

1.

```
GNU nano 2.0.6 File: matches_part.txt
Match 0:A - Y
Match 1:B - Z
Match 2:C - X
```

Solution 1 is correct.

Each company will receive their favorite student

2.

Best run time:

```
63 public static void execute(){
64     // copied pseudocode and converted java
65     while(!sue.isEmpty()){
66         int e = (int) sue.pop();
67         int s = pq[e].poll().getValue();
68         int eTemp = students[s];
69         if(students[s] == -1 ){
70             students[s] = e;
71             employers[e] = s;
72         }else if(a[s][e] < a[s][eTemp]){
73             students[s] = e;
74             employers[e] = s;
75             employers[eTemp] = -1;
76             sue.push(eTemp);
77         }else{
78             sue.push(e);
79         }
80     }
81 }
82 }
```

*Handwritten annotations:*

- $O(\log(n))$  points to the `poll().getValue()` operation.
- $n(\log(n))$  points to the `while` loop.
- $n$  points to the `sue.push(e)` operation.
- best case* is written near the `while` loop.

Poll has a runtime of  $O(\log(n))$

Assuming each match is created on first attempt for  $n$  employees and  $n$  employers the best runtime is  $n(\log(n))$

Worst run time:

$n^2(\log(n))$

Until all matches are complete each Employers requests their most favored student, the student then says maybe, and it is saved until the student gets requested by a company, they favor the most, this is done until it cannot be optimised more. Therefore it can take up to  $n^2$  time.

3.

a)

Code:

```
public static boolean isCorrectMatch(int[]e, int[]s,int[][]a,int[][]b){
    for(int i=0; i < e.length;i++){
        int cur = s[i];
        int r = b[i][cur];
        for(int j = 0; j < r;j++){//check if there is a student ranked better for the company
            int sMatch = -1;
            for(int k = 0; k< e.length; k++){//check how student ranked company and if there is a better match
                if(e[k] == j){
                    sMatch = k;
                    if(a[j][sMatch] > a[j][i]){//check if student match is ranked higher for from current student
                        return false;
                    }break;}
                }}}return true;}
```

Verification:

With non-stable match (example from pdf):

```
public static void main(String[] args){
    int[] e = {0,1,2}; //company A, company B, company C
    int[] s = {0,1,2}; // student x, student y, student z
    int[][] a = {{0,1,2},
                 {0,2,1},
                 {1,2,0}};
    int[][] b = {{0,1,2},
                 {0,1,2},
                 {0,1,2}};

    [DARSYS-MBP-5947:Desktop stodorovic$ java match
false]
```

With stable match (example from pdf):

```
int[] e = {0,1,2}; //company A, company B, company C
int[] s = {0,2,1}; // student x, student z, student y
int[][] a = {{0,1,2},
              {0,2,1},
              {1,2,0}};
int[][] b = {{0,1,2},
              {0,1,2},
              {0,1,2}};

[DARSYS-MBP-5947:Desktop stodorovic$ java match
true
DARSYS-MBP-5947:Desktop stodorovic$ ]
```

b)

```
public static boolean isCorrectMatch(int[]e, int[]s,int[][]a,int[][]b){
    for(int i=0; i < e.length;i++){
        int cur = s[i];
        int r = b[i][cur];
        for(int j = 0; j < r;j++){//check if there is a student ranked better for t
            int sMatch = -1;
            for(int k = 0; k< e.length; k++){//check how student ranked company and i
                if(e[k] == j){
                    sMatch = k;
                    if(a[j][sMatch] > a[j][i]){//check if student match is ranked higher fo
                        return false;
                    }break;}
                }}}return true;}
```

*Handwritten annotations:* A bracket on the left side of the innermost loop (for k) spans from its start to the end of the function, with a label  $n^3$  next to it. Another bracket is placed above the innermost loop, spanning from its start to the end of the middle loop (for j), with a label  $n$  next to it.

Worst runtime is  $O(n^3)$