NUM Upper Bounds

