



**MACQUARIE**  
University

# Quantitative Genetics (1)

## LECTURE 5: HERITABILITY

2022



# Background

## Quantifying VG

- so far limited to single locus

H, A, ne, P,

- Looking at genetics from a phenotypic level

- Used to attribute causality to traits (nature vs. nurture)

## Causal agents of phenotypes

- Alleles segregating at many loci

- Interactions among alleles (dominance and/or epistasis)

- Environmental effects

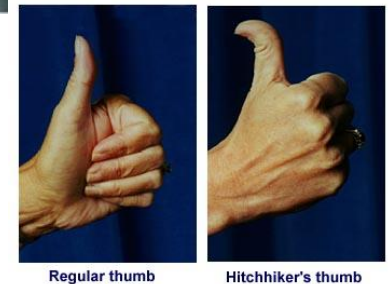
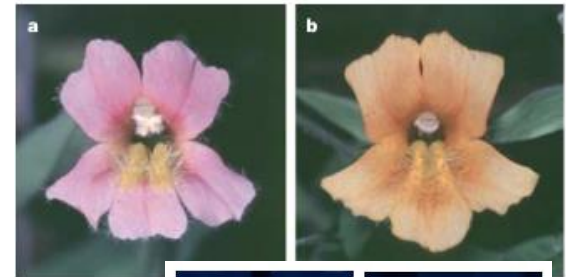
- Interactions & correlations between genetic and environmental effects

# Lecture Outline

- Quantitative and Qualitative Traits
- History of Heritability
- Heritability ( $H^2$ ) and Genetic Causes
- Relationship with Conservation Biology
- Worked Example for  $H^2$  (ANOVA)
- GxE Interaction
- Phenotypic Plasticity

# ‘Mendelian loci’

- Blood Type (A, B, O, AB)
- Flower colour (yellow, pink)
- Thumb shape
- Coat colour (black, orange –X linked)
- Goat beard (beard, no beard)
- Phenotypes take discrete values
- Predictable using Mendel’s laws



22,480 known Mendelian traits in man  
(as of 14 Aug 2014), OMIM:

<http://www.omim.org/>

3,057 known Mendelian traits in animals,  
OMIA: <http://omia.angis.org.au/home/>

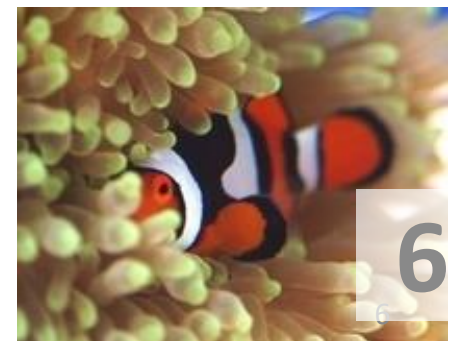
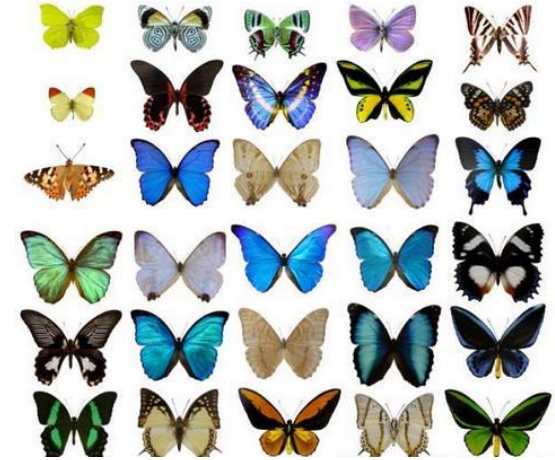
# Quantitative genetics

- The genetic appraisal and analysis of '**complex**', '**continuous**', or '**quantitative**' traits, where:
- A quantitative trait = a trait whose phenotypic expression is determined by many individual genes (i.e. variation at many individual loci) (polygenic)



# Examples of Quantitative Traits:

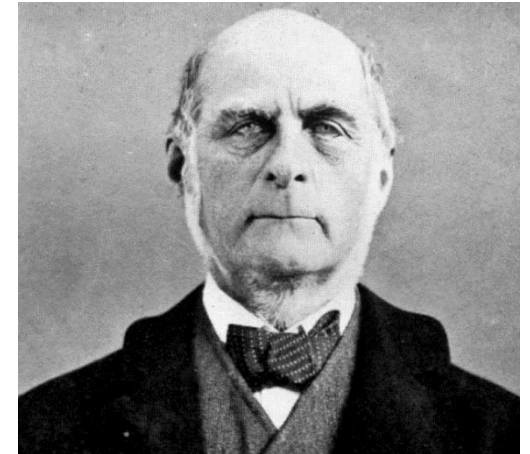
- Morphological traits:
  - Body size (height, weight)
  - Colouration (e.g. Bird plumage)
- Physiological traits
  - Enzyme activity
  - Blood pressure, cardiovascular performance
- Behavioural traits
  - Aggression, mate preferences, IQ etc.
- Life history traits
  - Developmental rates, age at maturity, etc.



# History of Quantitative Genetics

Francis Galton: 'the apostle of quantification'

- the weather (1863)
- height (1889)
- finger print patterns (1888; 1892; 1893)
- beauty (1909)
- boredom (1909)
- criminal characteristics (1885)
- the effectiveness of prayers (1872)



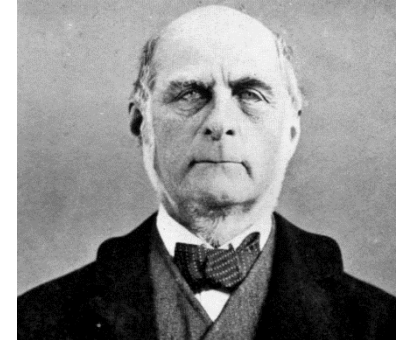
Introduced the terms 'nature' and 'nurture'  
(*English Men of Science*, 1874)



# History of Quantitative Genetics

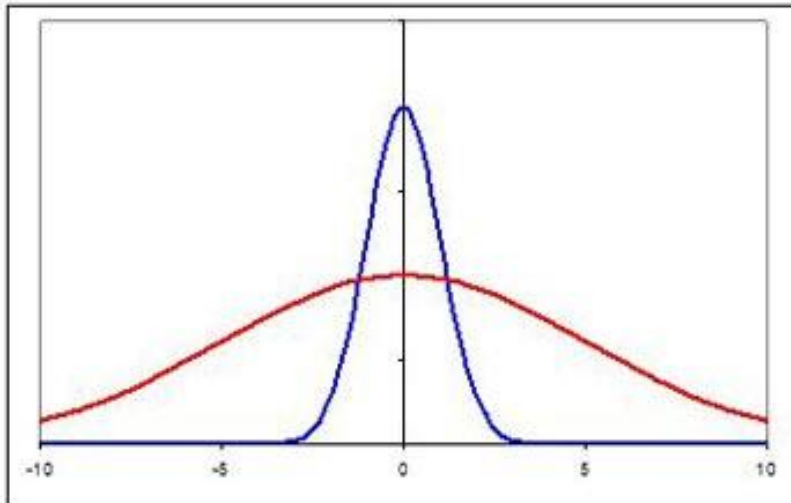
Francis Galton

Interested in *trait variation* rather than trait means

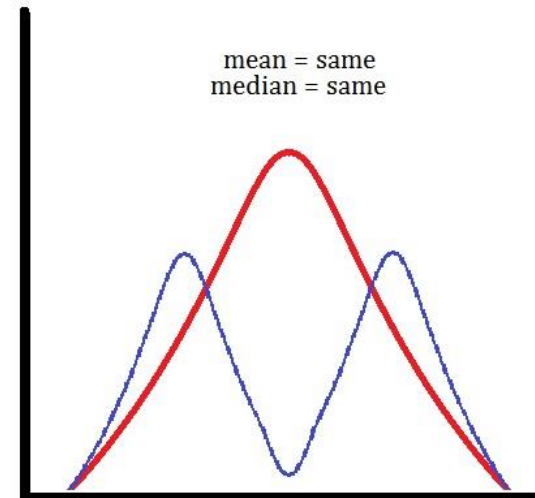


“It is difficult to understand why statisticians commonly limit their

er  
Th  
of  
w  
nu



reve  
harm  
s, w  
e th  
once



ews.  
tive  
and

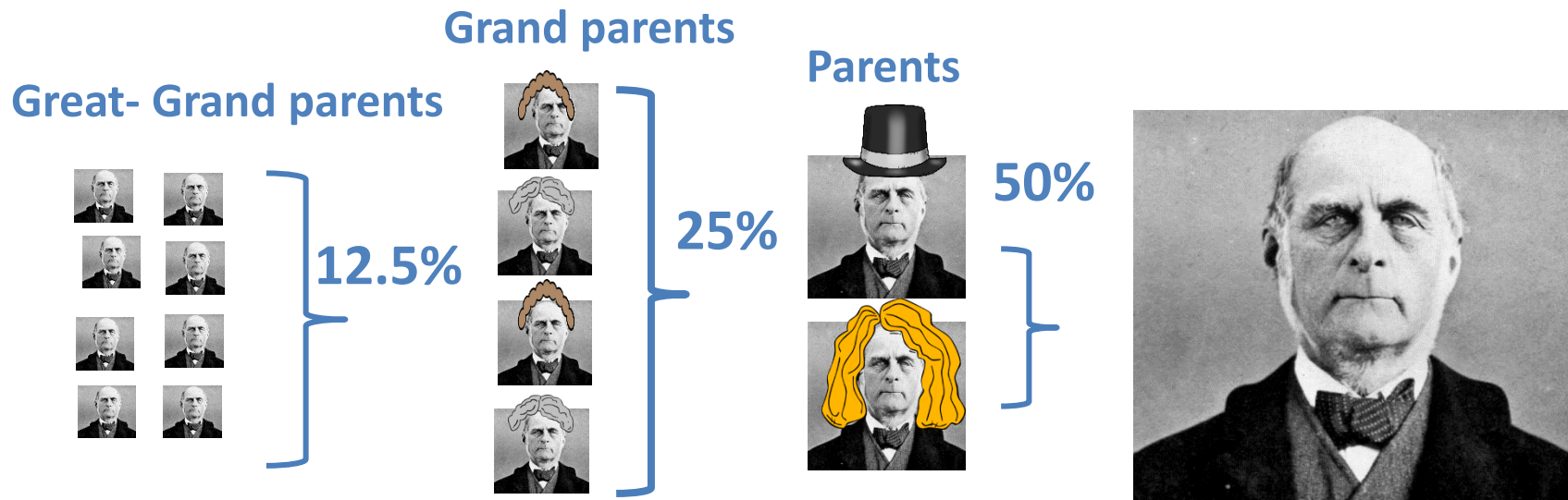


# History of Quantitative Genetics

## Francis Galton

### Different theory of inheritance:

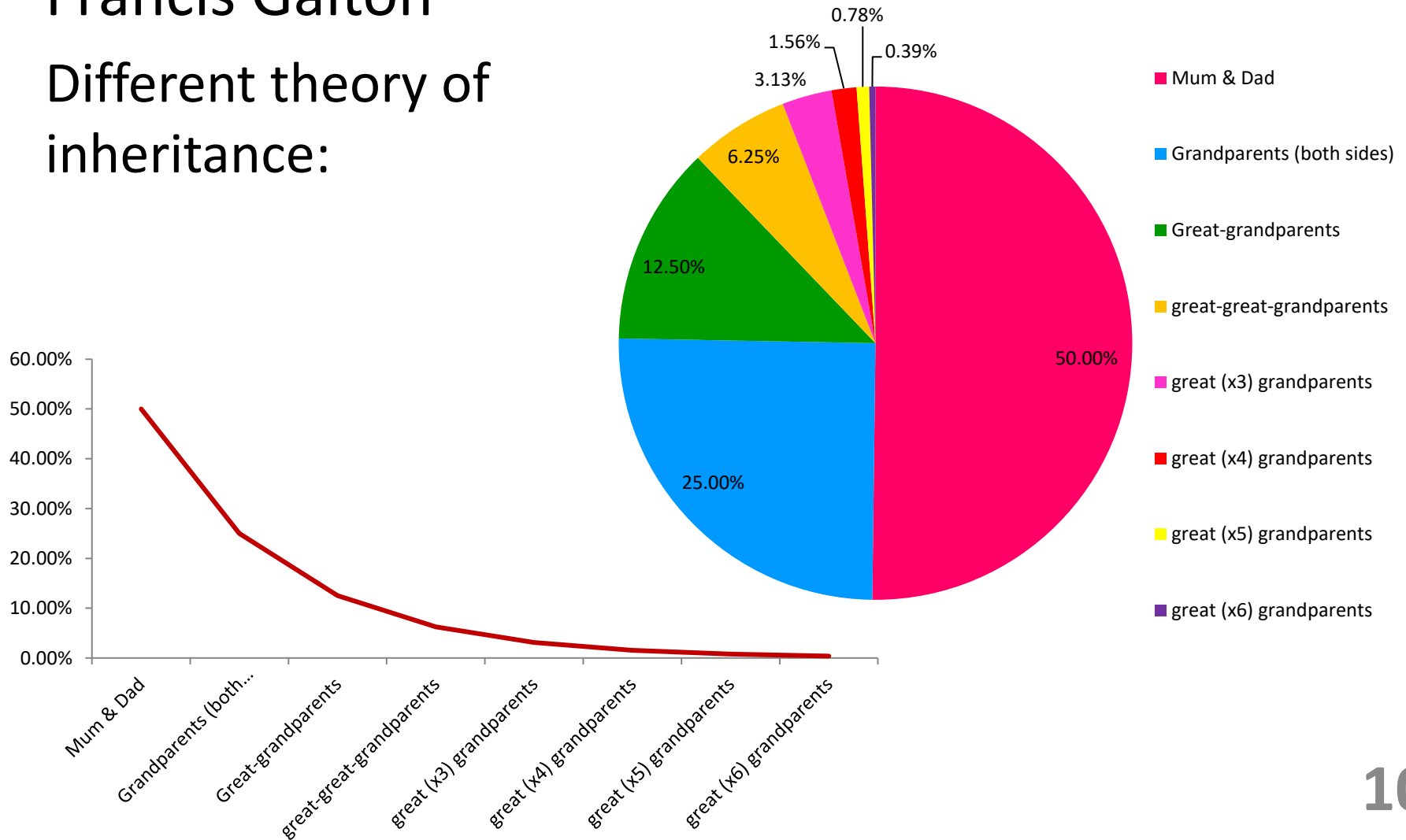
The parents of an individual together contribute on an average 50 percent of the total inherited characters, the 4 grandparents together 25 percent, the 3rd generation of ancestors together 12.5 percent, etc.



# History of Quantitative Genetics

Francis Galton

Different theory of inheritance:



# History: Galton vs. Mendel



**MENDELIAN GENETICS**

**Traits inherited in a Mendelian fashion. Phenotypes discrete characteristics**

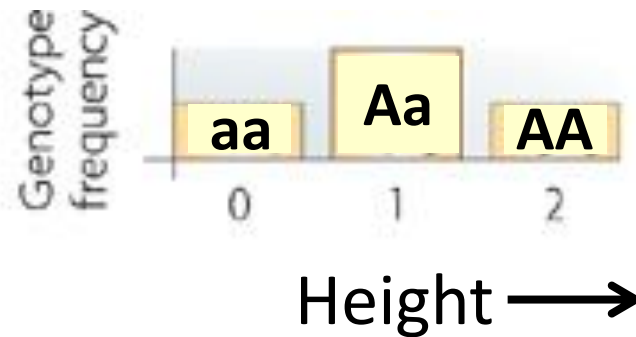


**QUANTITATIVE GENETICS**

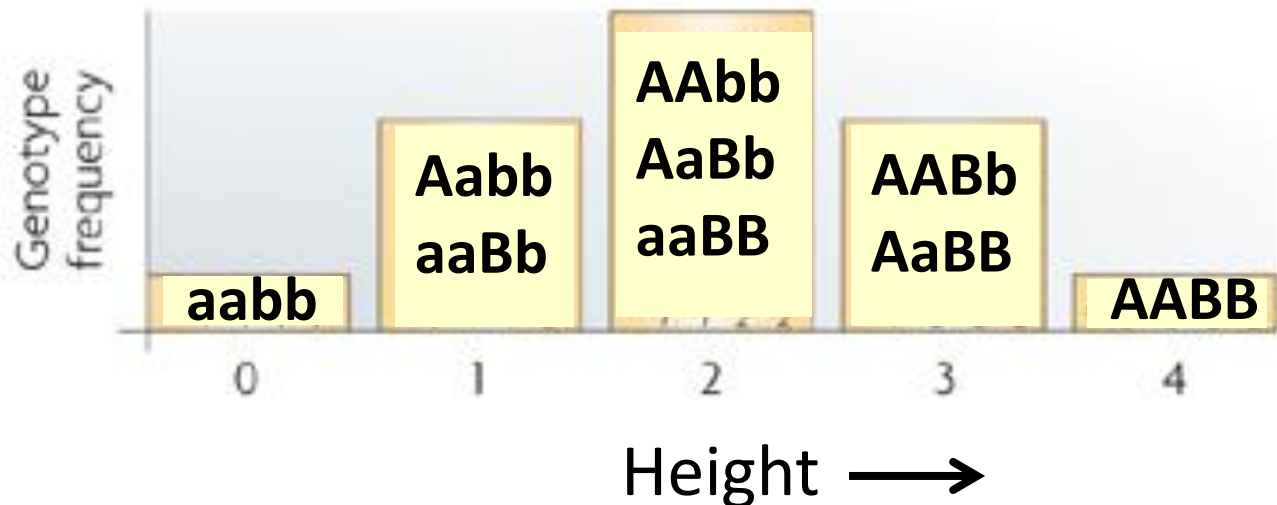
**Traits inherited as complex averages of ancestral phenotypes. Continuously varying phenotypes**

# Quantitative traits and Mendelian laws

a One locus  
(A):

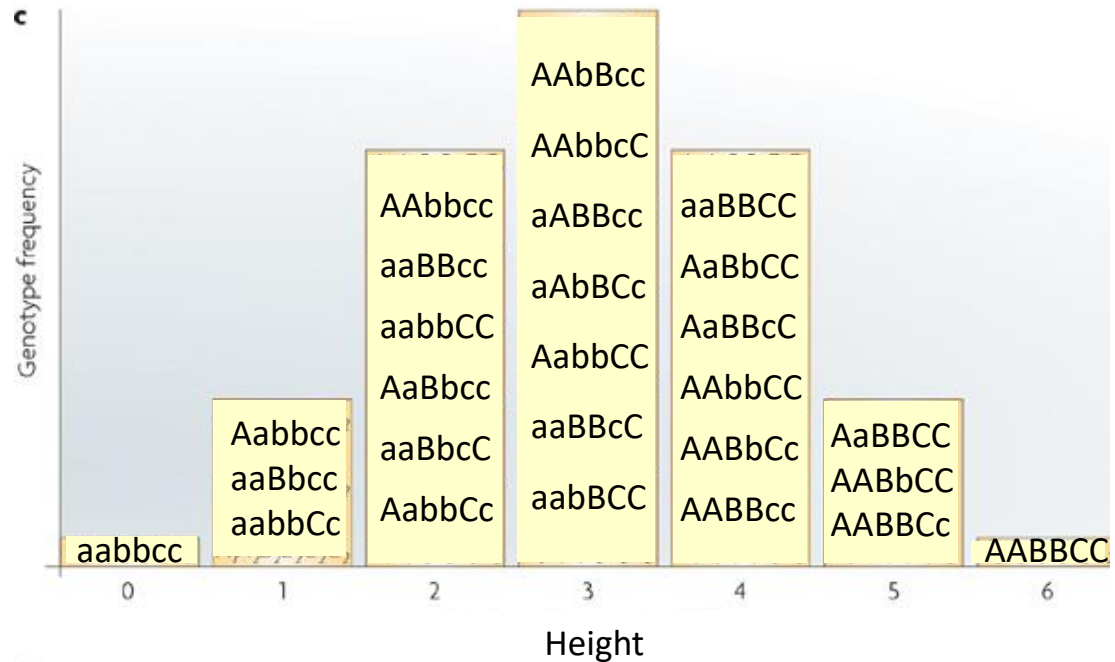


b Two  
Loci  
(A & B):

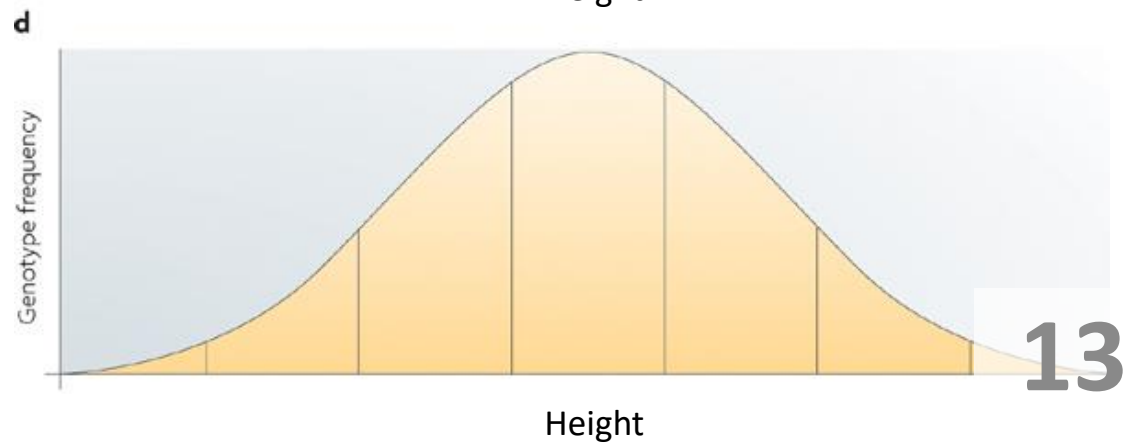


# Quantitative traits and Mendelian laws

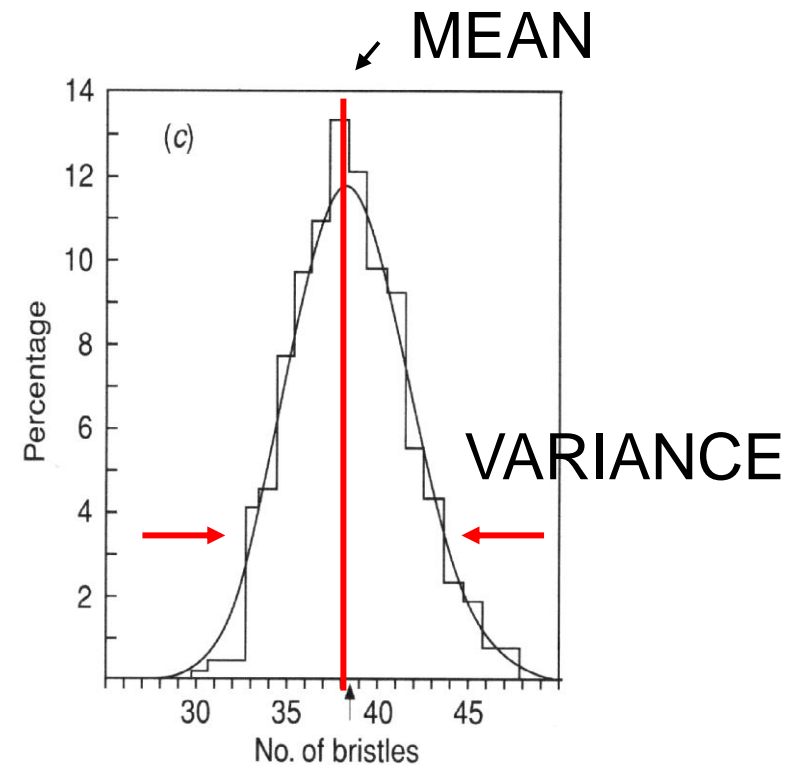
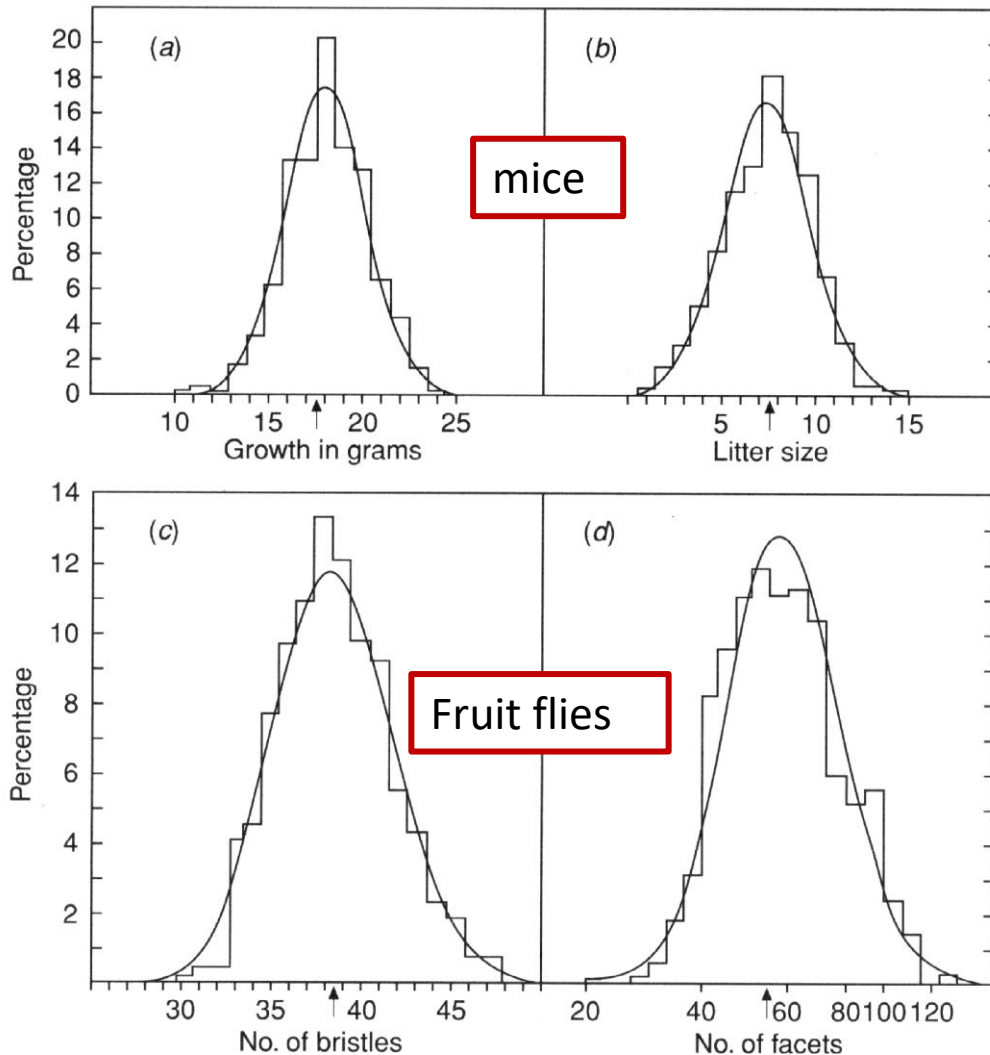
Three  
Loci  
(A, B & C):



Many  
loci:



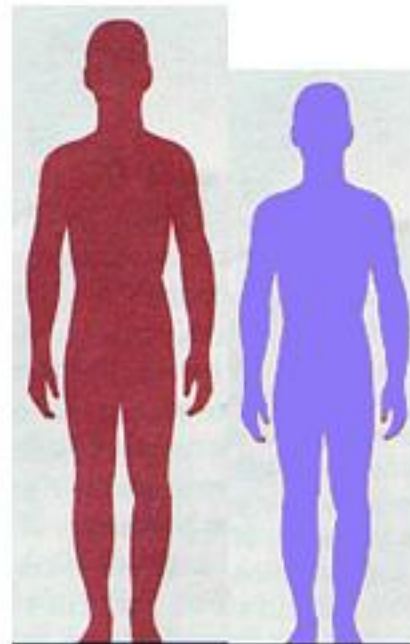
# Normal Distribution of Phenotypes



# Nature versus Nurture?

- Two influences on the expression of quantitative traits:
  - (1) Genetic (effects of many genes)
  - (2) Environmental (effects of environment)
- E.g. height:

Difference due  
to different  
genes



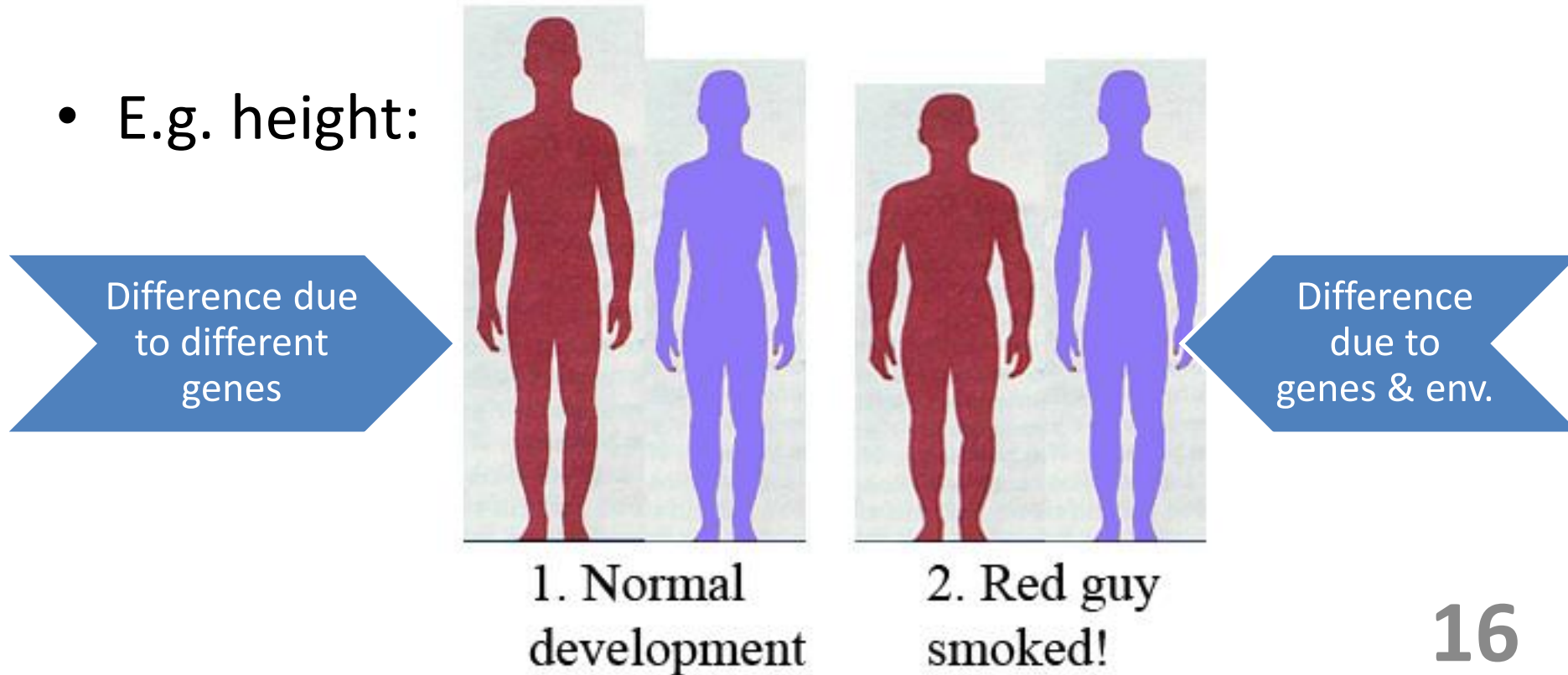
1. Normal  
development



# Nature versus Nurture?

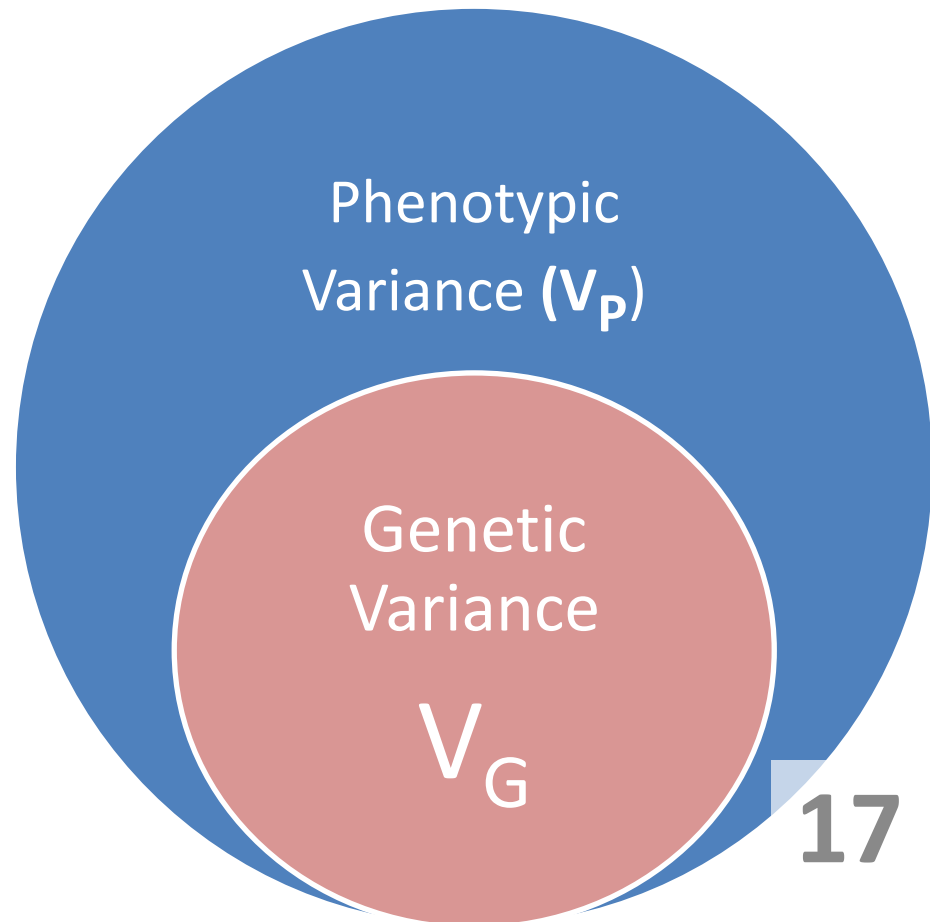
- Two influences on the expression of quantitative traits:
  - (1) Genetic (effects of many genes)
  - (2) Environmental (effects of environment)

- E.g. height:



# Partitioning trait variation:

- Most traits influenced by both genes and environment (nature & nurture)
- If we represent all the **phenotypic variation** in the population as a solid circle, we can recognise the portion that is due to different genes
- This is called '**genetic variance**'



# Heritability ( $H^2$ )

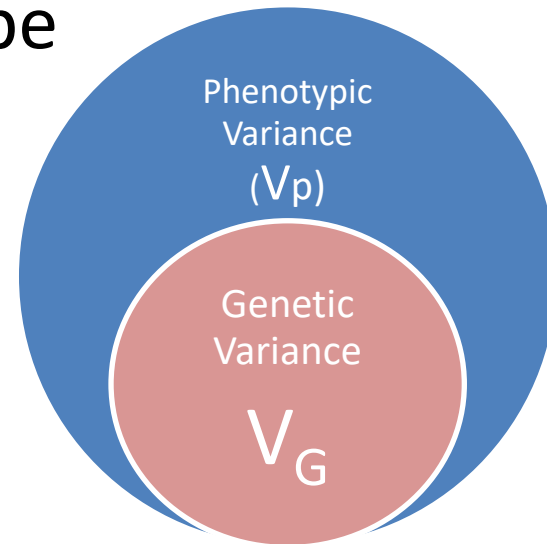
What Does it Measure?

Measure of how much *variation* in a phenotype is caused by *variation* in genotype

Assuming additivity:

$$VP = VG + VE$$

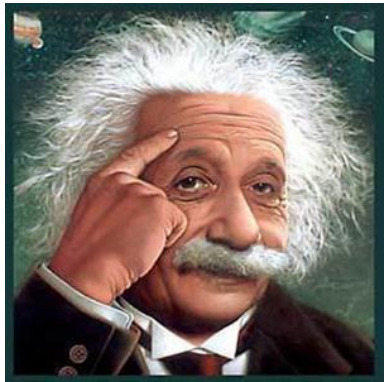
$$H^2 = VG/VP$$



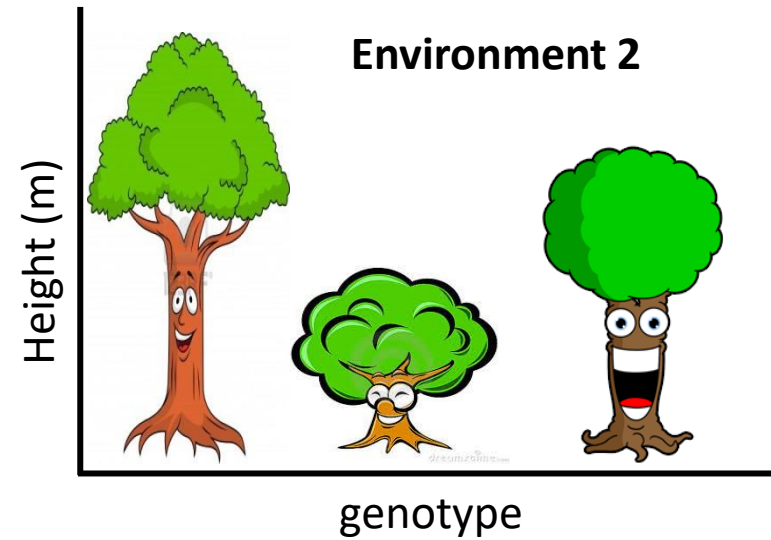
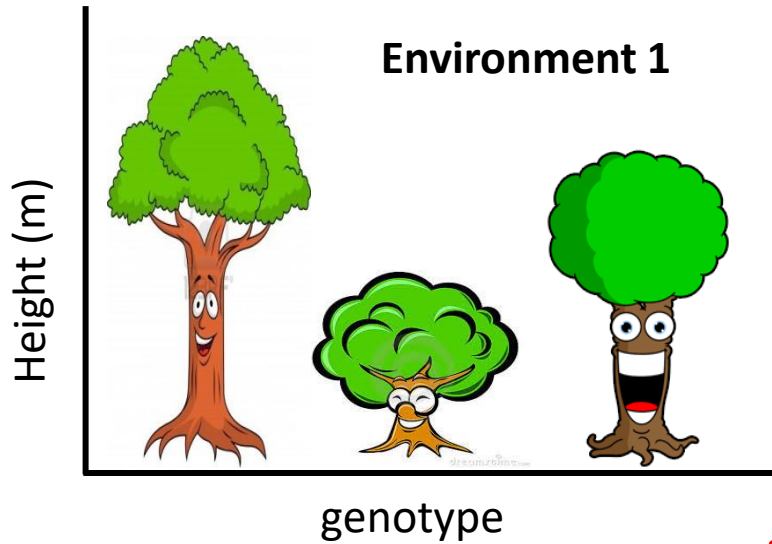
Proportion of Genetic variance to phenotypic variance

# Heritability and Causation

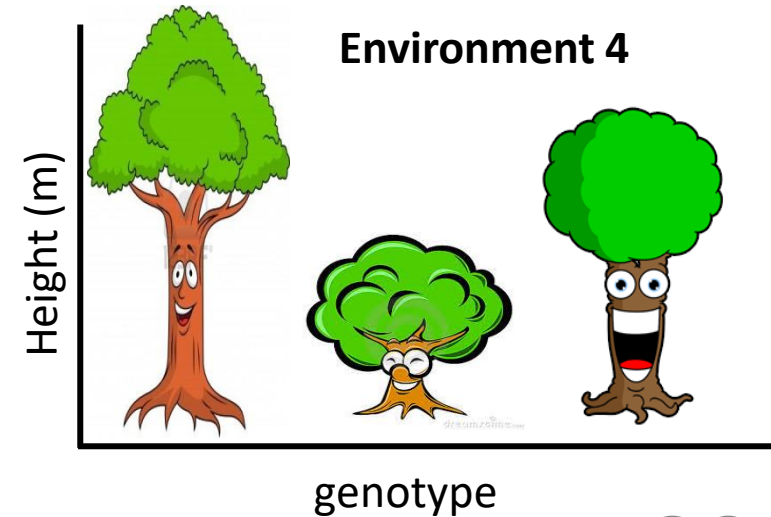
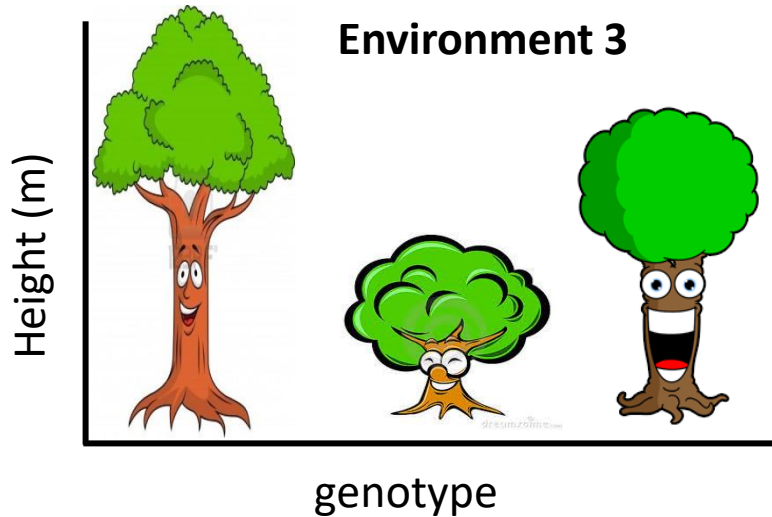
- Heritability can be used to make causal claims about the relative effects of genes (nature) and the environment (nurture)
- Which is more causally important?



- *Specific types* of causal claims



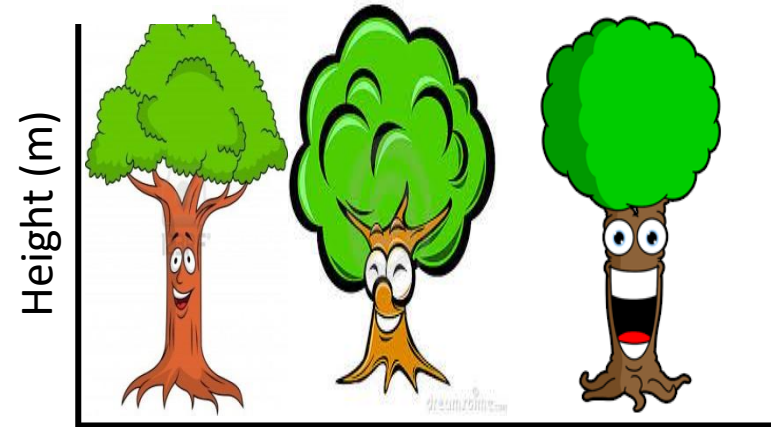
**H<sup>2</sup> HIGH**



**Environmental or Genetic?**

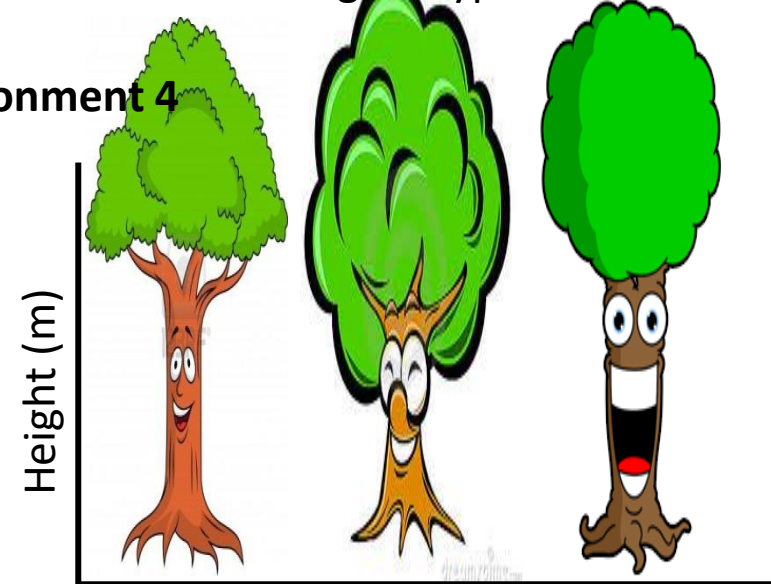
**H<sup>2</sup> LOW**

**Environment 2**



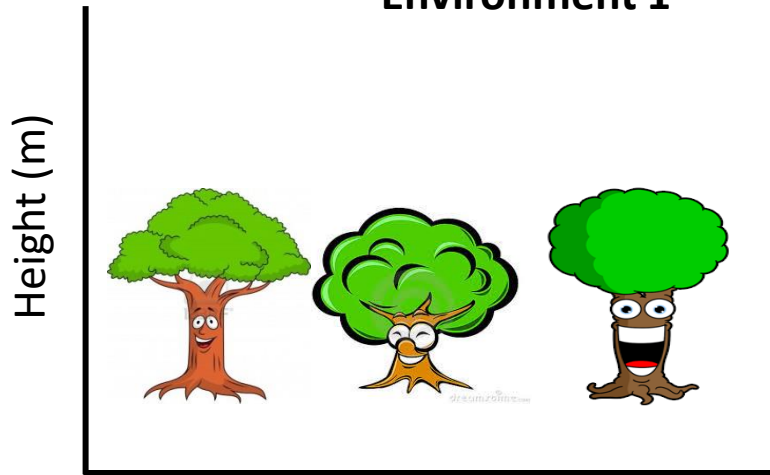
genotype

**Environment 4**



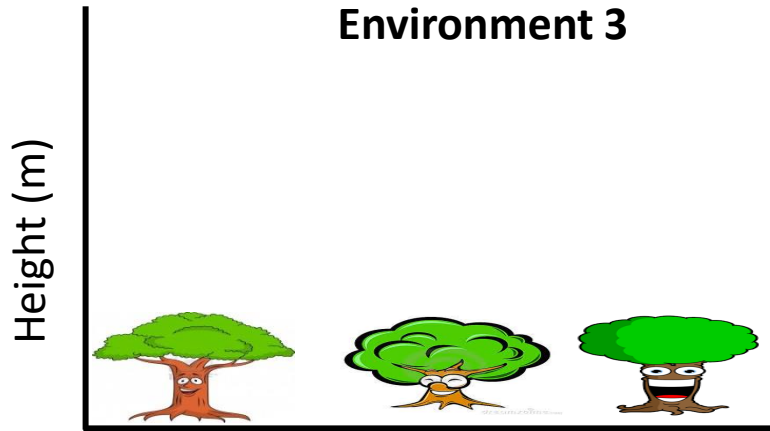
genotype

**Environment 1**



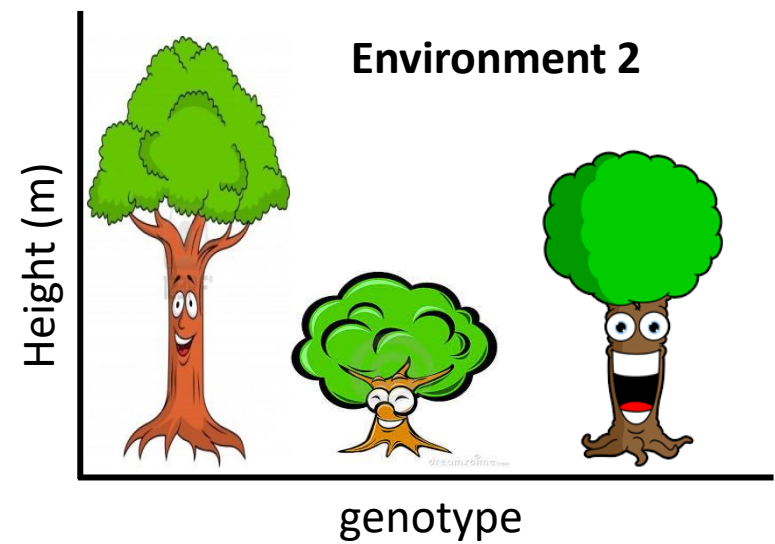
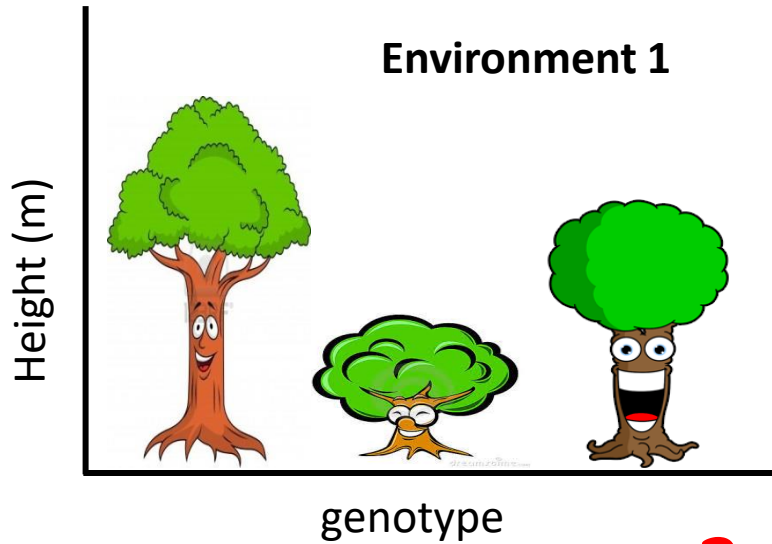
genotype

**Environment 3**

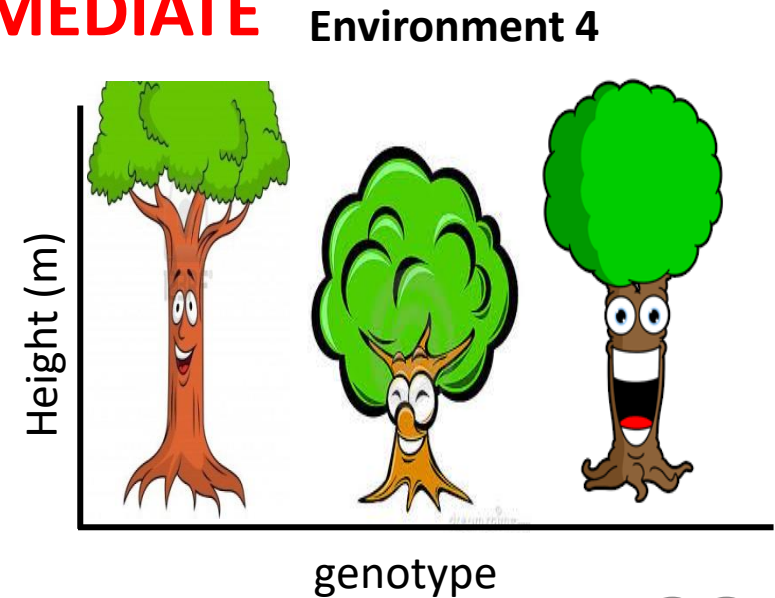
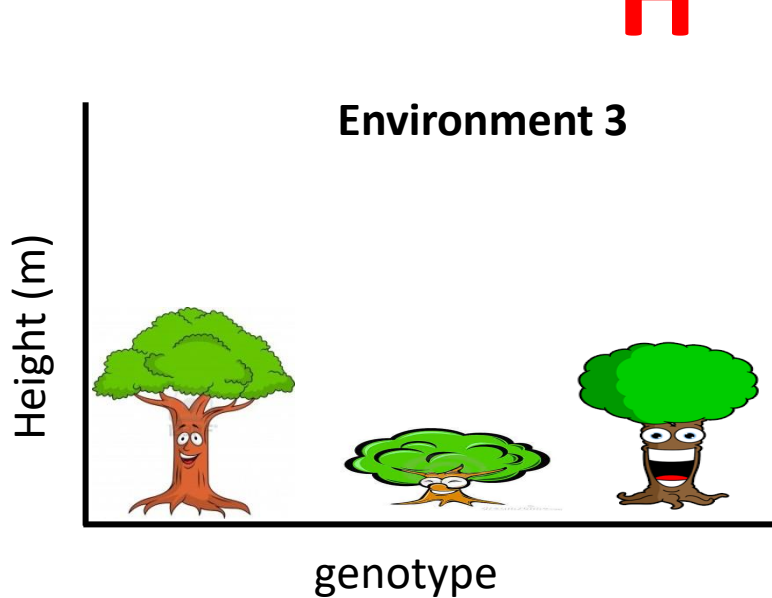


genotype

**Environmental or Genetic?**



**H<sup>2</sup> INTERMEDIATE**



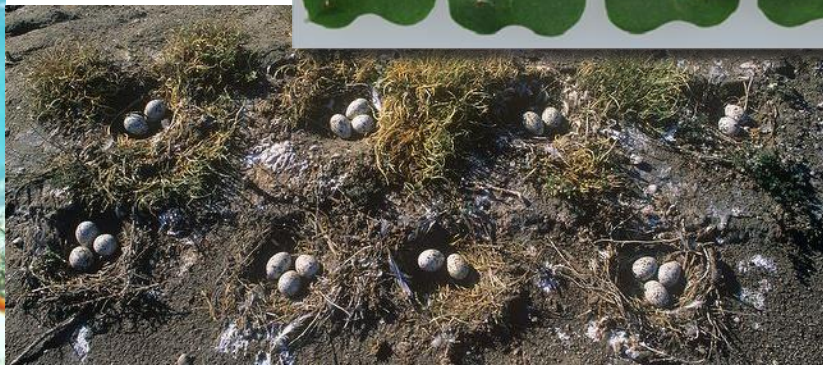
**Environmental or Genetic?**



# How does this relate to Conservation Biology?

## Knowledge of quantitative fitness traits

- Clutch size
- Resistance to disease / introduced organisms
- Resistance to climate change
- Lifetime fecundity
- Age of first litter
- Days to flowering



# Where do the values come from?

Heritability of postchallenge survival, an indicator of disease resistance, was estimated to be 0.35 ± 0.09.

Silverstein, J. T., et al. (2009). Rainbow trout resistance to bacterial cold-water disease is moderately heritable and is not adversely correlated with growth. *Journal of animal science* 87(3), 860-867.

Broad-sense heritabilities ranged from 0.55 in the F2 population (Fargo, N.D.) to 0.95 in the F<sub>2,4</sub> progenies at

León, A. J., Lee, M., & Andrade, F. H. (2001). Quantitative trait loci for growing degree days to flowering and photoperiod response in sunflower (*Helianthus annuus* L.). *Theoretical and Applied Genetics*, 102(4), 497-503.

and the heritability estimates (95 % confidence intervals) for boldness and aggressiveness were 0.76 (0.49, 0.90) and 0.36 (0.10, 0.72) respectively. Furthermore, there were

Ariyomo, T. O., Carter, M., & Watt, P. J. (2013). Heritability of Boldness and Aggressiveness in the Zebrafish. *Behavior genetics*, 43(2), 161-167.

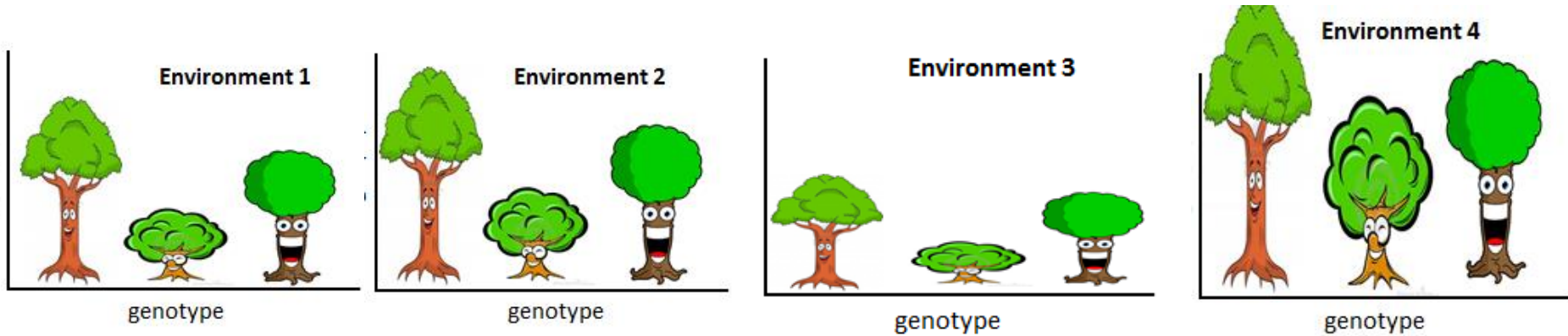
$$H^2 = VG / VP$$

$$VP = VG + VE$$

VG?

VE?

# Where do the values come from?



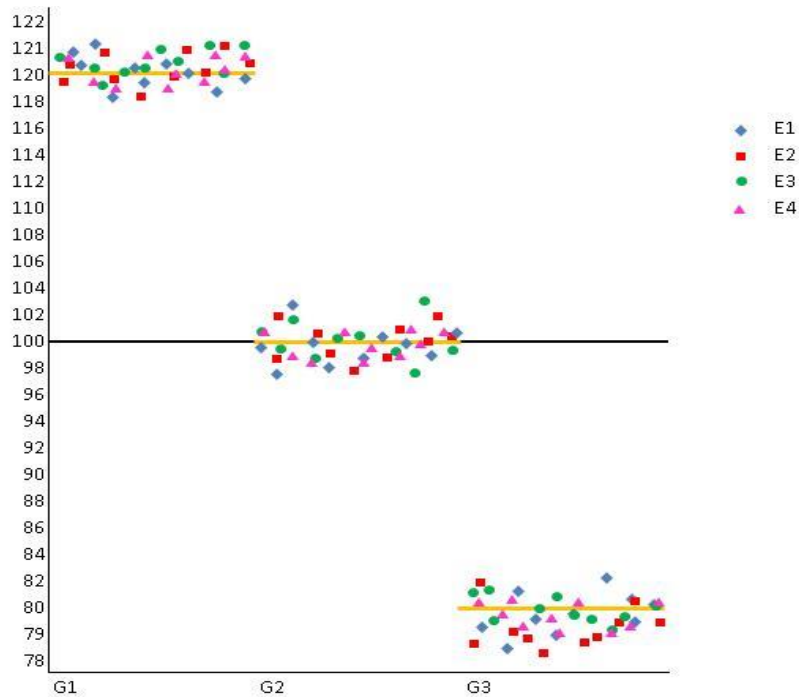
	E1 (75)	E2 (75)	E3 (75)	E4 (75)
G1 (100)				
G2 (100)				
G3 (100)				

# The height of the trees are measured...

	E1 ( $n_e = 75$ )	E2 ( $n_e = 75$ )	E3 ( $n_e = 75$ )	E4 ( $n_e = 75$ )	Genotype Means
G1 ( $n_g = 100$ )	$\mu = 120$	$\mu = 118$	$\mu = 119$	$\mu = 123$	$\mu_{G1} = 120$
G2 ( $n_g = 100$ )	$\mu = 100$	$\mu = 101$	$\mu = 98$	$\mu = 101$	$\mu_{G2} = 100$
G3 ( $n_g = 100$ )	$\mu = 80$	$\mu = 81$	$\mu = 78$	$\mu = 81$	$\mu_{G3} = 80$
Environment Means	$\mu_{E1} = 100$	$\mu_{E2} = 100$	$\mu_{E3} = 98.33$	$\mu_{E4} = 101.67$	$\bar{X} = 100$

Trees with G1 genotype are significantly taller than G2, who in turn are taller than G3. Differences between environments are negligible.

	E1 (n <sub>e</sub> =75)	E2 (n <sub>e</sub> =75)	E3 (n <sub>e</sub> =75)	E4 (n <sub>e</sub> =75)	N=300
G1 (n <sub>g</sub> =100)	μ= 120	μ= 118	μ= 119	μ= 123	μ <sub>G1</sub> = 120
G2 (n <sub>g</sub> =100)	μ= 100	μ= 101	μ= 98	μ= 101	μ <sub>G2</sub> = 100
G3 (n <sub>g</sub> =100)	μ= 80	μ= 81	μ= 78	μ= 81	μ <sub>G3</sub> = 80
N=300	μ <sub>E1</sub> =100	μ <sub>E2</sub> = 100	μ <sub>E3</sub> = 98.33	μ <sub>E4</sub> = 101.67	$\ddot{X} = 100$

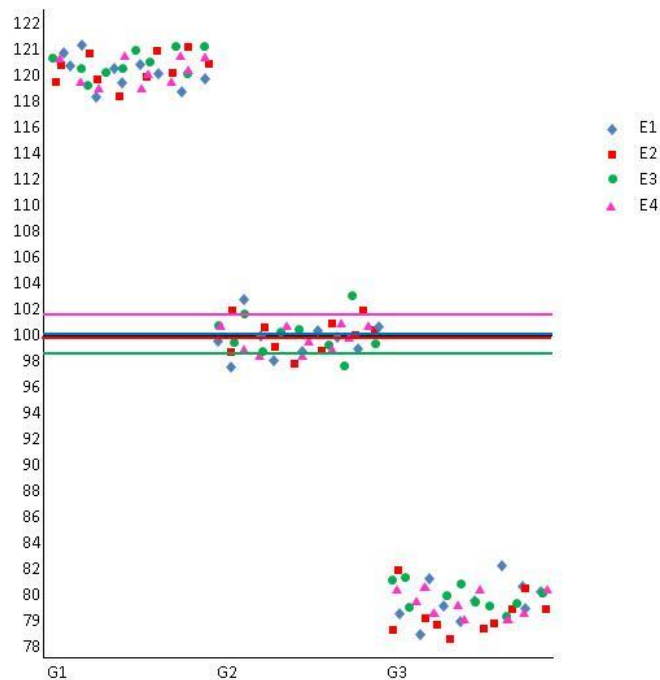


$$VG = \frac{(\mu_{G1} - \ddot{X})^2 + (\mu_{G2} - \ddot{X})^2 + (\mu_{G3} - \ddot{X})^2}{nG}$$

$$VG = \frac{(\underline{120} - \underline{100})^2 + (\underline{100} - \underline{100})^2 + (\underline{80} - \underline{100})^2}{3}$$

$$VG = 266.67$$

	E1 (n <sub>e</sub> =75)	E2 (n <sub>e</sub> =75)	E3 (n <sub>e</sub> =75)	E4 (n <sub>e</sub> =75)	N=300
G1 (n <sub>g</sub> =100)	μ= 120	μ= 118	μ= 119	μ= 123	μ <sub>G1</sub> = 120
G2 (n <sub>g</sub> =100)	μ= 100	μ= 101	μ= 98	μ= 101	μ <sub>G2</sub> = 100
G3 (n <sub>g</sub> =100)	μ= 80	μ= 81	μ= 78	μ= 81	μ <sub>G2</sub> = 80
N=300	μ <sub>E1</sub> =100	μ <sub>E2</sub> = 100	μ <sub>E3</sub> = 98.33	μ <sub>E4</sub> = 101.67	$\ddot{X} = 100$



$$VE = \frac{(\mu_{E1} - \ddot{X})^2 + (\mu_{E2} - \ddot{X})^2 + (\mu_{E3} - \ddot{X})^2 + (\mu_{E4} - \ddot{X})^2}{nE}$$

$$VE = \frac{(\underline{100} - \underline{100})^2 + (\underline{100} - \underline{100})^2 + (\underline{98.33} - \underline{100})^2 + (\underline{101.67} - \underline{100})^2}{4}$$

$$VE = 1.38$$

# Getting the heritability estimate

The phenotypic variance is assumed to be additive

$$VP = VG + VE$$

Heritability ( $H^2$ ) is the proportion of the genotypic variance from the total phenotypic variance

$$H^2 = VG / VP \quad \text{or} \quad VG / (VE + VG)$$



*Usually* a high heritability estimate accurately reflects an example in which differences in genotype are the major cause of differences in phenotype

$$VG = 266.67$$

$$VE = 1.38$$

$$VP = 268.05$$

Genetic var ( $H^2$ )

$$= VG / VP$$

$$= 266.67 / 268.05$$

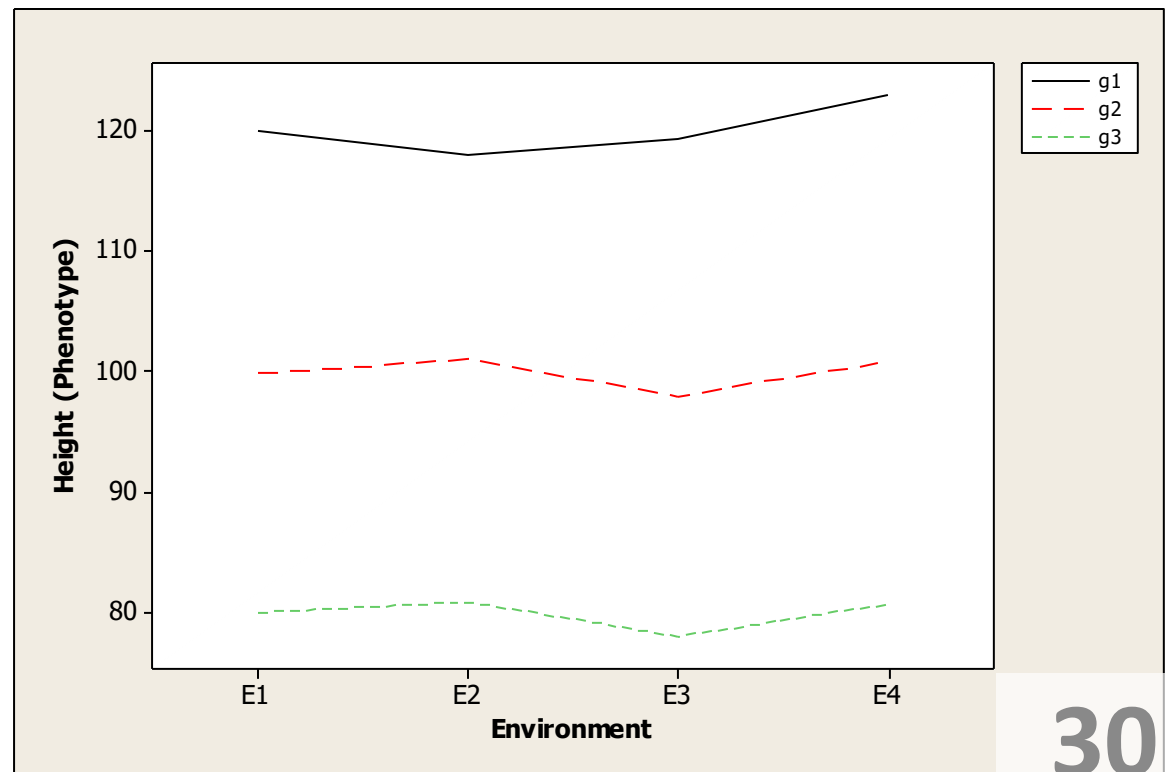
$$= 0.9948$$

Environmental var

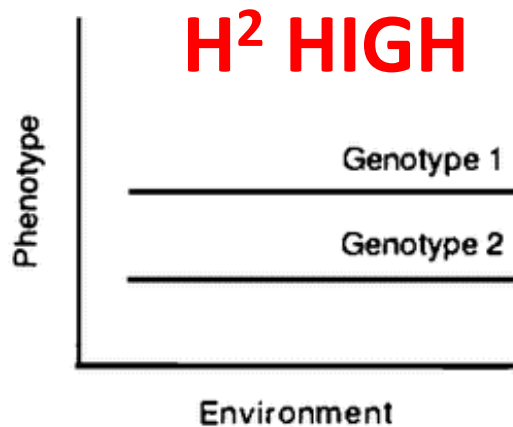
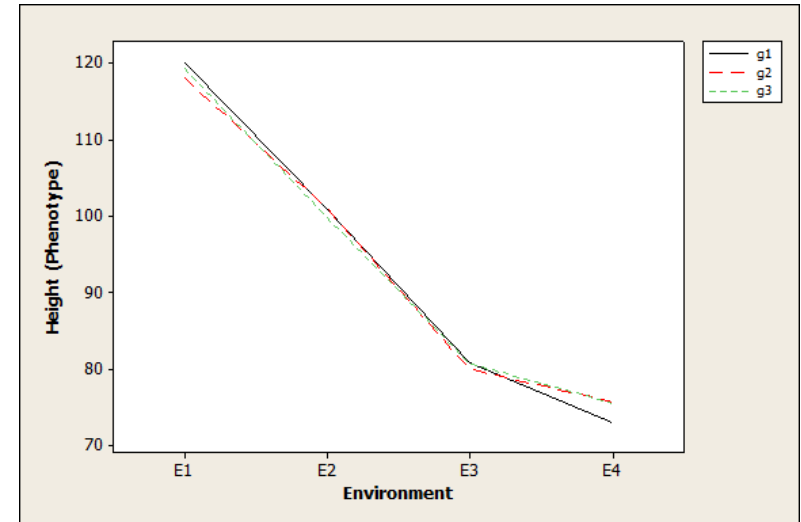
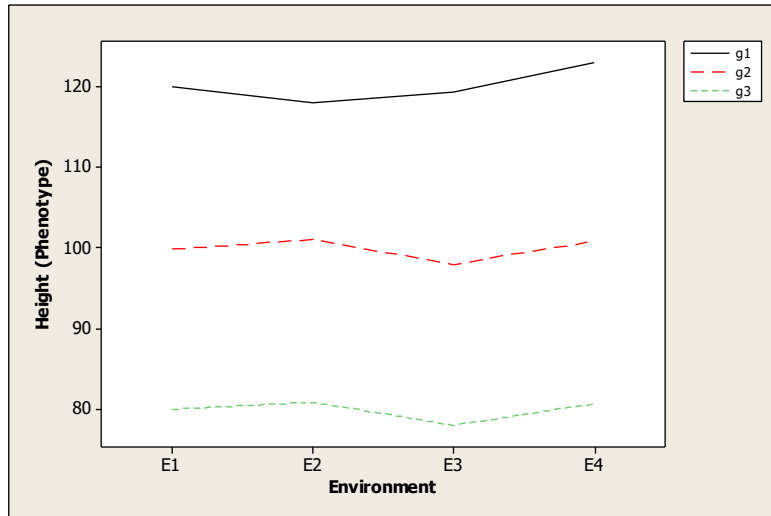
$$= VE / VP$$

$$= 1.38 / 268.05$$

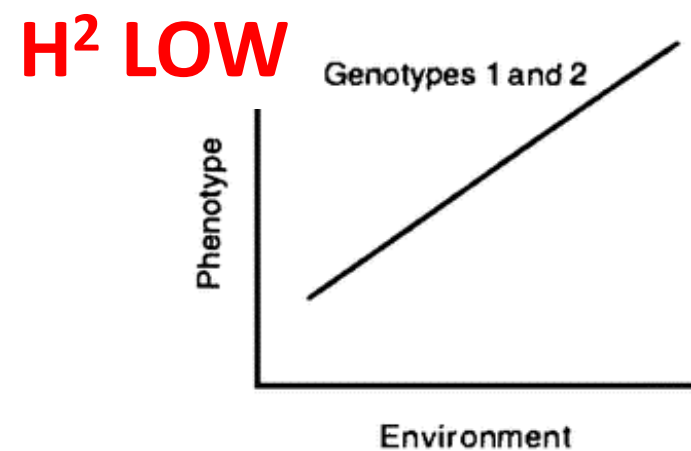
$$= 0.0052$$



# Norm of Reaction

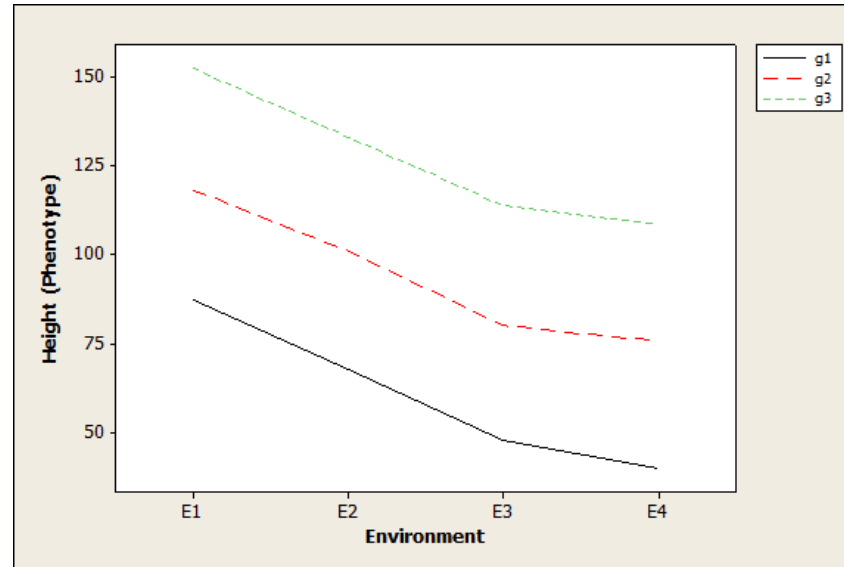


a) Biological determinism

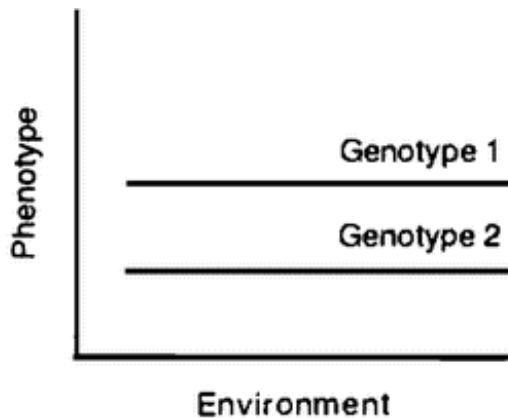


b) Social determinism

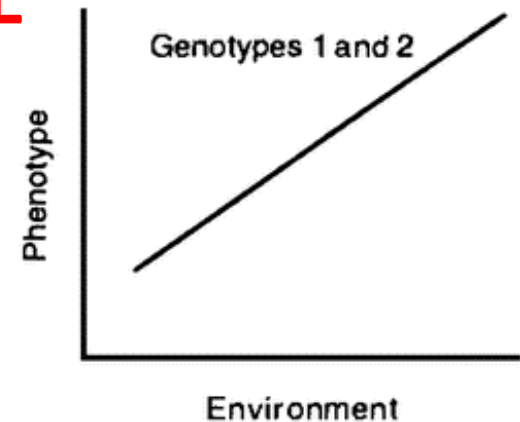
# Norm of Reaction



**H<sup>2</sup> INTERMEDIATE**

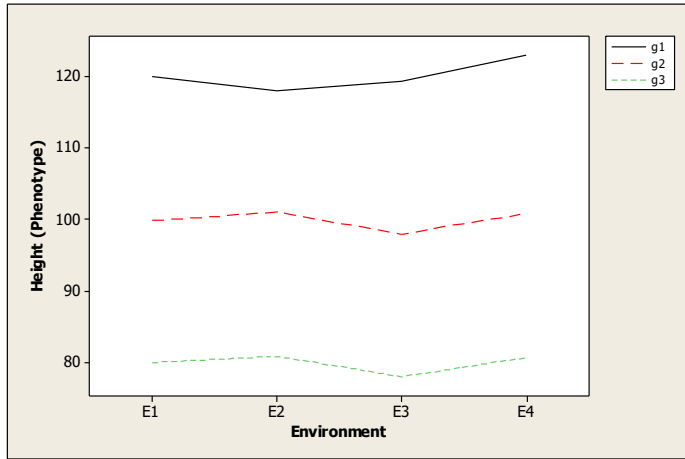


a) Biological determinism

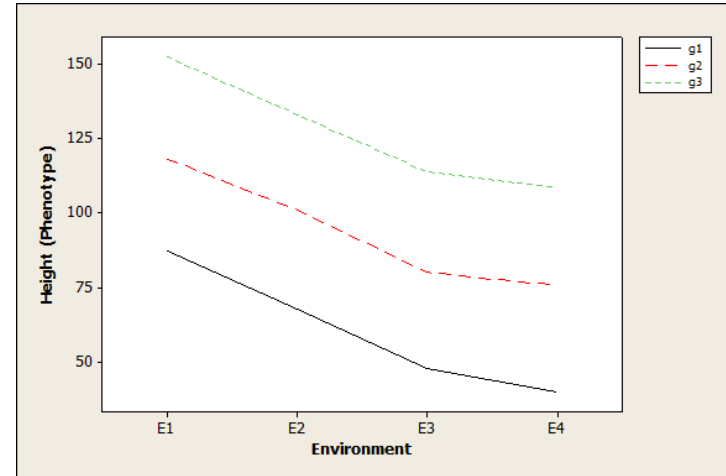


b) Social determinism

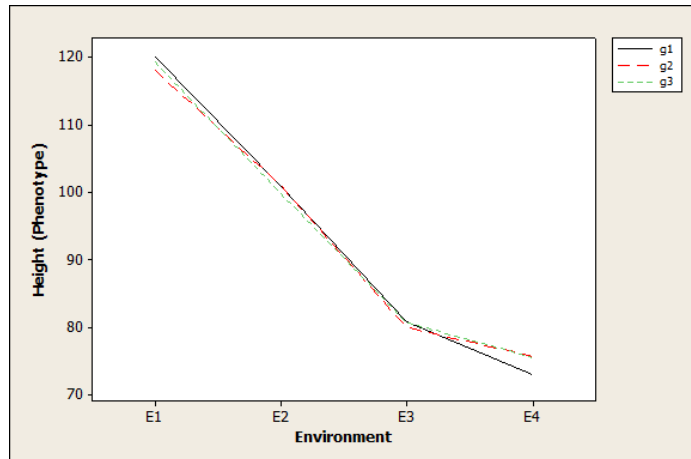
# Norm of Reaction - GxE (Interaction)



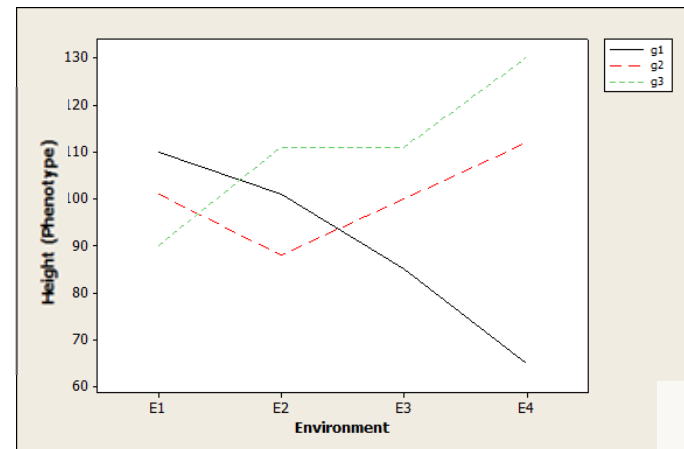
**H<sup>2</sup> HIGH**



**H<sup>2</sup> INTERMEDIATE**

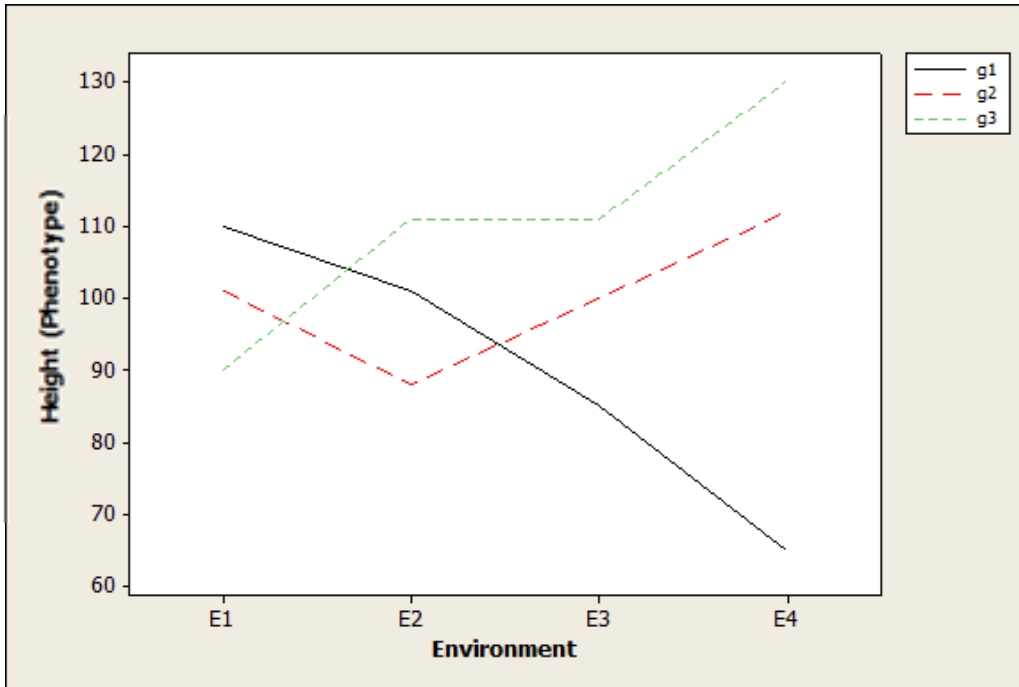


**H<sup>2</sup> LOW**



**H<sup>2</sup> ??**

# $H^2 = 0.968$ (VERY HIGH!)



$$VG = 266.67$$

$$VE = 8.8089$$

$$VP = 275.4789$$

$$266.67/275.4789$$

$$H^2 = 0.968$$

	E1	E2	E3	E4	Means
G1	110	100	85	65	90
G2	100	88	100	112	100
G3	90	110	110	130	110
Means	100	99.33333	98.33333	102.3333	$\bar{X} = 100$

$$VG = \frac{(\mu_{G1} - \bar{X})^2 + (\mu_{G2} - \bar{X})^2 + (\mu_{G3} - \bar{X})^2}{n_G}$$

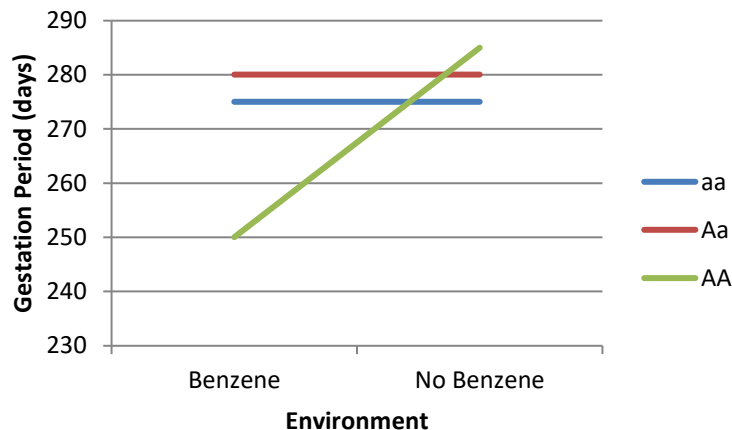
$$VG = 266.67$$

$$VE = \frac{(\mu_{E1} - \bar{X})^2 + (\mu_{E2} - \bar{X})^2 + (\mu_{E3} - \bar{X})^2 + (\mu_{E4} - \bar{X})^2}{n_E}$$

$$VE = 8.8089$$

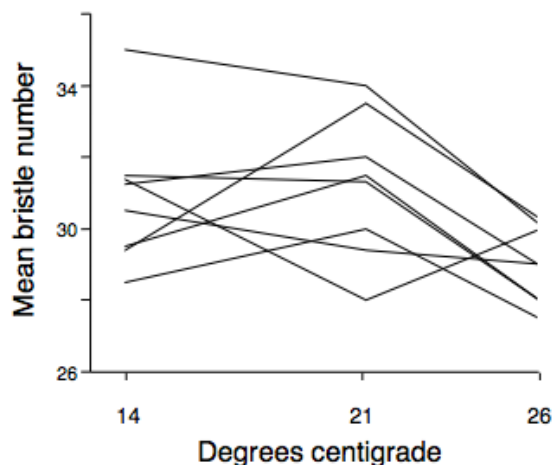
# GxE (Gene-Environment Interaction)

- Trait expression varies over different environments – may not be directional
- Genome produces different phenotypes depending on developmental environment
- Example 1: benzene exposure is significantly associated with shorter gestation periods in pregnant women possessing the AA allele of *CYP1A1*, while there is no association for those with Aa or aa (Wang et al. 2000)



# GxE (Gene-Environment Interaction)

- Trait expression varies over different environments – may not be directional
- Genome produces different phenotypes depending on developmental environment
- Example 2: Bristle number in drosophila is determined by genotypic differences, and temperature. How temperature affects bristle number depends on the flies genetic background (Gupta and Lewontin 1981)





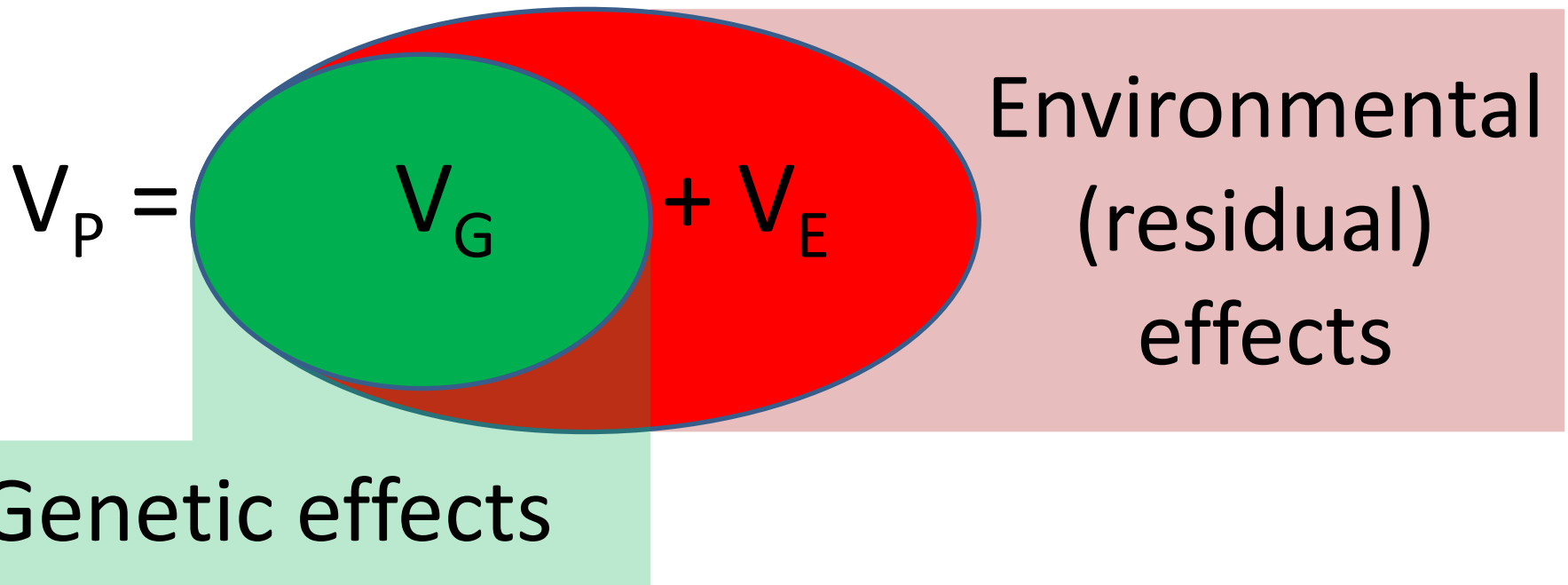
# GxE (Gene-Environment Interaction)

- GxE doesn't always mean an high heritability
- Could also result in low  $H^2$  if not accounted for
- Demonstrates when interaction occurs and is unaccounted for – one cannot get a good understanding without looking at the NOR.
- GxE can lead to a heritability estimate that does not accurately reflect the contribution of environmental or genetic variation
- Can add GxE term into heritability model so it no longer skews results

## Non-Additive

$$VP = VG + VE + V_{GxE} + 2CovGE + Error$$

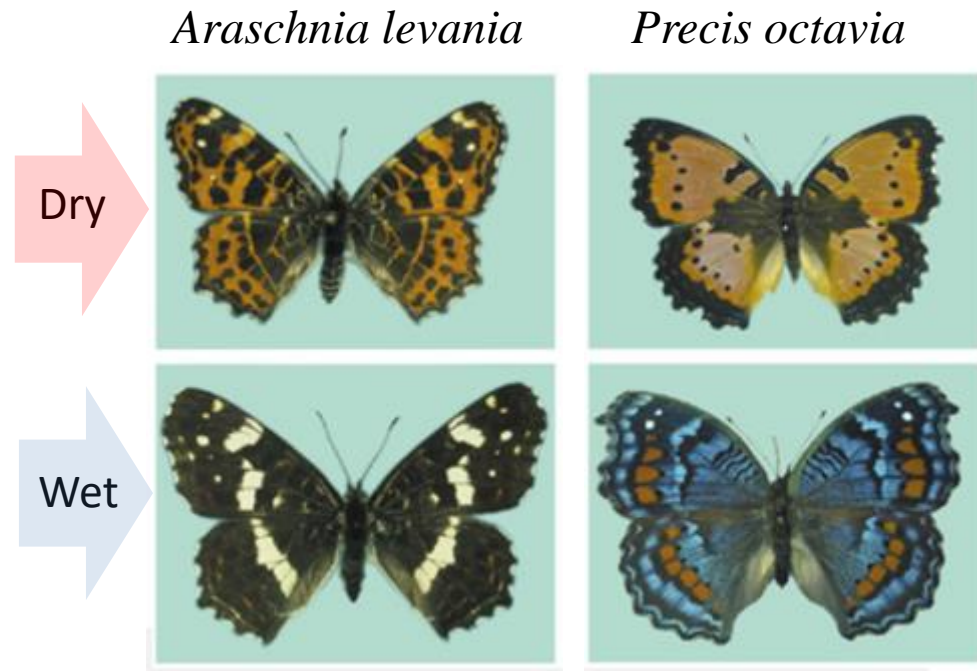
# NATURE... versus ...NURTURE



....assuming that genetic and environmental effects are **additive**

# Phenotypic plasticity

The ability of a single genome to produce different phenotypes depending upon the environment experienced during development



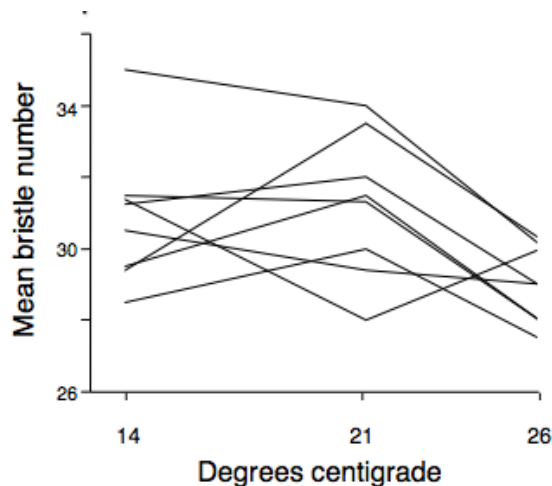
“Normal”

“Plague”

# GxE (Gene-Environment Interaction)

GxE = A form of phenotypic plasticity

Single genotype produces multiple phenotypes, depending on environmental interaction.



# Summary

- Quantitative traits are characterised by heritability estimates ( $H^2$ )
- Estimates partition the relative effects of environmental variation (VE) and genetic variation (VG) on differences in a phenotype (VP) *within a population*.

$$VP = VG + VE$$

$$H^2 = VG / VP$$

- Can estimate the influence of genes just by studying the phenotype (no molecular techniques needed)
- Conservation biologists are interested in the genetic basis of fitness traits
- Limitations to estimates: non-additivity (GxE interaction)

$$VP = VG + VE + V_{G \times E}$$

$$H^2 = VG / VP$$