gentoo male
                                          -805 56.7 327 -14.188 <.0001
   Adelie male - Chinstrap male
                                          105 64.2 327
                                                        1.627 0.1047
   Adelie male - Gentoo male
                                        -1441 53.7 327 -26.855 <.0001
##
   Chinstrap male - Gentoo male
                                        -1546 66.2 327 -23.345 <.0001
##
## P value adjustment: fdr method for 15 tests
```

### pairs() function from emmeans packages

Compare each combination

```
pairs(m_emms, adjust = "fdr")
```

#### **Differences in Body Mass**

- Female Adelie penguins are on average 158 g smaller than female Chinstrap penguins (P value = 0.015)
- Male Adelie penguins are **not** different from male Chinstrap penguins (P value = 0.105)
- Female Adelie penguins are on average 675 g lighter than male
   Adelie penguins (P value = 0)

```
contrast
                                      estimate
                                                SE df t.ratio p.value
   Adelie female - Chinstrap female
                                          -158 64.2 327 -2.465 0.0152
   Adelie female - Gentoo female
                                         -1311 54.4 327 -24.088 <.0001
   Adelie female - Adelie male
                                          -675 51.2 327 -13.174 <.0001
   Adelie female - Chinstrap male
                                          -570 64.2 327 -8.875 <.0001
   Adelie female - Gentoo male
                                         -2116 53.7 327 -39.425 <.0001
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                                                        1.627 0.1047
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```

# Post-Hoc Tests with Interactions

#### **Model: ANCOVA**

```
m <- lm(body_mass_g ~ flipper_length_mm * species, data = penguins)</pre>
```

## **Estimated Marginal Means**

• Here use **emtrends()** function from **emmeans** package

```
m_emms <- emtrends(m, specs = "species", var = "flipper_length_mm")
m_emms</pre>
```

```
flipper_length_mm.trend SE df lower.CL upper.CL
   species
   Adelie
                                32.8 4.63 336
                                                 23.7
                                                          41.9
   Chinstrap
                                                          47.1
                               34.6 6.35 336
                                                22.1
   Gentoo
                                54.6 5.17 336
                                                44.4
                                                          64.8
##
## Confidence level used: 0.95
```

These are the effects of Flipper Length on Body Mass in each Species.

#### On average...

- Adelie: Body Mass increases by 32.8 g for each 1 mm increase in Flipper Length.
- Chinstrap: Body Mass increases by 34.6 g for each 1 mm increase in Flipper Length.
- Gentoo: Body Mass increases by 54.6 g for each 1 mm increase in Flipper Length.

## Post-Hoc Tests with Interactions

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                                                           41.9
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                                                 22.1
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                                                 44.4
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But are these different from one another?

### pairs() function from emmeans packages

• Compare among species

```
pairs(m_emms, adjust = "fdr")
```

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```
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#### Differences in the effect of Flipper Length on Body Mass

• The effect of Flipper Length on Body Mass is **not** different between Adelie and Chinstrap penguins (P value = 0.825)

### pairs() function from emmeans packages

Compare among species

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#### Differences in the effect of Flipper Length on Body Mass

- The effect of Flipper Length on Body Mass is **not** different between Adelie and Chinstrap penguins (P value = 0.825)
- The effect of Flipper Length on Body Mass **is significantly less** in Adelie than in Gentoo penguins (Body Mass increases 21.8 g less per 1mm increase in Flipper Length; P value = 0.006)

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Compare among species

```
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```

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- The effect of Flipper Length on Body Mass **is significantly less** in Chinstrap than in Gentoo penguins (Body Mass increases 20 g less per 1mm increase in Flipper Length; P value = 0.022)

### pairs() function from emmeans packages

Compare among species

```
pairs(m_emms, adjust = "fdr")
```

#### Differences in the ef

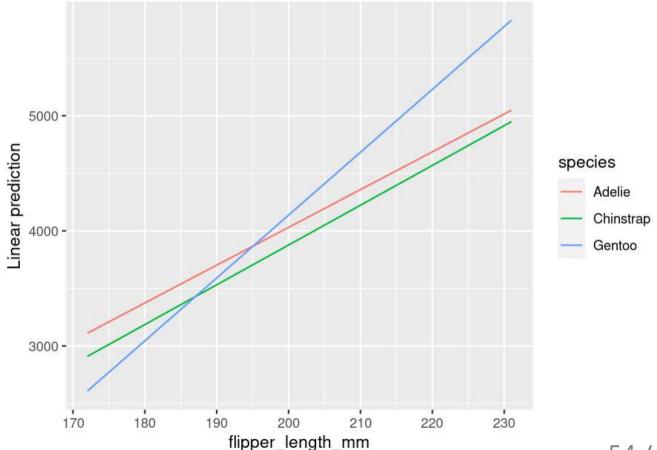
Best way is to use a figure at the same time!

- The effect of Flipper Length on Body Mass is **not** different between Adelie and Chinstrap penguins (P value = 0.825)
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# Visualizing Interactions

emmip(m, species ~ flipper\_length\_mm, cov.reduce = range)

- Here, Linear prediction = y = Body Mass
- Adelie and Chinstrap penguins have similar effects (i.e. slopes are **not** significantly different)
- Gentoo has a larger effect (i.e. slope is significantly larger) than either Adelie or Chinstrap penguins



# Homework (Practice)\*

Consider bill depth your response variable and species and year your predictor variables

1. Convert year to a categorical variable and remove Gentoo penguins

```
penguins_sub <- mutate(penguins, year = factor(year))
penguins_sub <- filter(penguins_sub, species != "Gentoo")</pre>
```

- 2. Create a figure comparing bill depth to species and year. Think about how to best tease apart the relationships.
- 3. Model the relationship between bill depth and the interaction between species and year.
- 4. Check diagnostics
- 5. How does the relationship of species and bill depth change among years?