

Then, focusing on  $G$ ,

$$\begin{aligned}
 G_m &= \operatorname{argmin}_G \sum_{i=1}^N w_i^{(m)} \exp\{y_i \frac{\alpha}{2} G(x_i)\} \\
 &= \operatorname{argmin}_G \left( \sum_{G(x_i)=y_i} w_i^{(m)} \exp\{-\frac{\alpha}{2}\} + \sum_{G(x_i) \neq y_i} w_i^{(m)} \exp\{\frac{\alpha}{2}\} \right) \\
 &= \operatorname{argmin}_G \left( \exp\{-\frac{\alpha}{2}\} \sum_{i=1}^N w_i^{(m)} + \right. \\
 &\quad \left. + \left( \exp\{\frac{\alpha}{2}\} - \exp\{-\frac{\alpha}{2}\} \right) \sum_{G(x_i) \neq y_i} w_i^{(m)} \right) \\
 &= \operatorname{argmin}_G \left( \exp\{-\frac{\alpha}{2}\} \sum_{i=1}^N w_i^{(m)} + \right. \\
 &\quad \left. + \left( \exp\{\frac{\alpha}{2}\} - \exp\{-\frac{\alpha}{2}\} \right) \sum_{i=1}^N w_i^{(m)} I(G(x_i) \neq y_i) \right)
 \end{aligned}$$

so  $G_m = \operatorname{argmin}_G \sum_{i=1}^N w_i^{(m)} I(y_i \neq G(x_i))$ . For the explanation of the steps, see lecture 11 notes (page 4).

Focusing on  $\alpha$ , instead,

$$\alpha_m = \operatorname{argmin}_{\alpha} \sum_{i=1}^N w_i^{(m)} \exp\{y_i \frac{\alpha}{2} G(x_i)\}$$

Deriving with respect to  $\alpha$

$$\begin{aligned}
 & - \sum_{G(x_i)=y_i} w_i^{(m)} \exp\{-\frac{\alpha}{2}\} + \sum_{G(x_i) \neq y_i} w_i^{(m)} \exp\{\frac{\alpha}{2}\} = 0 \\
 & - \sum_{G(x_i)=y_i} w_i^{(m)} + \sum_{G(x_i) \neq y_i} w_i^{(m)} \exp\{\alpha\} = 0 \\
 & \exp\{\alpha\} \frac{\sum_{G(x_i) \neq y_i} w_i^{(m)}}{\sum_{i=1}^N w_i^{(m)}} = \frac{\sum_{G(x_i)=y_i} w_i^{(m)}}{\sum_{i=1}^N w_i^{(m)}}
 \end{aligned}$$

and

$$\alpha_m = \log \left( \frac{1 - \operatorname{err}_m}{\operatorname{err}_m} \right)$$

where

$$\operatorname{err}_m = \frac{\sum_{i=1}^N w_i^{(m)} I(y_i \neq G_m(x_i))}{\sum_{i=1}^N w_i^{(m)}}$$