

## CS5008 Homework 7 Merge Sort

### Written Exercises

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1. Explain what you think the worst-case, big-Oh complexity and the best-case, big-Oh complexity of merge sort is. Why do you think that?

The worst case and best case big-Oh complexity of merge sort is  $O(N \cdot \log N)$ . From the understanding of the merge sort implementation, we have to repeatedly split the array into half part, and for a size of  $N$  array, we need to split  $\log N$  times (at most  $\log N + 1$  times). And for the merge step, we need to iterate over every element to decide the sequence. In total, the time complexity is  $O(N \cdot \log N)$ .

2. Explain what you think the worst-case, big-Oh complexity and the best-case, big-Oh complexity is for this iterative merge sort. Why do you think that?

For the iterative approach of merge sort, the time complexity in big-Oh is  $O(N \cdot \log N)$ . The first for loop runs for  $\log N$  times since the  $m$  increase by 2 multiply by  $m$  each time. The inner for loop and the merge method total takes  $N$  times since it must compare every position in the original array and total is  $N$  times.