EECE6036 - Homework 3

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1 Problem 1

1.1 Problem Summary

The goal of this problem is to create a multi-layer feed-forward neural network for classification of the MNIST dataset. The network was trained using gradient descent with back-propagation with momentum, and is trainable for arbitrary amounts and sizes of hidden layers. During training, the loss is calculated using J_2 loss with threshold values. For performance measurement, the loss is calculated as $1 - hit_rate$ using winner-take-all on the output layer to define the predicted class.

1.2 Results

1.2.1 System Description

Table 1 shows the hyper-parameters used in training the classifier. These hyper-parameters were found empirically, considering both minimizing the final loss and training time. More work can to find more optimal hyper-parameters, but this set of hyper-parameters produces pretty good results.

Table 1: Classifier Training Hyper-Parameters

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Parameter	Value	Description
$hidden_layer_size$	192	Neurons in hidden layer
$\mid \eta \mid$	0.05	Learning rate
α	0.8	Momentum
max_epochs	500	Maximum training epochs
$\mid L$	0.25	Lower activation threshold
$\mid H \mid$	0.75	Upper activation threshold
patience	3	Patience before early stopping
es_delta	0.01	Delta value for early stopping

Weight initialization is done randomly on a uniform distribution between (-a, +a) where $a = \sqrt{\left(\frac{6}{N_{source} + N_{target}}\right)}$, and N_{source} and N_{target} are the numbers of neurons on the source and target layers respectively.

The network utilizes early stopping by monitoring a validation set, which consists of 1000 training points that are set aside before training. If the validation loss does not improve for patience steps (1 step = 10 epochs), training halts. The validation is considered improved if the validation is es_delta lower than the previous improved validation loss. The weights used by the final network are the weights from the epoch with the lowest validation loss. To improve the frequency of checking for early stopping, the network only uses 1000 training points per epoch.

1.2.2 Network Results

Throughout the duration of training, the loss of the training and validation sets was tracked every 10 epochs. Figure 1 shows a plot of the loss values while training the classifier. The vertical line designates the point where the validation error is minimized, which occurs at epoch 50. The weights at that epoch are the weights used in the final network, where the test loss is 0.070.

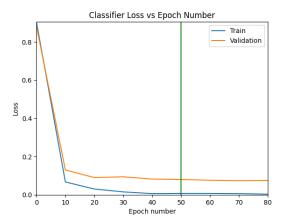


Figure 1: Training and validation loss of the classifier.

Figure 2 shows the confusion matrices for the train and test sets using the weights from the best epoch.

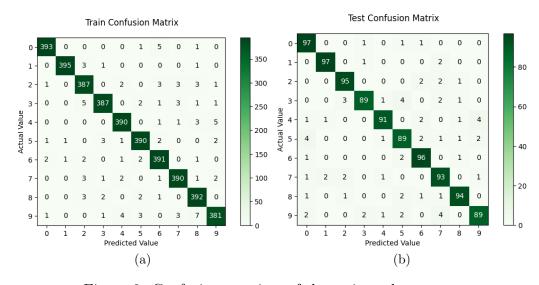


Figure 2: Confusion matrices of the train and test sets.

1.3 Discussion and Analysis of Results

Overall, the results look pretty good. The best weights happen pretty early at epoch 50 and get a fairly low loss of 0.070. While testing hyper-parameters, it was observed that when es_delta is set to 0 and patience is increased to around 5, the test loss would sometimes get as low as 0.05, but that generally occurred after several hundred epochs and is also dependent on weight initialization numbers and dataset shuffling during training. With the early stopping hyper-parameters used by this model, it sacrifices some performance, but it trains significantly faster, making these hyper-parameters ideal for implementing and troubleshooting the network from scratch.

The diagonal of the confusion matrices in Figure 2 is very dark, with hardly any coloring in the incorrect boxes. Many of the incorrect classifications are in two classes which look similar. For example, Figure 2a shows four 9s classified as 4s and five 4s classified as 9s. This mix-up makes a lot of sense, because the shapes of 4s and 9s tend to be similar, especially with some of the sloppy handwriting in MNIST.

1.4 Conclusion

This multi-layer feed-forward neural network classifier is able to effectively classify the MNIST dataset given in this problem. While the results are certainly not state-of-the-art, the trained network classifies over 90% of the test set digits correctly. Further testing in optimizing the hyper-parameters of the network can help to improve the accuracy even further.

2 Problem 2

2.1 Problem Summary

The goal of this problem is to create a multi-layer feed-forward neural network similar to Problem 1, except in this case it will be trained to be an autoencoder. This network has the same features as the network in Problem 1, except the performance measurement is calculated using J_2 loss instead of $1 - hit_rate$. Additionally, winner-take-all is not used in the output layer, because it does not make sense in the context of an autoencoder.

2.2 Results

2.2.1 System Description

Table 2 shows the hyper-parameters used in training the autoencoder. As with the classifier, these hyper-parameters were found empirically with the same consideration for minimizing final loss and training time.

Table 2: Autoencoder Training Hyper-Parameters

Parameter	Value	Description
$hidden_layer_size$	192	Neurons in hidden layer
η	0.005	Learning rate
α	0.8	Momentum
max_epochs	500	Maximum training epochs
L	0	Lower activation threshold
H	1	Upper activation threshold
patience	3	Patience before early stopping
es_delta	0.1	Delta value for early stopping

The weight initialization process is the same as in Problem 1, as are the processes for allocating the validation set and applying early stopping.

2.2.2 Network Results

Throughout the duration of training, the loss of the training and validation sets was tracked every 10 epochs. Figure 3 shows a plot of the loss values while training the autoencoder. The vertical line designates the point where the validation error is minimized, which occurs at epoch 160. The weights at that epoch are the weights used in the final network, where the test loss is 2.087.

After training, the loss in each class was measured. Figure 4 shows the loss of each class for the train and test sets using the weights from the best epoch.

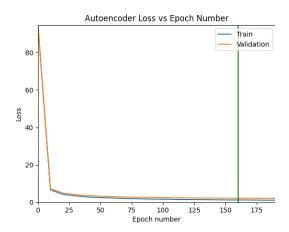


Figure 3: Training and validation loss of the autoencoder.

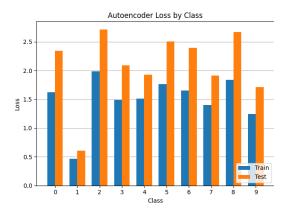


Figure 4: Loss of each class of the train and test sets.

2.2.3 Features

After training, the features learned by 20 arbitrary neurons in the hidden layer of both the classifier and autoencoder were observed by normalizing the weights from 0 to 1 and then displaying them like an image. The images are mapped so 1 is white and 0 is black. Figure 5 shows the features of the classifier, and Figure 6 shows the features of the autoencoder.

2.2.4 Sample Outputs

After training, the outputs of eight random data points from the test set were fed reconstructed the autoencoder, meaning the input data point was presented to the network and the output "prediction" was obtained. Figure 7 shows the original and reconstructed images.

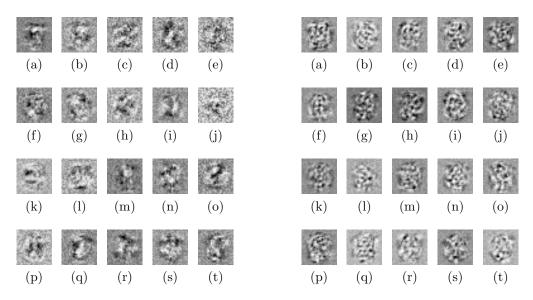


Figure 5: Classifier features.

Figure 6: Autoencoder features.

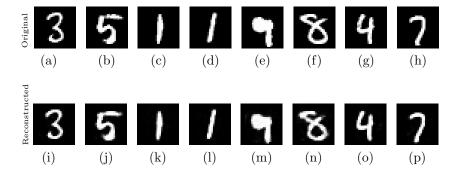


Figure 7: Original (top) and reconstructed (bottom) data points.

2.3 Discussion and Analysis of Results

Overall, the results look pretty good. The autoencoder takes longer to train, with its best weights occurring at epoch 160 with a loss of 2.087. In Figure 4, the loss for the 1s is particularly salient because it is drastically lower than the other classes loss values. This makes sense because a 1 is simply a straight line, so it should be quite simple to recognize and then reconstruct. While none of the loss values are as noticeably high as 1's loss is low, classes 2, 8, and 5 all have loss values above 2.5. I do not have any intuition as to why those numbers have the highest loss, but those digits are kind of similar in the sense that a 2 is roughly a backward 5, and stacking a 2 on top of a 5 roughly makes an 8. At first, I was surprised that 6 has a higher loss than

9, because 6 is just an upside-down 9, but it makes sense that 5 and 6 have similar features and ended up having similar loss values.

The features in Figure 5 and Figure 6 are somewhat difficult to interpret. Between the two feature sets, there is a trend where the center of the image appears to have some distinct patterns, while the edge of the image is either somewhat uniform gray or random TV static. In Figure 5, the shapes generally seem to be lines or curves, while in Figure 6 the features look like a bunch of dark dots with a few brighter spots.

2.4 Conclusion

This multi-layer feed-forward neural network autoencoder is able to effectively reconstruct digits from the MNIST dataset. Further testing in optimizing the hyper-parameters of the network can help to improve the reconstruction accuracy even further.

A Code

A.1 dataset.py

```
from settings import *
import numpy as np
import pathlib
import matplotlib.pyplot as plt
def shufflePair(data, labels):
    '''Shuffle a pair of data and labels in place
    Parameters:
            data, labels : np.ndarray
Data and labels to be shuffled
      Returns:
      assert len(data) == len(labels), \
      'Size mismatch between data and labels'
indeces = np.random.permutation(len(data))
data[...] = data[indeces]
      labels[...] = labels[indeces]
if __name__ == '__main__':
    # # Define important values from settings
         SEED = 69420
      # SEED = 69420
# CODE_DIR = pathlib.Path(__file__).parent.absolute()
# DATA_FILE = CODE_DIR.joinpath('data.txt')
# LABEL_FILE = CODE_DIR.joinpath('labels.txt')
# DATASET_DIR = CODE_DIR.joinpath('dataset')
# DATASET_DIR = CODE_DIR.joinpath('dataset')
# DATASET_DIR.Mkdir(mode=00755, exist_ok=True)
# TRAIN_DATA_FILE = DATASET_DIR.joinpath('train_data.npy')
# TRAIN_LABELS_FILE = DATASET_DIR.joinpath('train_labels.npy')
# TEST_DATA_FILE = DATASET_DIR.joinpath('test_data.npy')
# TEST_LABELS_FILE = DATASET_DIR.joinpath('test_labels.npy')
# Seed for consistency
# TRAIN_DATA_STILE = DATASET_DIR.joinpath('test_labels.npy')
      np.random.seed(SEED)
      # Import dataset
      # Check that the files exist
assert DATA_FILE.exists(), f'File not found: {str(data_file)}'
assert LABEL_FILE.exists(), f'File not found: {str(label_file)}'
# Read data and labels from txt file
      data = list()
      with open(DATA_FILE) as data_f:
      data = data_f.readlines()
data = [d.split() for d in data]
      labels = list()
with open(LABEL_FILE) as label_f:
    labels = label_f.readlines()
labels = [int(1) for 1 in labels]
# Make images and sort into bins based on class
data_points = dict()
classes = list()
for d, 1 in zip(data, labels):
    if 1 not in classes:
        classes annend(1)
      labels = list()
                   classes.append(1)
             data_points[1] = list()
data_points[1].append(d)
      classes.sort()
      # Turn data lists into numpy arrays
      for 1 in classes:
             data_points[1] = np.array(data_points[1], dtype=np.float64)
      # Partition dataset
      train_data = list()
train_labels = list()
      train_labels = list()
test_labels = list()
# Shuffle the data points first
for l in classes:
             np.random.shuffle(data_points[1])
```

A.2 layer.py

```
~~~~~
import numpy as np
class Layer:
    def __init_
             self.
              weight_file = None,
num_neurons = None,
         ): \hbox{$^{\prime\prime}$ initialize Layer object either randomly or by a weight file}
              weight_file : str, optional
File to load pre-existing weights from
num_neurons, inputs : int, optional
Number of hidden neurons and inputs to the layer
         Returns:
             Layer
                   The Layer object which was constructed
         if weight_file:
    self.loadWeights(weight_file)
              self.num_neurons = self.w.shape[0]
self.inputs = self.w.shape[1] - 1
              self.num_neurons = num_neurons
              self.inputs = inputs
self.initW()
         # States to save for back-prop
self.x = None # Input for current pass
         self.s = None # Net inputs pre-activation function
self.y = None # Final output of the layer
self.delta = None # Delta of this layer
         self.w_change = np.zeros(self.w.shape) # Weight changes
           ''Initialize weights for the perceptron using Xavier initialization
         Parameters:
              None
         Returns:
         None
         w_shape = (self.num_neurons, self.inputs + 1)
```

```
a = np.sqrt(6 / (self.inputs + self.num_neurons))
self.w = np.random.uniform(-a, a, size=w_shape)
self.w_change = np.zeros(self.w.shape)
def forwardPass(self, x):
    '''Pass the input forward through the layer
       Parameters:
      x : np.ndarray of np.float64
            np.array of np.float64
Output of the layer
       # Add bias input
x = np.concatenate(([1], x))
# Save inputs for back-prop
self.x = x
       seii.x = x
# Dot product weights * inputs
self.s = np.matmul(self.w, x)
# Pass through sigmoid activation
self.y = 1.0 / (1 + np.exp(-1 * self.s))
return self.y
def setDelta(self):
    '''Calculate delta value, different for Output and Hidden layer
    Must be implemented per-class
       raise NotImplementedError('Cannot call from Layer class')
def getWChange(self, eta=1, alpha=0.1):
       '''Calculate weight updates for the most recent forward pass
Requires delta to be calculated (varies between hidden/output layers)
            eta : float
      Learning rate for weight adjustments alpha: float
Momentum scalar
Returns:
       None
       # Set delta value
       self.setDelta()
      self.setDelta()
# Pre-scale weight change for momentum
self.w_change *= alpha
# Calculate new weight change
d = self.delta.reshape(len(self.delta), 1)
x = self.x.reshape(1, len(self.x))
new_change = eta * np.matmul(d, x)
self.w_change += new_change
def changeW(self):
       '''Apply w_change to the weights
Parameters:
             None
       Returns:
       self.w += self.w_change
def saveWeights(self, weight_file):
    '''Save weights to a file
       Parameters:
             weight_file : str
                    File name to save weights in
       Returns:
       np.save(str(weight_file), self.w)
def loadWeights(self, weight_file):
         ''Save weights to a file
       Parameters:
             weight_file : str
   File name to save weights in
```

A.3 output_layer.py

```
# Imports
·· ------
from layer import Layer
import numpy as np
class OutputLayer(Layer):
    def setLabel(self, label):

'''Set the labels for this batch
Needed for calculating delta for this layer
         Parameters:
        label : np.ndarray
One-hot encoded label
Returns:
        None
         self.label = label
    def setDelta(self):
           'Calculate delta for the output layer
         Parameters:
             None
         Returns:
        None
        e = self.label - self.y
        y_der = self.y * (1 - self.y)
self.delta = e * y_der
    def thresholdOutputs(self, L, H):
    '''Threshold outputs based on the labels
         Parameters:
        _, ... iroat

Low and high thresholds for outputs Returns:
        self.y[(self.y <= L) * (self.label == 0)] = 0
self.y[(self.y >= H) * (self.label == 1)] = 1
if __name__ == '__main__':
    print('Warning: Tests for this file are deprecated')
```

A.4 hidden_layer.py

```
Matrix of weight values for the next layer
delta : np.ndarray
Matrix of delta values for the next layer
Returns:
------
None
'''
self.downstream_sum = np.matmul(w[:,:-1].transpose(), delta)

def setDelta(self):
'''Calculate delta for the hidden layer
Parameters:
------
None
Returns:
------
None
Returns:
------
y''
# Derivative of sigmoid using last forward pass
output_der = self.y * (1 - self.y)
self.delta = output_der * self.downstream_sum

if __name__ == '__main__':
    print('Warning: Tests for this file are deprecated')
```

A.5 mlp.py

```
# Imports
# Custom imports
from settings import *
from dataset import shufflePair
from hidden_layer import HiddenLayer from output_layer import OutputLayer
# External imports import numpy as np
import enlighten # Progress bar for training
class MLP:
    def __init__(
           input_size=INPUTS,
       ):
'''Initialize Multi-Layer Perceptron object
           input_size : int
   Number of inputs to the network
        # Initialize parameters
self.layers = list()
        self.input_size = input_size
    def addLayer(self, file_name=None, neurons=None, output=False):
        '''Add a layer to the network
        if len(self.layers) == 0:
   input_size = self.input_size
        else:
            input_size = self.layers[-1].num_neurons
        if file_name:
            if output:
                self.layers.append(OutputLayer(weight_file=file_name))
               self.layers.append(HiddenLayer(weight_file=file_name))
        else:
            if output:
    self.layers.append(OutputLayer(num_neurons=neurons,
                   inputs=input_size))
                self.layers.append(HiddenLayer(num_neurons=neurons,
                    inputs=input_size))
    def predict(self, data, one_hot):
        ''','Predict the output given an input Parameters:
            data : np.ndarray
Data point to predict on
```

```
one_hot : bool
                        Whether the output should be one-hot or raw
        Returns:
               np.ndarray
Array of prediction
        # Forward pass through all the layers
layer_output = data
         for 1 in self.layers:
        layer_output = 1.forwardPass(layer_output)
if one_hot:
    max_idx = np.argmax(layer_output)
                 pred = np.eye(10)[max_idx]
        else:
        pred = layer_output
return pred
def trainPoint(self, data, label, eta, alpha, L, H):
    '''Update the weights for a single point
    Parameters:
                data : np.ndarray
                The data point
labels : np.ndarray
One-hot encoded label
eta : float
                Learning rate alpha : float
                Momentum scalar
L, H : float, optional
Low and high thresholds for training
        # Weight change for last layer
        # weight change for last layer
self.predict(data, one_hot=False)
self.layers[-i].setLabel(label)
self.layers[-i].thresholdOutputs(L, H)
self.layers[-i].getWChange(eta, alpha)
# Back-prop error
        for i in range(len(self.layers)-2, -1, -1):
                down_w = self.layers[i+1].w
down_delta = self.layers[i+1].delta
                self.layers[i].setDownstreamSum(down_w, down_delta)
self.layers[i].getWChange(eta, alpha)
        # Apply weight changes
for 1 in self.layers:
1.changeW()
def logError(self,
                train_data
                 train_labels,
                 valid_data,
                 valid_labels
                 epoch_num,
       ):
'''Log error for train/test data for a given epoch
        Parameters:
                train_data : np.ndarray
   Array of data points for the train set
train_labels : np.ndarray
   Array of labels for the train set
                valid_data : np.ndarray
Array of data points for the validation set
valid_labels : np.ndarray
Array of labels for the validation set
epoch_num : int
                        The current epoch number
        # Evaluate and log train error
train_err = self.eval(train_data, train_labels)
        train_err = seif.eval(train_data, train_labels)
self.train_err.append(train_err)
# Evaluate and log test error
valid_err = self.eval(valid_data, valid_labels)
self.valid_err.append(valid_err)
        self.valid_err.append(valid_err)
# Record epoch number
self.epoch_num.append(epoch_num)
# Print out metrics
print(f'Epoch {epoch_num}')
print(f'\tTrain Loss:\tt\tfrain_err:0.03f\')
print(f'\tValidation Loss:\t{valid_err:0.03f\')
def train(
```

```
self,
      labels.
      points_per_epoch,
      valid_points,
      max_epochs,
      eta,
      alpha,
     patience, es_delta,
      save_dir,
):
'''Train the network up to the desired number of epochs
Parameters:
     data : np.ndarray
Array of training data points
labels : np.ndarray
Array of training labels
      nilay of titaling and points.per_epoch : int
Number of training points to use in each epoch
      Number of training points to set aside for validation
      These points are set aside before training max_epochs : int
Maximum number of epochs to train
      eta : float
          Learning rate
      alpha : float
           Momentum scalar
     L, H : float
Low and high thresholds for training
           Amount of epochs with no improvement before early stopping
          Required improvement for early stopping
      save_dir : pathlib.Path or str
Directory to save best model parameters in
# Initialize progress bar
pbar_manager = enlighten.get_manager()
self.logError(
           train_data,
           train_labels, valid_data,
           valid_labels,
 # Iterate through epochs or until early stopping
impatience = 0
 self.best_weights_epoch = 0
best_loss = np.inf
for e in range(1, max_epochs+1):
    pbar.update()
    shufflePair(train_data, train_labels)
      epoch_train_data = train_data[:points_per_epoch]
epoch_train_labels = train_labels[:points_per_epoch]
for d, l in zip(epoch_train_data, epoch_train_labels):
      self.trainPoint(d, 1, eta, alpha, L, H)
# Log data every 10 epochs
if (e % 10) == 0:
           self.logError(
                      epoch_train_data
                      epoch_train_labels,
                      valid data.
                      valid_labels,
```

```
e,

)

# Check for early stopping

if ((best_loss - self.valid_err[-1]) >= es_delta):
        impatience = 0
        self.best_weights_epoch = e
        best_loss = self.valid_err[-1]
        for i, 1 in enumerate(self.layers):
            layer_name = save_dir.joinpath(f'layer_{i:02d}')
            l.saveWeights(layer_name)

else:
        impatience += 1
        # We have become too impatient
        if impatience >= patience:
            print(f'* * * Early stopping hit * * *')
        break

pbar.close()

if __name__ == '__main__':
    print('Warning: This file does not do anything.')
    print('Run either classifier.py or autoencoder.py.')
```

A.6 classifier.py

```
# Custom imports
from mlp import MLP
# External imports
import numpy as np
import matplotlib.pyplot as plt
class Classifier(MLP):
     def eval(self, data, labels):
    '''Evaluate error on a data set
            Parameters:
            data : np.ndarray
Array of data points
labels : np.ndarray
Array of labels for the data
Returns:
                 float
                        Error (1 - Hit Rate)
           correct = 0
for d, 1 in zip(data, labels):
    # Make prediction
    pred = self.predict(d, one_hot=True)
    # Check equality with label
    if (np.sum(np.abs(pred - 1)) == 0):
        correct += 1
hit_rate = correct / len(data)
return (1 - hit_rate)
if __name__ == '__main__':
    # Additional imports
    from settings import *
     import pathlib
import csv
# Seed for consistency
np.random.seed(SEED)
      # Delete old model
for f in CLASS_MODEL_DIR.iterdir():
    f.unlink()
      # Test network
      classifier = Classifier(input_size=INPUTS)
for h in HIDDEN_LAYER_SIZES:
            classifier.addLayer(neurons=h, output=False)
       classifier.addLayer(neurons=CLASSES, output=True)
      # Train the network
print('* * * Begin training classifier * * *')
classifier.train(
            train_data,
            train_labels,
            points_per_epoch=CLASS_POINTS_PER_EPOCH, valid_points=CLASS_VALID_POINTS,
```

```
max_epochs=CLASS_MAX_EPOCHS,
    eta=CLASS_ETA,
    alpha=CLASS_ALPHA,
    L=CLASS_L,
    H=CLASS_L,
    patience=CLASS_PATIENCE,
    es_delta=CLASS_ES_DELTA,
    save_dir=CLASS_MODEL_DIR,
)

# Plot loss over epochs
plt.figure()
plt.plot(classifier.epoch_num, classifier.valid_err)
plt.avxline(x=classifier.best_weights_epoch, c='g')
plt.legend(['Train', 'Validation'], loc='upper right')
plt.xlabel('Epoch number')
plt.xlabel('Epoch number')
plt.xlim([0, classifier.epoch_num[-1]])
plt.ylabel('Loss')
plt.ylim([0, max(max(classifier.train_err), max(classifier.valid_err))])
plt.savefig(str(CLASS_LOSS_PLOT), bbox_inches='tight', pad_inches=0)
plt.close()
# Save parameters to CSV
csv_rows = list()
csv_rows.append(['Parameter', 'Value', 'Description'])
csv_rows.append(['Shidden\\_layer\\\_size$', str(HIDDEn_LAYER_SIZES[0]),
    'Neurons in hidden layer'])
csv_rows.append(['$\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanha\tanh
```

A.7 autoencoder.py

```
import csv
    Seed for consistency
 np.random.seed(SEED)
 # Delete old model
for f in AUTO_MODEL_DIR.iterdir():
    f.unlink()
 # Training constants
# Test network
autoencoder = Autoencoder(input_size=INPUTS)
 for h in HIDDEN_LAYER_SIZES:
 autoencoder.addLayer(neurons=h, output=False)
autoencoder.addLayer(neurons=INPUTS, output=True)
 # Train the network
print('* * * Begin training autoencoder * * *')
autoencoder.train(
        train_data,
        train_data,
        points_per_epoch=AUTO_POINTS_PER_EPOCH, valid_points=AUTO_VALID_POINTS,
        max_epochs=AUTO_MAX_EPOCHS, eta=AUTO_ETA,
        alpha=AUTO_ALPHA,
        L=AUTO_L,
        H=AUTO_H,
        patience = AUTO_PATIENCE,
        es_delta=AUTO_ES_DELTA,
save_dir=AUTO_MODEL_DIR,
 plt.plot(autoencoder.epoch_num, autoencoder.train_err)
plt.plot(autoencoder.epoch_num, autoencoder.valid_err)
plt.axvline(x=autoencoder.best_weights_epoch, c='g')
plt.legend(['Train', 'Validation'], loc='upper right')
plt.title(f'Autoencoder Loss vs Epoch Number')
 plt.xlabel('Epoch number')
 plt.xlim([0, autoencoder.epoch_num[-1]])
plt.ylabel('Loss')
plt.ylim([0, max(max(autoencoder.train_err), max(autoencoder.valid_err))])
plt.savefig(str(AUTO_LOSS_PLOT), bbox_inches='tight', pad_inches=0)
csv_writer.writerows(csv_rows)
 # Write best epoch
with open(str(AUTO_BEST_EPOCH), 'w') as best_epoch_file:
    best_epoch_file.write(str(autoencoder.best_weights_epoch))
```

A.8 test_classifier.py

```
Array of data values
                       labels : np.ndarray
                       Array of labels as one-hot-vectors
plot_name : pathlib.Path or str
File name to save the matrix as
                       title :
                                            str
                                 Title of the confusion matrix
            Returns:
           plt.figure()
            plt.suptitle(title)
            plt.imshow(conf_mat, cmap='Greens')
           plt.imshow(conf_mat, cmap=')Greens')
for i in range(len(conf_mat)):
    for j in range(len(conf_mat[i])):
        color = 'k' if (conf_mat[i][j] <= 50) else 'w'
        plt.text(j, i, f'(int(conf_mat[i][j])}',
        va='center', ha='center', color=color)
plt.xlabel('Predicted Value')
plt.xticks(range(CLASSES))
plt.ylabel('Actual Value')
plt.xticks(range(CLASSES))</pre>
            plt.yticks(range(CLASSES))
plt.colorbar()
             plt.tight_layout()
            plt.savefig(str(plot_name), bbox_inches='tight', pad_inches=0)
            plt.close()
 # Seed for consistency
np.random.seed(SEED)
# File locations
# Load best weights back up and make confusion matrices
classifier = Classifier(input_size=INPUTS)
weight_files = sorted(CLASS_MODEL_DIR.iterdir())
for weight_file in weight_files[:-1]:
    classifier.addLayer(file_name=weight_file, output=False)
classifier.addLayer(file_name=weight_files[-1], output=True)
train_conf_title = 'Train Confusion Matrix'
makeConfMat(classifier, train_data, train_labels, CLASS_TRAIN_CONF,
    title=train_conf_title)
test_conf_title = 'Test Confusion Matrix'
makeConfMat(classifier, test_data, test_labels, CLASS_TEST_CONF,
    title=test_conf_title)
 np.random.seed(SEED)
 makeconfmat(classifier, test_data, test_labels, CL/
title=test_conf_title)
test_err = classifier.eval(test_data, test_labels)
print(f'Test error: {test_err:0.3f}')
with open(str(CLASS_TEST_LOSS), 'w') as loss_f:
    loss_f.write(f'{test_err:0.3f}')
```

A.9 test_autoencoder.py

```
def getLossByClass(autoencoder, data, labels):
       loss = list()
      form = first()
split_data = splitClasses(data, labels)
for i, d in enumerate(split_data):
    print(f'Evaluating class {i}')
             loss.append(autoencoder.eval(d, d))
       return loss
def getSamplePoints(data, n):
    '''Get sample points from the given data set
      Parameters:
            data : np.ndarray
            Array of data points n : int
                   Number of sample points
       Returns:
           np.ndarray
                   Reduced list of data points
      indeces = np.random.choice(np.arange(len(data)), 8, replace=False)
return data[indeces]
def drawSamples(autoencoder, data, num_samples, dir_name, title):
    '''Draw the output predictions and save them
             autoencoder : Autoencoder
             Autoencoder for use in inference
data : np.ndarray
Array of data points
             num_samples : int
             Number of sample points
dir_name : str
Name of the directory to save the images to
             title : str
Title of the plot
       sample_points = getSamplePoints(data, num_samples)
       for i, d in enumerate(sample_points):
    d_name = dir_name.joinpath(f'orig_{i}.png')
             matplotlib.image.imsave(str(d_name), d.reshape(28, 28, order='F'), cmap='Greys_r')
pred = autoencoder.predict(d, one_hot=False)
p_name = dir_name.joinpath(f'pred_{i}.png')
matplotlib.image.imsave(str(p_name), pred.reshape(28, 28, order='F'), cmap='Greys_r')
# Seed for consistency
np.random.seed(SEED)
# Load best weights back up
autoencoder = Autoencoder(input_size=INPUTS)
weight_files = sorted(AUTO_MODEL_DIR.iterdir())
for weight_file in weight_files[:-1]:
autoencoder.addLayer(file_name=weight_file, output=False)
autoencoder.addLayer(file_name=weight_files[-1], output=True)
# Test on all data and draw samples
test_err = autoencoder.eval(test_data, test_data)
print(f'Test loss: {test_err:0.3f}')
sample_title = 'Autoencoder Sample Outputs'
drawSamples(autoencoder, test_data, 8, AUTO_SAMPLE_DIR, sample_title)
# Graph loss by class
print('Testing train set')
train_loss = getLossByClass(autoencoder, train_data, train_labels)
print('Testing test set')
test_loss = getLossByClass(autoencoder, test_data, test_labels)
x = np.arange(len(train_loss))
plt.figure()
rect_width = 0.35
rect_width = 0.35
plt.bar(x-rect_width/2, train_loss, rect_width, label='Train')
plt.bar(x+rect_width/2, test_loss, rect_width, label='Test')
plt.title('Autoencoder Loss by Class')
plt.xlabel('Class')
plt.xticks(x)
plt.ylabel('Loss')
plt.grid(axis='y')
plt.gca().set_axisbelow(True)
plt.legend(loc='lower right')
plt.tight_layout()
plt.savefig(str(AUTO_BAR), bbox_inches='tight', pad_inches=0)
with open(str(AUTO_TEST_LOSS), 'w') as loss_f:
```

A.10 features.py

```
# Imports
 # Custom imports
 from settings import *
from classifier import Classifier
from autoencoder import Autoencoder
 # External imports
# External imports
import numpy as np
import pathlib
import matplotlib
import matplotlib.pyplot as plt
def drawFeatures(weights, dir_name):
    '''Draw the output predictions and save them
        Parameters:
               weights : np.ndarray
   Array of weights for the neurons
dir_name : str
   Name of the directory to save the images to
        for i, w in enumerate(weights):
                # Remove bias and normalize on [0, 1]
               cmap='Greys_r')
 # Seed for consistency
# Seed for consistency
np.random.seed(SEED)
# Load best weights back up for each model
autoencoder = Autoencoder(input_size=INPUTS)
for weight_file in sorted(AUTO_MODEL_DIR.iterdir()):
    autoencoder.addLayer(file_name=weight_file)
classifier = Classifier(input_size=INPUTS)
for weight_file in sorted(CLASS_MODEL_DIR.iterdir()):
    classifier.addLayer(file_name=weight_file)
# Neurons to check
classifier.addLayer(file_name=weight_file)
# Neurons to check
neuron_count = classifier.layers[0].num_neurons
neurons = np.random.choice(np.arange(neuron_count), 20, replace=False)
class_weights = classifier.layers[0].w[neurons]
drawFeatures(class_weights, CLASS_FEAT_DIR)
auto_weights = autoencoder.layers[0].w[neurons]
drawFeatures(auto_weights, AUTO_FEAT_DIR)
```