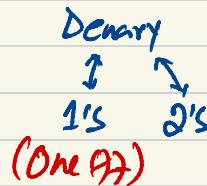
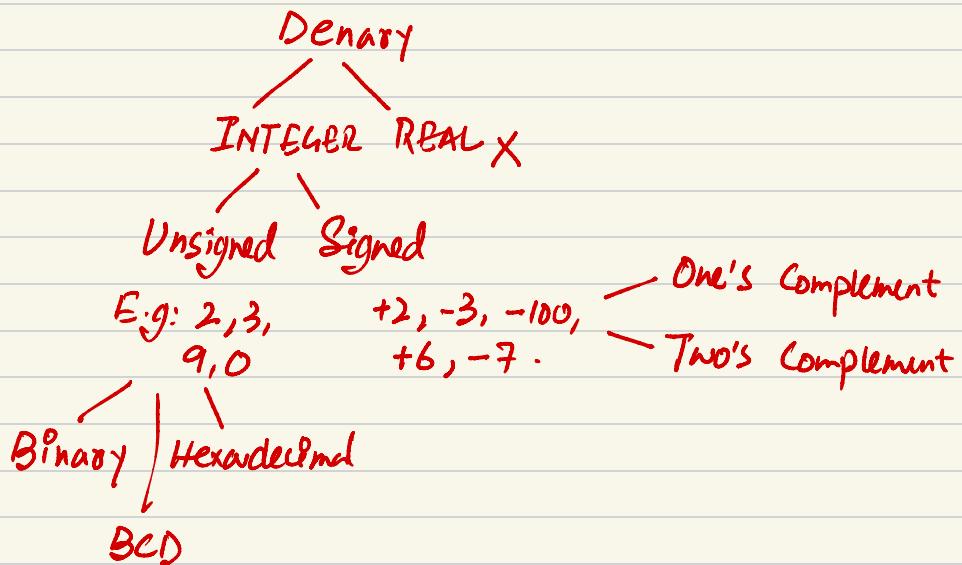




Number System:



Denary (Base 10):

0 1 2 3 4 5 6 7 8 9
 Total Digits in Denary = 10^{\downarrow}
 Base

$$\begin{array}{r}
 5693 \\
 \begin{array}{ccccccccc}
 5 & 6 & 9 & 3 & & & & & \\
 10^3 & 10^2 & 10^1 & 10^0 & \xrightarrow{\text{Position (right to left)}} & \text{Base} \\
 1000 & 100 & 10 & 1 & \xrightarrow{\text{Worth, weightages}} & \\
 5 \times 1000 & 6 \times 100 & 9 \times 10 & 3 \times 1 & & \\
 5000 + 600 + 90 + 3 & = & 5693
 \end{array}
 \end{array}$$

Binary (Base 2):

0 1 \rightarrow Binary Digits \rightarrow Bit
 Total bits = 2 \rightarrow Base 2.

Constraint: We can only write Binary numbers
 in the combinations of 8 bits. That is
 8 or 16 or 24 etc.

Syllabus requirement is to
 have up to 16 bits solutions.

Working:

$$(01100100)_2 = (100)_{10}$$

$$\begin{array}{r}
 0 \ 1 \ 1 \ 0 \ 0 \ 1 \ 0 \ 0 \\
 2^7 \ 2^6 \ 2^5 \ 2^4 \ 2^3 \ 2^2 \ 2^1 \ 2^0 \\
 128 \ 64 \ 32 \ 16 \ 8 \ 4 \ 2 \ 1 \\
 0+64+32+0+0+4+0+0 = 100
 \end{array}$$

Hexadecimal (Base 16): ✓

| | | |
|-------|---------------------|------------------------------|
| 0 — 9 | 0 1 2 3 4 5 6 7 8 9 | 10 |
| A — F | A B C D E F ✓ | $\frac{+6}{\text{Base } 16}$ |
| 7 | 0111 | 8 4 2 1 |
| 10 | 1010 | 0 0 0 0 |
| | | Smallest 1 1 1 1 Largest |

Reason for use:

1. Compact representation.
2. Memory addressing.
3. Color Representations.
4. Debugging and low-level programming.

| SINGLE BYTE Conversions | | BINARy | | | | | | | | HEX | | | | | |
|-------------------------|-----|--------|----|----|---|---|---|---|----|-----|---|---|---|---|--------|
| Denary | 128 | 64 | 32 | 16 | 8 | 4 | 2 | 1 | A | B | C | D | E | F | BIN |
| 100 | 0 | 1 | 1 | 0 | 0 | 1 | 0 | 0 | 64 | | | | | | 0 Even |
| 206 | 1 | 1 | 0 | 0 | 1 | 1 | 1 | 0 | CE | | | | | | 1 Odd. |
| 7 | 0 | 0 | 0 | 0 | 0 | 1 | 1 | 1 | 07 | | | | | | |
| 127 | 0 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 7F | | | | | | |
| 150 | 1 | 0 | 0 | 1 | 0 | 1 | 1 | 0 | 96 | | | | | | |
| 200 | 1 | 1 | 0 | 0 | 1 | 0 | 0 | 0 | C8 | | | | | | |
| 163 | 1 | 0 | 1 | 0 | 0 | 0 | 1 | 1 | A3 | | | | | | |

Range:

How many numbers?
Largest & smallest numbers?

For 4 bits

numbers 7 bits.

$$2^4 = 16 \begin{matrix} 0 \\ 15 \end{matrix}$$

$$2^{16} = 65536 \begin{matrix} 0 \\ 65535 \end{matrix}$$

$$2^8 = 256 \begin{matrix} 0 \\ 255 \end{matrix}$$

Two Bytes Conversions

$$(532)_{10} = (?)_2 = (?)_{16}$$

$$(214)_{10} = (532)_{10} = (0000001000010100)_2$$

$$\begin{array}{r} 532 \\ \hline 512 & 255 & 128 & 64 & 32 & 16 & 8 & 4 & 2 & 1 \\ 0 & 0 & 1 & 0 & 0 & 0 & 1 & 0 & 1 & 0 & 0 \\ \hline & 2 & & & & 1 & & 4 & & & \end{array}$$

BCD (Binary Coded Decimal)
 Decimal
 $0 \rightarrow 9$

4-bits BCD representation.
 $2^4 = 16$ → 0-9
 15
 0 1 2 3 4 5 6 7 8 9
 10 11 12 13 14 15

Format of BCD:

| | |
|---|------|
| 0 | 0000 |
| 1 | 0001 |
| 2 | 0010 |
| 3 | 0011 |
| 4 | 0100 |
| 5 | 0101 |

| | |
|---|------|
| 6 | 0110 |
| 7 | 0111 |
| 8 | 1000 |
| 9 | 1001 |

$$(29)_{10} = (00101001)_{BCD}$$

$$(128)_{10} = (00000001000101000)_{BCD}$$

10000001001010001
 1 3 7 1) BCD
 Denary (Decimal).

- Uses:
- * Digital Display
 - * Financial Calculations
 - * Embedded Systems.
 - * Legacy Computing Systems

Signed Binary Systems:

1's Complement:

+92 01011100
-92 10100011

Invert all

One's & two's complement.

Expectations are to convert:

- From Unsigned to Signed (binary)
- From Signed Denary to Bin.

Confined to a byte only.

Uses:
* Representation of -ve numbers.
* Simple arithmetic operations.

Binary additions and Subtractions:

In One's Complement
there are two zeros.

+0 +v zero 0000
-0 -v zero 1111

1's Complement additions:

-2+7

$$\begin{array}{r} \textcircled{0} \text{ +ve} \\ +2 \quad 00000010 \\ -2 \quad 11111101 \\ \hline \end{array}$$

$$+7 \quad 00000011$$

$$\begin{array}{r} \textcircled{1} \text{ -ve} \\ +7 \quad 00000011 \\ -2 \quad +11111101 \\ \hline \end{array}$$

① 100000100

~~+000000011~~

~~000000101~~

$$\begin{array}{r} C \quad S \\ \boxed{2} \quad 1 \\ 0 \quad 0 \quad 0 \\ 1 \quad 0 \quad 1 \\ 2 \quad 1 \quad 0 \\ 3 \quad 1 \quad 1 \end{array}$$

→ end-around Carry.

$$\begin{array}{r} +10 \quad 00001010 \\ -10 \quad 11110101 \end{array}$$

-10+3

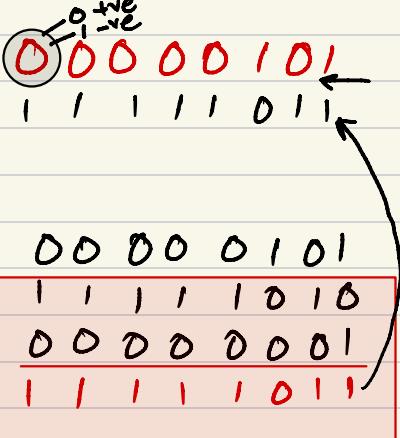
$$\begin{array}{r} 11111000 \\ 00000111 \end{array}$$

-7

+7

$$\begin{array}{r} -10 \quad 11110101 \\ +3 \quad 00000011 \\ \hline -7 \quad 11111000 \end{array}$$

Two's Complement:

| | | |
|--------------|---|--|
| $+5$ -5 |  $+5 \quad 00000101$ $-5 \quad 11111010$ $+ \quad 00000001$ \hline 11111011 | $+36 \quad 00100100$ $-36 \quad 11011100$ |
|--------------|---|--|

Features of 2's Complement:

- * There is only one representation for zero (00000000)
- * To find the negative of a number, you take its two's.
- * Arithmetic ops like addition and subtraction are more straight forward b/c there is no need to handle carry.

Uses:

- * Single zero
- * Ease of arithmetic ops.
- * Widely supported.

Addition & Subtraction:

a. $+24 - 4$

Range 2's Complement:

$-128 \longrightarrow +127$

$$\begin{array}{r}
 +24 \\
 - 4 \\
 \hline
 +20
 \end{array}$$

↓ dropped 9th bit
 ↓ overflow

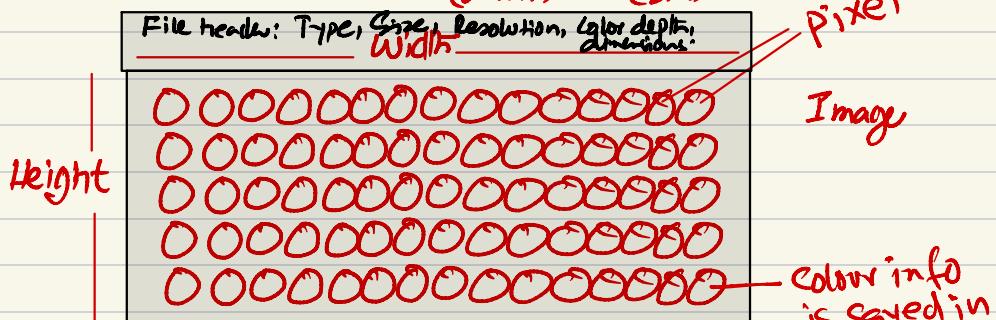
$$\begin{array}{r}
 1 \ 1 \ 1 \ 1 \ 0 \ 0 \ 0 \\
 0 \ 0 \ 0 \ 1 \ 1 \ 0 \ 0 \\
 + 1 \ 1 \ 1 \ 1 \ 1 \ 0 \ 0 \\
 \hline
 1 \ 0 \ 0 \ 0 \ 1 \ 0 \ 1 \ 0 \ 0 \\
 \underline{- \ 1 \ 6 \ + \ 4}
 \end{array}$$

If expected answers are within range (-128 - +127)
 then a carry drop doesn't matter.

$$\begin{array}{r}
 +5 +4 -3 \\
 +5 \\
 +4 \\
 -3 \\
 \hline
 +6
 \end{array}
 \quad
 \begin{array}{r}
 1 \ 1 \ 1 \ 1 \ 1 \ 1 \\
 0 \ 0 \ 0 \ 0 \ 0 \ 1 \ 0 \ 1 \\
 0 \ 0 \ 0 \ 0 \ 0 \ 1 \ 0 \ 0 \\
 1 \ 1 \ 1 \ 1 \ 1 \ 1 \ 0 \ 1 \\
 \hline
 1 / 0 \ 0 \ 0 \ 0 \ 0 \ 1 \ 1 \ 0
 \end{array}$$

$$\begin{array}{r}
 +4 \\
 +23 \\
 \hline
 +27
 \end{array}
 \quad
 \begin{array}{r}
 0 \ 0 \ 0 \ 0 \ 0 \ 1 \ 0 \ 0 \\
 0 \ 0 \ 0 \ 1 \ 0 \ 1 \ 1 \ 1 \\
 \hline
 0 \ 0 \ 0 \ 1 \ 1 \ 0 \ 1 \ 1 \\
 16 + 8 + 2 + 1 = 27
 \end{array}$$

Image: - Bitmap Image Size = $\frac{\text{Resolution}}{(\text{W} \times \text{H})} \times \frac{\text{Color depth}}{(\text{bits})}$



Pixel:

Image Resolution: Pixels in Height & Width
 $\text{Width} \times \text{Height}$

color info is saved in a pixel.
 No. of pixels used are color depth.

Screen Resolution:

Color Depth: How many bits are used to represent the color of each pixel.

$2^5 = 32$ Colors

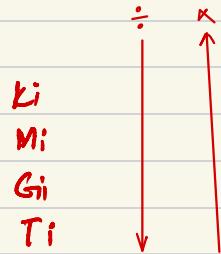
$1\text{-bit } 2^1 = 2$ Colors

16 bits $2^{16} = 65,536$ colors

8-bit $2^8 = 256$ colors

Sizing:

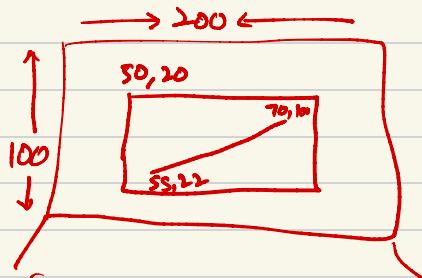
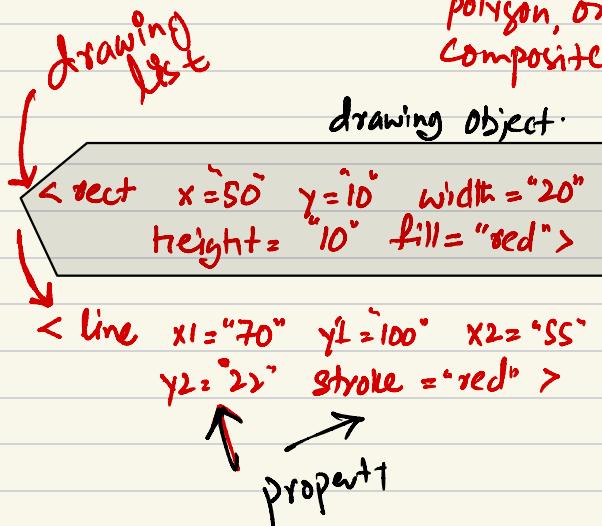
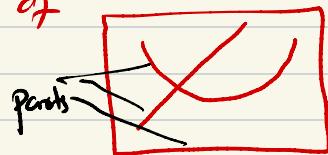
| | | |
|------------|------------|---------------|
| | 1 Byte | = 8 Bits. |
| 2^{10} = | 1024 Bytes | = 1 Kibibyte |
| 2^{20} = | 1024 KiB | = 1 Mebibyte |
| 2^{30} = | 1024 MiB | = 1 Gibibyte |
| 2^{40} = | 1024 GiB | = 1 Petibyte. |



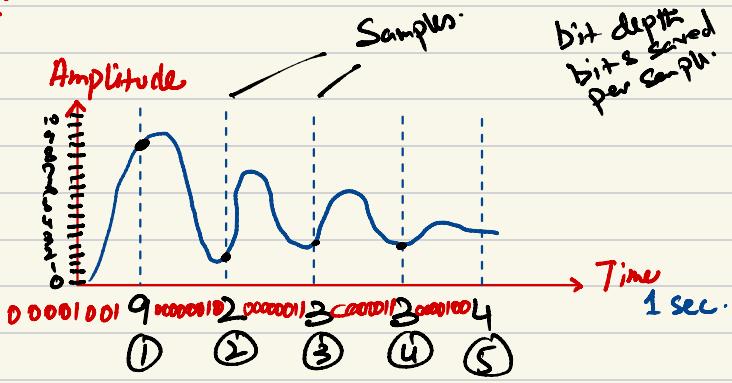
Vector Graphics:

Encoding: Geometric description,
scaled to any size without distortion.

Drawing Objects: Represent parts of
the image.
line, curve,
polygon, or a
composite.



Sound:



bit depth = 8 bits per sample.

Sound file Size = Sample resolution \times Sampling rate \times Time
(bit depth) Samples/sec (sec.)

$$\begin{aligned} & 8 \times 5 \times 5 \\ & = 200 \text{ bits / 8} \\ & = 25 \text{ Bytes.} \end{aligned}$$