

Control Theory
Assignment #1

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1. Using Laplace transform, solve $10y''(t) + 150y'(t) + 500y = 2 + 7e^{-t}$ for $y(t)$, given the initial conditions $y(0) = 9$ and $y'(0) = 6$. Confirm your solution using MATLAB.
2. Find the steady-state value for the system that is described by the differential equation above.
3. You are given a transfer function:

$$H(s) = \frac{1}{2s^2 + 20s + C}$$

Find the interval of C for which the system is stable using the knowledge of the poles placement in the complex plane, using the Hurwitz criterion, and using the Routh-Shur criterion.

Note: Since the poles are placed in the complex domain, remember to expand all your calculations to the complex domain as well!

4. Using MATLAB, for the $H(s)$ given above and $C = 512$, find the *rise time*, *settling time*, *peak time*, *peak value*, and *overshoot*. Also, plot the *impulse response* and *step response*.